```
1
  3 const double eps=1e-8;
  4 const double pi=acos(-1.0);
  5 const double inf=1e20;
  6 const int maxp=1111;
  7 int dblcmp(double d)
  8 {
  9
        if (fabs(d)<eps)return 0;</pre>
 10
        return d>eps?1:-1;
 11 }
 12 inline double sqr(double x) {return x*x;}
 13 /*
 14 point()
                                 - Empty constructor
 15 point(double x, double y) - constructor
 16 input()
                                 - double input
 17 output()
                                 - .2lf output
 18 operator ==
                                 - compares x and y
 19 operator <
                                 - compares first by x, then by y
 20 len()
                                 - gives length from origin
 21 len2()
                                 - gives square of length from origin
                            - gives distance from p
 22 distance(point p)
 23 add(point p)
                                - returns new point after adding curresponging x and y
 24 sub(point p)
                                 - returns new point after subtracting curresponging x
and y
 25 mul(double b)
                                - returns new point after multiplieing x and y by b
 26 div(double b)
                                - returns new point after divideing x and y by b
 27 dot(point p)
                                - dot product
 28 det(point p)
                                - cross product of 2d points
                              - Probably radius of circumcircle of the triangle
 29 rad(point a, point b)
 30 trunc(double r)
                                 - return point that is truncated the distance from
center to r
 31 rotleft()
                                 - returns 90 degree ccw rotated point
                       - returns 90 degree cw rotated point
 32 rotright()
 33 rotate(point p, double angle) - returns point after rotateing the point centering
at p by angle radian ccw
 34 */
 35 struct point
 36 {
 37
         double x,y;
        point()
 38
        point(double _x, double _y) { x = _x; y = _y;
 39
        40
 41
         bool operator == (point a) const{
 42
             return dblcmp(a.x - x) == 0 \&\& dblcmp(a.y - y) == 0;
 43
 44
 45
         bool operator<(point a)const{</pre>
 46
             return dblcmp(a.x - x) == 0 ? dblcmp(y - a.y) < 0 : x < a.x;
 47
 48
         point operator-(point a)const{
 49
             return point(x-a.x, y-a.y);
 50
         double len()
         double len() {    return hypot(x, y);
double len2() {    return x * x + y * y;
 51
 52
 53
         double distance(point p){return hypot(x - p.x, y - p.y);
         point add(point p) { return point(x + p.x, y + p.y);
 54
 55
        point sub(point p) { return point(x - p.x, y - p.y);
        point mul(double b) { return point(x * b, y * b);
 56
 57
        point div(double b) { return point(x / b, y / b);
        double dot(point p) {
    return x*p.x+y*p.y;
    double det(point p) {
        return x*p.y-y*p.x;
    }
}
 58
 59
 60
         double rad(point a,point b){
 61
             point p=*this;
 62
             return fabs(atan2(fabs(a.sub(p).det(b.sub(p))),a.sub(p).dot(b.sub(p)));
 63
```

```
64
        point trunc(double r){
 65
            double l=len();
 66
              if (!dblcmp(l))return *this;
              r/=1;
 67
 68
             return point(x*r,y*r);
 69
      point rotleft() {    return point(-y,x);
point rotright() {    return point(y,-x);
 70
 71
 72
        point rotate(point p,double angle){
 73
            point v=this->sub(p);
 74
             double c=cos(angle),s=sin(angle);
 75
             return point(p.x+v.x*c-v.y*s,p.y+v.x*s+v.y*c);
 76
 77 };
 78
 79 /*
 80 Stores two points
 81
 82 line()
                                           - Empty constructor
 83 line(point a, point b)
                                           - line through a and b
 84 operator ==
                                           - checks if two points are same
 85 line(point p, double angle) - one end p, another end at angle degree
 86 line(double a, double b, double c) - line of equation ax + by + c = 0
 87 input()
                                            - inputs a and b
 88 adjust()
                                            - orders in such a way that a < b
 89 length()
                                            - distance of ab
                                            - returns 0 <= angle < 180
 90 angle()
                                            - 0 if collinear
 91 relation()
                                              1 if ccw
 92
 93
                                              2 if cw
                                            - returns 1 if point is on segment
 94 pointonseg(point p)
 95 parallel(line v)
                                           - returns 1 if they are parallel
 96 segcrossseg(line v)
                                           - returns 0 if does not intersect
 97
                                              returns 1 if non-standard intersection
 98
                                             returns 2 if intersects
                                           - returns 1 if intersects strictly inside
 99 segcrossseg_inside(line v)
100
                                              returns 0 if not
                                            - v is line
101 linecrossseg(line v)
102 linecrossline(line v)
                                            - 0 if parallel
                                              1 if coincides
103
                                              2 if intersects
104
105 crosspoint(line v) - returns intersection point
106 dispointtoline(point p) - distance from point p to the line
107 dispointtoseg(point p) - distance from p to the segment
108 lineprog(point p) - returns projected point p on ab line
109 reflection point of p over ab
104
109 symmetrypoint(point p) - returns projected point p on ab line - returns reflection point of p over ab 110 */
111 struct line
112 {
     point a,b;
113
        line()
114
        line(point _a,point _b){ a=_a; b=_b;
115
116
        bool operator==(line v) { return (a==v.a)&&(b==v.b);
117
        line(point p,double angle){
118
            a=p;
119
            if (dblcmp(angle-pi/2)==0){
120
                  b=a.add(point(0,1));
121
             }else{
122
                  b=a.add(point(1,tan(angle)));
123
124
125
         //ax+by+c=0
126
        line(double _a,double _b,double _c){
127
         if (dblcmp(_a) == 0) {
128
                 a=point(0,-_c/_b);
129
                  b=point(1,-_c/_b);
```

```
130
              }else if (dblcmp(_b)==0){
131
                  a=point(-_c/_a,0);
                  b=point(-_c/_a,1);
132
              }else{
133
134
                  a=point(0,-_c/_b);
135
                  b=point(1,(-_c-_a)/_b);
136
137
138
          void input()
                                   a.input(); b.input();
139
          void adjust()
                                   if(b<a)swap(a,b);</pre>
140
          double length()
                                   return a.distance(b);
141
          double angle(){
142
              double k=atan2(b.y-a.y,b.x-a.x);
143
              if (dblcmp(k)<0)k+=pi;
144
              if (dblcmp(k-pi)==0)k-=pi;
145
              return k;
146
147
          int relation(point p){
148
              int c=dblcmp(p.sub(a).det(b.sub(a)));
149
              if (c<0)return 1;</pre>
150
              if (c>0)return 2;
151
              return 3;
152
153
          bool pointonseq(point p){
154
              return dblcmp(p.sub(a).det(b.sub(a)))==0&&dblcmp(p.sub(a).dot(p.sub(b)))<=0</pre>
155
156
          bool parallel(line v){
157
              return dblcmp(b.sub(a).det(v.b.sub(v.a)))==0;
158
159
          int segcrossseg(line v){
              int d1=dblcmp(b.sub(a).det(v.a.sub(a)));
160
161
              int d2=dblcmp(b.sub(a).det(v.b.sub(a)));
162
              int d3=dblcmp(v.b.sub(v.a).det(a.sub(v.a)));
163
              int d4=dblcmp(v.b.sub(v.a).det(b.sub(v.a)));
              if ((d1^d2)==-2&&(d3^d4)==-2)return 2;
164
165
              return (d1==0&&dblcmp(v.a.sub(a).dot(v.a.sub(b)))<=0
166
                  d2==0\&\&dblcmp(v.b.sub(a).dot(v.b.sub(b))) <=0
167
                  d3==0\&\&dblcmp(a.sub(v.a).dot(a.sub(v.b))) <=0
168
                  d4==0\&\&dblcmp(b.sub(v.a).dot(b.sub(v.b))) <=0);
169
170
          int segcrossseg_inside(line v){
              if(v.pointonseg(a) | v.pointonseg(b) | pointonseg(v.a) | pointonseg(v.b
171
)) return 0;
172
              int d1=dblcmp(b.sub(a).det(v.a.sub(a)));
173
              int d2=dblcmp(b.sub(a).det(v.b.sub(a)));
174
              int d3=dblcmp(v.b.sub(v.a).det(a.sub(v.a)));
175
              int d4=dblcmp(v.b.sub(v.a).det(b.sub(v.a)));
176
              if ((d1^d2) == -2&&(d3^d4) == -2) return 1;
177
              return (d1==0&&dblcmp(v.a.sub(a).dot(v.a.sub(b)))<=0
178
                  d2==0\&\&dblcmp(v.b.sub(a).dot(v.b.sub(b))) <=0
                  d3==0\&\&dblcmp(a.sub(v.a).dot(a.sub(v.b))) <=0
179
180
                  d4==0\&\&dblcmp(b.sub(v.a).dot(b.sub(v.b)))<=0);
181
          int linecrossseg(line v){//*this seg v line
182
              int d1=dblcmp(b.sub(a).det(v.a.sub(a)));
183
184
              int d2=dblcmp(b.sub(a).det(v.b.sub(a)));
185
              if ((d1^d2)==-2)return 2;
              return (d1==0 | d2==0);
186
187
          int linecrossline(line v){
188
189
              if ((*this).parallel(v)){
190
                  return v.relation(a) == 3;
191
192
              return 2;
193
```

```
194
        point crosspoint(line v){
 195
             double al=v.b.sub(v.a).det(a.sub(v.a));
 196
              double a2=v.b.sub(v.a).det(b.sub(v.a));
 197
             return point((a.x*a2-b.x*a1)/(a2-a1),(a.y*a2-b.y*a1)/(a2-a1));
 198
         double dispointtoline(point p){
 199
             return fabs(p.sub(a).det(b.sub(a)))/length();
 200
 201
 202
         double dispointtoseg(point p){
 203
             if (dblcmp(p.sub(b).dot(a.sub(b))) < 0 \mid dblcmp(p.sub(a).dot(b.sub(a))) < 0)
 204
                 return min(p.distance(a),p.distance(b));
 205
 206
             return dispointtoline(p);
 207
 208
         point lineprog(point p){
 209
             return a.add(b.sub(a).mul(b.sub(a).dot(p.sub(a))/b.sub(a).len2()));
 210
 211
         point symmetrypoint(point p){
 212
             point q=lineprog(p);
 213
             return point(2*q.x-p.x,2*q.y-p.y);
 214
 215 };
 216
 217
 218 a circle of point p and radius r
 219
 220 circle()
                                           -empty constructor
 221 circle(point p,double r)
                                           -circle of point p and radius r
222 circle(point a,point b,point c) -circumcircle of triangle of abc
223 circle(point a, point b, point c, bool t)-incircle of triangle of abc, bool t is
nothing
 224 input()
                                            -takes input of a circle
 225 output()
                                           -outputs a circle
 226 operator==
                                           -checks for equality
 227 operator<
                                           -comparison opertaor
 228 area()
                                           -area of the circle
 229 circumference()
                                           -circumference of the circle
 230 relation(point p)
                                           -0 outside
                                            1 on circumference
 231
                                            2 inside circle
 232
 233
     relationseg(line v)
                                           -0 outside
 234
                                            1 on circumference
                                            2 inside circle
 235
 236
     relationline(line v)
                                            -0 outside
 237
                                            1 on circumference
                                             2 inside circle
 238
 239
     getcircle(point a,point b,double r,circle&c1,circle&c2)
                                           -returns two circle c1,c2 through points a,b
 240
of radius r
 241
                                            returns 0 for nor circle
 242 getcircle(line u,point q,double r1,circle &c1,circle &c2)
 243
                                           -returns two circle c1,c2 which is tangent to
line u, goes through
 244
                                            point q and has radius rl
 245
                                            returns 0 for no circle ,1 if c1=c2 ,2 if
c1!=c2
 246 getcircle(line u,line v,double r1,circle &c1,circle &c2,circle &c3,circle &c4)
 247
                                           -returns 4 circles which is tangent to line
u, v has radius r1.
 248 getcircle(circle cx,circle cy,double r1,circle&c1,circle&c2)
 249
                                           -not sure
 250 pointcrossline(line v,point &p1,point &p2)
 251
                                           -not sure
 252 relationcircle(circle v)
                                            -1 for
                                            2
 253
                                             3
 254
```

```
255
256
257
     pointcrosscircle(circle v,point &p1,point &p2)
258
                                             -not sure what it does
259
     tangentline(point q,line &u,line &v) -not sure what it does
260 areacircle(circle v)
                                             -intersection area of circle v
261 areatriangle(point a,point b)
                                             -intersection area of circle and triangle of
point a,b,p
262 */
263 struct circle
264
265
          point p;
266
          double r;
267
          circle()
268
          circle(point _p,double _r):
                                         p(_p),r(_r){
269
          circle(double x, double y, double _r): p(point(x,y)),r(_r){};
270
          circle(point a, point b, point c){
271
              p=line(a.add(b).div(2),a.add(b).div(2).add(b.sub(a).rotleft())).crosspoint(
line(c.add(b).div(2),c.add(b).div(2).add(b.sub(c).rotleft())));
272
              r=p.distance(a);
273
2.74
          circle(point a, point b, point c, bool t) {
275
              line u, v;
276
              double m=atan2(b.y-a.y,b.x-a.x),n=atan2(c.y-a.y,c.x-a.x);
277
              u.a=a;
278
              u.b=u.a.add(point(cos((n+m)/2),sin((n+m)/2)));
279
              v.a=b;
280
              m=atan2(a.y-b.y,a.x-b.x), n=atan2(c.y-b.y,c.x-b.x);
281
              v.b=v.a.add(point(cos((n+m)/2),sin((n+m)/2)));
282
              p=u.crosspoint(v);
283
              r=line(a,b).dispointtoseg(p);
284
285
          void input()
                                   p.input();scanf("%lf",&r);
          void output() { printf("%.21f %.21f %.21f\n",p.x,p.y,r);
286
          bool operator==(circle v){
287
288
              return ((p==v.p)&&dblcmp(r-v.r)==0);
289
290
          bool operator<(circle v)const{</pre>
291
              return ((p<v.p) | (p==v.p)&&dblcmp(r-v.r)<0);
292
          double area()
293
                                   return pi*sqr(r);
294
          double circumference(){ return 2*pi*r;
295
          int relation(point b){
296
              double dst=b.distance(p);
297
              if (dblcmp(dst-r)<0)return 2;</pre>
298
              if (dblcmp(dst-r)==0)return 1;
299
              return 0;
300
301
          int relationseg(line v){
302
              double dst=v.dispointtoseg(p);
303
              if (dblcmp(dst-r)<0)return 2;</pre>
304
              if (dblcmp(dst-r)==0)return 1;
305
              return 0;
306
307
          int relationline(line v){
308
              double dst=v.dispointtoline(p);
309
              if (dblcmp(dst-r)<0)return 2;</pre>
310
              if (dblcmp(dst-r)==0)return 1;
311
              return 0;
312
          int getcircle(point a,point b,double r,circle&c1,circle&c2){
313
314
              circle x(a,r),y(b,r);
315
              int t=x.pointcrosscircle(y,c1.p,c2.p);
316
              if (!t)return 0;
317
              c1.r=c2.r=r;
318
              return t;
```

```
319
320
          int getcircle(line u,point q,double r1,circle &c1,circle &c2){
321
              double dis=u.dispointtoline(q);
              if (dblcmp(dis-r1*2)>0)return 0;
322
              if (dblcmp(dis)==0){
323
324
                  c1.p=q.add(u.b.sub(u.a).rotleft().trunc(r1));
325
                  c2.p=q.add(u.b.sub(u.a).rotright().trunc(r1));
326
                  c1.r=c2.r=r1;
327
                  return 2;
328
329
              line ul=line(u.a.add(u.b.sub(u.a).rotleft().trunc(r1)),u.b.add(u.b.sub(u.a
).rotleft().trunc(r1)));
330
              line u2=line(u.a.add(u.b.sub(u.a).rotright().trunc(r1)),u.b.add(u.b.sub(u.a
).rotright().trunc(r1)));
331
              circle cc=circle(q,r1);
332
              point p1,p2;
333
              if (!cc.pointcrossline(u1,p1,p2))cc.pointcrossline(u2,p1,p2);
334
              c1=circle(p1,r1);
335
                                   c2=c1;return 1;
              if (p1==p2)
336
              c2=circle(p2,r1);
337
              return 2;
338
          int getcircle(line u, line v, double r1, circle &c1, circle &c2, circle &c3, circle &
339
c4){
340
              if (u.parallel(v))return 0;
341
              line ul=line(u.a.add(u.b.sub(u.a).rotleft().trunc(r1)),u.b.add(u.b.sub(u.a
).rotleft().trunc(r1)));
342
              line u2=line(u.a.add(u.b.sub(u.a).rotright().trunc(r1)),u.b.add(u.b.sub(u.a
).rotright().trunc(r1)));
              line v1=line(v.a.add(v.b.sub(v.a).rotleft().trunc(r1)),v.b.add(v.b.sub(v.a
343
).rotleft().trunc(r1)));
              line v2=line(v.a.add(v.b.sub(v.a).rotright().trunc(r1)),v.b.add(v.b.sub(v.a
344
).rotright().trunc(r1)));
              c1.r=c2.r=c3.r=c4.r=r1;
345
346
              c1.p=u1.crosspoint(v1);
347
              c2.p=u1.crosspoint(v2);
348
              c3.p=u2.crosspoint(v1);
349
              c4.p=u2.crosspoint(v2);
350
              return 4;
          }
351
352
353
          int getcircle(circle cx,circle cy,double r1,circle&c1,circle&c2){
354
              circle x(cx.p,r1+cx.r),y(cy.p,r1+cy.r);
355
              int t=x.pointcrosscircle(y,c1.p,c2.p);
356
              if (!t)return 0;
357
              c1.r=c2.r=r1;
358
              return t;
359
360
          int pointcrossline(line v,point &p1,point &p2){
361
              if (!(*this).relationline(v))return 0;
              point a=v.lineprog(p);
362
363
              double d=v.dispointtoline(p);
364
              d=sqrt(r*r-d*d);
365
              if (dblcmp(d)==0) { p1=a; p2=a; return 1;
366
              p1=a.sub(v.b.sub(v.a).trunc(d));
              p2=a.add(v.b.sub(v.a).trunc(d));
367
368
              return 2;
369
370
          int relationcircle(circle v){
371
              double d=p.distance(v.p);
372
              if (dblcmp(d-r-v.r)>0)return 5;
373
              if (dblcmp(d-r-v.r)==0)return 4;
374
              double l=fabs(r-v.r);
375
              if (dblcmp(d-r-v.r)<0&&dblcmp(d-1)>0)return 3;
376
              if (dblcmp(d-1)==0)return 2;
377
              if (dblcmp(d-1)<0)return 1;</pre>
```

```
378
379
         int pointcrosscircle(circle v,point &p1,point &p2){
380
             int rel=relationcircle(v);
381
             if (rel==1 | rel==5)return 0;
382
             double d=p.distance(v.p);
383
             double l=(d+(sqr(r)-sqr(v.r))/d)/2;
384
             double h=sqrt(sqr(r)-sqr(l));
385
             p1=p.add(v.p.sub(p).trunc(l).add(v.p.sub(p).rotleft().trunc(h)));
386
             p2=p.add(v.p.sub(p).trunc(1).add(v.p.sub(p).rotright().trunc(h)));
387
             if (rel==2 | rel==4)return 1;
             return 2;
388
389
390
         int tangentline(point q,line &u,line &v){
391
             int x=relation(q);
392
             if (x==2) return 0;
393
             if (x==1){
394
                 u=line(q,q.add(q.sub(p).rotleft()));
                 v=u; return 1;
395
396
397
             double d=p.distance(q);
             double l=sqr(r)/d;
398
399
             double h=sqrt(sqr(r)-sqr(l));
             u=line(q,p.add(q.sub(p).trunc(l).add(q.sub(p).rotleft().trunc(h)));
400
401
             v=line(q,p.add(q.sub(p).trunc(l).add(q.sub(p).rotright().trunc(h))));
402
             return 2;
403
404
         double areacircle(circle v){
             int rel=relationcircle(v);
405
406
             if (rel>=4)return 0.0;
407
             if (rel<=2)return min(area(), v.area());</pre>
408
             double d=p.distance(v.p);
409
             double hf=(r+v.r+d)/2.0;
             double ss=2*sqrt(hf*(hf-r)*(hf-v.r)*(hf-d));
410
411
             double al=acos((r*r+d*d-v.r*v.r)/(2.0*r*d));
412
             a1=a1*r*r;
413
             double a2=acos((v.r*v.r+d*d-r*r)/(2.0*v.r*d));
             a2=a2*v.r*v.r;
414
415
             return a1+a2-ss;
416
417
         double areatriangle(point a,point b){
418
             if (dblcmp(p.sub(a).det(p.sub(b))==0))return 0.0;
419
             point q[5];
420
             int len=0;
421
             q[len++]=a;
422
             line l(a,b);
423
             point p1,p2;
424
             if (pointcrossline(1,q[1],q[2])==2){
425
                  if (dblcmp(a.sub(q[1]).dot(b.sub(q[1])))<0)q[len++]=q[1];</pre>
426
                 if (dblcmp(a.sub(q[2]).dot(b.sub(q[2])))<0)q[len++]=q[2];</pre>
427
428
             q[len++]=b;
429
             if (len=4&&(dblcmp(q[0].sub(q[1]).dot(q[2].sub(q[1])))>0))swap(q[1],q[2]);
430
             double res=0;
             int i;
431
432
             for (i=0;i<len-1;i++){</pre>
433
                  if (relation(q[i])==0 | relation(q[i+1])==0) 
434
                      double arg=p.rad(q[i],q[i+1]);
435
                      res+=r*r*arg/2.0;
436
437
                  else res = fabs(q[i].sub(p).det(q[i+1].sub(p))/2.0);
438
439
             return res;
440
441
    };
442
443
     / *
```

```
444 n, p, line 1 for each side
 445
 446 input(n)
                                       - inputs n size polygon
 447 add(point p)
                                      - adds a point at end of the list
 448 getline()
                                      - populates line array
 449 cmp
                                       - comparison in convex_hull order
 450 norm()
                                      - sorting in convex_hull order
451 getconvex(polygon &convex) - returns convex hull in convex (monotone chain)
 452 isconvex()
                                      - checks if convex
 453 relationpoint(point q)
                                      - returns 3 if q is a vertex
 454
                                                 2 if on a side
                                                 1 if inside
 455
 456
                                                 0 if outside
 457 relationline(line u)
                                       - returns 1 if there is some intersection
 458
                                                 0 if no intersection
 459
                                                 2 if intersect at corner
 460 convexcut(line u,polygon &po) - left side of u in po
 461 getcircumference()
                                      - returns side length
 462 getarea()
                                      - returns area
 463 getdir()
                                      - returns 0 for cw, 1 for ccw
 464 getbarycentre()
                                      - returns barycenter / cq
465 areaintersection(polygon po) - not implemented
466 areaunion(polygon po) - not implemented
467 areacircle(circle c) - intersection are
 467 areacircle(circle c)
                                      - intersection area of circle and polygon
468 relationcircle(circle c) - returns 0 if outside circle
                                                 1 if tangent
 469
                                                 2 if inside
 470
 471 mincircle()
                                      - returns minimum enclosing circle
 472 circlecover()
                                      - i think there is mistake. it tries to find
minimum enclosing circle
473 pointinpolygon(point q)
                                      - -1 if not on polygon, non negative number.. side
index
474 inside_polygon(point q, int on_edge=1)
 475
                  - returns on_edge if on edge, otherwise 0 for outside 1 for inside
 476 isdiagonal(int a, int b) - checks if p[a], p[b] is diagonal or not. returns
0/1
 477 */
 478 struct polygon
 479
         int n;
 480
        point p[maxp];
line l[maxp];
 481
 482
         void input(int _n){
 483
              n=_n;
 484
              for (int i=0;i<n;i++) p[i].input();</pre>
 485
 486
 487
        void add(point q) { p[n++]=q;
         void getline(){
 488
 489
              for (int i=0;i<n;i++)</pre>
 490
                  l[i]=line(p[i],p[(i+1)%n]);
 491
 492
         struct cmp{
 493
              point p;
 494
              cmp(const point &p0) {p=p0;}
 495
              bool operator()(const point &aa,const point &bb){
 496
                  point a=aa,b=bb;
 497
                  int d=dblcmp(a.sub(p).det(b.sub(p)));
 498
                  if (d==0)
 499
                      return dblcmp(a.distance(p)-b.distance(p))<0;</pre>
 500
                  return d>0;
 501
              }
 502
         };
 503
        void norm(){
 504
             point mi=p[0];
 505
              for (int i=1;i<n;i++)mi=min(mi,p[i]);</pre>
 506
              sort(p,p+n,cmp(mi));
```

```
507
508
          void getconvex(polygon &convex){
509
              int i;
510
              sort(p,p+n);
511
              convex.n=n;
512
              for (i=0;i<min(n,2);i++) convex.p[i]=p[i];</pre>
513
              if (n<=2)return;</pre>
514
              int &top=convex.n;
515
              top=1;
516
              for (i=2;i<n;i++){
                   while (top_{\&}convex.p[top].sub(p[i]).det(convex.p[top-1].sub(p[i])) <= 0)
517
518
                       top--;
519
                   convex.p[++top]=p[i];
520
521
              int temp=top;
522
              convex.p[++top]=p[n-2];
523
              for (i=n-3;i>=0;i--)
524
                   while (top!=temp&&convex.p[top].sub(p[i]).det(convex.p[top-1].sub(p[i
]))<=0)
525
                       top--;
526
                   convex.p[++top]=p[i];
527
528
          bool isconvex(){
529
530
              bool s[3];
531
              memset(s,0,sizeof(s));
532
              int i,j,k;
              for (i=0;i<n;i++){</pre>
533
534
                   j=(i+1)%n;
535
                   k=(j+1)%n;
536
                   s[dblcmp(p[j].sub(p[i]).det(p[k].sub(p[i])))+1]=1;
537
                   if (s[0]&&s[2])return 0;
538
539
              return 1;
540
          int relationpoint(point q){
541
542
              int i,j;
543
              for (i=0;i<n;i++){</pre>
544
                   if (p[i]==q)return 3;
545
546
              getline();
547
              for (i=0;i<n;i++){</pre>
548
                   if (l[i].pointonseg(q))return 2;
549
550
              int cnt=0;
              for (i=0;i<n;i++){</pre>
551
552
                   j=(i+1)%n;
553
                   int k=dblcmp(q.sub(p[j]).det(p[i].sub(p[j])));
                   int u=dblcmp(p[i].y-q.y);
554
                   int v=dblcmp(p[j].y-q.y);
555
556
                   if (k>0&&u<0&&v>=0)cnt++;
557
                   if (k<0&&v<0&&u>=0)cnt--;
558
559
              return cnt!=0;
560
561
          int relationline(line u){
562
              int i,k=0;
563
              getline();
564
              for (i=0;i<n;i++){</pre>
565
                   if (1[i].segcrossseg(u)==2)return 1;
566
                   if (l[i].segcrossseg(u)==1)k=1;
567
568
              if (!k)return 0;
569
              vector<point>vp;
570
              for (i=0;i<n;i++){</pre>
571
                   if (l[i].segcrossseg(u)){
```

```
572
                      if (l[i].parallel(u)){
573
                           vp.pb(u.a);
574
                           vp.pb(u.b);
575
                           vp.pb(l[i].a);
576
                           vp.pb(l[i].b);
577
                           continue;
578
579
                      vp.pb(l[i].crosspoint(u));
580
581
              sort(vp.begin(), vp.end());
582
583
              int sz=vp.size();
584
              for (i=0;i<sz-1;i++){</pre>
585
                  point mid=vp[i].add(vp[i+1]).div(2);
586
                  if (relationpoint(mid)==1)return 1;
587
588
             return 2;
589
590
         void convexcut(line u,polygon &po){
591
              int i;
592
              int &top=po.n;
593
              top=0;
594
              for (i=0;i<n;i++){
595
                  int d1=dblcmp(p[i].sub(u.a).det(u.b.sub(u.a)));
596
                  int d2=dblcmp(p[(i+1)%n].sub(u.a).det(u.b.sub(u.a)));
597
                  if (d1>=0)po.p[top++]=p[i];
598
                  if (d1*d2<0)po.p[top++]=u.crosspoint(line(p[i],p[(i+1)%n]));
599
600
601
         double getcircumference(){
             double sum=0;
602
603
              int i;
604
              for (i=0;i<n;i++)</pre>
605
                  sum+=p[i].distance(p[(i+1)%n]);
606
             return sum;
607
608
         double getarea(){
609
             double sum=0;
              int i;
610
611
              for (i=0;i<n;i++)</pre>
612
                  sum+=p[i].det(p[(i+1)%n]);
613
             return fabs(sum)/2;
614
615
         bool getdir(){
              double sum=0;
616
              int i;
617
              for (i=0;i<n;i++)</pre>
618
619
                  sum+=p[i].det(p[(i+1)%n]);
620
              if (dblcmp(sum)>0)return 1;
621
             return 0;
622
623
         point getbarycentre(){
624
             point ret(0,0);
625
             double area=0;
             int i;
626
627
              for (i=1;i<n-1;i++){</pre>
628
                  double tmp=p[i].sub(p[0]).det(p[i+1].sub(p[0]));
629
                  if (dblcmp(tmp)==0)continue;
630
                  area+=tmp;
631
                  ret.x+=(p[0].x+p[i].x+p[i+1].x)/3*tmp;
632
                  ret.y+=(p[0].y+p[i].y+p[i+1].y)/3*tmp;
633
634
              if (dblcmp(area))ret=ret.div(area);
635
             return ret;
636
637
         double areaintersection(polygon po){
```

```
638
         double areaunion(polygon po){
639
             return getarea()+po.getarea()-areaintersection(po);
640
641
         double areacircle(circle c){
642
             int i,j,k,l,m;
             double ans=0;
643
644
              for (i=0;i<n;i++){</pre>
645
                  int j=(i+1)%n;
646
                  if (dblcmp(p[j].sub(c.p).det(p[i].sub(c.p)))>=0)
647
                      ans+=c.areatriangle(p[i],p[j]);
648
                  else ans-=c.areatriangle(p[i],p[j]);
649
650
             return fabs(ans);
651
652
         int relationcircle(circle c){
653
             getline();
654
              int i, x=2;
655
              if (relationpoint(c.p)!=1)return 0;
656
              for (i=0;i<n;i++){</pre>
657
                  if (c.relationseg(l[i])==2)return 0;
                  if (c.relationseq(l[i])==1)x=1;
658
659
660
             return x;
661
662
         void find(int st,point tri[],circle &c){
663
              if (!st) c=circle(point(0,0),-2);
664
              if (st==1) c=circle(tri[0],0);
665
              if (st==2) c=circle(tri[0].add(tri[1]).div(2),tri[0].distance(tri[1])/2.0);
              if (st==3) c=circle(tri[0],tri[1],tri[2]);
666
667
         void solve(int cur,int st,point tri[],circle &c){
668
             find(st,tri,c);
669
670
              if (st==3)return;
671
              int i;
              for (i=0;i<cur;i++){</pre>
672
                  if (dblcmp(p[i].distance(c.p)-c.r)>0){
673
674
                      tri[st]=p[i];
675
                      solve(i,st+1,tri,c);
676
              }
677
678
679
         circle mincircle(){
680
             random_shuffle(p,p+n);
681
             point tri[4];
682
              circle c;
683
              solve(n, 0, tri, c);
684
             return c;
685
686
         int circlecover(double r){
              int ans=0,i,j;
687
688
              vector<pair<double,int> >v;
689
              for (i=0;i<n;i++){</pre>
690
                  v.clear();
691
                  for (j=0;j<n;j++)if (i!=j){</pre>
692
                      point q=p[i].sub(p[j]);
693
                      double d=q.len();
694
                      if (dblcmp(d-2*r) <= 0)
695
                          double arg=atan2(q.y,q.x);
696
                          if (dblcmp(arg)<0)arg+=2*pi;</pre>
697
                          double t=acos(d/(2*r));
698
                          v.push_back(make_pair(arg-t+2*pi,-1));
699
                          v.push_back(make_pair(arg+t+2*pi,1));
700
701
702
                  sort(v.begin(),v.end());
703
                  int cur=0;
```

```
704
                                        for (j=0;j<v.size();j++){</pre>
  705
                                                  if (v[j].second==-1)++cur;
  706
                                                  else --cur;
  707
                                                  ans=max(ans,cur);
  708
  709
  710
                               return ans+1;
  711
  712
                      int pointinpolygon(point q){
  713
                               if (getdir())reverse(p,p+n);
                                if (dblcmp(q.sub(p[0]).det(p[n-1].sub(p[0])))==0){
  714
  715
                                         if (line(p[n-1],p[0]).pointonseg(q))return n-1;
  716
                                        return -1;
  717
  718
                               int low=1,high=n-2,mid;
  719
                               while (low<=high){</pre>
  720
                                        mid=(low+high)>>1;
  721
                                         if (dblcmp(q.sub(p[0]).det(p[mid].sub(p[0])))>=0&&dblcmp(q.sub(p[0]).
det(p[mid+1].sub(p[0])))<0){
  722
                                                 polygon c;
  723
                                                 c.p[0]=p[mid];
  724
                                                 c.p[1]=p[mid+1];
  725
                                                  c.p[2]=p[0];
  726
                                                  c.n=3;
  727
                                                  if (c.relationpoint(q))return mid;
  728
                                                 return -1;
  729
  730
                                         if (dblcmp(q.sub(p[0]).det(p[mid].sub(p[0])))>0) low=mid+1;
  731
                                        else high=mid-1;
  732
  733
                               return -1;
  734
  735
  736
                      double xmult(point a, point b, point c){
  737
                               return (b - a).det(c - a);
  738
  739
                       int inside_polygon(point q, int on_edge=1){
  740
  741
                               point q2;
  742
                               int i=0,count;
  743
                               while (i<n){</pre>
  744
                                         for(count = i = 0, q2.x = rand()+10000, q2.y = rand() + 10000; i < n; i
++)
  745
                                                  if(dblcmp(xmult(q,p[i],p[(i+1)%n]))==0 \&\& (p[i].x-q.x)*(p[(i+1)%n].
x-q.x)<eps && (p[i].y-q.y)*(p[(i+1)%n].y-q.y)<eps)
  746
                                                           return on edge;
  747
                                                  else if(dblcmp(xmult(q,q2,p[i]))==0)
  748
  749
                                                  \textbf{else if}(xmult(q,p[i],q2)*xmult(q,p[(i+1)*n],q2)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p[i],q,a)<-eps&&xmult(p
p[(i+1)%n])*xmult(p[i],q2,p[(i+1)%n])<-eps)
  750
                                                           count++;
  751
  752
                               return count&1;
  753
  754
                      int isdiagonal(int a, int b){
  755
                               int i;
  756
                               if(a == b | (a + 1)%n == b | (b + 1)%n == a) return 0;
                               getline();
  757
  758
                               line x(p[a], p[b]);
  759
                               for(i = 0; i < n; i++) if(a != i && b != i)
  760
                                         if(x.pointonseg(p[i]))
  761
                                                 return 0;
  762
                               for(i = 0; i < n; i++)</pre>
  763
                                         if(l[i].segcrossseg_inside(x))
  764
                                                 return 0;
  765
                               point y = p[a].add(p[b]).div(2.);
```

```
766
              if(inside_polygon(y, 0) == 0) return 0;
767
              return 1;
768
769
     };
770
    const int maxn=500;
771
772 struct circles
773
774
         circle c[maxn];
775
         double ans[maxn];
776
         double pre[maxn];
777
         int n;
         circles()
778
779
         void add(circle cc) {
                                    c[n++]=cc;
780
         bool inner(circle x, circle y) {
781
              if (x.relationcircle(y)!=1)return 0;
782
              return dblcmp(x.r-y.r) <= 0?1:0;
783
784
         void init_or(){
785
              int i, j, k=0;
              bool mark[maxn]={0};
786
              for (i=0;i<n;i++){</pre>
787
788
                  for (j=0;j<n;j++)if (i!=j&&!mark[j]){</pre>
                       if ((c[i]==c[j]) | |inner(c[i],c[j]))break;
789
790
791
                  if (j<n)mark[i]=1;
792
793
              for (i=0;i<n;i++)if (!mark[i])c[k++]=c[i];</pre>
794
             n=k;
795
796
         void init_and(){
797
              int i,j,k=0;
798
              bool mark[maxn]={0};
799
              for (i=0;i<n;i++){</pre>
800
                  for (j=0;j<n;j++)if (i!=j&&!mark[j])</pre>
                       if ((c[i]==c[j]) | |inner(c[j],c[i]))break;
801
802
                  if (j<n)mark[i]=1;
803
              for (i=0;i<n;i++)if (!mark[i])c[k++]=c[i];</pre>
804
805
             n=k;
806
807
         double areaarc(double th,double r){
808
              return 0.5*sqr(r)*(th-sin(th));
809
810
         void getarea(){
              int i,j,k;
811
812
              memset(ans, 0, sizeof(ans));
813
              vector<pair<double,int> >v;
814
              for (i=0;i<n;i++){</pre>
815
                  v.clear();
                  v.push_back(make_pair(-pi,1));
816
817
                  v.push_back(make_pair(pi,-1));
818
                  for (j=0;j<n;j++)if (i!=j){</pre>
819
                      point q=c[j].p.sub(c[i].p);
820
                       double ab=q.len(),ac=c[i].r,bc=c[j].r;
821
                       if (dblcmp(ab+ac-bc)<=0){
822
                           v.push_back(make_pair(-pi,1));
                           v.push_back(make_pair(pi,-1));
823
824
                           continue;
825
826
                       if (dblcmp(ab+bc-ac)<=0)continue;</pre>
827
                       if (dblcmp(ab-ac-bc)>0) continue;
828
                      double th=atan2(q.y,q.x), fai=acos((ac*ac+ab*ab-bc*bc)/(2.0*ac*ab));
829
                       double a0=th-fai;
830
                       if (dblcmp(a0+pi)<0)a0+=2*pi;</pre>
831
                       double al=th+fai;
```

```
832
                       if (dblcmp(a1-pi)>0)a1-=2*pi;
 833
                       if (dblcmp(a0-a1)>0){
 834
                            v.push_back(make_pair(a0,1));
                            v.push_back(make_pair(pi,-1));
 835
 836
                            v.push_back(make_pair(-pi,1));
 837
                            v.push_back(make_pair(a1,-1));
 838
                       }else{
 839
                            v.push_back(make_pair(a0,1));
                            v.push_back(make_pair(a1,-1));
 840
 841
 842
                   sort(v.begin(),v.end());
 843
 844
                   int cur=0;
 845
                   for (j=0;j<v.size();j++){</pre>
 846
                       if (cur&&dblcmp(v[j].first-pre[cur])){
 847
                            ans[cur]+=areaarc(v[j].first-pre[cur],c[i].r);
 848
                            ans[cur]+=0.5*point(c[i].p.x+c[i].r*cos(pre[cur]),c[i].p.y+c[i]
].r*sin(pre[cur])).det(point(c[i].p.x+c[i].r*cos(v[j].first),c[i].p.y+c[i].r*sin(v[j].
first)));
 849
 850
                       cur+=v[j].second;
 851
                       pre[cur]=v[j].first;
 852
 853
 854
               for (i=1;i<=n;i++) ans[i]-=ans[i+1];</pre>
 855
 856
      };
 857
      struct halfplane: public line
 858
          double angle;
 859
 860
          halfplane()
          halfplane(point _a,point _b) { a=_a; b=_b;
 861
 862
          halfplane(line v)
                                    a=v.a; b=v.b;
 863
          void calcangle()
                                    angle=atan2(b.y-a.y,b.x-a.x);
          bool operator<(const halfplane &b)const{</pre>
 864
 865
               return angle<b.angle;</pre>
 866
 867
      };
 868
      struct halfplanes
 869
 870
          int n;
 871
          halfplane hp[maxp];
 872
          point p[maxp];
 873
          int que[maxp];
 874
          int st,ed;
          void push(halfplane tmp) { hp[n++]=tmp;
 875
 876
          void unique(){
               int m=1,i;
 877
 878
               for (i=1;i<n;i++){</pre>
 879
                   if (dblcmp(hp[i].angle-hp[i-1].angle))hp[m++]=hp[i];
 880
                   else if (dblcmp(hp[m-1].b.sub(hp[m-1].a).det(hp[i].a.sub(hp[m-1].a))>0
))hp[m-1]=hp[i];
 881
 882
               n=m;
 883
 884
          bool halfplaneinsert(){
 885
               int i;
 886
               for (i=0;i<n;i++)hp[i].calcangle();</pre>
 887
               sort(hp,hp+n);
 888
               unique();
 889
               que[st=0]=0;
 890
               que[ed=1]=1;
 891
               p[1]=hp[0].crosspoint(hp[1]);
 892
               for (i=2;i<n;i++){
 893
                   while (st < ed_{\&}dblcmp((hp[i].b.sub(hp[i].a).det(p[ed].sub(hp[i].a)))) < 0)
ed--;
```

```
894
                                     while (st < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(p[st+1].sub(hp[i].a)))) < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(p[st+1].sub(hp[i].a)))) < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(p[st+1].sub(hp[i].a)))) < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(p[st+1].sub(hp[i].a)))) < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(hp[i].a))) < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(hp[i].a))) < ed_{\&\&}dblcmp((hp[i].b.sub(hp[i].a).det(hp[i].a))) < ed_{\&\&}dblcmp((hp[i].a).det(hp[i].a)) < ed_{\&\&}dblcmp((hp[i].a).det(hp[i].a).det(hp[i].a)) < ed_{\&\&}dblcmp((hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].a).det(hp[i].
0)st++;
 895
                                     que[++ed]=i;
 896
                                     if (hp[i].parallel(hp[que[ed-1]]))return false;
 897
                                     p[ed]=hp[i].crosspoint(hp[que[ed-1]]);
 898
                              \label{lem:while} \textbf{ (st<ed&&dblcmp(hp[que[st]].b.sub(hp[que[st]].a).det(p[ed].sub(hp[que[st]].a)).} 
 899
st]].a)))<0)ed--;
                             while (st < ed_{\&}dblcmp(hp[que[ed]].b.sub(hp[que[ed]].a).det(p[st+1].sub(hp[que[ed]].a))
 900
que[ed]].a)))<0)st++;
 901
                             if (st+1>=ed)return false;
 902
                             return true;
 903
 904
                    void getconvex(polygon &con){
 905
                             p[st]=hp[que[st]].crosspoint(hp[que[ed]]);
 906
                             con.n=ed-st+1;
 907
                             int j=st,i=0;
 908
                             for (;j<=ed;i++,j++) con.p[i]=p[j];</pre>
 909
           };
 910
 911
 912
          3d point
 913 rotate function is not complete. every else is same as 2d
 914
           * /
 915
           struct point3
 916
                    double x,y,z;
 917
 918
                    point3()
 919
                    point3(double _x,double _y,double _z):
 920
                    x(\underline{x}), y(\underline{y}), z(\underline{z})
                    void input()
                                                                        scanf("%lf%lf",&x,&y,&z);
 921
                                                             printf("%.21f %.21f %.21f\n",x,y,z);
 922
                    void output()
 923
                    bool operator == (point3 a) {
 924
                             return dblcmp(a.x-x)==0\&\&dblcmp(a.y-y)==0\&\&dblcmp(a.z-z)==0;
 925
 926
                    bool operator<(point3 a)const {</pre>
 927
                             return dblcmp(a.x-x)==0?dblcmp(y-a.y)==0?dblcmp(z-a.z)<0:y<a.y:x<a.x;
 928
 929
                    double len()
                                                                        return sqrt(len2());
 930
                    double len2()
                                                                       return x*x+y*y+z*z;
 931
                    double distance(point3 p){
 932
                             return sqrt((p.x-x)*(p.x-x)+(p.y-y)*(p.y-y)+(p.z-z)*(p.z-z));
 933
 934
                    point3 add(point3 p){
                                                                       return point3(x+p.x,y+p.y,z+p.z);}
 935
                    point3 sub(point3 p){
                                                                       return point3(x-p.x,y-p.y,z-p.z);
 936
                    point3 mul(double d){
                                                                       return point3(x*d,y*d,z*d);
 937
                    point3 div(double d){
                                                                       return point3(x/d,y/d,z/d);
 938
                    double dot(point3 p){
                                                                       return x*p.x+y*p.y+z*p.z;
 939
                    point3 det(point3 p){
 940
                             return point3(y*p.z-p.y*z,p.x*z-x*p.z,x*p.y-p.x*y);
 941
 942
                    double rad(point3 a,point3 b){
 943
                             point3 p=(*this);
 944
                             return acos(a.sub(p).dot(b.sub(p))/(a.distance(p)*b.distance(p)));
 945
                    point3 trunc(double r){
 946
 947
                             r/=len();
 948
                             return point3(x*r,y*r,z*r);
 949
 950
                    point3 rotate(point3 o,double r)
 951
 952
 953
            };
 954
 955
 956
            3d line
```

```
957
 958
      * /
 959
     struct line3
 960
 961
          point3 a,b;
 962
          line3()
 963
          line3(point3 _a,point3 _b){ a=_a; b=_b;
 964
          bool operator==(line3 v){ return (a==v.a)&&(b==v.b);
 965
          void input()
                                   a.input(); b.input();
 966
                                   return a.distance(b);
          double length()
 967
          bool pointonseg(point3 p) {
              return dblcmp(p.sub(a).det(p.sub(b)).len())==0&&dblcmp(a.sub(p).dot(b.sub(p
 968
) ) ) <= 0 ;
 969
 970
          double dispointtoline(point3 p){
 971
              return b.sub(a).det(p.sub(a)).len()/a.distance(b);
 972
 973
          double dispointtoseg(point3 p){
 974
              if (dblcmp(p.sub(b).dot(a.sub(b)))<0 | |dblcmp(p.sub(a).dot(b.sub(a)))<0)
 975
                  return min(p.distance(a),p.distance(b));
 976
 977
              return dispointtoline(p);
 978
 979
          point3 lineprog(point3 p){
 980
              return a.add(b.sub(a).trunc(b.sub(a).dot(p.sub(a))/b.distance(a)));
 981
 982
          point3 rotate(point3 p,double ang){
              if (dblcmp((p.sub(a).det(p.sub(b)).len()))==0)return p;
 983
 984
              point3 f1=b.sub(a).det(p.sub(a));
 985
              point3 f2=b.sub(a).det(f1);
 986
              double len=fabs(a.sub(p).det(b.sub(p)).len()/a.distance(b));
              f1=f1.trunc(len);f2=f2.trunc(len);
 987
 988
              point3 h=p.add(f2);
              point3 pp=h.add(f1);
 989
 990
              return h.add((p.sub(h)).mul(cos(ang*1.0))).add((pp.sub(h)).mul(sin(ang*1.0)
)));
 991
      };
 992
     / *
 993
 994
     plane
 995
     * /
 996
     struct plane
 997
 998
          point3 a,b,c,o;
 999
          plane()
1000
          plane(point3 _a,point3 _b,point3 _c){
1001
              a=_a;
1002
              b=_b;
1003
              C = _C;
1004
              o=pvec();
1005
          plane(double _a,double _b,double _c,double _d) {
1006
1007
              //ax+by+cz+d=0
1008
              o=point3(_a,_b,_c);
1009
              if (dblcmp(_a)!=0){ a=point3((-_d-_c-_b)/_a,1,1);
1010
              else if (dblcmp(_b)!=0){
1011
                  a=point3(1,(-_d-_c-_a)/_b,1);
1012
1013
              else if (dblcmp(_c)!=0) {a=point3(1,1,(-_d-_a-_b)/_c);}
1014
1015
          void input(){
1016
              a.input();
1017
              b.input();
1018
              c.input();
1019
              o=pvec();
1020
          }
```

```
1021
                                   return b.sub(a).det(c.sub(a));
          point3 pvec()
1022
          bool pointonplane(point3 p) {
1023
              return dblcmp(p.sub(a).dot(o))==0;
1024
1025
1026
          int pointontriangle(point3 p){
1027
              if (!pointonplane(p))return 0;
              double s=a.sub(b).det(c.sub(b)).len();
1028
1029
              double s1=p.sub(a).det(p.sub(b)).len();
1030
              double s2=p.sub(a).det(p.sub(c)).len();
1031
              double s3=p.sub(b).det(p.sub(c)).len();
1032
              if (dblcmp(s-s1-s2-s3))return 0;
1033
              if (dblcmp(s1)&&dblcmp(s2)&&dblcmp(s3))return 2;
1034
              return 1;
1035
1036
          bool relationplane(plane f){
1037
              if (dblcmp(o.det(f.o).len()))return 0;
1038
              if (pointonplane(f.a))return 2;
1039
              return 1;
1040
1041
          double angleplane(plane f){
1042
              return acos(o.dot(f.o)/(o.len()*f.o.len()));
1043
1044
          double dispoint(point3 p){
1045
              return fabs(p.sub(a).dot(o)/o.len());
1046
          point3 pttoplane(point3 p){
1047
1048
              line3 u=line3(p,p.add(o));
1049
              crossline(u,p);
1050
              return p;
1051
1052
          int crossline(line3 u,point3 &p){
1053
              double x=o.dot(u.b.sub(a));
              double y=o.dot(u.a.sub(a));
1054
1055
              double d=x-y;
              if (dblcmp(fabs(d))==0)return 0;
1056
1057
              p=u.a.mul(x).sub(u.b.mul(y)).div(d);
1058
              return 1;
1059
          int crossplane(plane f,line3 &u){
1060
1061
              point3 oo=o.det(f.o);
1062
              point3 v=o.det(oo);
1063
              double d=fabs(f.o.dot(v));
1064
              if (dblcmp(d)==0)return 0;
1065
              point3 g=a.add(v.mul(f.o.dot(f.a.sub(a))/d));
1066
              u=line3(q,q.add(oo));
1067
              return 1;
1068
1069
      };
1070
1071
      polygon a,b;
1072
      int main()
1073
1074
          int i,j,k;
1075
          a.n=b.n=4;
1076
          double w,h,g;
1077
          cin>>w>>h>>g;
1078
          g/=180.0;
1079
          g*=pi;
1080
          a.p[0]=point(-w/2.0,-h/2.0);
1081
          a.p[1]=point(w/2.0, -h/2.0);
1082
          a.p[2]=point(w/2.0,h/2.0);
1083
          a.p[3]=point(-w/2.0,h/2.0);
1084
          for (i=0;i<4;i++)
1085
1086
              b.p[i]=(a.p[i]).rotate(point(0,0),g);
```

```
1087     }
1088     polygons p;
1089     p.push(a);p.push(b);
1090     printf("%.12lf\n",p.polyareaunion());
1091     return 0;
1092     }
```