

Example 2.5 A 15-KVA, 2300/230 V transformer is to be tested to determine its excitation branch components, its series impedances and its voltage regulation.

Data:

Open circuit test (low voltage side)	short circuit test (high voltage side)
$V_{oc} = 230V$	$V_{sc} = 47V$
$I_{oc} = 2.1A$	$I_{sc} = 6.0A$
$P_{oc} = 50W$	$P_{sc} = 160W$

- (a) Find the eq circuit of its transformer referred to high voltage side.
- (b) for low-voltage side.
- (c) Calculate the full-load voltage regulation at 0.8 lagging power factor, 1.0 power factor and 0.8 leading power

factor using the exact equation for V_p .

(e) What is the efficiency of the transformer at full load with a power factor of 0.8 lagging?

Answer

(a)

I_s

R_{eq}

jX_{eq}

I_p



$$R_e = \frac{(V_{oc})^2}{P_{oc}}$$

$$= \frac{(230)^2}{50} = 1058 \Omega$$

$$X_m = \frac{(V_{oc})^2}{\sqrt{(V_{oc} I_{oc})^2 - P_{oc}^2}} = \frac{(230)^2}{\sqrt{(230 \times 2.1)^2 - (50)^2}} = 110.115 j\Omega$$

$P_{oc} = 50W$
 $V_{oc} = 230V$

$$R_{eq} = \frac{P_{sc}}{I_{sc}^2} = \frac{160}{(6)^2} = 4.44$$

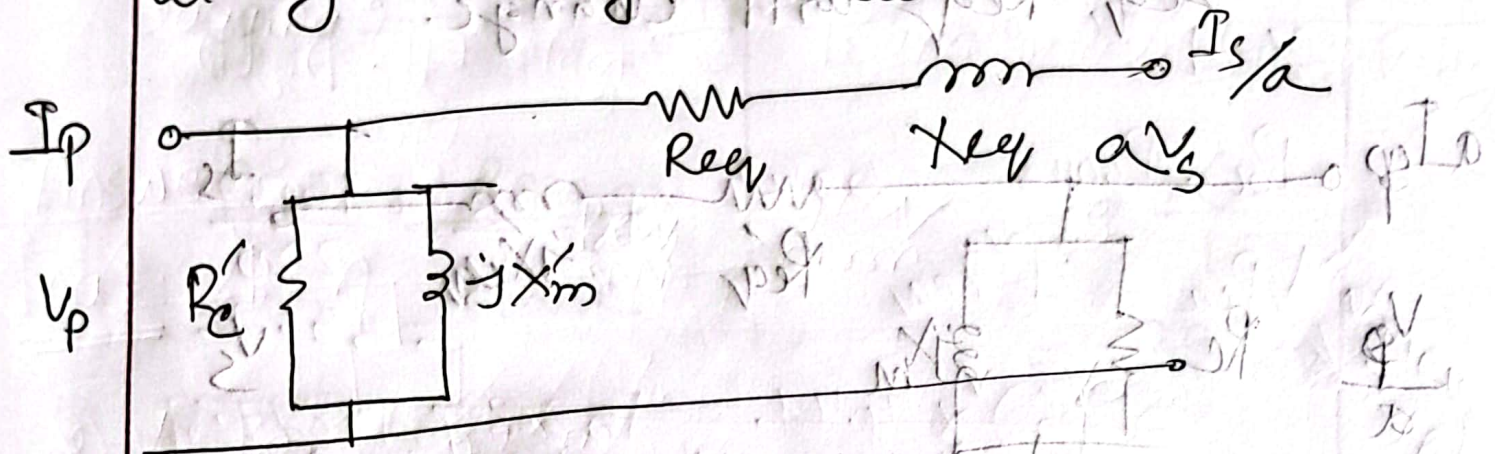
$$X_{eq} = \frac{\sqrt{(V_{sc} I_{sc})^2 - (P_{sc})^2}}{I_{sc}^2} = \frac{\sqrt{(47 \times 6)^2 - (160)^2}}{(6)^2} = 6.450 \, \Omega$$

$$a = \frac{V_s}{V_p} = \frac{2300}{230} = 10$$

R_{eq}, X_{eq} are \rightarrow Primary

$R_c, X_m \rightarrow$ Secondary

at high voltage referred to primary



$$R'_c = R_c \times a^2 = 1058 \times 100 = 105.8 \text{ K}\Omega$$

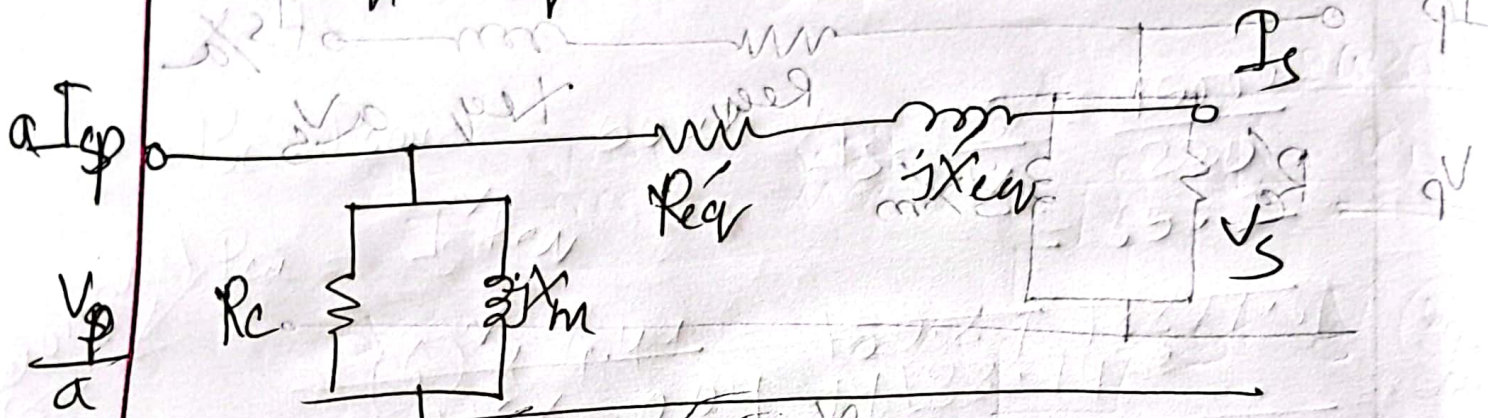
$$X'_m = X_m \times a^2 = 110.58 \times 100 = 11.0 \text{ K}\Omega$$

R_{eq}, X_{eq} same.

$$X_m = \frac{1}{\frac{1}{V_p} \times 100 \times 100} = 100 \times 100$$

$$110.115$$

- (b) At low voltage referred to secondary
 (R_e, X_m same)
 X_{eq}, R_{eq} will change.



$$R_{eq} = 444 \Omega$$

$$X_{eq} = 645 j\Omega$$

$$R'_{eq} = R_{eq} \times \frac{1}{a^2} = 0.0444 \Omega$$

$$X'_{eq} = X_{eq} \times \frac{1}{a^2} = 0.0645 \Omega$$

$$(c) V_{reg} = \sqrt{(S_{pu} R_{pu} + \cos \theta)^2 + (S_{pu} X_{pu} + \sin \theta)^2} - 1$$

$$S_{pu} = \frac{15000 \text{ VA}}{1 \text{ pu}} \quad Z_{base, P} = \frac{(V_s)^2}{S_{pu}}$$

$$R_{pu} = \frac{R_{eq}}{Z_{base}}$$

$$Z_{base, P} = \frac{(2300)^2}{15000} = 352.667$$

$$\Rightarrow \frac{4.44}{352.667} = 0.01258$$

$$X_{pu} = \frac{X_{eq}}{Z_{base}} = \frac{6.45}{352.667} = 0.01828$$

$$\theta = \cos^{-1}(0.8) = 36.86$$

अदि lagging
36.86
leading - 36.86

$$V_{reg} = \sqrt{(1 \times 0.01258 + \cos(36.86))^2 + (1 \times 0.01828 + \sin(36.86))^2} - 1$$

$$= 1.72\%$$

$$\textcircled{c} \quad \eta = \frac{x(V_A)_{\text{full}} \times P_f}{x(V_A)_{\text{full}} \times P_f + P_{\text{core}} + x^2 P_{\text{cu}}}$$

$$x = 1$$

$$P_{\text{cu}} = P_{\text{core}} = 50 \text{ W}$$

$$I_s = \frac{S}{V_s} = \frac{15000}{230} = 65.2$$

secondary
into

$$P_{\text{cu}} = I_s^2 R_{\text{eq}}$$

$$\begin{aligned} &= (6)^2 \times 4.44 = 159.84 \\ &= (65.2)^2 \times 0.0444 = 188.74 \end{aligned}$$

$$\eta = \frac{1 \times 15000 \times 0.8}{1 \times 15000 \times 0.8 + 50 + (1)^2 \frac{159.84}{188.74} \times 65.2}$$

$$= \frac{0.9811}{0.9828} = 98.28\%$$

$$28.28 = (8.0) \times 100 = 0$$

$$(28.28 - 8510.0 \times 1) +$$

$$1^\circ \text{ SF.1}$$

for half load:

$$\alpha = \frac{1}{2}$$

$$I'_S = \left(\frac{I_S}{2} \right)$$

$$\eta = \frac{\frac{1}{2} \times 15000 \times 0.8}{\frac{1}{2} \times 15000 \times 0.8 + 50 + 47.18}$$

$$= 0.984$$

$$= 98.4\%$$