ML Assignment 4

R Markdown

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see http://rmarkdown.rstudio.com.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

Note that the echo = FALSE parameter was added to the code chunk to prevent printing of the R code that generated the plot.

Loading the Data

```
rm(list = ls())
library(tidyverse)
## -- Attaching packages ----- tidyverse
1.3.0 --
## v ggplot2 3.3.2 v purrr 0.3.4
## v tibble 3.0.4 v dplyr 1.0.2
## v tidyr 1.1.2 v stringr 1.4.0
## v readr 1.4.0 v forcats 0.5.0
## Warning: package 'tibble' was built under R version 4.0.3
## Warning: package 'tidyr' was built under R version 4.0.3
## Warning: package 'readr' was built under R version 4.0.3
## Warning: package 'dplyr' was built under R version 4.0.3
## -- Conflicts -----
tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
#install.packages("factoextra")
library(factoextra)
## Warning: package 'factoextra' was built under R version 4.0.3
## Welcome! Want to learn more? See two factoextra-related books at
https://goo.gl/ve3WBa
```

```
library(ISLR)
set.seed(123)
DFUniver<-read.csv("Universities.csv")</pre>
colnames(DFUniver)
    [1] "College.Name"
                                     "State"
##
  [3] "Public..1...Private..2."
                                     "X..appli..rec.d"
## [5] "X..appl..accepted"
                                     "X..new.stud..enrolled"
## [7] "X..new.stud..from.top.10." "X..new.stud..from.top.25."
## [9] "X..FT.undergrad"
                                     "X..PT.undergrad"
                                     "out.of.state.tuition"
## [11] "in.state.tuition"
## [13] "room"
                                     "board"
## [15] "add..fees"
                                     "estim..book.costs"
## [17] "estim..personal.."
                                     "X..fac..w.PHD"
## [19] "stud..fac..ratio"
                                     "Graduation.rate"
#summary(DFUniver)
#Changing the column names to suitable ones.
DFUniver<-DFUniver%>%rename(
  Pub.Private=Public..1...Private..2.,
  ApplRec=X..appli..rec.d,
  ApplAccept=X..appl..accepted,
  NewStdEnr=X..new.stud..enrolled,
  Top10=X..new.stud..from.top.10.,
  Top25=X..new.stud..from.top.25.,
  FTUnderG=X..FT.undergrad,
  PTUnderG=X..PT.undergrad,
  InStateFee=in.state.tuition,
  OutStateFee=out.of.state.tuition,
  BookCost=estim..book.costs,
  PerCost=estim..personal..,
  PHD=X..fac..w.PHD,
  StFactRatio=stud..fac..ratio
)
colnames(DFUniver)
                                             "Pub.Private"
##
    [1] "College.Name"
                           "State"
                                                                "ApplRec"
  [5] "ApplAccept"
                           "NewStdEnr"
                                             "Top10"
                                                                "Top25"
## [9] "FTUnderG"
                           "PTUnderG"
                                                                "OutStateFee"
                                             "InStateFee"
## [13] "room"
                           "board"
                                             "add..fees"
                                                                "BookCost"
## [17] "PerCost"
                           "PHD"
                                             "StFactRatio"
"Graduation.rate"
```

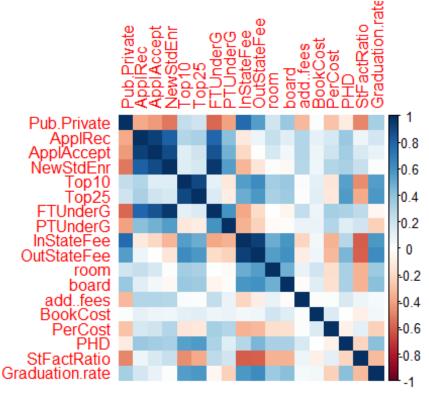
Removing missing records from the Dataset (Measurements)

```
#Total NULL fields in the data frame
count(DFUniver[!complete.cases(DFUniver),])
```

Finding the Data Summary and Measure of Dependence

```
#Summary Data
summary(DFUniver1)
##
    College.Name
                          State
                                           Pub.Private
                                                              ApplRec
    Length:471
##
                       Length:471
                                          Min.
                                                 :1.000
                                                           Min.
                                                                      77
                                                                 :
                                                           1st Qu.: 802
##
   Class :character
                       Class :character
                                          1st Qu.:1.000
##
   Mode :character
                       Mode :character
                                          Median :2.000
                                                           Median: 1646
##
                                                  :1.728
                                                                : 3147
                                          Mean
                                                           Mean
##
                                          3rd Qu.:2.000
                                                           3rd Qu.: 3862
##
                                                  :2.000
                                                                  :48094
                                          Max.
                                                           Max.
##
      ApplAccept
                        NewStdEnr
                                           Top10
                                                            Top25
                            : 27.0
##
   Min. :
               61.0
                      Min.
                                       Min.
                                              : 1.00
                                                        Min.
                                                               : 9.00
    1st Qu.: 635.5
##
                      1st Qu.: 264.0
                                       1st Qu.:15.00
                                                        1st Qu.: 40.00
   Median : 1227.0
                                       Median :23.00
                                                        Median : 54.00
##
                      Median : 443.0
##
          : 2063.0
   Mean
                      Mean
                             : 780.7
                                       Mean
                                              :28.01
                                                        Mean
                                                               : 55.65
##
    3rd Qu.: 2456.0
                      3rd Qu.: 896.5
                                       3rd Qu.:36.00
                                                        3rd Qu.: 69.00
##
   Max.
          :26330.0
                      Max.
                             :6392.0
                                       Max.
                                              :96.00
                                                        Max.
                                                               :100.00
##
       FTUnderG
                       PTUnderG
                                        InStateFee
                                                       OutStateFee
## Min.
          : 249
                                1.0
                                             : 608
                                                              : 1044
                    Min.
                           :
                                      Min.
                                                       Min.
##
   1st Qu.: 1018
                    1st Qu.:
                               81.5
                                      1st Qu.: 3650
                                                       1st Qu.: 7290
##
   Median : 1715
                    Median : 299.0
                                      Median: 9858
                                                       Median:10100
   Mean
         : 3563
                    Mean
                           : 797.5
                                      Mean
                                            : 9407
                                                       Mean
                                                            :10575
##
   3rd Qu.: 4056
                    3rd Qu.: 869.0
                                      3rd Ou.:13246
                                                       3rd Ou.:13286
##
   Max.
           :31643
                           :21836.0
                                      Max.
                                             :20100
                                                       Max.
                                                              :20100
                    Max.
                                    add..fees
##
         room
                       board
                                                       BookCost
PerCost
## Min.
           : 640
                                  Min.
                                            10.0
                                                   Min.
                                                             90.0
                                                                     Min.
                   Min.
                          : 531
                                         :
250
## 1st Qu.:1740
                   1st Qu.:1750
                                  1st Qu.: 137.5
                                                   1st Qu.: 500.0
                                                                     1st Qu.:
850
                                  Median : 280.0
## Median :2090
                   Median :2082
                                                    Median : 500.0
                                                                     Median
:1200
                                                   Mean
## Mean
           :2221
                          :2122
                                  Mean
                                         : 379.0
                                                           : 548.8
                                                                     Mean
                   Mean
:1312
## 3rd Qu.:2663
                   3rd Qu.:2420
                                                    3rd Qu.: 600.0
                                  3rd Qu.: 486.0
                                                                     3rd
Qu.:1600
## Max.
           :4816
                          :4541
                                  Max.
                                          :3247.0
                                                           :2340.0
                                                                     Max.
                   Max.
                                                    Max.
:6800
##
         PHD
                      StFactRatio
                                     Graduation.rate
## Min.
         : 8.00
                            : 2.90
                                     Min.
                                          : 15.00
                     Min.
##
   1st Qu.: 63.00
                     1st Qu.:11.30
                                     1st Qu.: 53.00
## Median : 76.00
                     Median :13.40
                                     Median : 66.00
## Mean : 73.21
                     Mean :13.96
                                     Mean : 65.56
```

```
3rd Ou.: 87.00
                     3rd Ou.:16.45
                                     3rd Ou.: 79.00
## Max.
           :103.00
                     Max.
                            :28.80
                                     Max.
                                             :118.00
#Finding the correlation between the data set
#Selecting numerical columns only
DFNumerical<-DFUniver1[,c(-1,-2)]</pre>
library(corrplot)
## Warning: package 'corrplot' was built under R version 4.0.3
## corrplot 0.84 loaded
corrplot(cor(DFNumerical), method = "color")
```



In the correlation

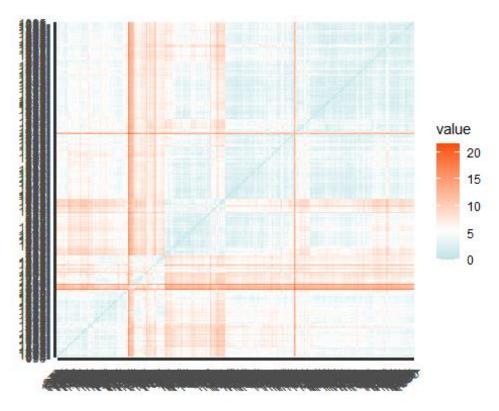
graph, Darker Blue(+1) and Dark Orange(-1) shows the higher correlated data. Using this data to understand any correlation among the column data.

Applying K-means clustering for Numeric Data

```
#Scaling the Data
DFNumerical<-scale(DFNumerical)

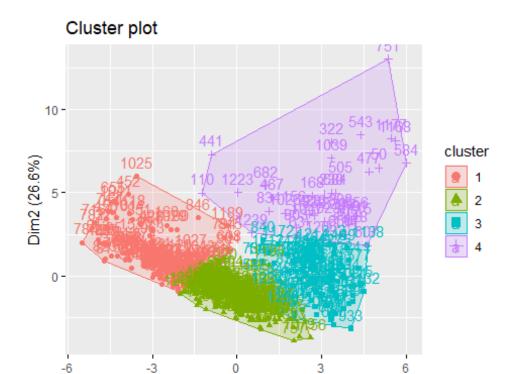
#Distance Between Observations
distance <- get_dist(DFNumerical)

fviz_dist(distance, gradient = list(low = "#00AFBB", mid = "white", high = "#FC4E07"))</pre>
```



```
#Finding Kmeans using cluster size =4
k4 <- kmeans(DFNumerical, centers = 4, nstart = 25) # k = 4, number of
restarts = 25
str(k4)
## List of 9
## $ cluster : Named int [1:471] 2 3 1 2 2 3 2 2 2 2 ...
   ... attr(*, "names")= chr [1:471] "1" "3" "10" "12" ...
                : num [1:4, 1:18] 0.575 0.61 -1.516 -1.416 0.117 ...
## $ centers
    ... attr(*, "dimnames")=List of 2
##
    .. ..$ : chr [1:4] "1" "2" "3" "4"
##
    ....$ : chr [1:18] "Pub.Private" "ApplRec" "ApplAccept" "NewStdEnr" ...
##
##
   $ totss
                 : num 8460
                 : num [1:4] 1231 1553 901 980
## $ withinss
## $ tot.withinss: num 4664
## $ betweenss : num 3796
## $ size
                 : int [1:4] 129 207 94 41
## $ iter
                : int 3
## $ ifault
                : int 0
  - attr(*, "class")= chr "kmeans"
# Visualize the output
k4$centers # output the centers
```

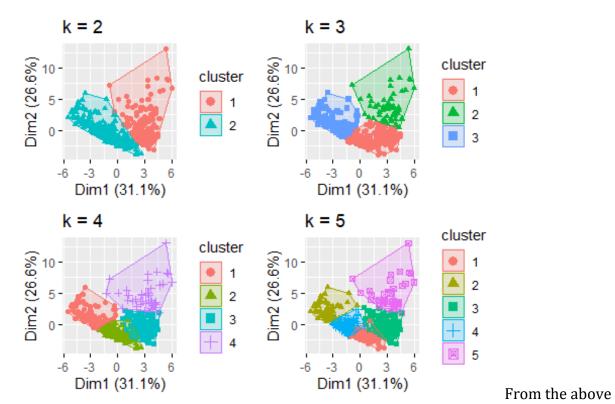
```
Pub.Private ApplRec ApplAccept NewStdEnr Top10
      0.5754205  0.11722831 -0.005168206 -0.1421639  1.0266549  0.9981228
## 1
      0.6102340 -0.51123189 -0.497187527 -0.5094276 -0.3760952 -0.4016802
## 2
## 3 -1.5157965 0.02245762 0.051502226 0.1968843 -0.6529467 -0.6177846
## 4 -1.4161661 2.16076910 2.408373353 2.5678908 0.1656150 0.3039442
                 PTUnderG InStateFee OutStateFee
##
      FTUnderG
                                                      room
                                                                 board
## 1 -0.2109459 -0.3189375 1.15189926 1.2186862 0.7642290 0.81696559
## 2 -0.5000169 -0.2631323 0.06788283 -0.1844498 -0.2837257 -0.13014031
## 3 0.2524856 0.2243992 -1.28898602 -1.0950488 -0.4342977 -0.80027141
## 4 2.6093137 1.8175077 -1.01175768 -0.3925568 0.0236506 -0.07863426
                                               PHD StFactRatio
##
      add..fees
                   BookCost
                               PerCost
Graduation.rate
## 1 -0.00526603 0.14578619 -0.38510673 0.84849798 -0.74794298
0.9053670
## 2 -0.30637755 -0.07869207 -0.07148593 -0.64092902 -0.03452639
0.1830111
## 3 0.43150476 -0.11321423 0.28883658 -0.06099844 0.90018939
0.7708289
## 4 0.57409815 0.19817016 0.91038335 0.70609563 0.46375131
0.1573444
#number of Universities in each cluster
k4$size
## [1] 129 207 94 41
# Visualize the cluster output
fviz cluster(k4, data =DFNumerical)
```



Dim1 (31.1%)

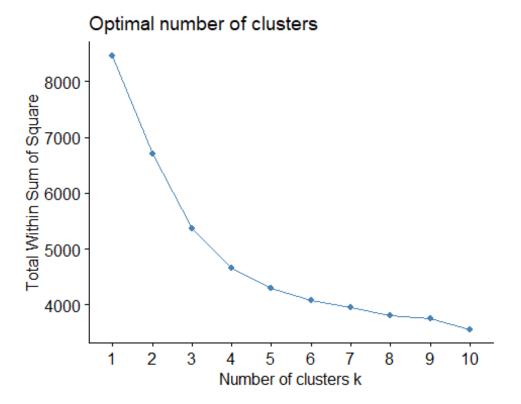
Comparision different cluster values

```
k2 <- kmeans(DFNumerical, centers = 2, nstart = 25)
k3 <- kmeans(DFNumerical, centers = 3, nstart = 25)
k4 <- kmeans(DFNumerical, centers = 4, nstart = 25)</pre>
k5 <- kmeans(DFNumerical, centers = 5, nstart = 25)
# plots to compare
p1 <- fviz_cluster(k2, geom = "point", data = DFNumerical) + ggtitle("k = 2")</pre>
p2 <- fviz_cluster(k3, geom = "point", data = DFNumerical) + ggtitle("k =</pre>
3")
p3 <- fviz_cluster(k4, geom = "point", data = DFNumerical) + ggtitle("k =
p4 <- fviz_cluster(k5, geom = "point", data = DFNumerical) + ggtitle("k =
5")
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
       combine
##
grid.arrange(p1, p2, p3, p4, nrow = 2)
```



comparison it seems that 3 clusters would be good.

set.seed(123)
#Finding optimal number of clusters - Elbow Method
fviz_nbclust(DFNumerical, kmeans, method = "wss")



#From the Elbow method it seems 3 or 4 clusters would be optimum. From previous cluster plotting we have seen that optimal cluster size would be 3.

Using the categorical measurements that were not used in the analysis (State and Private/Public) to characterize the different clusters.

```
#State wise values present in the cluster
table(DFUniver1$State, k3$cluster)
##
##
             2
                 3
          1
##
     ΑK
          2
             0
                 0
##
     AL
          3
             0
                 1
          4
##
     AR
             0
                 0
          0
             2
                 0
##
     ΑZ
##
     CA
          3
             1 11
          5
##
     CO
             0
                 1
          2
                 7
##
     CT
             1
##
     DC
          0
             0
                 4
          1
             1
                 0
##
     DE
##
          3
             1
                 4
     FL
##
     GA
          3
             1
                 3
##
             1
                 0
     ΗI
##
     IA 14
             1
                 3
##
          2
             0
                 0
     ID
             3
                 6
##
     ΙL
          6
                 7
##
     ΙN
          8
             0
```

```
##
     KS
         7
            0
               0
               2
##
     ΚY
         4
            0
##
         2
            1
               2
     LA
##
     MA
        7
            3 12
##
     MD
         1
            1
               1
##
     ME
         4
            0
               2
            2
##
     ΜI
        7
               4
##
        4
            2
                5
     MN
     MO 12
               2
##
            1
        4
            1
##
     MS
               0
##
        2
            0
               0
     ΜT
##
     NC 14
            6
               3
##
         5
               0
     ND
            0
##
     NE
        5
            1
               1
##
     NH
         4
            1
               1
         9
##
            1
               3
     NJ
     NM 2
##
            0
               0
##
     NY 15
            4 19
##
     OH 12
            4
               8
        5
##
     OK
            1
               0
##
               4
     OR
        1
            0
##
     PA 19
            3 20
##
     RΙ
        1
            1
               2
##
     SC
         6
            0
               3
##
     SD 4
            0
               0
##
     TN 11
            1
                3
     TX 14
            4
               2
##
##
     UT
        1
            1
               0
##
     VA
        8
            3
               4
##
        5
            1
               1
     VT
##
     WA
        0 0
               2
        4
            1
##
     WI
               4
         2
               0
##
     WV
            0
         1
            0
##
     WY
               0
#Merging the clusters to the original Dat frame
Clusters<-data.frame(k3$cluster)</pre>
Clusters<-Clusters%>%rename(clusters=k3.cluster)
UnivAnalysis<-cbind(DFUniver1, Clusters)</pre>
head(UnivAnalysis)
##
                              College.Name State Pub.Private ApplRec
ApplAccept
## 1
                 Alaska Pacific University
                                               ΑK
                                                             2
                                                                    193
146
## 3
           University of Alaska Southeast
                                               ΑK
                                                             1
                                                                    146
117
               Birmingham-Southern College
                                                             2
## 10
                                               ΑL
                                                                    805
588
## 12
                        Huntingdon College
                                               ΑL
                                                             2
                                                                    608
```

520 ## 22			Tallade	ga Co	llege AL		2 4414	
1500	University	, of Alah	ama at	Binmi	ngham AL		1 1797	
1260	oniversity	OI ALAD	allia at	DTLIIIT	ngnaii AL		1 1/9/	
##	NewStdEnr	Top10 To	p25 FTU	nderG	PTUnderG In	StateFee	OutStateFee	room
board ## 1	55	16	44	249	869	7560	7560	1620
2500	,,,	10	44	243	809	7300	7300	1020
## 3	89	4	24	492	1849	1742	5226	5 2514
2250	207	67	00	4276	207	11660	11.000	2050
## 10 2430	287	67	88	1376	207	11660	11666	2050
## 12	127	26	47	538	126	8080	8086	1380
2540								
## 22 1540	335	30	60	908	119	5666	5666	1424
## 26	938	24	35	6960	4698	2220	4446	1935
3240								
##					StFactRatio			
## 1	130	800	150		11.9		15 20	1
## 3 ## 10	34 120	500 400			9.5 14.0		39 72	1 3
## 10	100	500			11.4		7 Z 44	1
## 22	418	1000					46	1
## 26	291	750			6.7		33	1
#Cluster Summary Analysis								
ClusterStat<-								
<pre>UnivAnalysis%>%group_by(clusters)%>%summarise(Acceptance_rate=sum(ApplAccept)</pre>								
/sum(ApplRec),								
AvgOutStateTution=mean(OutStateFee), AvgInStateTution=mean(InStateFee),								
AvgGradRate=mean(Graduation.rate))								
<pre>## `summarise()` ungrouping output (override with `.groups` argument)</pre>								
ClusterStat								
<pre>## # A tibble: 3 x 5 ## clusters Acceptance_rate AvgOutStateTution AvgInStateTution AvgGradRate</pre>								
## <int> <dbl> <dbl> <dbl> <dbl></dbl></dbl></dbl></dbl></int>								
## 1	1		0.707		8279.		7249.	57.5
## 2	2		0.684		8107.		3179.	61.1
## 3	3		0.585		15229.		15173.	80.5

Use the categorical measurements that were not used in the analysis (State and Private/Public) to characterize the different clusters. Is there any relationship between the clusters and the categorical information?

```
PublicPrivate<-
UnivAnalysis%>%group by(clusters)%>%summarise(Acceptance rate=sum(ApplAccept)
/sum(ApplRec),
AvgOutStateTution=mean(OutStateFee), AvgInStateTution=mean(InStateFee),
AvgGradRate=mean(Graduation.rate), PublicUnivCount=sum(Pub.Private==1),
PrivateUnivCount=sum(Pub.Private==2))
## `summarise()` ungrouping output (override with `.groups` argument)
PublicPrivate
## # A tibble: 3 x 7
     clusters Acceptance_rate AvgOutStateTuti~ AvgInStateTution AvgGradRate
##
                                          <dbl>
                                                           <dbl>
        <int>
                        <dbl>
                                                                        <dbl>
## 1
            1
                        0.707
                                          8279.
                                                           7249.
                                                                         57.5
## 2
            2
                        0.684
                                          8107.
                                                           3179.
                                                                        61.1
## 3
            3
                        0.585
                                         15229.
                                                                        80.5
                                                          15173.
## # ... with 2 more variables: PublicUnivCount <int>, PrivateUnivCount <int>
```

Consider Tufts University, which is missing some information. Compute the Euclidean distance of this record from each of the clusters that you found above (using only the measurements that you have). Which cluster is it closest to? Impute the missing values for Tufts by taking the average of the cluster on those measurements.

```
# Initial Dataframe DFUniver with no imputation
#Tuft University Data
Tuft<-filter(DFUniver, College.Name=="Tufts University")</pre>
Tuft
##
         College.Name State Pub.Private ApplRec ApplAccept NewStdEnr Top10
Top25
## 1 Tufts University
                         MΑ
                                       2
                                            7614
                                                       3605
                                                                 1205
                                                                         60
90
     FTUnderG PTUnderG InStateFee OutStateFee room board add..fees BookCost
##
                                         19701 3038 2930
## 1
         4598
                    NA
                            19701
                                                                503
                                                                         600
     PerCost PHD StFactRatio Graduation.rate
##
## 1
         928 99
                        10.3
                                           92
#Not Present in the imputed Data Frame
filter(DFUniver1, College.Name=="Tufts University")
## [1] College.Name
                                         Pub.Private
                                                         ApplRec
                        State
## [5] ApplAccept
                        NewStdEnr
                                         Top10
                                                         Top25
## [9] FTUnderG
                        PTUnderG
                                         InStateFee
                                                         OutStateFee
## [13] room
                        board
                                         add..fees
                                                         BookCost
## [17] PerCost
                        PHD
                                         StFactRatio
                                                         Graduation.rate
## <0 rows> (or 0-length row.names)
#set.seed(123)
#kmeans clustering, using manhattan distance
```

```
#k = kcca(DFNumerical, k=3, kccaFamily("kmedians"))
#k

#Apply the predict() function
#clusters_index <- predict(k)
#image(k)
#points(DFNumerical, col=clusters_index, pch=19, cex=0.3)</pre>
```