Assignment-5 Hierarchical Clustering

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R Markdown

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When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

Hierarchical clustering

```
rm(list = ls())
library(caret)

## Loading required package: lattice

## Loading required package: ggplot2

library(ISLR)
library(factoextra)
```

Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

```
library(cluster)
library(NbClust)

#Loadinng the data
DFCereals<-read.csv("Cereals.csv")

#EDA of the data set
summary(DFCereals)</pre>
```

```
##
                            {\tt mfr}
        name
                                                type
                                                                   calories
##
    Length:77
                        Length:77
                                            Length:77
                                                                     : 50.0
##
    Class :character
                        Class : character
                                            Class :character
                                                                1st Qu.:100.0
    Mode :character
                        Mode :character
                                            Mode :character
                                                                Median :110.0
##
                                                                Mean
                                                                      :106.9
##
                                                                3rd Qu.:110.0
##
                                                                Max.
                                                                      :160.0
##
##
       protein
                          fat
                                          sodium
                                                          fiber
```

```
Min.
          :1.000
                   Min.
                          :0.000
                                   Min. : 0.0
                                                  Min.
                                                         : 0.000
##
   1st Qu.:2.000
                   1st Qu.:0.000
                                   1st Qu.:130.0
                                                  1st Qu.: 1.000
   Median :3.000
                                                  Median : 2.000
                   Median :1.000
                                   Median :180.0
         :2.545
                                        :159.7
##
  Mean
                   Mean
                         :1.013
                                   Mean
                                                  Mean
                                                        : 2.152
##
   3rd Qu.:3.000
                   3rd Qu.:2.000
                                   3rd Qu.:210.0
                                                  3rd Qu.: 3.000
##
   Max.
          :6.000
                  Max.
                          :5.000
                                   Max.
                                         :320.0
                                                         :14.000
                                                  Max.
##
##
       carbo
                      sugars
                                       potass
                                                      vitamins
##
   Min.
          : 5.0
                  Min.
                         : 0.000
                                   Min.
                                         : 15.00
                                                   Min.
                                                          : 0.00
   1st Qu.:12.0
                  1st Qu.: 3.000
                                   1st Qu.: 42.50
                                                   1st Qu.: 25.00
##
   Median:14.5
                  Median : 7.000
                                   Median : 90.00
                                                   Median : 25.00
                         : 7.026
                                        : 98.67
                                                         : 28.25
   Mean
         :14.8
                  Mean
                                   Mean
                                                   Mean
##
                  3rd Qu.:11.000
                                   3rd Qu.:120.00
                                                   3rd Qu.: 25.00
##
   3rd Qu.:17.0
##
   Max.
          :23.0
                  Max.
                         :15.000
                                         :330.00
                                                   Max.
                                                          :100.00
                                   Max.
##
   NA's
         :1
                  NA's
                         :1
                                   NA's
                                        :2
##
       shelf
                       weight
                                       cups
                                                      rating
##
          :1.000
                          :0.50
                                         :0.250
                                                        :18.04
   Min.
                  Min.
                                  Min.
                                                 Min.
   1st Qu.:1.000
                   1st Qu.:1.00
                                  1st Qu.:0.670
                                                 1st Qu.:33.17
##
  Median :2.000
                  Median:1.00
                                 Median :0.750
                                                 Median :40.40
## Mean
         :2.208
                   Mean :1.03
                                  Mean :0.821
                                                 Mean
                                                        :42.67
##
   3rd Qu.:3.000
                   3rd Qu.:1.00
                                  3rd Qu.:1.000
                                                 3rd Qu.:50.83
##
  Max.
          :3.000
                   Max.
                          :1.50
                                  Max.
                                        :1.500
                                                 Max.
                                                        :93.70
##
colMeans(is.na(DFCereals))
##
                                     calories
                                                protein
        name
                    mfr
                              type
                                                               fat
                                                                       sodium
##
       fiber
                  carbo
                            sugars
                                       potass
                                                vitamins
                                                             shelf
                                                                       weight
## 0.00000000 0.01298701 0.01298701 0.02597403 0.00000000 0.00000000 0.00000000
##
                 rating
        cups
## 0.0000000 0.0000000
#Median imputation of missing data
preProcess_1<-preProcess(DFCereals, method = c("medianImpute"))</pre>
ImputedDF<-predict(preProcess_1, DFCereals)</pre>
#No more NULL values presnt
colMeans(is.na(ImputedDF))
##
                        type calories protein
                                                    fat
                                                         sodium
                                                                   fiber
      name
                mfr
##
         0
                  0
                           0
                                    0
                                             0
                                                     0
                                                              0
                                                                       0
##
      carbo
             sugars
                      potass vitamins
                                         shelf
                                                 weight
                                                           cups
                                                                  rating
##
         0
                  0
                                             0
                                                     0
                                                              0
#Scaling the DF
ImputedDF<-subset(ImputedDF, select= -c(1,2,3))</pre>
ImputedDF<-scale(ImputedDF)</pre>
# Compute with agnes and with different linkage methods
hc_single <- agnes(ImputedDF, method = "single")</pre>
```

```
hc_complete<-agnes(ImputedDF, method="complete")
hc_average <- agnes(ImputedDF, method = "average")
hc_ward <- agnes(ImputedDF, method = "ward")

# Compare Agglomerative coefficients
print(hc_single$ac)

## [1] 0.6029274

print(hc_complete$ac)

## [1] 0.8353216

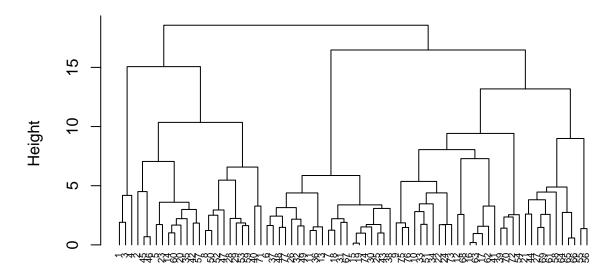
print(hc_average$ac)

## [1] 0.7777555

print(hc_ward$ac)

## [1] 0.9027089

# The approach used by Ward describes the best clustering mechanism of the four approaches tested #visualize the dendrogram pltree(hc_ward, cex = 0.6, hang = -1, main = "Dendrogram of agnes")</pre>
```

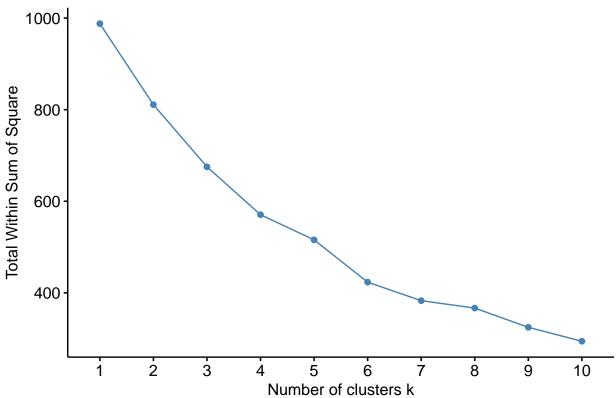


ImputedDF agnes (*, "ward")

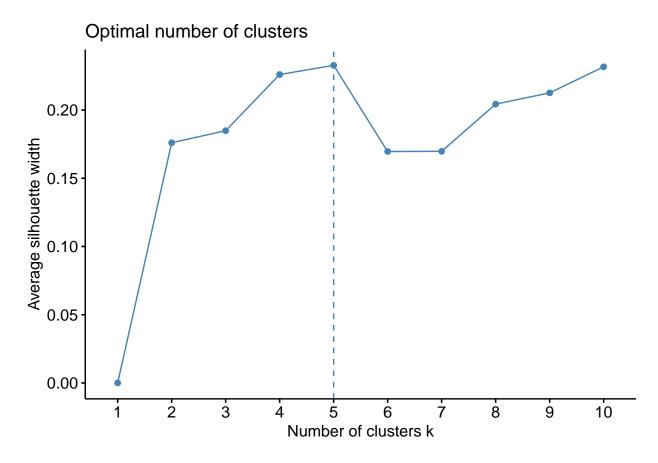
Q> Comment on differences between hierarchical Clustering and K-means

```
set.seed(123)
#Finding optimal number of clusters - Elbow Method
fviz_nbclust(ImputedDF, kmeans, method = "wss")
```





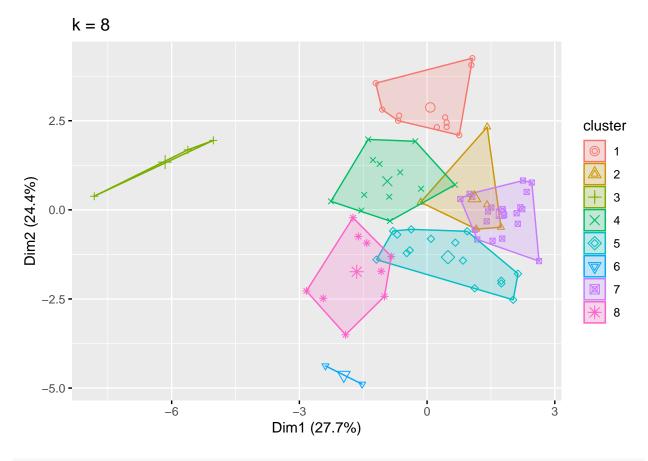
#Determining Optimal Cluster by Average Silhouette Method
fviz_nbclust(ImputedDF, kmeans, method = "silhouette")



```
#Silhouette method shows that 8 numbers of clusters would be optimum.

k8 <- kmeans(ImputedDF, centers = 8, nstart = 25)

fviz_cluster(k8, geom = "point", data = ImputedDF) + ggtitle("k = 8")
```



```
# slicing the dendogram on the longest path, 8 is the optimal level of clusters.
# Cut tree into 8 groups
sub_grp <- cutree(hc_ward, k = 8)
C2 <- as.data.frame(cbind(ImputedDF,sub_grp))
head(C2)</pre>
```

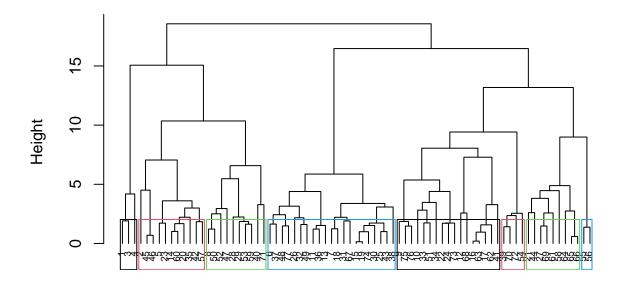
```
##
                                                       fiber
       calories
                   protein
                                  fat
                                           sodium
                                                                  carbo
## 1 -1.8929836 1.3286071 -0.01290349 -0.3539844
                                                  3.29284661 -2.5243405
## 2 0.6732089 0.4151897 3.96137277 -1.7257708 -0.06375361 -1.7514808
                1.3286071 -0.01290349
                                      1.1967306
                                                  2.87327158 -2.0091007
## 3 -1.8929836
## 4 -2.9194605
                1.3286071 -1.00647256 -0.2346986
                                                  4.97114672 -1.7514808
## 5 0.1599704 -0.4982277
                           0.98066557
                                       0.4810160 -0.48332864 -0.2057614
## 6 0.1599704 -0.4982277 0.98066557
                                       0.2424445 -0.27354112 -1.1074310
##
         sugars
                   potass
                            vitamins
                                          shelf
                                                    weight
                                                                 cups
                                                                          rating
## 1 -0.2358694
                2.6126578 -0.1453172
                                      0.9515734 -0.1967771 -2.1100340 1.8321876
## 2 0.2239266
                0.5260824 -1.2642598 0.9515734 -0.1967771 0.7690100 -0.6180571
                                      0.9515734 -0.1967771 -2.1100340 1.1930986
## 3 -0.4657674
                3.1882648 -0.1453172
## 4 -1.6152574 3.3321665 -0.1453172 0.9515734 -0.1967771 -1.3795303 3.6333849
     0.2239266 -0.1214755 -0.1453172 0.9515734 -0.1967771 -0.3052601 -0.5894990
## 6 0.6837226 -0.4092790 -0.1453172 -1.4507595 -0.1967771 -0.3052601 -0.9365625
##
     sub_grp
## 1
          1
## 2
           2
## 3
           1
## 4
           1
          2
## 5
```

```
## 6 3
```

```
# Number of members in each cluster
table(sub_grp)

## sub_grp
## 1 2 3 4 5 6 7 8
## 3 11 21 10 17 9 4 2

#plot dendrogram
pltree(hc_ward, cex = 0.6, hang = -1, main = "Dendrogram of agnes")
rect.hclust(hc_ward, k = 8, border = 1:4)
```

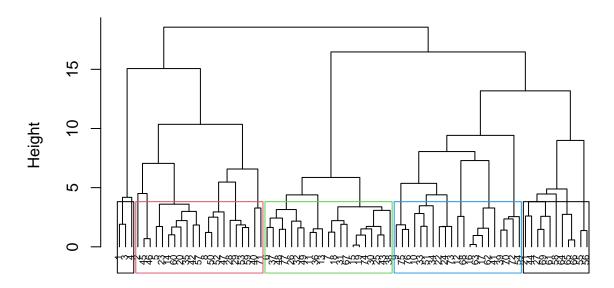


ImputedDF agnes (*, "ward")

```
#From the Dendrogram it seems that clustering at level of 5 would have been optimum.

pltree(hc_ward, cex = 0.6, hang = -1, main = "Dendrogram of agnes")

rect.hclust(hc_ward, k = 5, border = 1:4)
```



ImputedDF agnes (*, "ward")

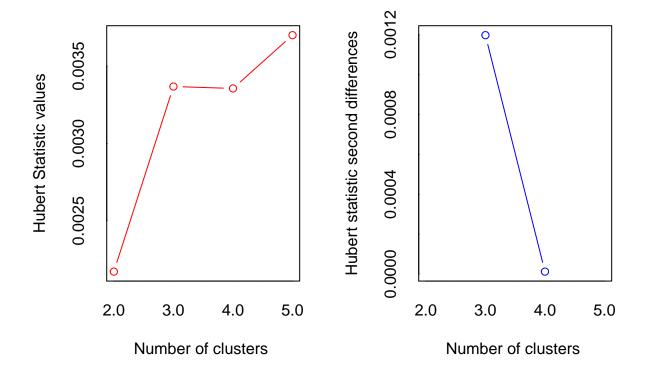
```
#Thus, Hierarchical clustering would be better approach than kmeans to find the suitable no. of cluster

# Gap statistic
set.seed(42)
fviz_nbclust(ImputedDF, kmeans,
    nstart = 25,
    method = "gap_stat",
    nboot = 500
) + # reduce it for lower computation time (but less precise results)
    labs(subtitle = "Gap statistic method")
```

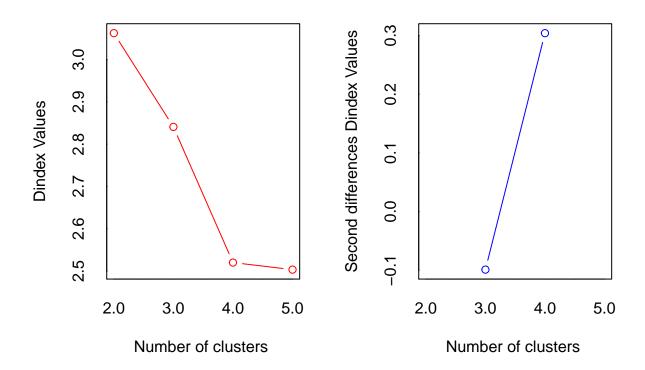
Optimal number of clusters Gap statistic method 0.55 0.50 Gap statistic (k) 0.45 0.40 0.35 2 ż 4 5 6 7 8 9 10

#The optimal number of clusters is the one that maximizes the gap statistic. This method suggests only
#Three methods do not necessarily lead to the same result. Here, all 3 approaches suggest a different n
#A fourth alternative is to use the NbClust() function, which provides 30 indices for choosing the best
nbclust_out <- NbClust(
 data = ImputedDF,
 distance = "euclidean",
 min.nc = 2, # minimum number of clusters
 max.nc = 5, # maximum number of clusters
 method = "kmeans" # one of: "ward.D", "ward.D2", "single", "complete", "average", "mcquitty", "median")</pre>

Number of clusters k



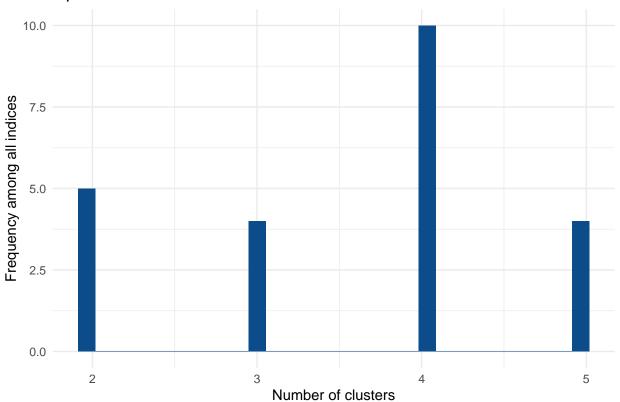
```
## *** : The Hubert index is a graphical method of determining the number of clusters.
## In the plot of Hubert index, we seek a significant knee that corresponds to a
## significant increase of the value of the measure i.e the significant peak in Hubert
## index second differences plot.
##
```



```
*** : The D index is a graphical method of determining the number of clusters.
                In the plot of D index, we seek a significant knee (the significant peak in Dindex
##
                second differences plot) that corresponds to a significant increase of the value of
##
##
##
## * Among all indices:
## * 5 proposed 2 as the best number of clusters
\#\# * 4 proposed 3 as the best number of clusters
## * 10 proposed 4 as the best number of clusters
## * 4 proposed 5 as the best number of clusters
##
##
                   **** Conclusion ****
##
\#\# * According to the majority rule, the best number of clusters is 4
##
##
# create a dataframe of the optimal number of clusters
nbclust_plot <- data.frame(clusters = nbclust_out$Best.nc[1, ])</pre>
# select only indices which select between 2 and 5 clusters
nbclust_plot <- subset(nbclust_plot, clusters >= 2 & clusters <= 5)</pre>
# create plot
```

```
ggplot(nbclust_plot) +
  aes(x = clusters) +
  geom_histogram(bins = 30L, fill = "#0c4c8a") +
  labs(x = "Number of clusters", y = "Frequency among all indices", title = "Optimal number of clusters
  theme_minimal()
```

Optimal number of clusters



#Based on all 30 indices, the best number of clusters is 5 clusters.
I would choose 5 clusters.

Q> Comment on the structure of the clusters and on their stability.

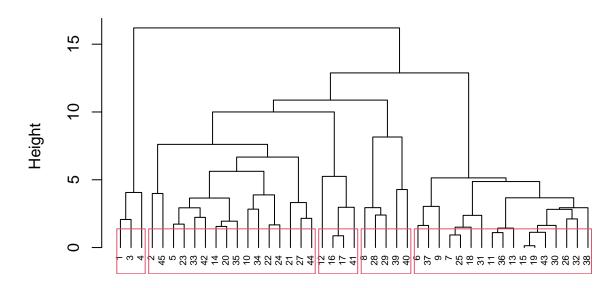
```
library(caret)
DF<-ImputedDF

# Cluster partition
trainDF<-DF[1:45,] # Partition A
testDF<-DF[46:77,] # Partition B
trainDF <- scale(trainDF)
testDF<-scale(testDF)

# The approach used earlier describes that ward is the best clustering mechanism
hc_train <- agnes(trainDF, method = "ward")

#visualize the dendrogram</pre>
```

```
pltree(hc_train, cex = 0.6, hang = -1, main = "Dendrogram of agnes")
rect.hclust(hc_train, k = 5)
```



trainDF agnes (*, "ward")

```
CWcut <- cutree(hc_train, k = 5)
CWtotal <- as.data.frame( cbind(trainDF,CWcut))
head(CWtotal)</pre>
```

```
##
                  protein
                                         sodium
                                                      fiber
      calories
                                 fat
                                                                  carbo
## 1 -2.2902757 1.3899279 -0.1190407 -0.5218048 2.74720044 -2.27995823
## 2 0.7589079 0.4964028 3.4521808 -2.0963468 -0.07044104 -1.51239124
## 3 -2.2902757 1.3899279 -0.1190407
                                     1.2581124 2.39499525 -1.76824691
## 4 -3.5099491 1.3899279 -1.0118461 -0.3848881 4.15602117 -1.51239124
## 5 0.1490712 -0.3971223 0.7737647 0.4366121 -0.42264622 0.02274273
    0.1490712 -0.3971223 0.7737647 0.1627787 -0.24654363 -0.87275209
##
                                            shelf
                                                      weight
         sugars
                     potass
                              vitamins
## 1 -0.44514757
                 2.45188569 -0.1330313 0.9770643 -0.3068967 -1.8861150
## 2 0.05564345 0.51266701 -1.6296338 0.9770643 -0.3068967 0.7128963
## 3 -0.69554308
                 2.98684257 -0.1330313 0.9770643 -0.3068967 -1.8861150
                3.12058179 -0.1330313 0.9770643 -0.3068967 -1.2266644
## 4 -1.94752061
## 5 0.05564345 -0.08915948 -0.1330313 0.9770643 -0.3068967 -0.2568840
## 6 0.55643446 -0.35663792 -0.1330313 -1.6092824 -0.3068967 -0.2568840
##
        rating CWcut
## 1 1.9353757
                   1
## 2 -0.4509040
## 3 1.3129704
```

```
## 4 3.6895518
## 5 -0.4230914
## 6 -0.7610947
CWclust1 <- CWtotal[CWtotal$CWcut==1,]</pre>
colMeans(CWclust1)
## calories
                           fat
                                  sodium
                                            fiber
                                                      carbo
              protein
                                                               sugars
## -2.6968335 1.3899279 -0.4166425 0.1171398 3.0994056 -1.8535321 -1.0294038
     potass vitamins
                         shelf
                                  weight
                                             cups
                                                     rating
                                                                CWcut
## 2.8531034 -0.1330313 0.9770643 -0.3068967 -1.6662981 2.3126327 1.0000000
CWclust2 <- CWtotal[CWtotal$CWcut==2,]</pre>
colMeans(CWclust2)
                                    sodium
                                                 fiber
     calories
               protein
                             fat
## 0.03472681 0.44055751 0.27156164 -0.62021364 0.01761026 0.15067056
      sugars
                 potass vitamins
                                      shelf
                                                weight
rating
                 CWcut
## 0.40553275 2.00000000
CWclust3 <- CWtotal[CWtotal$CWcut==3,]</pre>
colMeans(CWclust3)
              protein
                                  sodium
                                            fiber
   calories
                           fat
                                                      carbo
                                                               sugars
## 0.1490712 -0.8701650 -0.1190407 0.1144552 -0.5262360 -0.3685659 0.8952049
     potass vitamins shelf
                                 weight
                                         cups
                                                    rating
                                                               CWcut
## -0.6359169 -0.1330313 -0.7725232 -0.3068967 0.2861930 -0.8097474 3.0000000
CWclust4 <- CWtotal[CWtotal$CWcut==4,]</pre>
colMeans(CWclust4)
##
    calories
                                     sodium
                                                 fiber
               protein
                             fat
## 1.00284261 0.31769781 0.05952036 0.29969545 0.28176415 0.58562518
               potass vitamins
                                      shelf
                                                weight
      sugars
## 0.30603895 0.43242348 1.66289165 0.97706430 2.45517366 -0.18705985
      rating
                  CWcut
## -0.14518909 4.00000000
CWclust5 <- CWtotal[CWtotal$CWcut==5,]</pre>
colMeans(CWclust5)
##
     calories
                 protein
                                fat
                                         sodium
                                                     fiber
                                                                 carbo
vitamins
                                          shelf
       sugars
                  potass
                                                    weight
## -1.384130721 -0.607398956 -0.133031332 -1.285989048 -0.306896708 1.440231546
       rating
## 0.266307344 5.000000000
```

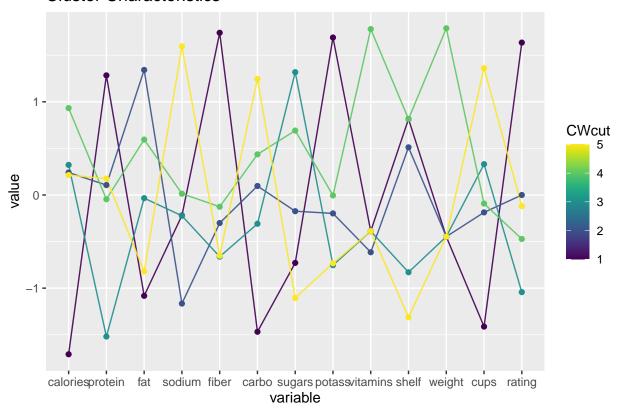
```
CWmeans1 <- rbind(colMeans(CWclust1),colMeans(CWclust2),colMeans(CWclust3),colMeans(CWclust4) ,colMeans
head(CWmeans1)</pre>
```

```
##
         calories
                  protein
                               fat
                                     sodium
                                               fiber
                                                        carbo
## [1,] -2.696833500 1.3899279 -0.41664251
                                  0.1171398
                                           3.09940562 -1.8535321
      0.034726813
                0.4405575 0.27156164 -0.6202136 0.01761026
## [3,]
      0.149071198 -0.8701650 -0.11904072
                                  0.1144552 -0.52623598 -0.3685659
## [4,]
      0.5856252
## [5,] -0.003387982   0.4964028 -0.34224206   1.5319458 -0.51069752
                                                     1.6218406
                 potass
                        vitamins
                                   shelf
                                           weight
         sugars
                                                     cups
## [3,]
      0.8952049 -0.6359169 -0.1330313 -0.7725232 -0.3068967 0.2861930
## [4,]
      0.3060390 0.4324235 1.6628917 0.9770643 2.4551737 -0.1870599
## [5,] -1.3841307 -0.6073990 -0.1330313 -1.2859890 -0.3068967 1.4402315
##
         rating CWcut
## [1,]
      2.3126327
## [2,] 0.4055327
                  2
                  3
## [3,] -0.8097474
## [4,] -0.1451891
                  4
## [5,] 0.2663073
                  5
```

Q> The elementary public schools would like to choose a set of cereals to include in their daily cafeterias. Every day a different cereal is offered, but all cereals should support a healthy diet. For this goal, you are requested to find a cluster of "healthy cereals." Should the data be normalized? If not, how should they be used in the cluster analysis?

```
#install.packages("hrbrthemes")
library(GGally)
## Registered S3 method overwritten by 'GGally':
##
     method from
     +.gg
            ggplot2
library(ggplot2)
library(hrbrthemes)
## NOTE: Either Arial Narrow or Roboto Condensed fonts are required to use these themes.
         Please use hrbrthemes::import_roboto_condensed() to install Roboto Condensed and
##
##
         if Arial Narrow is not on your system, please see https://bit.ly/arialnarrow
library(viridis)
## Loading required package: viridisLite
```

Cluster Characteristics



Based on the characteristics of the cluster, it is clear that Cluster 1 is the strongest with low cal ###In general, when we use the distance metric algorithm the data should be normalized, because the data

Q> How do you compare hierarchical clustering and k-means? What are they main advantages of hierarchical clustering compared to k-means?

Ans: Clustering is a subjective statistical analysis and there can be more than one appropriate algorithm, depending on the dataset at hand or the type of problem to be solved. So choosing between k-means and hierarchical clustering is not always easy. If the cluster size is known or if we know that there is a specific number of clusters in our dataset (for example if we would like to distinguish diseased and healthy patients depending on some characteristics but we do not know in which group patients belong to), we should probably opt for the k-means clustering as this technique is used when the number of groups is specified in advance. If the number of groups or clusters in the dataset is unknown (for instance in marketing when trying to distinguish clients without any prior belief on the number of different types of customers), then we should probably opt for the hierarchical clustering to determine in how many clusters the data should be divided.