

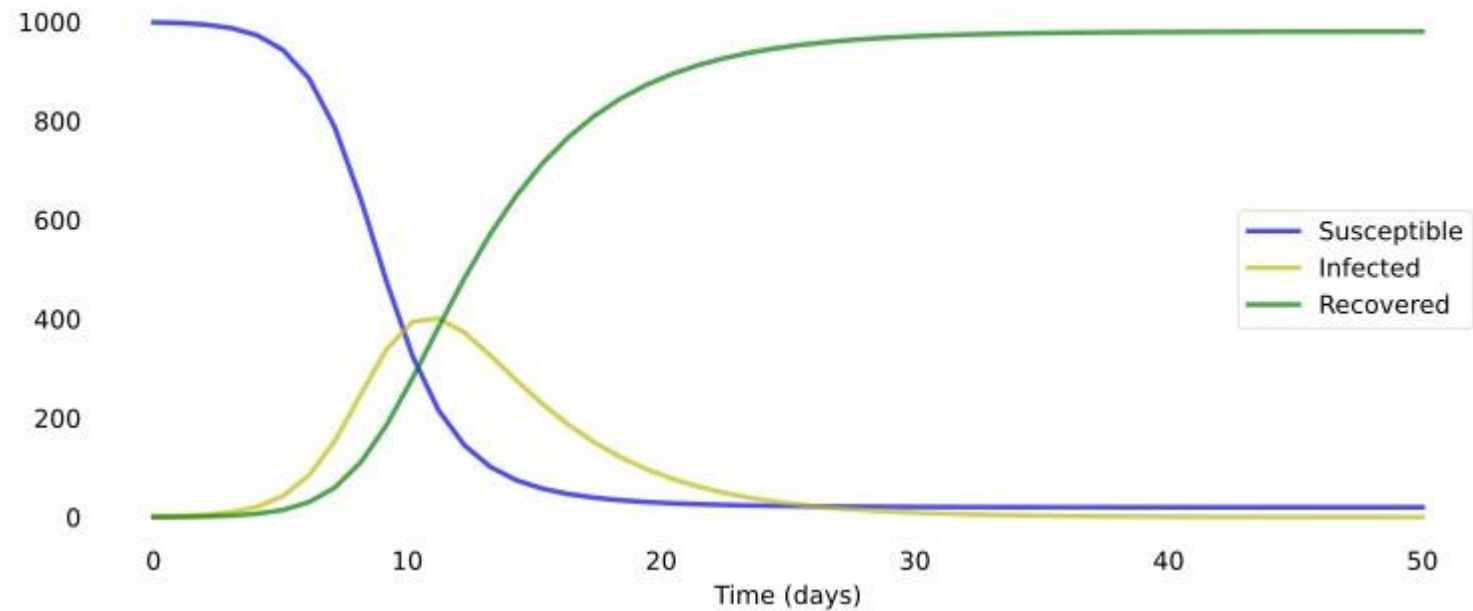
**Phân tích dữ liệu thông minh**

## **Infectious Disease Modelling**

TS. Nguyễn Tiến Huy

[ntienhuy@fit.hcmus.edu.vn](mailto:ntienhuy@fit.hcmus.edu.vn)

# Infectious Disease Modelling - SIR



# SIR model

- **N**: total population
- **S(t)**: number of people susceptible on day t
- **I(t)**: number of people infected on day t
- **R(t)**: number of people recovered on day t
- **$\beta$** : expected amount of people an infected person infects per day
- **D**: number of days an infected person has and can spread the disease
- **$\gamma$** : the proportion of infected recovering per day ( $\gamma = 1/D$ )
- **$R_0$** : the total number of people an infected person infects ( $R_0 = \beta / \gamma$ )

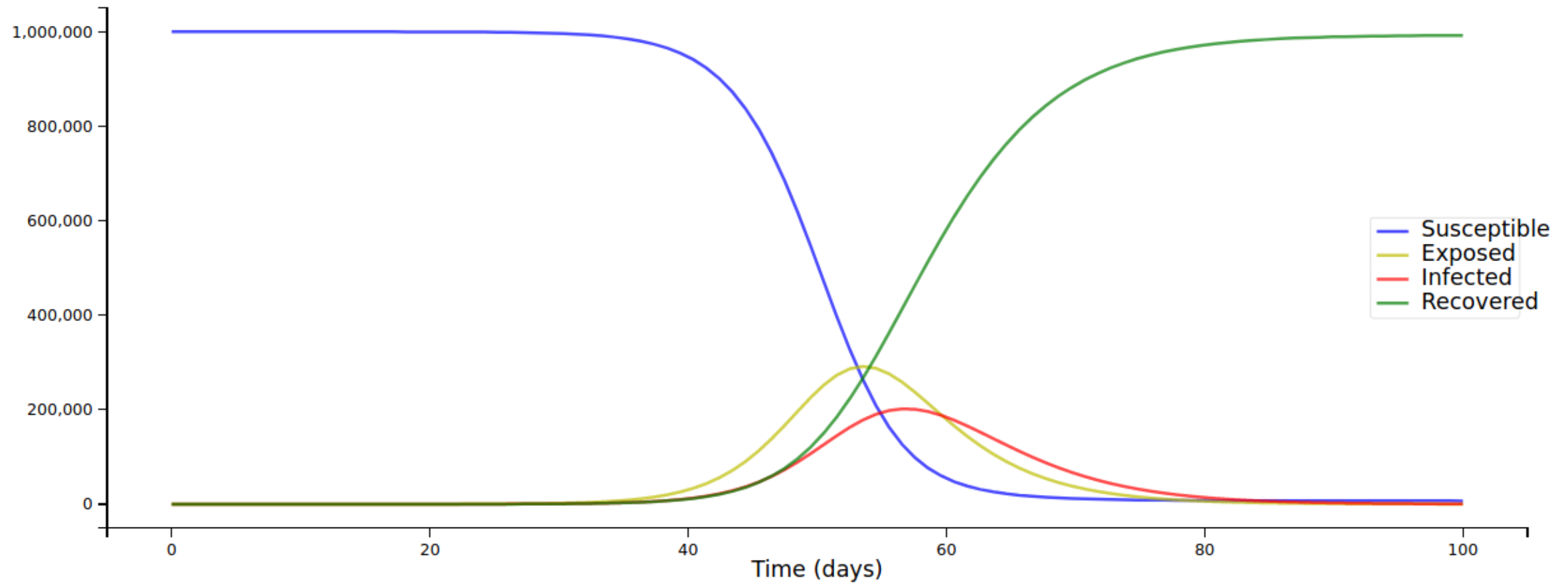
# SIR model

- $N = 100$
- $\beta=1$ ,  $D=7$  and  $\gamma=1/7$
- Let's say that on day  $t$ , 60 people are infected (so  $I(t)=60$ ), and 30 people are still susceptible (so  $S(t)=30$  and  $R(t)=100-60-30=10$ ).
- Now, how do  $S(t)$  and  $I(t)$  and  $R(t)$  change to the next day?
  - Change of  $S(t)$  to the next day  $S'(t) = -\beta \cdot I(t) \cdot S(t) / N$ .
  - $I'(t) = \beta \cdot I(t) \cdot S(t) / N - \gamma \cdot I(t)$
  - $R'(t) = \gamma \cdot I(t)$

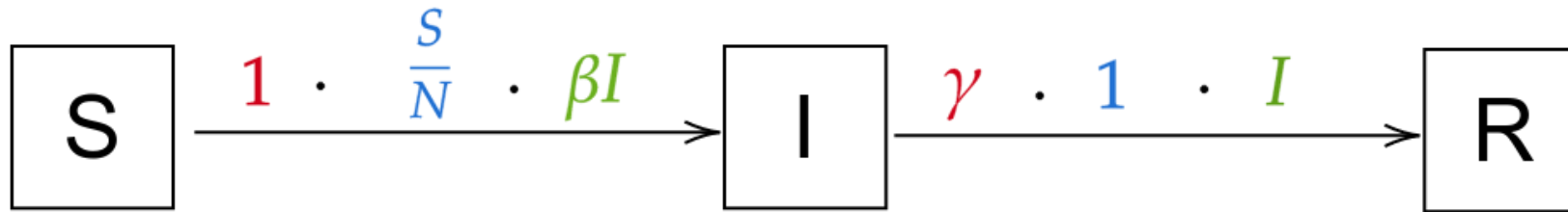
# SIR model - *ordinary differential equations*

$$\begin{aligned}\frac{dS}{dt} &= -\beta \cdot I \cdot \frac{S}{N} \\ \frac{dI}{dt} &= \beta \cdot I \cdot \frac{S}{N} - \gamma \cdot I \\ \frac{dR}{dt} &= \gamma \cdot I\end{aligned}$$

# Beyond the basic SIR



# Models as State Transitions



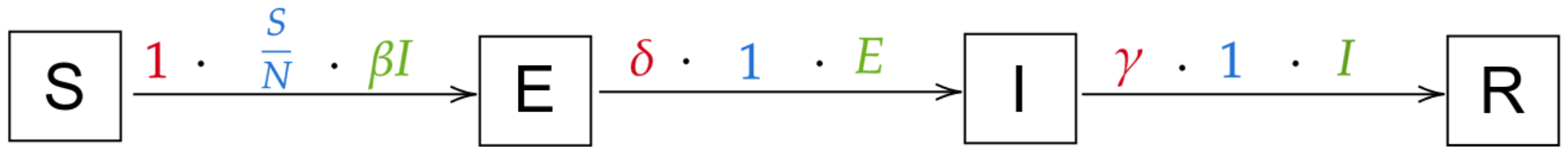
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$$\frac{dS}{dt} = -\beta \cdot I \cdot \frac{S}{N}$$

$$\frac{dI}{dt} = \beta \cdot I \cdot \frac{S}{N} - \gamma \cdot I$$

$$\frac{dR}{dt} = \gamma \cdot I$$

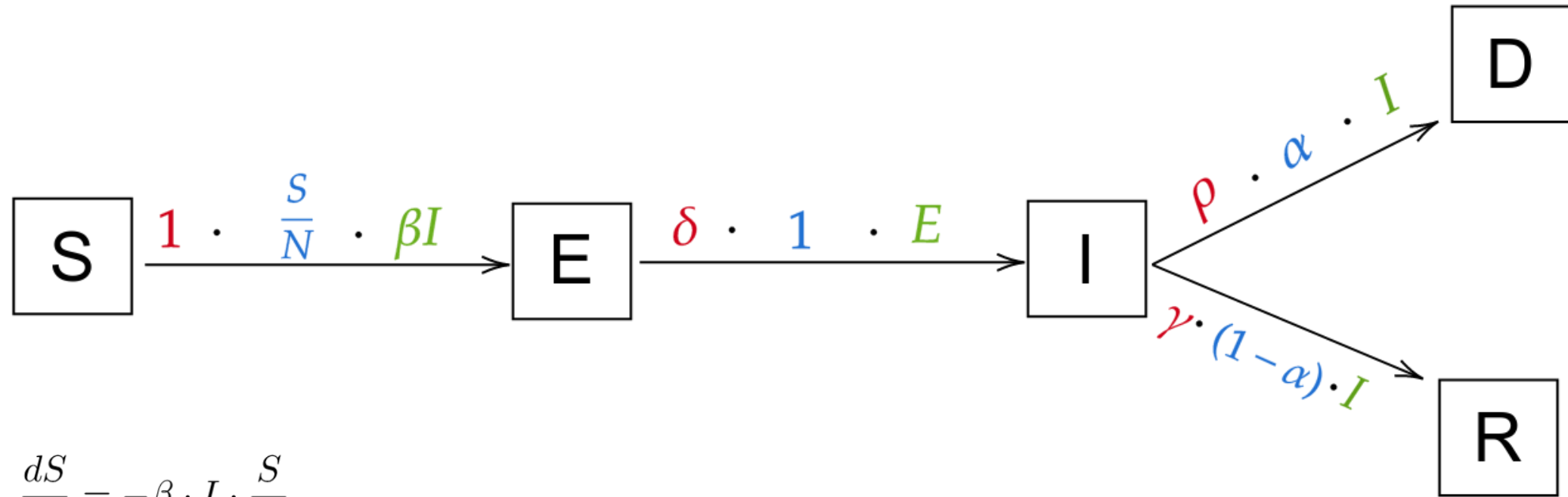
*rate · probability · population*



$$\begin{aligned}\frac{dS}{dt} &= -\beta \cdot I \cdot \frac{S}{N} \\ \frac{dE}{dt} &= \beta \cdot I \cdot \frac{S}{N} - \delta \cdot E \\ \frac{dI}{dt} &= \delta \cdot E - \gamma \cdot I \\ \frac{dR}{dt} &= \gamma \cdot I\end{aligned}$$



# Deriving the Dead-Compartment



$$\frac{dS}{dt} = -\beta \cdot I \cdot \frac{S}{N}$$

$$\frac{dE}{dt} = \beta \cdot I \cdot \frac{S}{N} - \delta \cdot E$$

$$\frac{dI}{dt} = \delta \cdot E - (1 - \alpha) \cdot \gamma \cdot I - \alpha \cdot \rho \cdot I$$

$$\frac{dR}{dt} = (1 - \alpha) \cdot \gamma \cdot I$$

$$\frac{dD}{dt} = \alpha \cdot \rho \cdot I$$

# Time-Dependent Variables

- On day  $L$ , a strict “lockdown” is enforced => pushing  $R_0$  to 0.9

```
def R_0(t):  
    return 5.0 if t < L else 0.9
```

```
def beta(t):  
    return R_0(t) * gamma
```

- <https://colab.research.google.com/drive/16uL8ASmEnBxUqmQX4-aSfNPIR0Rp8-Eh?usp=sharing>

Cảm ơn đã theo dõi!