

NCERT Discrete - 11.5.9.2

EE23BTECH11201 - Abburi Tanusha*

Question: The sum of three numbers in an arithmetic progression (AP) is 24 and the product of those three numbers is 440, find the values of the three numbers.

Solution: The following information is provided in the question:

Parameter	Value	Description
d	3	common difference
x(n)	$(x(0) + n \cdot d) u(n)$	$(n + 1)$ th term
y(n)	24	sum of $(n + 1)$ terms
p(n)	440	product of $(n + 1)$ terms

TABLE 0
PARAMETERS

Let the three numbers in the arithmetic progression be denoted as $x(0)$, $x(1)$, and $x(2)$.

From Table 0

$$y(2) = x(0) + x(1) + x(2) \quad (1)$$

$$= (x(1) - d) + x(1) + (x(1) + d) \quad (2)$$

$$\Rightarrow 3x(1) = 24 \quad (3)$$

$$x(1) = 8 \quad (4)$$

$$p(2) = x(0) \cdot x(1) \cdot x(2) \quad (5)$$

$$= 440 \quad (6)$$

$$(8) \cdot (8 - d) \cdot (8 + d) = 440 \quad (7)$$

$$d = 3 \quad (8)$$

$$x(0) = x(1) - d \quad (9)$$

$$\Rightarrow x(0) = 5 \quad (10)$$

$$x(n) = (x(0) + n \cdot d) u(n) \quad (11)$$

$$= (5 + 3n) u(n) \quad (12)$$

$$\text{From equation (??)} \quad (13)$$

$$X(z) = \frac{5 - 8z^{-1}}{(1 - z^{-1})^2}; \quad |z| > |1| \quad (14)$$

Therefore, the required three numbers in AP are 5, 8, and 11.

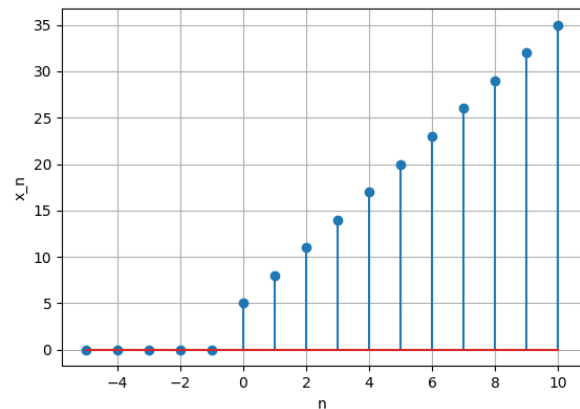


Fig. 0. stem plots of $x(n)$