



By the diagram:

$r$  = horizontal distance between  $x$  (placed) and  $x=5$   
 $= 5 - x$

$h$  = vertical distance between  $y = 4 - x$  and  $y = (2 - \sqrt{x})^2$   
 $= (4 - x) - (2 - \sqrt{x})^2$

$$V = \int_0^4 2\pi (5-x) \left( (4-x) - (2-\sqrt{x})^2 \right) dx$$

$$= 2\pi \int_0^4 -10x + 20\sqrt{x} + 2x^2 - 4x^{3/2} dx$$

$$= 2\pi \left( -\int_0^4 10x dx + \int_0^4 20\sqrt{x} dx + \int_0^4 2x^2 dx - \int_0^4 4x^{3/2} dx \right)$$

$$\rightarrow \int_0^4 10x dx = 80, \int_0^4 20\sqrt{x} dx = \frac{320}{3}, \int_0^4 2x^2 dx = \frac{128}{3}, \int_0^4 4x^{3/2} dx = \frac{256}{5}$$

$$\rightarrow 2\pi \left( -80 + \frac{320}{3} + \frac{128}{3} - \frac{256}{5} \right)$$

$$= 2\pi \left( \frac{272}{15} \right)$$

$$= \frac{544}{15} \pi \rightarrow \text{Final Answer}$$