

9.4

Serial	1	2	3	4	5	6	7	8	9	10	11	12	13
Observation	5	8	7	10	7	6	9	4	4	2	7	7	12
Serial	14	15	16	17	18	19	20	21	22	23	24	25	
Observation	9	11	3	7	8	5	6	7	6	9	11	4	

Random	5	11	17	23
Signal	7	7	7	9

$$N = 25$$

$$\text{Sample} = 4$$

$$k = \frac{25}{4}$$

$$6.25$$

$$S^2 = \frac{1}{n-1} \left[ \sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{4-1} \left[ \sum (7+7+7+9)^2 - \frac{(7+7+7+9)^2}{4} \right]$$

$$= \frac{1}{4-1} \left[ (7+7+7+9)^2 - \frac{(7+7+7+9)^2}{4} \right]$$

$$= 1$$

Variance of sample mean  $V(\bar{x})$

$$= \frac{N-n}{Nn} \times S^2$$

$$= \frac{25-4}{25 \times 4} \times 1 = 0.21$$

Standard error of estimate of mean

$$= \sqrt{V(\bar{x})}$$

$$= \sqrt{0.21} = 0.458$$

The estimate of standard error

$$V(\bar{x}) = N^2 V(\bar{x}) - (25)^2 \times 0.21$$

$$= 131.25$$

$$\bar{x} = \sqrt{V(\bar{x})} = \sqrt{131.25} = 11.46$$

b) proportion  $p = \frac{3}{4} = 0.75$



95

serial	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Observation	4	3	0	2	6	7	4	3	2	0	1	0	3	0	6
serial	16	17	18	19	20	21	22	23	24	25	26	27	28	29	
Observation	8	0	1	4	3	2	6	3	7	5	2	0	2	2	
															30
															Σ

random digit	11	16	9	12	19
Observation	1	2	2	0	4

$$\begin{aligned}
 S^2 &= \frac{1}{n-1} \times \left[ \sum x^2 - \frac{(\sum x)^2}{n} \right] \\
 &= \frac{1}{5-1} \left[ (1^2 + 8^2 + 2^2 + 0^2 + 4^2) - \frac{(1+8+2+0+4)^2}{5} \right] \\
 &= 10
 \end{aligned}$$

Variance of sample

$$\begin{aligned}
 V(\bar{x}) &= \frac{N-n}{Nn} \times S^2 \\
 &= \frac{30-5}{30 \times 5} \times (10)^2 \\
 &= 1.67
 \end{aligned}$$

Standard error of estimate of mean

$$\sqrt{V(\bar{x})} = \sqrt{1.67} = 1.292$$

The estimate of standard error of population

$$\begin{aligned}
 \sqrt{V(\bar{x})} &= N^2 \times V(\bar{x}) = (30)^2 \times 1.67 \\
 &= 1503
 \end{aligned}$$

$$\begin{aligned}
 \bar{x} &= \sqrt{V(\bar{x})} = \sqrt{1503} \\
 &= 38.77
 \end{aligned}$$

9.6

proportion  $p = 0.45$

margin of error  $= 0.1$

$$n = \frac{z^2 pq}{d^2}$$

$$= \frac{(1.96)^2 \times 0.45 \times 0.55}{(0.1)^2}$$

$$= 95.08 = 95$$

9.7

Serial	1	2	3	4	5	6	7	8	9	10	11	12	
Observations	16	7	6	9	11	4	2	7	7	9	11	45	
Serial	13	14	15	16	17	18	19	20	21	22	23	24	25
Observations	8	7	10	7	6	9	11	4	2	7	7		

$N = 23$  and  $n = 4$

Random 2045	11	6	9	12
Observations	11	7	7	45



$$S^2 = \frac{1}{n-1} \times \left[ \sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{4-1} \times (11^2 + 7^2 + 7^2 + 45^2) - \frac{(11+7+7+45)^2}{4}$$

$$= 339.67$$

variance of sample mean  $V(\bar{x})$

$$= \frac{N-n}{Nn} \times S^2$$

$$= \frac{23-4}{23 \times 4} \times 339.67$$

$$= 70.15$$

Standard error of estimate of mean  $\sqrt{V(\bar{x})}$

$$\sqrt{70.15}$$

$$8.376$$

$$\underline{9.8}$$

Proportion  $P = 0.3$

Margin of error  $= 0.05$

$$\text{Size } n = \frac{Z^2 P Q}{d^2}$$

$$= \frac{(1.96)^2 \times 0.3 \times 0.7}{(0.05)^2} = 322.694$$

$$= 323$$