

Regular Expression

Course Code: CSC3220

Course Title: Compiler Design



Dept. of Computer Science
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Lecturer No:		Week No:		Semester:	
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Lecture Outline



1. Definition of a Regular Expression
2. Rules of a Regular Expression
3. Examples
4. Exercises

Objectives and Outcomes



Objectives:

- Understand the basic concept of Regular expression
- Understand the regular expression algorithm

Outcome:

- Students should be able to design the nondeterministic finite automate from regular expression.
- Students should be able to know the applications of a regular expression.

Regular Expression



Definition: A sequence of symbols and characters expressing a string or pattern to be searched for within a longer piece of text.

Another words to say a regular expression is a method used in programming for pattern matching. Regular expressions provide a flexible and concise means to match strings of text.

The regular expressions are built recursively out of smaller regular expressions, using some rules.

Each regular expression r denotes a language $L(r)$, which is also defined recursively from the languages denoted by r 's subexpressions.

Regular Expression



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Rules of Regular Expression

Here are the rules that define the regular expressions over some alphabet Σ and the languages that those expressions denote.

- Basis
- Induction
- Precedence



Rules of Regular Expression

BASIS: There are two rules that form the basis:

- E is a regular expression, and $L(E)$ is $\{\epsilon\}$, that is, the language whose sole member is the empty string.
- If a is a symbol in E , then **a** is a regular expression, and $L(\mathbf{a}) = \{a\}$, that is, the language with one string, of length one, with a in its one position. Here italics is used for symbols, and boldface for their corresponding regular expression.



Rules of Regular Expression

INDUCTION: There are four parts to the induction. Suppose r and s are regular expressions denoting languages $L(r)$ and $L(s)$, respectively.

- $(r)|(s)$ is a regular expression denoting the language $L(r) \cup L(s)$.
- $(r)(s)$ is a regular expression denoting the language $L(r)L(s)$.
- $(r)^*$ is a regular expression denoting $(L(r))^*$.
- (r) is a regular expression denoting $L(r)$. The last rule says that we can add additional pairs of parentheses around expressions without changing the language they denote.



Example of a Regular expression

Let $E = \{a, b\}$.

- 1. The regular expression **$a|b$** denotes the language $\{a, b\}$.
- 2. **$(a|b)(a|b)$** denotes $\{aa, ab, ba, bb\}$, the language of all strings of length two over the alphabet E .
- Another regular expression for the same language is **$aa|ab|ba|bb$** .
- 3. **a^*** denotes the language consisting of all strings of zero or more a 's, that is, $\{E, a, aa, aaa, \dots\}$.



Example of a Regular expression

Let $E = \{a, b\}$.

- 4. $(a|b)^*$ denotes the set of all strings consisting of zero or more instances of a or b , that is, all strings of a 's and b 's: $\{E, a, b, aa, ab, ba, bb, aaa, \dots\}$.
- Another regular expression for the same language is $(a^*b^*)^*$.
- $a|a^*b$ denotes the language $\{a, b, ab, aab, aaab, \dots\}$, that is, the string a and all strings consisting of zero or more a 's and ending in b .



Operations of a Regular expression

Operations:

The various operations on languages are:

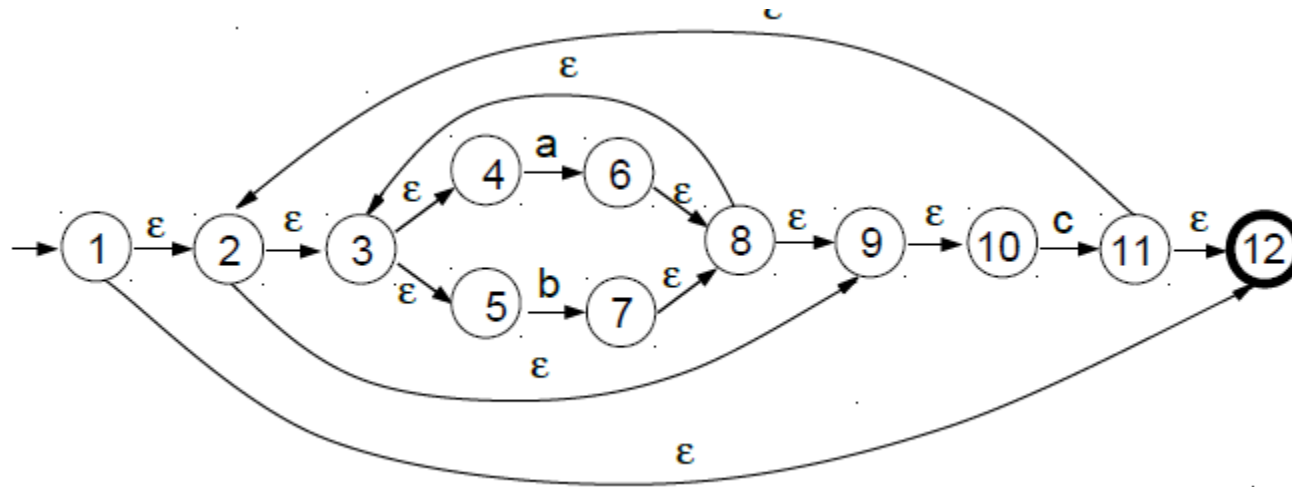
- Union of two languages L and M is written as
 $L \cup M = \{s \mid s \text{ is in } L \text{ or } s \text{ is in } M\}$
- Concatenation of two languages L and M is written as
 $LM = \{st \mid s \text{ is in } L \text{ and } t \text{ is in } M\}$
- The Kleene Closure of a language L is written as
 $L^* = \text{Zero or more occurrence of language } L.$

Regular Expression To NFA



Outline the NFA generated by the construction of Thompson relevant to the following regular expression:

Example: $((a \mid b)^*c)^*$

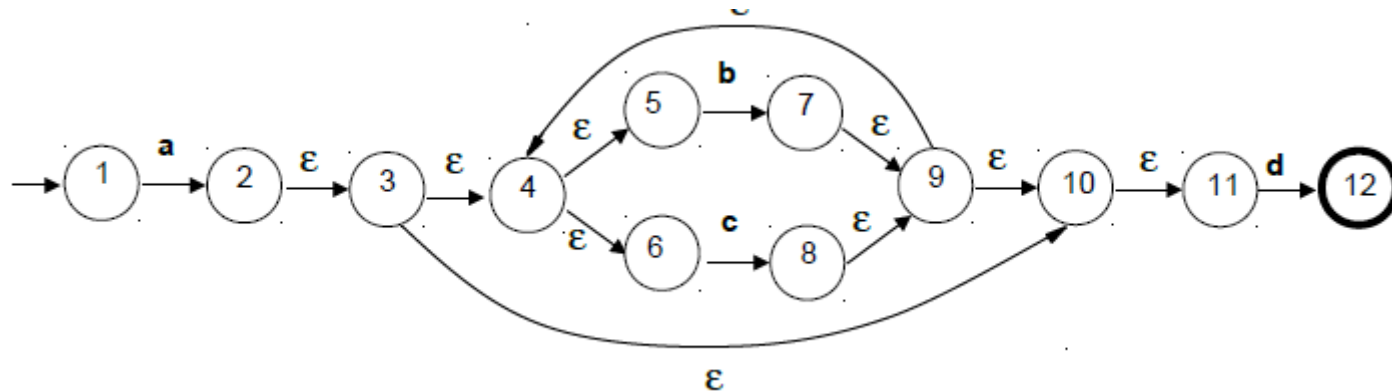


Regular Expression To NFA



By means of the construction of Thompson, outline the NFA relevant to the following regular expression:

Example: $a(b \mid c)^*d$



Regular Expression To NFA



By means of the construction of Thompson, outline the NFA relevant to the following regular expression:

Example: $a(b \mid c)^*d$



Class Exercises

1. $(aUb)^*abc$

1. $(abUbc(abUc)^*)^*$



Lecture References

A. Aho, R. Sethi and J. Ullman, ***Compilers: Principles, Techniques and Tools***
(The Dragon Book), [Second Edition]



References

1. A. Aho, R. Sethi and J. Ullman, ***Compilers: Principles, Techniques and Tools***(The Dragon Book), [Second Edition]
2. **Principles of Compiler Design** (2nd Revised Edition 2009) A. A. Puntambekar
3. Basics of Compiler Design Torben Mogensen