

10.3 We need to test  $H_0: p_1 = p_2 = p_3 = p_4$  Vs  $H_1: AT$

At least one of the doesn't hold tent ratio.

tent ratio.

$$\chi^2 = \sum \frac{O_i^2}{E_i} - n \quad \left| \begin{array}{l} E_i = \frac{n}{K} \\ = \frac{206}{4} \\ = 51.5 \end{array} \right.$$

$$= \frac{\sum (50)^2 + (42)^2 + (32)^2 + (82)^2}{51.5}$$

$$= 27.25$$

Since,  $\chi^2 > \chi^2_{(K-1)} = 3$ , So,  $H_0$  is not accepted.

Hence, the proportions of road accidents in various highways of Bangladesh is not similar.

10.4 We need to test  $H_0: p_1 = p_2 = p_3 = p_4$  Vs  $H_1: at$

least one of the female student doesn't hold the heart ratio.

$$\chi^2 = \sum \frac{O_i^2}{E_i} - n \quad \left| \begin{array}{l} E_i = \frac{n}{K} = \frac{1000}{4} = 250 \\ = \frac{(250)^2 + (450)^2 + (150)^2 + (50)^2}{250} - 1000 \\ = 240 \end{array} \right.$$

Since  $\chi^2 > \chi^2_{(k-1)} = 3 \Rightarrow \chi^2_3 > 7.81$ .  $H_0$  is accepted.

Hence, the proportions of female students in various department is not similar.

Q.5/ Let,  $x \sim N(\mu, \sigma^2)$ ,  $\sigma^2$  is unknown

We need to test  $H_0: \mu = \mu_0 = 21$  vs  $H_1: \mu \neq \mu_0$ .

$$\therefore \bar{x} = \frac{1}{n} \sum x = \frac{1}{36} \times 761.6 = 21.15$$

$$S^2 = \frac{1}{n-1} \left[ \sum x^2 - \left( \frac{\sum x}{n} \right)^2 \right] = \frac{1}{36-1} \left[ 16125.5 - \frac{580034.56}{36} \right]$$

$$= 0.39 \therefore S = 0.63$$

T-test statistic:  $Z = \frac{\bar{x} - \mu_0}{S/\sqrt{n}}$

$$= \frac{21.15 - 21}{0.63/\sqrt{36}} = 1.42$$

Since,  $|Z| < Z_{(0.05)}$ , so,  $H_0$  is accepted. Hence, we can consider the population mean as 21.

Since,  $|Z| < Z_{(0.05)}$ .  $H_0$  is accepted.

$$10.7 / n=25 ; a=8 \therefore p = \frac{a}{n} = \frac{8}{25} = 0.32$$

$$P_0 = 0.40, Q_0 = 0.60$$

$$H_0 \Rightarrow P = P_0 = 0.40$$

$$\therefore z = \frac{P - P_0}{\sqrt{P_0 Q_0 / n}} = \frac{0.32 - 0.40}{\sqrt{0.40 \times 0.60 / 25}} = -0.816$$

$|z| < 1.96$  ; So,  $H_0$  is accepted.

$$10.91 n_1 = 100, n_2 = 125, a_1 = 25, a_2 = 18$$

$$\therefore P_1 = \frac{25}{100} = 0.25 \quad P = \frac{43}{225} = 0.191$$

$$P_2 = \frac{18}{125} = 0.144 \quad \therefore Q = 1 - 0.191 = 0.809$$

$$\therefore z = \frac{P_1 - P_2}{\sqrt{P Q (\frac{1}{n_1} + \frac{1}{n_2})}}$$

$$= \frac{0.25 - 0.144}{\sqrt{(0.191 \times 0.809) \times (\frac{1}{100} + \frac{1}{125})}}$$

$$= 2.009$$

Since  $|z| > 1.96$ ,  $H_0$  is rejected.

10.11/

Blood Pressure	Heart Problem		Total
	Yes	No	
High	150	120	270
Not High	122	158	280
Total	272	278	550

$H_0$ : High pressure is not associated with heart problem.

$H_1$ : High pressure is associated with heart problem.

$$\chi^2 = \frac{550(150 \times 158 - 120 \times 122)^2}{270 \times 280 \times 272 \times 278} = 7.89$$

Since  $\chi^2 > \chi_1^2 = 3.84$ .  $H_0$  is rejected.

10.12/

$H_0$ : No association between origin and full attention.

$H_1$ : Origin and full attention are associated

$$\chi^2 = \frac{350(138 \times 84 - 64 \times 64)^2}{202 \times 148 \times 202 \times 148} = 22.004$$

Since  $\chi^2 > \chi_1^2 = 3.84$ .

$H_0$  is rejected.