

Assignment 3

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18-36303-1

10.2

H_0 vs H_1

Test state $\chi^2 = \sum \frac{O_i^2}{E_i} - n = \frac{1}{51.5} [50^2 + 42^2 + 82^2 + 32^2] - 206$

$$E_i = \frac{n}{k} = \frac{206}{4} = 51.5 \quad | \quad = 27.25$$

Since, $\chi^2 > \chi^2_{(k-1)} = \chi^2_3 = -31.1$

if ~~to~~ we can say H_0 is not accepted as the value is significantly different between the pairs, hence, road accidents in varying highways is different.

10.4

H_0 vs H_1 : at least one of the female students doesn't meet the test state.

Test state,

$$\chi^2 = \sum \frac{O_i^2}{E_i} - n$$

$$E_i = \frac{n}{k} = \frac{1000}{4} = 250$$

$$= \frac{1}{250} [250^2 + 450^2 + 150^2 + 150^2] - 1000$$
$$= 240$$

$$\chi^2_{(k-1)} = \chi^2_3 = \frac{1}{333.33} [310000] - 1000$$

$$E_i = \frac{n}{k} = 333.33$$

$$= -69.99$$

Since χ^2_3 is a negative value, we can reject H_0 as the the values are significantly different from the pairs, ~~con~~ concluding that the number of females are not similar in various departments.

10.5

$$x \sim N(\mu, \sigma^2)$$

$$H_0: \mu = \mu_0 = 21 \quad \text{vs} \quad H_1: \mu \neq \mu_0$$

$$\therefore \bar{x} = \frac{1}{n} \sum x$$

$$= \frac{1}{36} \times 761.6 = 21.15$$

$$S^2 = \frac{1}{n-1} \left[\sum x^2 - \frac{(\sum x)^2}{n} \right] = 0.39$$

Test statistic,

$$Z = \frac{\bar{x} - \mu_0}{S/\sqrt{n}} = \frac{21.15 - 21}{\frac{0.63}{\sqrt{36}}} = 1.42$$

Since $Z < Z_{(0.1)}$, H_0 is accepted which means population mean is 21.

10.7

$$H_0: P = P_0 = 0.40 \quad \text{vs} \quad H_1: P \neq P_0$$

$$P = \frac{a}{n} = \frac{8}{25} = 0.32$$

$$Q_0 = 1 - P_0 = 0.60$$

$$\text{Test statistic: } |Z| = \left| \frac{P - P_0}{\sqrt{\frac{P_0 Q_0}{n}}} \right| = \left| \frac{0.32 - 0.40}{\sqrt{\frac{0.4 \times 0.6}{25}}} \right| = 0.81$$

Since, $|Z| < 1.96$ H_0 is accepted so it can be considered the overall proportion of female students is 0.40.

10.9

$$Z_{10}: \frac{P_1 - P_2}{\sqrt{PQ \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}} \sim N(0,1)$$

$$H_0: P_1 = P_2 \quad \text{vs} \quad H_1: P_1 \neq P_2$$

$$P = \frac{25 + 18}{100 + 125} = 0.14$$

$$Q = 1 - P = 0.81$$

$$P_1 = \frac{25}{100} = 0.25; \quad P_2 = \frac{18}{125} = 0.14 \quad \therefore |Z| = \left| \frac{0.25 - 0.14}{\sqrt{(0.14)(0.81) \left(\frac{1}{100} + \frac{1}{125} \right)}} \right| = 12.09$$

Since $|Z| > 1.96$, H_0 is rejected.