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Section = [0]

Serial = 07

Assignment-04

| x | y | xy | x ² | y ² |
|--------------------|------------------|-----------------------|------------------------|------------------------|
| 11.8 | 10.4 | 122.72 | 139.24 | 108.16 |
| 12.5 | 16.5 | 206.25 | 156.25 | 272.25 |
| 15.7 | 22.9 | 359.53 | 246.49 | 524.41 |
| 19.2 | 26.6 | 510.72 | 368.64 | 707.56 |
| 21.9 | 33.8 | 740.22 | 479.61 | 1142.44 |
| 23.3 | 42.8 | 997.24 | 542.89 | 1831.84 |
| $\Sigma x = 104.4$ | $\Sigma y = 153$ | $\Sigma xy = 2936.68$ | $\Sigma x^2 = 1933.12$ | $\Sigma y^2 = 4586.66$ |

(a)

$$SS(x) = \Sigma x^2 - \frac{(\Sigma x)^2}{n}$$

$$= 1933.12 - \frac{(104.4)^2}{6} = 116.56$$

$$SS(y) = \Sigma y^2 - \frac{(\Sigma y)^2}{n}$$

$$= 4586.66 - \frac{(153)^2}{6} = 685.16$$

$$SP(xy) = \Sigma xy - \frac{\Sigma x \Sigma y}{n}$$

$$= 2936.68 - \frac{104.4 \times 153}{6}$$

$$= 274.48$$

Now.

$$r = \frac{SP(xy)}{\sqrt{SS(x)SS(y)}} = \frac{274.48}{\sqrt{116.56 \times 685.16}} = 0.97$$

Inflation rate(x) and lending rate(y) are positively correlated.

⑥ we need to test $H_0: p = 0$ vs $H_1: p \neq 0$

$$H_0: \rho = 0 \quad \forall \quad H_1: \rho \neq 0$$

Test statistic,

$$t = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}}$$

$$z = \frac{0.97\sqrt{6-2}}{\sqrt{1-0.97^2}}$$

$$= 7.98$$

Since $|t| > \tau_{n-2} = 2.776$

So, H_0 is Rejected,

So, H_0 is rejected,
we can conclude that lending rate of
the inflation rate is not significantly
correlated.

$$SS(x) = 116.56 \quad [\text{for question no-a}]$$

$$SS(y) = 685.16 \rightarrow n \quad r \quad s \quad a$$

$$SP(xy) = 274.48$$

Now,

$$b = \frac{SP(xy)}{SS(x)} = \frac{274.48}{116.56} = 2.35$$

$$a = \bar{y} - b\bar{x} = \frac{\sum y}{n} - b \frac{\sum x}{n}$$

$$= \frac{153}{6} - 2.35 \left(\frac{104.4}{6} \right)$$

$$= -15.39$$

Fitted line $\hat{y} = a + bx = -15.39 + 2.35x$

④ If $x = 25.5$

Then, $\hat{y} = -15.39 + 2.35(25.5)$

$$= -15.39 + 59.92$$

$$= 44.535$$

⑤ We need to test $H_0: \beta = 0$ vs $H_1: \beta \neq 0$

Test statistic $t = \frac{b}{\sqrt{\frac{sr}{SS(x)}}} = \frac{2.35}{\sqrt{\frac{(10.03)^2}{116.56}}} = 2.52$

Now,

$$s^2 = \frac{SS(y) - bSP(xy)}{n-2} = \frac{685.16 - 2.35(274.48)}{6-2}$$

$$= 10.03$$

Since $|t| < t_{n-2; \alpha}$ H_0 is Accepted.

Hence the regression is significant.