

Zubair Chowdhury

Serial: 6

19-4/241-2

Ans no 1

Trend Value

Year	2008	2009	2010	2011	2012	2013
Income	43	51	64	76	81	96

Year	Income	3 Year total	3 Year avg	Trend Values
2008	43	158	52.67	$52.67 - 10.55 = 42.11$
2009	51			$42.11 + 10.55 = 52.67$
2010	64			$52.67 + 10.55 = 63.22$
2011	76	253	84.33	$63.22 + 10.55 = 73.77$
2012	81			$73.77 + 10.55 = 84.32$
2013	96			$84.32 + 10.55 = 94.87$

Difference between central years = $2012 - 2009$

= 3

∴ Semi average = $84.33 - 52.67$

= 31.66

increase in trend value = $\frac{31.66}{3} = 10.55$

Ans no 3

The transition probability matrix

$$P = \begin{bmatrix} P_{00} & P_{01} \\ P_{10} & P_{11} \end{bmatrix} = \begin{bmatrix} 0.6 & 0.4 \\ 0.8 & 0.2 \end{bmatrix}$$

we need P_{005} in P^5

$$P^2 = \begin{bmatrix} 0.6 & 0.4 \\ 0.8 & 0.2 \end{bmatrix} \begin{bmatrix} 0.6 & 0.4 \\ 0.8 & 0.2 \end{bmatrix}$$

$$= \begin{bmatrix} 0.68 & 0.32 \\ 0.64 & 0.36 \end{bmatrix}$$

$$P^4 = \begin{bmatrix} 0.68 & 0.32 \\ 0.64 & 0.36 \end{bmatrix} \begin{bmatrix} 0.68 & 0.32 \\ 0.64 & 0.36 \end{bmatrix}$$

$$= \begin{bmatrix} 0.6672 & 0.3328 \\ 0.6656 & 0.3344 \end{bmatrix}$$

$$P^5 = \begin{bmatrix} 0.6672 & 0.3328 \\ 0.6656 & 0.3344 \end{bmatrix} \begin{bmatrix} 0.6 & 0.4 \\ 0.8 & 0.2 \end{bmatrix}$$

$$= \begin{bmatrix} 0.66656 & 0.33344 \\ 0.66688 & 0.33312 \end{bmatrix}$$

Required probability is 0.66656

i) More than 1 minute

$$P(T > 1) = e^{-\pi t} = e^{-2 \times 1} = 0.1353$$

ii) less than 2 minute

$$\begin{aligned} P(T < 2) &= 1 - e^{-\pi t} \\ &= 1 - e^{-2 \times 2} \\ &= 1 - e^{-4} \\ &= 0.9816 \end{aligned}$$

iii) Between 1 to 2 minute

$$\begin{aligned} P(1 < T < 2) &= e^{-\pi t} - e^{-\pi t_2} \\ &= e^{-2 \times 1} - e^{-2 \times 2} \\ &= e^{-2} - e^{-4} \\ &= 0.1353 - 0.0183 \\ &= 0.117 \end{aligned}$$