

Name: Sidul Islam Sohag

Serial-16

Id: 20-42668-1 Section: 0

Assignment-4

11.1

Solution:

x	y	$\sum xy$	$\sum x^2$	$\sum y^2$
11.8	10.4	122.72	139.24	108.16
12.5	16.5	206.25	156.25	272.25
15.7	22.9	359.53	246.49	524.41
19.2	26.6	510.72	368.64	707.56
21.9	33.8	740.22	479.61	1142.44
23.3	42.8	997.24	542.89	1831.34
$\sum x = 104.4$	$\sum y = 153$	$\sum xy = 2936.68$	$\sum x^2 = 1933.12$	$\sum y^2 = 4586.66$

$$a) SS(x) = \sum x^2 - \frac{(\sum x)^2}{4}$$

$$= 1933.12 - \frac{(104.4)^2}{4}$$

$$= 116.56$$

$$SS(y) = \sum y^2 - \frac{(\sum y)^2}{4}$$

$$= 4586.66 - \frac{(153)^2}{4} = 685.15$$

$$SP(xy) = \sum xy - \frac{\sum x \cdot \sum y}{n} = 2936.68 - \frac{(104.4) \times (153)}{6}$$

$$= 274.48$$

$$r = \frac{SP(xy)}{\sqrt{SS(x) \times SS(y)}} = \frac{274.48}{\sqrt{116.56 \times 685.15}} = 0.9713$$

$$b) H_0: \rho = 0 \quad \text{vs} \quad H_1: \rho \neq 0$$

$$t = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}} = \frac{0.97\sqrt{6-2}}{\sqrt{1-(0.97)^2}}$$

$$= 8.162 > t_4$$

We conclude that inflation rate is significantly correlated with the lending rate.

$$c) b = \frac{SP(xy)}{SS(x)} = \frac{274.48}{116.56} = 2.35$$

$$a = \frac{\sum y}{n} - b \frac{\sum x}{n} = \frac{153}{6} - 2.35 \frac{104.4}{4} = -15.4747$$

$$\hat{y} = a + bx = -15.4747 + 2.35x$$

d) if $x = 25.5$; then. $\hat{y} = -15.4747 + (2.35 \times 25.5)$
 $= 44.474$

e) $H_0: \beta = 0$ vs $H_1: \beta \neq 0$

$$s^2 = \frac{SS(y) - b SP(xy)}{n-2} = \frac{685.16 - 2.35 \times (274.48)}{6-2}$$

$$= 9.7$$

$$t = \frac{b}{\sqrt{s^2 / SS(x)}} = \frac{2.35}{\sqrt{9.7 / 116.56}} = 8.16 > t_4$$

Regression is significant.