

ID = 17-35338-3

SL = 02

Class	(f)	(x)	f(x)	f log x	$\sum f_i$	$x - \bar{x}$ Hence $\bar{x} = \frac{75}{20} = 3.75$	$f_i(x_i - \bar{x})$	$f_i(x_i - \bar{x})^2$
1 - 2	1	1.5	1.5	0.176	0.66	-2.25	2.25	5.06
2 - 3	3	2.5	7.5	1.104	1.2	-1.25	3.75	4.687
3 - 4	8	3.5	28	4.352	2.286	-0.25	2	0.5
4 - 5	6	4.5	27	3.910	1.33	0.75	4.5	3.375
5 - 6	2	5.5	11	1.48	0.384	1.75	3.5	6.125
total	20	75	75	11.12	5.87		16	15.75

$$\frac{\partial}{\partial x} = \frac{1}{20} - \frac{x}{20} + \frac{3}{20} = (0.05) x + 1.5$$

a) $A.M = \frac{1}{n} \sum_{i=0}^n f_i x_i = \frac{75}{20} = 3.75$

b) $G.M = \text{Antilog} \left(\frac{1}{n} \sum_{i=1}^n f_i \log x_i \right)$
 $= \text{Antilog} \left(\frac{11.12}{20} \right)$
 $= 3.597$

c) $H.M = \frac{n}{\sum_{i=1}^n \frac{f_i}{x_i}} = \frac{20}{5.87} = 3.41$

d) Mean deviation, $M.D = \frac{1}{n} \sum_{i=1}^n f_i |x_i - \bar{x}| = \frac{16}{20} = 0.8$

e) Variance, $\sigma^2 = \frac{1}{n} \sum_{i=1}^n f_i (x_i - \bar{x})^2 = \frac{15.75}{20} = 0.787$

Standard deviation, $S = \sqrt{\sigma^2} = \sqrt{0.787} = 0.99$

f) Coefficient of Variance, $CV = \frac{S}{\bar{x}} = \frac{0.99}{20} \times 100\% = 26.5\%$

3.1)

$$A = \{3, 6, 9, 12, 15, 18\} \quad [\text{multiple of } 3]$$

$$B = \{5, 10, 15, 20\} \quad [n=5]$$

So that,

$$P(A) = \frac{6}{20} \quad \text{and} \quad P(B) = \frac{4}{20}$$

Now,

$$(A \cap B) = \{15\} \therefore P(A \cap B) = \frac{1}{20}$$

$$\therefore P(A \cup B) = \frac{6}{20} + \frac{4}{20} - \frac{1}{20} = \frac{9}{20}$$

(Ans)

3.2)

$$\text{Total students} = 15 + 10 = 25$$

$$\begin{aligned} \text{Probability of selecting 1 girl and 2 boys} &= \frac{10C_1 \times 10C_2}{25C_3} \\ &= \frac{21}{46} \text{ (Ans)} \end{aligned}$$

3.3)

$$\text{Total balls} = 4 + 5 + 6 = 15$$

$$\text{Getting All red} = \frac{5C_3}{15C_3} = \frac{2}{31} \text{ (Ans)}$$

3.4)

$$\text{Total engineers} = 5 + 6 = 11$$

$$\text{a) All E.E} = \frac{5C_4}{11C_4} = \frac{1}{16}$$

$$\text{b) 2 E.E and 2 C.E} = \frac{5C_2 \times 6C_2}{11C_4} = \frac{5}{11} \text{ (Ans)}$$

Computational Statistics and Probability [O]

Khan, Mohiur Rahman

18-36303-1

Assignment 3

3.1

Tickets 1-20

Let a = multiple of 3 = {3, 6, 9, 12, 15, 18}

Let b = multiple of 5 = {5, 10, 15, 20}

$$P(a) = \frac{6}{20}$$

$$P(a \cap b) = \frac{1}{20}$$

$$P(a \cup b) = \frac{6}{20} + \frac{4}{20} - \frac{1}{20} = \frac{9}{20}$$

3.2

P $n=25$ (15B, 10G)

P(G, B, B)

P(GGBB, BGGB, BBGG) =

let B = one girl, two boys = $10C_1 \times 15C_2$

$$\therefore P(B) = \frac{10C_1 \times 15C_2}{25C_3} = 0.457$$

3.3

4W, 5R, 6B

Total = 15 balls

$$\text{let } P(C) = R, R, P = \frac{5C_3}{15C_3} = \frac{2}{91}$$

3.4

5EE, 6CE

a) Let $E = \text{All 4 Electronic} = \frac{5C_4}{11C_4} = \frac{1}{66}$

b) Let $G = 2EE, 2CE = \frac{5C_2 \times 6C_2}{11C_4} = \frac{5}{11}$

Serial: 4

Moshur
Rahman
Khan

Class	f	cf	x	$\Sigma(x)$	$\Sigma f \log(x)$	$\frac{\Sigma f}{n}$
1-2	1	1	1.5	1.5	0.17	0.667
2-3	3	4	2.5	7.5	1.19	1.20
3-4	8	12	3.5	28	4.38	2.28
4-5	6	18	4.5	27	3.91	1.33
5-6	2	20	5.5	11	1.48	0.36
Total	20			75	11.12	5.837

$$\text{Arithmetic mean} = \frac{1}{n} \sum_{i=1}^n f_i x_i = \frac{75}{20} = 3.75$$

$$\text{Geometric mean} = \text{Antilog} \left(\frac{11.12}{20} \right) = 3.60$$

$$\text{Harmonic mean} = \frac{20}{\frac{20}{5.837}} = 3.426$$

$$\text{Median} = \frac{n}{2} = 10$$

(f for class (3-4) is 4 > (3-4) \geq 12

$$\therefore \text{median} = 3 + \frac{\frac{20}{2} - 4}{8} \times 1 \\ = 3.75$$

Mode = f for class (3-4) is 8
highest frequency

$$\begin{array}{l|l}
\begin{array}{l}
f_m = 8 \\
f_1 = 3 \\
f_2 = 6 \\
L = 3 \\
n = 1
\end{array} &
\begin{array}{l}
\text{mode} = 3 + \frac{8-3}{(2 \times 8) - 3 - 6} \times 1 \\
= 3.71
\end{array}
\end{array}$$

Class	\bar{x}	$ x - \bar{x} $	$f(x - \bar{x})$	$f(x - \bar{x})^2$
1-2	2.25	2.25	2.25	5.06
2-3	3.75	1.25	3.75	4.68
3-4	3.75	0.25	2	0.5
4-5	0.75	0.75	4.5	3.37
5-6	1.75	1.75	3.5	6.12
		16	19.75	

$$MD = \frac{16}{20} = 0.8$$

$$d^2 = \frac{19.75}{20} = 0.98$$

$$\sigma_x = \sqrt{0.98} = 0.99$$

$$CV = \frac{\sigma_x}{\bar{x}} \times 100\% = \frac{0.99}{3.75} \times 100\%$$

$$= 26.4\%$$

Name: Joy Muttubben
ID : 20-41959-1

Section:- O
Serial: 07

Class	frequency (f)	cumulative frequency (cf)	Mid (x)	$f \cdot x$	$f \log x$	$\frac{f}{n}$
1-2	1	1	1.5	1.5	0.17	0.067
2-3	3	4	2.5	7.5	1.18	0.120
3-4	8	12	3.5	28	4.35	0.28
4-5	6	18	4.5	27	3.01	0.33
5-6	2	20	5.5	11	1.48	0.06
Total:	n = 20			75	11.12	0.84

(a) Arithmetic Mean:-

$$AM = \frac{1}{n} \sum_{i=1}^n f_i x_i = \frac{75}{20} = 3.75$$

Geometric Mean:-

$$GM = \text{Antilog} \left(\frac{1}{n} \sum_{i=1}^n f_i \log x_i \right) = \\ = \text{Antilog} \left(\frac{11.12}{20} \right) = 3.60$$

Harmonic Mean:-

$$HM = \frac{n}{\sum_{i=1}^n \frac{f_i}{x_i}} = \frac{20}{5.84} = 3.42$$

(b)

Median:- Hence, $n/2 = 10$;

for class 3-4, $cf > 10$, so median class is (3-4)

We know that,

$$\begin{aligned} \text{Median} &= L + \frac{\frac{n}{2} - c}{f} \times h \\ &= 3 + \frac{\frac{20}{2} - 4}{8} \times 1 \\ &= 3.75 \end{aligned}$$

- lower limit of median class (L) = 3
- size of Median class h = 1
- freq. of median class f = 8
- cf of previous class of median class (c) = 4

Name: Joy Matreber

Serial: 07

Mode: The class 3-4 contains the highest frequency
So, the model class is (3-4)

We know that

$$\text{Mode} = L + \frac{f_m - f_1}{2f_m - f_1 - f_2} \times h$$
$$= 3 + \frac{8 - 3}{(2 \times 8) - 3 - 6} \times 1$$
$$= 3.71$$

$f_m = 8$
 $f_1 = 3$
 $f_2 = 6$
 $L = 3$
 $n = 20$

CLASS	f	x	fx	\bar{x}	$ x - \bar{x} $	$f x - \bar{x} $	$f(x - \bar{x})^2$
1-2	1	1.5	1.5		2.25	2.25	5.06
2-3	3	2.5	7.5		1.25	3.75	4.68
3-4	8	3.5	28	3.75	0.25	2	0.5
4-5	6	4.5	27	3.75	0.75	4.5	3.37
5-6	2	5.5	11	3.75	1.75	3.5	6.12
Total:	$n = 20$		75			16	19.75

Mean deviation:

$$MD = \frac{1}{n} \sum_{i=1}^n f|x - \bar{x}| = \frac{16}{20} = 0.8$$

Variance: $\sigma^2 = \frac{1}{n} \sum_{i=1}^n f(x - \bar{x})^2 = \frac{19.75}{20}$
 $= 0.98$

Name: Joy Martubben

Serial: 07

Standard deviation, coefficient of variation and skewness

$$SD = \sigma = \sqrt{0.98} = 0.989$$

Coefficient of variation:

$$CV = \frac{\sigma \times 100\%}{\bar{x}} = \frac{0.989}{3.75} \times 100\% = 26.89\%$$

$$\sigma = \sigma$$

$$\bar{x} = \bar{x}$$

$$\text{Skewness} = \text{Mean} - \text{Median}$$

$$= 3.75 - 3.75 = 0$$

So, the distribution is symmetrical.

probability

(3.1)

Tickets are numbered as 1 to 20.

A = Multiple of 3 = {3, 6, 9, 12, 15, 18}; So, $P(A) = \frac{6}{20}$

B = {5, 10, 15, 20}; So, $P(B) = \frac{4}{20}$

So, $A \cap B = \{15\}$; So, $P(A \cap B) = \frac{1}{20}$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{6}{20} + \frac{4}{20} - \frac{1}{20}$$

$$= 0.45$$

$$\therefore \text{Ans} = \frac{0.45}{0.9} = 45\%$$

Name: Joy Matubben
 Serial: 07
 ID: 20-41959-1

(3.2)

There are 15 boys and 10 girls in a class
 So, Total number of student = 25

Now, 1 girl and 2 boys total three students
 select at randomly,
 The probability will be $= \frac{15C_2 \times 10C_1}{25C_3}$

$$= 0.456 \quad \textcircled{a} \\ = 45.6\% \quad \underline{\text{Ans:}}$$

(3.3) A bag contains 4 white, 5 red, and 6 blue balls.
 Total balls are 15.

If, 3 drawn three balls at randomly

The probability that all of them are red

$$\text{will be } = \frac{5C_3}{15C_3}$$

$$= \frac{2}{91} \quad \underline{\text{Ans:}}$$

(3.4)

The mobile operator's office there are 5 electronic engineers and 6 computer engineers.

$$1. \text{ total} = 6 + 5 = 11$$

A Committee of 4 is to be formed randomly to perform a duty. Then the probability will consist.

(a) All electronic engineers, $= \frac{5c_4}{11c_4}$

$$= \frac{1}{66}$$

(3.4)

$$= 1.51\%$$

(b)

2 electronic engineers and 2 computer engineers, the probability will be.

$$P(B) = \frac{5c_2 \times 6c_2}{11c_4}$$

$$= \frac{5}{11}$$

$$= 45.45\%$$

Name: Javed Mohammad

ID: 20-92006-1

Serial no: 08

class interval	frequency f	cumulative cf	midpoint, x	f _{OL}	\bar{x}	f _{OLy_{OL}}	f _{OL}	x - \bar{x}	x - \bar{x}	f _{OL} x - \bar{x}	f _{OLy_{OL}} x - \bar{x}
1-2	1	1	1.5	1.5	7.5720 3.75	0.176	0.667	-2.25	2.25	2.25	5.062
2-3	3	4	2.5	7.5	3.75	1.94	1.2	-1.25	1.25	3.75	14.062
3-4	8	12	3.5	28	3.25	9.352	2.286	-0.25	0.25	2	9
4-5	6	18	4.5	27	3.25	3.919	1.333	0.75	0.75	0.75	4.5
5-6	2	20	5.5	11	3.75	1.481	0.369	1.75	1.75	3.5	12.25
Total	20			75		11.19	5.85			16	55.624

$s=8$

Arithmetic mean ;

$$A_m = 75/20 = \cancel{3.75} \quad 3.75$$

Geometric mean ;

$$G_m = \text{Antilog} \left(\frac{\sum u}{20} \right) = 3.60$$

Harmonic mean

$$H_m = \frac{20}{\frac{1}{8.85}} = 3.419$$

Mean Deviation ;

$$MD = \frac{16}{20} = 0.8$$

Variance ;

$$\sigma^2 =$$

$$\frac{55.624}{20} = 2.781$$

$s = 8$

Standard Deviation

$$s = \sqrt{2.781} = 1.668$$

Median

$$3 + \left[\frac{10 - 3}{8} \right] \times 1$$

$$= 3.75$$

Mode

$$3 + \frac{8 - 3}{2 \times 2 - 3 - 6} \times 1$$

$$= 3.71$$

coefficient of variation

$$CV = \frac{1.668}{3.75} \times 100\% \\ = 44.48\%$$

S=8

Probability

3.1)

Let A = multiple of 3 = {3, 6, 9, 12, 15, 18} = $P(A) = \frac{6}{20}$

B = multiple of 5 = {5, 10, 15, 20} = $P(B) = \frac{4}{20}$

$$A \cap B = \{15\} = \frac{1}{20}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{6}{20} + \frac{4}{20} - \frac{1}{20}$$

$$= \frac{9}{20}$$

5 = 8

3.2] There are total $15+20$ students

$$\text{answering} = 25$$

~~total~~ 1 girl and 2 boys $P(A) = \frac{15e_2 \times 10e_1}{25e_3}$

$$= \frac{21}{45}$$

3.3] there are total $4+6+5 = 15$ balls

\therefore All three red. $P(B) = \frac{5e_3}{15e_3}$

$$= \frac{2}{9}$$

S = 8

3.9)

There are $5+b \leq 11$ engineers

a) all electronic engineers $P(A) = \frac{5 \text{ eq}}{11 \text{ eq}}$

$$= \frac{1}{66}$$

b) 2 electronic and 2 non computer engineers

$$P(B) = \frac{5 \text{ eq} \times 6 \text{ eq}}{11 \text{ eq}}$$

$$= \frac{30}{11}$$

[ABU TAHER MAHIM SARKAR, ID: 20-42042-1, SL-09]

Ans.No-15

Class Interval	Frequency, f	cf	Mid Point, x	fx	x'	flogx	f/x	xi-x'	f xi-x'	f(xi-x')^2
1-2	1	1	1.5	1.5	3.75	0.18	0.67	2.25	2.25	5.06
2-3	3	4	2.5	7.5		1.19	1.20	1.25	3.75	4.69
3-4	8	12	3.5	28		4.35	2.29	0.25	2	0.50
4-5	6	18	4.5	27		3.92	1.33	0.75	4.5	3.38
5-6	2	20	5.5	11		1.48	0.36	1.75	3.5	6.13
Total	20			75		11.12	5.85		16	19.75

From the table.

$$(a) \text{ Arithmetic mean} = \frac{75}{20} = 3.75$$

$$\text{Geometric mean} = \text{antilog} \left(\frac{5.85}{20} \right)$$

$$= 3.597$$

$$\text{Harmonic mean} = \frac{20}{\frac{5.85}{20}} = 3.419$$

$$(b) \text{ Total, } n = 20; \text{ Hence, } \frac{n}{2} = \frac{20}{2} = 10$$

For the class (3-4), we get cf = 12 > 10

Hence, this is our median class.

$$\text{Median, } M_e = L + \frac{\frac{n}{2} - C}{f} \times h$$

$$= 3 + \frac{10 - 4}{8} \times 1 = 3.75$$

For the class (3-4), we have the highest frequency 8. Hence, this is our modal class.

$$\text{Mode, } M_o = L + \frac{f_m - f_1}{2f_m - f_1 - f_2} \times h$$

$$= 3 + \frac{8 - 3}{2 \times 8 - 3 - 6} \times 1 = 3.71$$

(c) Here, mean = 3.75
 From b, median = 3.75
 $Sk = \text{mean} - \text{median}$
 $= 3.75 - 3.75$
 $= 0$; that is symmetric.
 So, the distribution is symmetric.

(d) Mean deviation = $\frac{16}{20} = 0.80$.

(e) Variance, $\sigma^2 = \frac{19.75}{20} = 0.99$.

Standard deviation, $\sigma = \sqrt{0.99} = 0.995$

(f) Coefficient of variation = $\frac{0.995}{3.75} \times 100\% = 26.53\%$

$$\frac{\sum (x_i - \bar{x})^2}{n} + 1 = \text{std. deviation}$$

$$[Ans]$$

"Exercise-3"

3.1. Tickets are numbered as 1 to 20.

Let, A = multiple of 3
 tickets = {3, 6, 9, 12, 15, 18}.

$$\text{So, } P(A) = \frac{6}{20} = \frac{3}{10}$$

Let, B = multiple of 5
 tickets = {5, 10, 15, 20}

$$\text{So, } P(B) = \frac{4}{20} = \frac{1}{5}$$

$$A \cap B = \{15\}; \text{ So, } P(A \cap B) = \frac{1}{20}$$

We know, $A + B - A \cap B = \text{Total}$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{3}{10} + \frac{1}{5} - \frac{1}{20}$$

$$= \frac{9}{20} = 0.45$$

[Ans]

3.2. There are 15 boys and 10 girls in a class.

$$\text{Total student} = (15 + 10) = 25.$$

Hence, 1 girl and 2 boys are selected at random.

$$\text{The probability will be, } = \frac{15C_2 \times 10C_1}{25C_3}$$

$$= \frac{21}{91} = 0.457 \quad [\text{Ans}]$$

3.3. A bag contains 4 white, 5 red and 6 blue balls.

$$\text{Total ball} = (4 + 5 + 6) = 15$$

$$\begin{aligned} \text{The probability of red ball} &= \frac{5C_1}{15C_3} \\ &= \frac{2}{91} = 0.021 \end{aligned} \quad [\text{Ans}]$$

3.4. There are 5 electronic engineers and 6 computer engineers in a mobile operator's office.

$$\text{Total engineer} = (5 + 6) = 11$$

(a) Let, A = all electronic engineers.

$$P(A) = \frac{5C_4}{11C_4} = \frac{1}{66} = 0.015$$

(b) Let, B = 2 electronic engineers and 2 computer engineers.

$$\begin{aligned} P(B) &= \frac{5C_2 \times 6C_2}{11C_4} \\ &= \frac{5}{11} = 0.45 \end{aligned} \quad [\text{Ans}]$$

Rifath Bin mashruw
ID: 20-42079-1, Serial: 10

Ans to the Que No. 15

Cls Interval	freq of f	c.f	Mid point, x_i	$f x_i$	x_i^2	$f \log x_i$	f/x_i	$ x_i - x' $	$f x_i - x' $	$f(x_i - x')^2$
1-2	1	1	1.5	1.5		0.18	0.67	2.25	2.25	5.06
2-3	3	4	2.5	7.5		1.19	1.20	1.25	3.75	4.69
3-4	8	12	3.5	28	3.75	4.39	2.29	0.25	2	0.50
4-5	6	18	4.5	27		3.92	1.33	0.25	4.5	3.38
5-6	2	20	5.5	11		1.48	0.36	1.25	3.5	6.13
Total	20					11.12	5.85		16	19.75

From the table,

a) Arithmetic mean = $\frac{75}{20} = 3.75$

Geometric mean = $\text{antilog} \left(\frac{5.85}{20} \right) = 3.597$

Harmonic mean = $\frac{20}{5.85} = 3.419$

b) Total, $n = 20$, $\therefore \frac{n}{2} = \frac{20}{2} = 10$

class (3-4), we get of = 12 > 10

This is our median class.

$$\begin{aligned} \text{Median, } M_e &= L + \frac{\frac{n}{2} - c}{f} \times h \\ &= 3 + \frac{10 - 4}{8} \times 1 = 3.75 \end{aligned}$$

we have the highest frequency 8. Hence,

This is our modal class

$$\text{Mode, } M_o = L + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h = 3 + \frac{8 - 3}{2 \times 8 - 3 - 6} \times 1$$

$$= 3.71$$

c) Mean = $\frac{3.75 + 3.75 + 3.75 + 3.75 + 3.75 + 3.75 + 3.75 + 3.75 + 3.75 + 3.75}{10}$ = 3.75

from b, median = 3.75

SK = mean - median = $3.75 - 3.75$

d) Mean deviation = $\frac{16}{20} = 0.86$

e) Variance $s^2 = \frac{19.75}{20} = 0.99$

Standard deviation $s = \sqrt{0.99} = 0.995$

f) coefficient of variation = $\frac{0.995}{3.75} \times 100\%$

= 26.53% (Ans)

Ex - 3

Ques. 8. Find the probability that a ticket drawn at random is numbered 3 or 12.

Ex - 3

Ans. Tickets are numbered from 1 to 20. Let, A = multiple of 3 {3, 6, 9, 12, 15, 18}

$$\therefore P(A) = \frac{6}{20} = \frac{3}{10}$$

B = multiple of 5 {5, 10, 15, 20}

$$\therefore P(B) = \frac{4}{20} = \frac{1}{5}$$

$$A \cap B = \{15\} ; P(A \cap B) = \frac{1}{20}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{3}{10} + \frac{1}{5} = \frac{1}{20}$$

$$= \frac{9}{20} = 0.45$$

Ans.

$$P(E) =$$

(2)

→ find probability of getting 1 girl & 2 boys in a class.

∴ There are 15 boys and 10 girls in a class.

$$\text{Total student} = (10+15) = 25$$

∴ 1 girl and two boys are selected at random.

$$\begin{aligned}\text{The Probability} &= \frac{15C_2 \times 10C_1}{25C_3} \\ &= \frac{21}{46} = 0.45 \times (\text{Ans})\end{aligned}$$

3) There are 5 electronic engineering and 6 computer engineers in a mobile operators office.

$$\text{Total engineer} = (5+6) = 11$$

a) Let, A = all electronic Engineers,

$$P(A) = \frac{5C_4}{11C_4} = \frac{1}{66} = 0.015$$

Serial-16

b) $B = 2$ electronic engineers and 2 computer engineers.

$$P(B) = \frac{5C_2 \times 6C_2}{11C_4} = \frac{5}{11} \approx 0.45$$

$$\frac{1301 \times 521}{1325} = 67.0\%$$

$$521 \times 0.07 = \frac{15}{11}$$

(Q1)

$$11 = (2 + 2) = \text{number of lotteries}$$

$$2/11 = \frac{1}{11} = \frac{1}{11} = 0.0909$$

Assignment - 03 (Sec: 0)
Serial no - 12

Name: Md. Mamunur Rahman Moon

ID: 20-42439-1

Class interval of faded signals	No. of stations (f _i)	No. of stations (f _i)	Midpoint , x _i	f _i x _i	f _i log x _i	$\frac{f_i}{x_i}$	\bar{x}
1-2	1	1	1.5	1.5	0.18	0.67	
2-3	3	4	2.5	7.5	1.19	1.2	
3-4	8	12	3.5	28	4.36	2.28	3.75
4-5	6	18	4.5	27	3.92	1.33	
5-6	2	20	5.5	11	1.49	0.36	
Total	20			75	11.14	5.84	

(a) Arithmetic mean:

$$AM = \frac{1}{n} \sum_{i=0}^n f_i x_i = \frac{75}{20} = 3.75$$

Geometric mean:

$$G.M = \text{Antilog} \left(\frac{1}{n} \sum_{i=0}^n f_i \log x_i \right)$$

$$= \text{Antilog} \left(\frac{11.14}{20} \right) = 3.72$$

Harmonic mean:

$$HM = \frac{n}{\sum_{i=0}^n \frac{f_i}{x_i}} = \frac{20}{5.84} = 3.43$$

(b)

Class	f	cf	$ x_i - \bar{x} $	$f_i x_i - \bar{x} $	$f_i (x_i - \bar{x})^2$
1-2	1	1	2.25	2.25	5.06
2-3	3	4	1.25	3.75	4.68
3-4	8	12	0.25	2	0.5
4-5	6	18	0.75	4.5	3.38
5-6	2	20	1.75	3.5	6.12
Total	20			16	19.74

Median:

$$Me = L + \frac{\frac{n}{2} - c}{f} \times h$$

$$= 3 + \frac{\frac{20}{2} - 4}{8} \times 1$$

$$= 3.75$$

L = Lower limit

n = total frequency

h = class size

c = cumulative frequency of previous class.

f_m = frequency of modal classf₁ = frequency of previous classf₂ = frequency of next class

$$\underline{\text{Mode:}} \quad Mo = L + \frac{f_m - f_1}{2f_m - f_1 - f_2} \times h$$

$$= 3 + \frac{8 - 3}{2(8) - 3 - 6} \times 1$$

$$= 3.71$$

(c) As, Mean > Median > Mode. So, the distribution is positively skewed.

$$(d) \text{ Mean deviation, } MD = \frac{1}{n} \sum_{i=1}^n f_i |x_i - \bar{x}| = \frac{16}{20} = 0.8$$

$$(e) \text{ Variance, } \sigma^2 = \frac{1}{n} \sum_{i=1}^n f_i (x_i - \bar{x})^2 = \frac{19.74}{20} = 0.987$$

$$\text{Standard deviation, } \sigma = \sqrt{\text{Variance}} = \sqrt{0.987} = 0.99$$

$$(f) \text{ Co-efficient of variation, } CV = \frac{\sigma}{\bar{x}} = \frac{0.99}{3.75} \times 100\% \\ = 26.4\%$$

Probability

3.1/ Let, A = Multiple of 3 = {3, 6, 9, 12, 15, 18}
 B = Multiple of 5 = {5, 10, 15, 20}

$$P(A) = \frac{6}{20}, \quad P(B) = \frac{4}{20}$$

$$\therefore P(A \cap B) = \{15\}$$

$$P(A \cap B) = \frac{1}{20}$$

We Know,

$$\begin{aligned}P(A \cup B) &= P(A) + P(B) - P(A \cap B) \\&= \frac{6}{20} + \frac{4}{20} - \frac{1}{20} \\&= \frac{9}{20}\end{aligned}$$

3.2/ Given, 15 Boys, 10 girls in a class.

Probability to find 1 girl and 2 boys randomly,

$$\begin{aligned}&+ \quad = \frac{10C_1 \times 15C_2}{25C_3} \\&= \frac{21}{96} \quad (\text{Ans.})\end{aligned}$$

3.3/ Given, A bag contains, 4 white, 5 red and 6 blue balls.

Probability of three drawn ball of one red of all of them,

$$\begin{aligned}&\frac{5C_3}{15C_3} \quad | \quad \text{Total ball} = 4+5+6 \\&= \frac{10}{455} = \frac{2}{91} \quad (\text{Ans.}) \quad | \quad = 15\end{aligned}$$

3.4/ Given,

5 electronic engineers
6 computer engineers } Total = 11 engineers

Among the committee of 9, the probability
of,

$$(a) \text{ all electronic engineers} = \frac{5C_4}{11C_4} = \frac{1}{16} \quad (\text{Ans})$$

(b) 2 electronic engineers and 2 computer engineers,

$$\begin{aligned} &= \frac{5C_2 \times 6C_2}{11C_4} \\ &= \frac{5}{11} \quad (\text{Ans.}) \end{aligned}$$

Zaid Amin Rawfin
ID: 20-42459-1

Serial: 13

Class	f	u	$f \log u$	$f \log e$	$\frac{f}{\log e}$	$(\frac{u - \bar{u}}{\bar{u}} = \frac{75 - 3.75}{3.75} = 3.75)$	$f(u - \bar{u})$	$f(u - \bar{u})^2$
1-2	1	1.5	1.5	0.176	0.66	-2.25	2.25	506
2-3	3	2.5	7.5	1.194	1.2	-1.25	3.75	4687
3-4	8	3.5	2.8	4.352	2.286	-0.25	2	0.5
4-5	6	4.5	27	3.919	1.33	0.75	4.5	3.375
5-6	2	5.5	11	1.48	0.384	1.75	3.5	6.125
Total	20		75	11.12	5.87		16	19.75

a) AM = $\frac{75}{20} = 3.75$

GM = Antilog $\left(\frac{11.12}{20}\right) = 3.597$

HM = $\frac{20}{5.87} = 3.41$

b)

class	frequency	cumulative Frequency (C)
1-2	1	1
2-3	3	4
3-4	8	12
4-5	6	18
5-6	2	20

$$\text{median} = 3 + \frac{\frac{20}{2} - 4}{8} \times 1 = 3.75$$

$$\text{mode} = 3 + \frac{8-3}{8 \times 2 - 3 - 6} \times 1 = 3.75$$

c) As, mean > median > mode, It is positively skewed.

d) MD = $\frac{16}{20} = 0.8$

e) variance, $\sigma^2 = \frac{19.75}{20} = 0.9875$

SD, $\sigma = 0.99$

f) CV = $\frac{0.99}{3.75} \times 100\% = 26.5\%$

3.1) let, A = multiple of 3 = {3, 6, 9, 12, 15, 18}
 B = " S = {5, 10, 15, 20}

$$\therefore P(A) = \frac{6}{20}; \quad P(B) = \frac{4}{20}$$

$$\therefore A \cap B = \{15\} \quad \therefore P(A \cap B) = \frac{1}{20}$$

$$\therefore P(A \cup B) = \frac{6}{20} + \frac{4}{20} - \frac{1}{20} = \frac{9}{20}$$

(Ans.)

3.2) Total Students = $15+0=25$

Probability of selecting 1 girl and

$$2 \text{ boys} = \frac{10_4 \times 15_{c_2}}{25_{c_3}}$$

$$= \frac{21}{46} \text{ (Ans)}$$

3.3) Total numbers of balls = $4+5+6=15$

Probability of getting all reds

$$= \frac{5_{c_3}}{15_{c_3}} = \frac{2}{91} \text{ (Ans.)}$$

3.4) Total Engineers = $5 \cdot 6 = 11$

a) $\frac{5_{c_4}}{11_{c_4}} = \frac{1}{16}$

b) $\frac{5_{c_2} 6_{c_2}}{11_{c_4}} = \frac{5}{11} \text{ (Ans.)}$

Name: Md. Tanvir Hosen.
ID :- 20-42488-1

SL:- 14

Class	Frequency (f)	Mid value (x)	$f(x)$	$f \log x$	$\frac{f}{n}$	$\frac{x_i - \bar{x}}{\bar{x} - \bar{x}_0} \quad (\bar{x}_0 = \frac{7.5}{20} = 3.75)$	$ f_i(x_i - \bar{x}) $	$f_i(x_i - \bar{x})^2$
1-2	1	1.5	1.5	0.176	0.06	-2.25	2.25	5.06
2-3	3	2.5	7.5	1.104	0.12	-1.25	3.75	4.687
3-4	8	3.5	28	4.352	0.286	-0.75	2	0.5
4-5	6	4.5	27	3.019	0.133	0.75	4.5	3.875
5-6	2	5.5	11	1.48	0.084	1.75	3.5	6.125
Total	20(n)	75	11.12	5.87			16	19.75

a) Arithmetic mean, $AM = \frac{1}{n} \sum_{i=0}^n f_i x_i = \frac{75}{20} = 3.75$

b) Geometric mean, $GM = \text{Antilog} \left(\frac{1}{n} \sum_{i=1}^n f_i \log x_i \right)$
 $= \text{Antilog} \left(\frac{11.12}{20} \right)$
 $= 3.597$

Harmonic mean, $HM = \frac{n}{\sum_{i=1}^n \frac{f_i}{x_i}} = \frac{20}{5.87} = 3.41$

b)

Class	Frequency (f)	Cumulative frequency (e)
1-2	1	1
2-3	3	4
3-4	8	12
4-5	6	18
5-6	2	20

$$\text{Median} = L + \frac{\frac{n}{2} - c}{f} \times h = 3 + \frac{\frac{20}{2} - 4}{8} \times 1 = 3.75$$

$$\text{Mode} = L + \frac{f_m - f_2}{2f_m - f_1 - f_2} \times h = 3 + \frac{8-3}{8 \times 2 - 3 - 6} \times 1 = 3.71$$

c) As mean > Median > mode, it is positively skewed.

d) Mean deviation, MD = $\frac{1}{n} \sum_{i=1}^n f_i |x_i - \bar{x}| = \frac{16}{20} = 0.8$

e) Variance, $\sigma^2 = \frac{1}{n} \sum_{i=1}^n f_i (x_i - \bar{x})^2 = \frac{19.75}{20} = 0.9875$

standard deviation, $\sigma = \sqrt{\sigma^2} = 0.99$

f) Coefficient of variation, CV = $\frac{\sigma}{\bar{x}} = \frac{0.99}{3.75} \times 100\% = 26.5\%$

$\therefore 11 = 3+2 = \text{maximum value}$

$$\frac{1}{31} = \frac{0.99}{N^2} \quad (1)$$

$$\frac{2}{11} = \frac{0.99}{N^2} \quad (2)$$

3.1 Let, A = multiple of 3 : {3, 6, 9, 12, 15, 18} Ans

B = " " " S = {5, 10, 15, 20}

$$\therefore P(A) = \frac{6}{20}; P(B) = \frac{4}{20}$$

$$\therefore A \cap B = \{15\} \quad \therefore P(A \cap B) = \frac{1}{20}$$

$$\therefore P(A \cup B) = \frac{6}{20} + \frac{4}{20} - \frac{1}{20} = \frac{9}{20}$$

3.2 Total students = 15 + 10 = 25

Probability of selecting 1 girl and 2 boys = $\frac{10C_1 \times 15C_2}{25C_3}$

$$= \frac{21}{210} \text{ Ans}$$

3.3 Total number of balls = 4 + 5 + 6 = 15

Probability of getting all red = $\frac{5C_3}{15C_3} = \frac{2}{91} \text{ Ans}$

3.4 Total engineers = 5 + 6 = 11

a) $\frac{5C_4}{11C_4} = \frac{1}{16}$

b) $\frac{5C_2 \times 6C_2}{11C_4} = \frac{5}{11} \text{ Ans}$

Assignment-3

Name: MD. Shajidul Islam Sadkin
 ID. 20-2P2621-1, serial: 15

From the given dataset.

Interval	f_i	x_i	$f_i x_i$	\bar{x}	$f_i \log x_i$	f_i/x_i
1-2	1	1.5	1.5		$1 \cdot \log(1.5)$	$\frac{1}{1.5}$
2-3	3	2.5	7.5		$3 \log(2.5)$	$\frac{3}{2.5}$
3-4	8	3.5	28	$\frac{75}{20} = 3.75$	$8 \log(3.5)$	$\frac{8}{3.5}$
4-5	6	4.5	27		$6 \log(4.5)$	$\frac{6}{4.5}$
5-6	2	5.5	11		$2 \log(5.5)$	$\frac{2}{5.5}$
Total	20		75		11.122	5.85

① Arithmetic mean $AM = \bar{x} = \frac{1}{n} \sum_{i=1}^n f_i x_i = \frac{75}{20} = 3.75$.

Geometric mean $GM = \bar{x}_G = \text{Antilog} \left(\frac{1}{n} \sum_{i=1}^n f_i \log x_i \right)$

$$= \text{Antilog} \left(\frac{11.122}{20} \right) = 3.60$$

Harmonic mean $HM = \bar{x}_H = \frac{n}{\sum_{i=1}^n \frac{f_i}{x_i}} = \frac{20}{5.85} = 3.42$

$$AM > GM > HM$$

b)

Interval	frequency	Cumulative freq.
1-2	1	1
2-3	3	4
3-4	8	12
4-5	6	18
5-6	2	20

$$\text{Median } m_e = L + \frac{\frac{n}{2} - c}{f} \times h$$

$$= 3 + \frac{\frac{20}{2} - 4}{8} \times 1$$

$$= 3 + \frac{10 - 4}{8}$$

$$= 3 + 0.75$$

$$= 3.75$$

 L = lower limit. n = size of class f = frequency of median class c = cumulative sum of previous class

$$\text{Mode} = L + \frac{f_m - f_1}{2f_m - f_1 - f_2} \times h$$

$$= 3 + \frac{8 - 3}{16 - 3 - 6} \times 1$$

$$= 3 + \frac{5}{7}$$

$$= 3.71$$

 f_m = modal class frequency f_1 = modal class previous frequency f_2 = modal class next frequency.

c) Skewness = mean - median

$$= 3.75 - 3.75$$

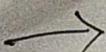
$$= 0.0$$

Skewness ≈ 0 the distribution would be positively skewed. Symmetrical.

d)

Interval	f_i	x_i	$f_i x_i$	\bar{x}	$x_i - \bar{x}$	$ f_i(x_i - \bar{x}) $	$f_i x_i - \bar{x} $
1 - 2	1	1.5	1.5		-2.25	2.25	5.06
2 - 3	3	2.5	7.5		-1.25	3.75	4.67
3 - 4	8	3.5	28	<u>75</u>	-0.25	2	0.5
4 - 5	6	4.5	27	<u>20</u>	0.75	4.5	3.375
5 - 6	2	5.5	11	<u>3.75</u>	1.75	3.5	6.25
Total	= 20		= 75			= 16	= 19.75

Mean deviation: $MD = \frac{1}{n} \sum_{i=1}^n (f_i |x_i - \bar{x}|) = \frac{16}{20} = 0.8$



e)

$$\text{Variance } \sigma^2 = \frac{1}{n} \sum_{i=1}^n f_i(x_i - \bar{x})^2$$

$$= \frac{19.75}{20} = 0.9875$$

Standard deviation $\sigma = \sqrt{\text{variance}} = \sqrt{\sigma^2}$

$$= \sqrt{0.9875} = 0.994$$

f)

$$\text{Coefficient of variation CV: } = \frac{\sigma}{\bar{x}} \times 100\%$$

$$CV = \frac{0.994}{3.75} \times 100\% = 26.51\%$$

$\bar{x} - \mu$	$\bar{x} - \mu$	\bar{x}	$\bar{x} - \mu$	\bar{x}	$\bar{x} - \mu$	\bar{x}	$\bar{x} - \mu$
20.2	22.2	22.2	22.2	22.2	22.2	22.2	22.2
23.4	25.8	25.1	25.1	25.1	25.1	25.1	25.1
2.0	2	20.0	2F	22	2.0	2	2.0
25.8	2.0	2F.0	2F.0	2F.0	2F.0	2F.0	2F.0
22.1	2F.1	2F.1	2F.1	2F.1	2F.1	2F.1	2F.1
21	21	21	21	21	21	21	21

$$S = \sqrt{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}$$

$$S = \sqrt{21^2 + 21^2 + \dots + 21^2}$$

$$S = \sqrt{21^2 \times 20}$$

3.1

Let, A is multiple of 3 = $\{3, 6, 9, 12, 15, 18\}$ with the
 number 1 to 20, $P(A) = \frac{6}{20}$

B is multiple of 5 = $\{5, 10, 15, 20\} = \frac{4}{20}$

$$A \cap B = \{15\} = \frac{1}{20}$$

The Probability of the drawn ticket number is
 multiple of 3 or 5 would be

$$\begin{aligned} P(A \cup B) &= P(A) + P(B) - P(A \cap B) \\ &= \frac{6}{20} + \frac{4}{20} - \frac{1}{20} \\ &= \frac{9}{20} = 0.45 \approx 45\% \end{aligned}$$

3.2

15 boys and 10 girls. Total 25 students.

$$\text{Let, } A = 1 \text{ girl and 2 boys } P(A) = \frac{15C_2 \times 10C_1}{25C_3}$$

$$\begin{aligned} &= \frac{21}{46} = 0.457 \\ &= 45.7\% \end{aligned}$$

3.3

4 white, 5 red. and 6 blue ball Total 15 balls
in the beg.

$$\text{Let } A = \text{all 3 ball is red} \quad P(A) = \frac{5C_3}{15C_3}$$

$$= \frac{2}{91}$$

3.4

5 electrical engineer and 6 computer engineers
total 11 engineers.

a) Let, A = all 4 are electrical engineers

$$P(A) = \frac{5C_4}{11C_4} = \frac{1}{66}$$

b) Let, B = 2 electric and 2 computer engineers

$$P(B) = \frac{5C_2 \times 6C_2}{11C_4} = \frac{5}{11}$$

Name: Sidul Islam Sohag

Serial - 16

Id: 20-42668-1 Section: 0

Class	Frequencies (f)	Mid value (x̄)	f(x̄)	f log x̄	$\frac{f}{n}$	$x_i - \bar{x}$ ($\bar{x} = \frac{75}{20} = 3.75$)	$f_i / n - \bar{x}$	$f(x_i - \bar{x})^2$
1-2	1	1.5	1.5	0.176	0.06	-2.25	2.25	5.06
2-3	3	2.5	7.5	1.194	0.12	-1.25	3.75	4.87
3-4	8	3.5	28	4.352	0.286	-0.25	2	0.5
4-5	6	4.5	27	3.919	0.33	0.75	4.5	3.375
5-6	2	5.5	11	1.48	0.08	1.75	3.5	6.125
Total	20(x̄)		75	11.12	5.87		16	19.75

a) arithmetic mean, $AM = \frac{1}{n} \sum_{i=0}^n f_i x_i$

$$AM = \frac{1}{20} \sum_{i=0}^n f_i x_i = \frac{75}{20} = 3.75$$

b) Geometric mean, $GM = \text{Antilog} \left(\frac{1}{n} \sum_{i=1}^n f_i \log x_i \right)$

$$GM = \text{Antilog} \left(\frac{11.12}{20} \right) = 3.597$$

Harmonic mean, $HM = \frac{n}{\sum_{i=1}^n \frac{f_i}{x_i}} = \frac{20}{5.87} = 3.41$

1.5972 x 10^-12

b)

Class	Frequency (f)	Cumulative frequency (cf)
1-2	1	1
2-3	3	4
3-4	8	12
4-5	6	18
5-6	2	20

$$\text{Median} = L + \frac{\frac{n}{2} - C}{f} \times h$$

$$= 3 + \frac{20/2 - 4}{8} \times 1 = 3.75$$

$$\text{Mode} = L + \frac{f_m - f_{m-1}}{2f_m - f_1 - f_2} \times h$$

$$= 3 + \frac{8 - 3}{16 - 3 - 6} \times 1$$

$$= 3.71$$

c) As Mean > Median > Mode,
If is Positively skewed.

d) Mean deviation, $M.D. = \frac{1}{n} \sum_{i=1}^n f_i |x_i - \bar{x}|$

$\text{Mean} = \frac{16}{20} = 0.8$

e) Variance, $S^2 = \frac{1}{n} \sum_{i=1}^n f_i (x_i - \bar{x})^2 = \frac{55.62}{20}$

standard deviation, $S = \sqrt{\text{Variance}} = \sqrt{2.781} = 1.66$

$S = 1.66$ (Ans)

f) coefficient of variation, $CV = \frac{S}{\bar{x}} \times 100$

$$= \frac{1.66}{3.75} \times 100$$

$$= 44.27$$

$C.V = \frac{S}{\bar{x}} \times 100$ to find mean lot size (E.S.)

$C.V = \frac{S}{\bar{x}} \times 100$ to find standard deviation

3.1) Let, A = multiple of 3 = {3, 6, 9, 12, 15, 18}

B = multiple of 5 = {5, 10, 15, 20}

$$\therefore P(A) = \frac{6}{20}; P(B) = \frac{4}{20}$$
$$\therefore P(A \cap B) = \frac{1}{20}$$
$$\therefore A \cap B = \{15\}$$

$$\therefore P(A \cup B) = \frac{6}{20} + \frac{4}{20} - \frac{1}{20} = \frac{9}{20}$$

Ans.

3.2) Total students = 15 + 0 = 25

Probability of selecting 1 girl and

$$2 \text{ boys} = \frac{10C_1 \times 15C_2}{25C_3}$$

$$= \frac{27}{46}$$

Ans.

3.3) Total number of balls = 4 + 5 + 6 = 15

Probability of getting all red = $\frac{5C_3}{15C_3}$

Ans

3.4] Total engineers = $5+6=11$

a) $\frac{5c_4}{11c_4} = \frac{1}{16}$

b) $\frac{5c_2}{11c_4} = \frac{5}{11}$ Ans,

— End —