

Name : Md. Altabur Rahman

ID : 20-92107-1

Assignment

11.1

x	y	Σxy	Σx^2	Σy^2
11.8	10.4	122.72	139.24	108.16
12.5	16.5	206.25	156.25	272.25
15.7	22.9	359.53	246.49	524.41
19.2	26.6	510.72	368.64	707.56
21.9	33.8	740.22	479.61	1142.44
23.3	42.8	997.24	542.89	1831.34
$\Sigma x = 104.4$	$\Sigma y = 153$	$\Sigma xy = 2936.68$	$\Sigma x^2 = 1933.12$	$\Sigma y^2 = 4586.66$

$$\begin{aligned}(a) \quad SS(x) &= \Sigma x^2 - \frac{(\Sigma x)^2}{n} \\&= 1933.12 - \frac{(104.4)^2}{6} \\&= 116.56\end{aligned}$$

$$\begin{aligned}
 SS(y) &= \sum y^2 - \frac{(\sum y)^2}{n} \\
 &= 4586.66 - \frac{(153)^2}{6} \\
 &= 685.15
 \end{aligned}$$

$$\begin{aligned}
 SP(xy) &= \sum xy - \frac{\sum x \sum y}{n} \\
 &= 2936.68 - \frac{(104.4) \times (153)}{6} \\
 &= 279.98
 \end{aligned}$$

$$\begin{aligned}
 r &= \frac{SP(xy)}{\sqrt{SS(x) \times SS(y)}} \\
 &= \frac{279.98}{\sqrt{116.56 \times 685.15}} \\
 &= 0.9713
 \end{aligned}$$

$$(b) H_0 : \rho = 0 \quad \text{vs} \quad H_1 : \rho \neq 0$$

$$\begin{aligned} t &= \frac{r\sqrt{n-2}}{\sqrt{1-r^2}} \\ &= \frac{0.97\sqrt{6-2}}{\sqrt{1-(0.97)^2}} \\ &= 8.162 > t_4 \end{aligned}$$

$$\begin{aligned} (c) \quad b &= \frac{SP(xy)}{SS(x)} \\ &= \frac{274.48}{116.56} \\ &= 2.35 \end{aligned}$$

$$\begin{aligned} a &= \frac{\sum y}{n} - b \frac{\sum x}{n} \\ &= \frac{153}{6} - 2.35 \times \frac{104.4}{6} \\ &= -15.4747 \end{aligned}$$

$$\begin{aligned} \hat{y} &= a + bx \\ &= -15.4747 + 2.35x \end{aligned}$$

$$(d) \text{ if } x = 25.5;$$

$$y = -15.47 + (2.35 \times 25.5) \\ = 44.475$$

$$(e) H_0: \beta = 0 \text{ vs } H_1: \beta_1 \neq 0$$

$$s^2 = \frac{ss(y) - b(sp(xy))}{n-2} \\ = \frac{685.16 - 2.35(274.48)}{9} \\ = 9.7$$

$$t = \frac{b}{\sqrt{\frac{s^2}{ss(x)}}} \\ = \frac{2.35}{\sqrt{9.7/116.36}} \\ = 8.16 > t_{\alpha}$$

Regression is significant.