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2.4. a/ Here the population size is 25 ~~and  $N=25$~~   
and sample size  $n$

So, Sampling interval  $H = \frac{N}{n} = \frac{25}{4} = 6.25 \approx 6$

Now  
 $1-H = 1-6$  any random number  $1-H$  in 5

Select numbers 5, 11, 17, 23

Serial	5	11	17	23
Observation value	7	7	7	9

$$\text{Now } s^2 = \frac{1}{n-1} \left[ \sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{4-1} \left[ 228 - \frac{100}{4} \right] = 4$$

$$V(L) = \frac{(N-n)}{Nn} s^2 = \frac{25-4}{25 \times 4}$$

$$V(L)^2 = \frac{21}{100} = 0.21$$



And  $\bar{v}(\bar{x}) = \sqrt{p \cdot 21} = 0.4583$

the estimate of standard error of population

total is

$$v(\hat{x}) = N^2 (v\bar{x}) = 25^2 \times 0.21 = 131.25$$

and  $\bar{v} = \sqrt{v(\hat{x})} = \sqrt{131.25} = 11.4569$

b. Estimated the population of days when less than 8 signal are received.

In our selected sample there are 3 signal are less than 8 so,  $n = 3$

$$p = \frac{q}{n} = \frac{3}{4} = 0.75$$

9.5 using simple random sampling method

the 5 random numbers are 11, 16, 9, 12, 10

random number	11	16	9	12	10
observation	1	8	2	0	4



$$\text{Hence } s^2 = \frac{1}{n-1} \left[ \sum x^2 - \frac{(\sum x)^2}{n} \right]$$

The variance of sample mean is  $V(\bar{x}) =$

$$\frac{N-n}{N} s^2$$

$$= \frac{30-5}{30} (10)$$

$$= 1.67$$

$$\text{and } \sigma = \sqrt{V(\bar{x})} = \sqrt{1.67} = 1.292$$

The estimate of standard error of population  
is

$$V(\bar{x}) = N \sigma^2 = 30^2 \times 1.67 = ~~1503~~ 1503$$

$$\text{and } \sigma = \sqrt{V(\bar{x})} = \sqrt{1503} = 38.768$$

Q.6] Given that

margin of error  $d = 0.1$

$$p = 0.45$$

$$n = 0.55$$

$$z = 1.96$$



The ~~sample~~ size is given by  $n = \frac{z^2 p q}{d^2}$

$$= \frac{(1.96)^2 \times 0.45 \times 0.55}{(0.1)^2}$$

$$= 95.07 \approx 95$$

Q.7] Using simple random sampling selected

11, 16, 9, 12

Now

12 random days	11	16	9	12
observation	11	7	7	45

Here  $s^2 = \frac{1}{n-1} \left[ \sum x_i^2 - \frac{(\sum x_i)^2}{n} \right]$

$$= \left[ 2244 - \frac{4100}{4} \right] = 339.67$$

The variance of sample mean is  $V_{\bar{y}} = \frac{N-n}{N} s^2$

$$= \frac{23-4}{23 \times 4} \times 339.67$$

$$= 70.15$$



The standard error of estimate of mean is

$$s_{\bar{y}} = \sqrt{V(\bar{y})} = \sqrt{70 \cdot 15} = 8.37$$

Q.8) Given that

margin of  $d = 0.05$

$$p = 0.3$$

$$q = 0.7$$

$$\text{and } z = 1.96$$

The sample size  $n$  is given by  $n = \frac{z^2 pq}{d^2}$

$$= \frac{(1.96)^2 \times 0.3 \times 0.7}{(0.05)^2}$$

$$= 322.67 \approx 323$$