

Final Assignment - 01

Section: 0

Serial: 12

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Problem - 01

Trend values using Semi-average method:

Year	Income	3-year semi-total	3-year semi-average	Trend values
2008	43	158	52.66	$52.66 - 10.56 = 42.1$
2009	51			$42.1 + 10.56 = 52.66$
2010	64			$52.66 + 10.56 = 63.22$
2011	76	253	84.33	$63.22 + 10.56 = 73.78$
2012	81			$73.78 + 10.56 = 84.34$
2013	96			$84.34 + 10.56 = 94.9$

Difference between central years = $2012 - 2009$
 $= 3$ years

Difference between the semi-averages,

$$= 84.33 - 52.66$$

$$= 31.67$$

Increase in trend value for 1-year,

$$= 31.67 / 3$$

$$= 10.56$$

Problem - 02

Year	Loan	3-year semi Total	3-year semi average
2004	40	—	—
2005	42	121	40.33
2006	39	106	35.33
2007	25	91	30.33
2008	27	103	34.33
2009	51	106	35.33
2010	28	105	35
2011	26	85	28.33
2012	31	87	29
2013	30	109	36.33
2014	48	—	—

Problem - 03 //

Given, Probability of,

(9-10) and (10-11) is 0.6

(10-11) is 0.8

∴ The probability of entering customers up to 2PM to 9 AM (starting) is at Stage - 05.

$$\therefore P = \begin{bmatrix} P_{00} & P_{01} \\ P_{10} & P_{11} \end{bmatrix} = \begin{bmatrix} 0.6 & 0.4 \\ 0.8 & 0.2 \end{bmatrix}$$

$$\begin{aligned} \therefore P^5 &= [P] \times [P] \times [P] \times [P] \times [P] \\ &= \begin{bmatrix} 0.6665 & 0.3334 \\ 0.6668 & 0.3331 \end{bmatrix} \end{aligned}$$

∴ The required probability is 0.6665 or 66.65 %

(Ans.)

Problem - 04

Given,

Poisson rate of email entering, $\lambda = 2$ per minute

Probability of elapsed time between the entrance of 10th and 11th mail is,

(i) more than 1 minute,

$$P(T > 1) = e^{-\lambda t} = e^{-(2 \times 1)} = 0.13533$$

(ii) less than 2 minutes,

~~$$P(T < 0.5)$$~~

$$\begin{aligned} P(T < 2) &= 1 - e^{-\lambda t} = 1 - e^{-(2 \times 2)} \\ &= 1 - 0.01831 \\ &= 0.98169 \end{aligned}$$

(iii) between 1 to 2 minutes,

$$\begin{aligned} P(1 < T < 2) &= e^{-\lambda t_1} - e^{-\lambda t_2} = e^{-(2 \times 1)} - e^{-(2 \times 2)} \\ &= (0.13533 - 0.01831) \\ &= 0.11702 \quad (\text{Ans.}) \end{aligned}$$