

"Ans-no $\Rightarrow 10.2$ "

Test statistic,

$$\begin{aligned} \chi^2 &= \sum \frac{O_i^2}{E_i} - n & E_i &= \frac{n}{K} \\ & & &= \frac{206}{4} = 51.5 \\ &= \frac{1}{51.5} \times [50^2 + 42^2 + 32^2 + 82^2] \\ &= 27.243 \end{aligned}$$

$$\text{Since, } \chi^2 > \chi_{K-1}^2 = \chi^2 > \chi_{4-1}^2 = \chi^2 > \chi_{3}^2 = 7.815$$

H_0 is not accepted, The proportion of road accident are not similar in various highways of Bangladesh. [Ans]

"Ans-no $\Rightarrow 10.4$ "

Test statistic,

$$\begin{aligned} \chi^2 &= \sum \frac{O_i^2}{E_i} - n & E_i &= \frac{n}{K} = \frac{1000}{4} \\ & & &= 250. \\ &= \frac{1}{250} \times [250^2 + 450^2 + 150^2 + 150^2] - 1000 \end{aligned}$$

$$\text{Since, } \chi^2 > \chi_{K-1}^2 = \chi^2 > \chi_{4-1}^2 = \chi^2 > \chi_{3}^2$$

$= 7.815$; H_0 is not accepted, the proportion of female students are not similar in various department of ATUB. [Ans]

"Ans-no $\Rightarrow 10.5$ "

$$\text{Here, } \bar{x} = \frac{1}{n} \sum x$$

$$= \frac{1}{36} \times 761.6 = 21.15$$

$$s^2 = \frac{1}{n-1} \left[\sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{35} \times \left[16125.5 - \frac{(761.6)^2}{36} \right]$$

$$= 0.384$$

$$s = \sqrt{0.384} = 0.6197.$$

$$\begin{aligned}\text{Test statistic, } z &= \frac{\bar{x} - \mu_0}{s/\sqrt{n}} \\ &= \frac{21.15 - 21}{0.6197/\sqrt{36}} \\ &= 1.452 < 1.96\end{aligned}$$

So, H_0 is accepted, the population mean 21. [Ans]

"Ans-no \Rightarrow 10.7"

We need to test, $H_0: P = P_0 = 0.40$ vs

$H_1: P \neq P_0$.

$$p = \frac{a}{n} = \frac{8}{25} = 0.32$$

$$\begin{aligned}\text{Test statistic, } z &= \frac{p - P_0}{\sqrt{\frac{P_0 Q_0}{n}}} \\ &= \frac{0.32 - 0.40}{\sqrt{\frac{0.40 \times 0.60}{25}}} = -0.816\end{aligned}$$

Since, $|z| < 1.96$, H_0 is accepted, It can be considered overall proportion of female students 0.40 in AIUB.

[Ans]

"Ans-no \Rightarrow 10.9"

We need to test $H_0: P_1 = P_2$ vs $H_1: P_1 \neq P_2$

Test statistic,

$$\begin{aligned}z &= \frac{P_1 - P_2}{\sqrt{PQ \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}} \\ &= \frac{0.25 - 0.144}{\sqrt{0.191 \times 0.809 \times \left(\frac{1}{100} + \frac{1}{125} \right)}} \\ &= 2\end{aligned}$$

$$\begin{aligned}P_1 &= \frac{25}{100} = 0.25 \\ P_2 &= \frac{18}{125} = 0.144 \\ P &= \frac{a_1 + a_2}{n_1 + n_2} = \frac{25 + 18}{100 + 125} \\ &= 0.191 \\ Q &= 1 - P = 0.809\end{aligned}$$

Since $|Z| > 1.96$; H_0 is rejected. The production problem is not same for boys and girls at AIUB [Ans] -

Ans-no $\Rightarrow 10.11$

Blood Pressure	Heart Problem		Total
	Yes	No	
High	150	120	270
Not high	122	158	280
Total	272	278	550

H_0 : heart problem; does not depend on blood pressure.

H_1 : blood pressure associated with heart problem.

$$\begin{aligned} \chi^2 &= \frac{n(ad - bc)^2}{(a+b)(a+c)(b+d)(c+d)} \\ &= \frac{550 \times (150 \times 158 - 120 \times 122)^2}{270 \times 272 \times 278 \times 280} \\ &= 7.897. \end{aligned}$$

Since, $\chi^2 > \chi^2_{\alpha} = 3.84$; H_0 is rejected
So, blood pressure associated with heart problem. [Ans]

Ans-no $\Rightarrow 10.12$

Residential Origin	Full attention		Total
	Yes	No	
Rural	138	64	202
Urban	64	84	148
Total	202	148	350

H_0 : Students does not classified by their residential origin and full attention

H_1 : Origin and full attention are associated.

$$\begin{aligned} \chi^2 &= \frac{n(ad - bc)^2}{(a+b)(a+c)(b+d)(c+d)} \\ &= \frac{350 \times (138 \times 84 - 64 \times 64)^2}{202 \times 202 \times 148 \times 148} \\ &= 22. \end{aligned}$$

Since, $\chi^2 > \chi^2_{12} = 3.84$, H_0 is rejected; origin and full attention are associated.

[Ans]