

Final Assignment 4

Name: Khan, Md. Shamim Masud

Serial: 3

Section: 0

ID: 18-36264-1

11.11

x	y	xy	x^2	y^2
11.8	10.4	122.72	139.24	108.16
12.5	16.5	206.25	156.25	272.25
15.7	22.9	359.53	246.49	524.41
19.2	26.6	510.72	368.64	707.56
21.9	33.8	740.22	479.61	1142.44
28.3	42.8	997.24	542.89	1831.84
$\sum x = 104.4$	$\sum y = 153$	$\sum xy = 2936.68$	$\sum x^2 = 1933.12$	$\sum y^2 = 2936.68$

Compute Correlation Coefficient

$$\begin{aligned}
 SS(x) &= \sum x^2 - \frac{(\sum x)^2}{n} \\
 &= 1933.12 - \frac{(104.4)^2}{6} \\
 &= 116.56
 \end{aligned}$$

$$\begin{aligned}
 SS(Y) &= \sum y^2 - \frac{(\sum y)^2}{n} \\
 &= 4586.66 - \frac{(153)^2}{6} \\
 &= 685.16
 \end{aligned}$$

$$\begin{aligned}
 SP(xy) &= \sum xy - \frac{\sum x \sum y}{n} \\
 &= 2936.68 - \frac{(104.4 \times 153)}{6} \\
 &= 274.48
 \end{aligned}$$

$$\therefore r = \frac{SP(xy)}{\sqrt{SS(x)SS(y)}} = \frac{274.48}{\sqrt{116.56 \times 685.16}} = .98$$

\therefore The correlation between variable (x) and (y) is strongly positive.

Performing hypothesis test

$H_0: \rho = 0$ against $H_A: \rho \neq 0$

$$t = \frac{r \sqrt{n-2}}{\sqrt{1-r^2}} \sim t_{n-2}$$

$$= \frac{.98 \sqrt{6-2}}{\sqrt{1-(.98)^2}}$$

$$= 9.84$$

$|t| > t_{(n-2)=4}$; thus H_0 is rejected.

© fitting regression line of y on x

$$a = \bar{y} - b\bar{x} = \frac{\sum y}{n} - b \frac{\sum x}{n}$$

$$= \frac{153}{6} - b \frac{1044}{6} \quad \text{--- (1)}$$

$$b = \frac{SP(xy)}{SS(x)} = \frac{274.48}{116.56} \\ = 2.36$$

From (1) \Rightarrow

$$a = \frac{153}{6} - (2.36) \frac{1044}{6}$$

$$= -15.564$$

$$\text{Fitted line: } \hat{y} = -15.564 + 2.36x$$

④ Lending rate when the inflation rate will be 25.5

$$\text{If } x = 25.5, \text{ then } y = -15.564 + (2.36 \times 25.5)$$

$$= 44.616 \text{ (ans)}$$

⑥ We need to test $H_0: \beta = 0$ vs $H_1: \beta \neq 0$

test static:

$$|t| = \frac{b}{\sqrt{\frac{S^v}{SS(x)}}$$

$$S^v = \frac{SS(y) - bSP(xy)}{n-2} = \frac{685.15 - (2.36 \times 274.18)}{6-2}$$
$$= 523.2168$$

$$|t| = \frac{2.36}{\sqrt{\frac{523.2168}{116.56}}}$$
$$= 1.11$$

$\therefore |t| < t_4 = 2.776$, So, H_0 is Accepted