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Assignment-2

Q.4/ We know,

$$\text{Sampling interval, } K = \frac{N}{n} \\ = \frac{25}{4} = 6.25 \approx 6$$

Here, $K=6$ and 6 is one digit number, we need to find out only one value (first value) between $(1-K)$ and it must be less from the value of K .

Random Number	5	11	17	23
Signal Received	7	7	7	9

Observation(x)	6	8	7	10	7	6	9	11	4	2	7	7	12
Serial No	1	2	3	4	5	6	7	8	9	10	11	12	13

Observation(x)	9	11	3	7	8	5	6	7	6	9	11	4
Serial No	14	15	16	17	18	19	20	21	22	23	24	25

a) Here,

$$\text{mean, } (\bar{x}) = \frac{30}{4} \\ = 7.5$$

$$\therefore \text{Total number} = N\bar{x} \\ = (25 \times 7.5) \\ = 187.5$$

$$\therefore \text{Standard error of total } s.e(\bar{x}) = \sqrt{V(\bar{x})} \\ V(\bar{x}) = N^2 V(x)$$

Here,

$$V(\bar{x}) = \frac{N-n}{Nn} S^2$$

$$S^2 = \frac{1}{n-1} \left| \sum x^2 - \frac{(2n)^2}{n} \right|$$

$$= \frac{1}{3} \left| 228 - \frac{(30)^2}{4} \right|$$

$$= 1$$

$$\therefore V(\hat{n}) = \frac{25-4}{25 \times 4} (1)$$

$$= 0.21$$

$$\therefore V(\hat{n}) = (25)^2 \times (0.21)$$

$$= 131.25$$

Now,

$$s.e(\hat{x}) = \sqrt{V(\hat{x})}$$

$$= \sqrt{131.25} = 11.46 \text{ Ans.}$$

b) The Proportion of days which less than 8 days is given by $P = \frac{a}{n}$.

Here, $a = 3$ [Number of days which less than 8]

$$n = 4 \text{ [given];}$$

$$P = \frac{3}{4}$$

$$= 0.75 \text{ Ans}$$

9.5]

x	4	3	0	2	6	7	4	3	2	0	1	0	3	0	6	8
Serial	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
x	0	1	4	3	2	6	3	7	5	8	0	2	3	5		
Serial	17	18	19	20	21	22	23	24	25	26	27	28	29	30		

Here,
 $N=30$. We need to select sample
 Size, $n=5$ using Random table. As,
 $N=28$ which is 2 digits number.
 So, We need to select random
 number of two digits.

Random no.	11	16	09	12	19
Faded out Signals	1	8	2	0	4

$$\therefore \text{Mean} = \frac{1}{n} \sum x = \frac{15}{5} = 3$$

$$\therefore \text{Estimate total, } \hat{\mu} = N\bar{x} \\ = 30 \times 3 \\ = 90$$

Standard error of total, $s.e(\hat{X}) = \sqrt{V(\hat{X})}$

Here,

$$V(\hat{X}) = N^2 V(\bar{x})$$

$$\therefore V(\bar{x}) = \frac{N-n}{Nn} s^2$$

$$s^2 = \frac{1}{n-1} \left[\sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{4} \left[85 - \frac{(15)^2}{5} \right]$$

$$= \frac{1}{4} \times 40$$

$$= 10$$

$$\therefore V(\bar{x}) = \frac{30-5}{30 \times 5} \times 10$$

$$= 1.67$$

$$\therefore \text{Variance, } V(\hat{\mu}) = (30)^2 \cdot (1.67) \\ = 1503$$

$$\therefore \text{Standard error of total. s.e}(\bar{x}) = \sqrt{V(\bar{x})}$$

$$= \sqrt{1503}$$

$$= 38.77$$

Ans.

9.6]

Hence,

$$p = 0.45, q = 0.55$$

$$d = 0.1$$

We know,

The sample size n is given by,

$$n = \frac{z^2 pq}{d^2}$$

$$= \frac{(1.96)^2 (0.45)(0.55)}{(0.1)^2}$$

$$= 95$$

Q.7)

X	10	7	6	9	11	4	2	7	7	9	11	45	8	7
Serial No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14
X	10	7	6	9	11	4	2	7	7					
Serial No.	15	16	17	18	19	20	21	22	23					

Here, $N = 23$ which is 2 digits. So, we need to select Random number of 2 digits, upto 4 sample, by following Random number Table.

Random Number	11	16	09	12
Mails received	11	7	7	45

$$\therefore \text{Mean} = \frac{1}{n} \sum x = \frac{70}{4} = 17.5 \approx 17$$

$$\therefore \text{Standard error of mean, } s.e(\bar{x}) = \sqrt{V(\bar{x})}$$

Hence,

$$\text{Variance, } V(\bar{x}) = \frac{N-n}{Nn} s^2$$

$$\therefore s^2 = \frac{1}{n-1} \left[\sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{3} \left[2244 - \frac{4900}{4} \right]$$

$$= 339.67$$

$$\therefore V(x) = \frac{23-4}{23 \times 4} \times 339.67$$
$$= 70.15$$

Standard error of Mean, $S.E(\bar{x}) = \sqrt{V(\bar{x})}$

$$= \sqrt{70.15}$$
$$= 8.38$$

Ans,

9.8

Hence,

$$p = 0.3, q = 0.7$$

$$d = 0.05, n = ?$$

We know,

$$\text{The sample size of, } n = \frac{z^2 pq}{d^2}$$
$$= \frac{(1.96)^2 \times 0.3 \times 0.7}{(0.05)^2}$$

$$= \cancel{332}$$

$$\therefore n = 322.69$$

Ans.