

Assignment - 2

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Q.9

$$k = \frac{N}{n}$$
$$= \frac{25}{4}$$

$$= 6.25 \sim 6$$

$k=6$ is an one digit number. We need to find the first value.

Random number	5	11	17	23
Signals received	7	7	7	9

Observation _(x)	5	8	7	10	7	6	9	11	9	2	7	7	
Serial no.	1	2	3	4	5	6	7	8	9	10	11	12	
Observation(x)	12	9	11	3	7	8	5	6	7	6	9	11	9
Serial no.	13	14	15	16	17	18	19	20	21	22	23	24	25

$$(a) \text{ mean } (\bar{x}) = \frac{30}{4}$$

$$= 7.5$$

$$\text{Total number} = N\bar{x}$$

$$= (25 \times 7.5)$$

$$= 187.5$$

$$\therefore \text{standard error of total } \hat{x} = \sqrt{V(\hat{x})}$$

$$V(\hat{x}) = N^2 V(\bar{x})$$

$$\text{there, } V(\bar{x}) = \frac{N-n}{Nn} s^2$$

$$s^2 = \frac{1}{n-1} \left[\sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{3} \left[220 - \frac{(30)^2}{4} \right]$$

$$= 1$$

$$\therefore V(\hat{x}) = \frac{25-4}{25 \times 4} (1)$$

$$= 0.21$$

$$\therefore V(\hat{x}) = (2.5)^2 \times (0.21)$$

$$= 131.25$$

$$se. (\hat{x}) = \sqrt{V(\hat{x})}$$

$$= \sqrt{131.25}$$

$$= 11.46. \text{ (Ans)}$$

9.5

observation (y)	9	3	0	2	6	7	4	3	2	0	1	0	3	0	6
serial	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Observation (x)	8	0	1	9	3	2	6	3	7	5	8	0	2	3	5
Serial	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30

$$N = 30$$

$n = 5$ as 2 digit number

Random no.	11	16	9	12	19
faded out signals	1	8	2	0	9

$$\text{mean} = \frac{1}{n} \sum x$$

$$= \frac{15}{5}$$

$$= 3$$

$$\text{Estimated total } \hat{\mu} = N \bar{x}$$

$$= 30 \times 3$$

$$= 90$$

standard error of total $se(\bar{x}) = \sqrt{V(\bar{x})}$

$$V(\bar{x}) = N^2 v(\bar{x})$$

$$\therefore v(\bar{x}) = \frac{N-n}{Nn} s^2$$

$$s^2 = \frac{1}{n-1} \left[\sum x_i^2 - \frac{(\sum x_i)^2}{n} \right]$$

$$= \frac{1}{9} \left[85 - \frac{(15)^2}{5} \right]$$

$$= \frac{1}{9} \times 90$$

$$= 10$$

$$v(\bar{x}) = \frac{30-5}{30 \times 5} \times 10$$

$$= 1.67$$

$$\text{variance, } v(\bar{x}) = (30)^2 \cdot (1.67)$$

$$= 1503$$

Standard error of total,

$$se(\bar{x}) = \sqrt{v(\bar{x})}$$

$$= \sqrt{1503}$$

$$= 38.77. \text{ (Ans.)}$$

9.6

given,

$$p = 0.45$$

$$q = 0.55$$

$$d = 0.1$$

$$n = \frac{z^2 p q}{d^2}$$

$$= \frac{(1.96)^2 (0.45)(0.55)}{(0.1)^2}$$

$$= 95$$

9.7

observation (x)	10	7	6	9	11	4	2	7	7	9	11	45
Serial no.	1	2	3	4	5	6	7	8	9	10	11	12
observation (x)	8	7	10	7	6	9	11	4	2	7	7	
Serial no.	13	14	15	16	17	18	19	20	21	22	23	24

$N = 23$

sample = 4

Random number	11	16	9	12
mails received	11	7	7	45

$$\therefore \text{mean} = \frac{1}{n} \sum x$$

$$= \frac{70}{4}$$

$$= 17.5 \sim 17$$

$$se(\bar{x}) = \sqrt{v(\bar{x})}$$

variance $V(\bar{x}) = \frac{N \cdot n}{Nn} s^2$

$$s^2 = \frac{1}{n-1} \left[\sum x^2 - \frac{(\sum x)^2}{n} \right]$$

$$= \frac{1}{3} \left[2244 - \frac{9900}{9} \right]$$

$$= 339.67$$

$$V(\bar{x}) = \frac{23-4}{23 \times 4} \times 339.67$$

$$= 70.15$$

$$se(\bar{x}) = \sqrt{V(\bar{x})}$$

$$= \sqrt{70.15}$$

$$= 8.30.$$

(Ans)

[9.8]

$$p = 0.3$$

$$q = 0.7$$

$$d = 0.05$$

$$n = ?$$

$$\begin{aligned}\text{The sample size of, } n &= \frac{z^2 p q}{d^2} \\ &= \frac{(1.96)^2 \times 0.3 \times 0.7}{(0.05)^2} \\ &= 322.69\end{aligned}$$

(Ans)