

Algorithm Code Book

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Chapter 1

Data Structure

1.1 Trie

1.1.1 Static Trie

```
1 #define Max 10005
2 int getId(char c)
3 {
4     return c>='a'?c-'a':c-'A'+26;
5 }
6 struct Trie
7 {
8     struct Tree
9     {
10         int Next[52];
11         bool word;
12         void clear()
13         {
14             word=false;
15             memset(Next,-1,sizeof(Next));
16         }
17     }T[Max];
18     int ptr;
19     void clear()
20     {
21         ptr=1;
22         T[0].clear();
23         memset(T[0].Next,0,sizeof(T[0].Next));
24     }
25     void Insert(const char *str)
26     {
27         int p=0;
28         for(int i=0;str[i];i++)
29         {
30             int id=getId(str[i]);
31             if(T[p].Next[id]<=0)
32             {
33                 T[p].Next[id]=ptr;
34                 T[ptr++].clear();
35             }
36             p=T[p].Next[id];
37         }
38         T[p].word=true;
39     }
40     bool Search(const char *str)
41     {
42         int p=0;
43         for(int i=0;str[i];i++)
44         {
45             int id=getId(str[i]);
46             if(T[p].Next[id]>0)
47             {
```

```

48         p=T[p].Next[id];
49     }
50     else return false;
51 }
52 return T[p].word;
53 }
54 };
55 Trie A;

```

1.2 RMQ

1.2.1 Bit

1D Bit

```

1 #define MaxVal 100000
2 int Bit[MaxVal];
3 /**find sum from 1 to idx**/
4 int read(int idx)
5 {
6     int sum = 0;
7     while (idx > 0)
8     {
9         sum += Bit[idx];
10        idx -= (idx & -idx);
11    }
12    return sum;
13 }
14 /**update value ind to MaxVal**/
15 void update(int idx ,int val)
16 {
17     while (idx <= MaxVal)
18     {
19         Bit[idx] += val;
20         idx += (idx & -idx);
21     }
22 }
23
24 /**Find the value of idx**/
25 int readSingle(int idx)
26 {
27     int sum = Bit[idx]; /// sum will be decreased
28     if (idx > 0) /// special case
29     {
30         int z = idx - (idx & -idx); /// make z first
31         idx--; /// idx is no important any more, so instead y, you can use idx
32         while (idx != z) /// at some iteration idx (y) will become z
33         {
34             sum -= Bit[idx]; /// substruct Bit frequency which is between y and "the
35             same path"
36             idx -= (idx & -idx);
37         }
38     }
39     return sum;

```

2D Bit

```

1 void updatey(int x , int y , int val)
2 {
3     while (y <= max_y)
4     {
5         tree[x][y] += val;
6         y += (y & -y);
7     }
8 }
9 void update(int x , int y , int val)
10 {
11     while (x <= max_x)

```

```

12     {
13         updatey(x , y , val); // this function should update array tree[x]
14         x += (x & -x);
15     }
16 }

```

1.2.2 Square Root Decomposition

```

1  #include<bits/stdc++.h>
2  using namespace std;
3  const int sz=100005;
4  const int inf=(1<<28);
5  template<typename t> t MIN3(t a,t b, t c)
6  {
7      return min(a,min(b,c));
8  }
9  int BLOCK[400];
10 int arr[sz];
11 int getId(int indx,int blockSZ)
12 {
13     return indx/blockSZ;
14 }
15 void init(int sz)
16 {
17     for(int i=0; i<=sz; i++)BLOCK[i]=inf;
18 }
19 void update(int val,int indx,int blockSZ)
20 {
21     int id=getId(indx,blockSZ);
22     BLOCK[id]=min(BLOCK[id],val);
23 }
24 int query(int L,int R,int blockSZ)
25 {
26     int lid=getId(L,blockSZ);
27     int rid=getId(R,blockSZ);
28     if(lid==rid)
29     {
30         int ret=inf;
31         for(int i=L; i<=R; i++)ret=min(ret,arr[i]);
32         return ret;
33     }
34     int m1=inf,m2=inf,m3=inf;
35     for(int i=L; i<(lid+1)*blockSZ; i++)m1=min(m1,arr[i]);
36     for(int i=lid+1; i<rid; i++)m2=min(m2,BLOCK[i]);
37     for(int i=rid*blockSZ; i<=R; i++)m3=min(m3,arr[i]);
38     return MIN3(m1,m2,m3);
39 }
40 int main()
41 {
42     int N,Q;
43     scanf("%d %d",&N,&Q);
44     int blockSZ=sqrt(N);
45     init(blockSZ);
46     for(int i=0; i<N; i++)
47     {
48         int x;
49         scanf("%d",&x);
50         arr[i]=x;
51         update(x,i,blockSZ);
52     }
53     while(Q--)
54     {
55         int x,y;
56         scanf("%d %d",&x,&y);
57         printf("%d\n",query(x,y,blockSZ));
58     }
59     return 0;
60 }

```

1.2.3 MO's Algorithm

```

1  /**
2   MO's Algorithm
3   problem: http://www.spoj.com/problems/DQUERY
4
5   MOs algorithm is just an order in which we process the queries.
6   We were given M queries , we will re-order the queries in a particular order and
7   then process them.
8   Clearly, this is an off-line algorithm. Each query has L and R, we will call
9   them opening and closing.
10  Let us divide the given input array into Sqrt(N) blocks.
11  Each block will be  $N / \text{Sqrt}(N) = \text{Sqrt}(N)$  size.
12  Each opening has to fall in one of these blocks.
13  Each closing has to fall in one of these blocks.
14
15  All the queries are first ordered in ascending order of their block number (
16  block number is the block in which its opening falls).
17  Ties are ordered in ascending order of their R value.
18
19  */
20 #include<bits/stdc++.h>
21 using namespace std;
22 #define Mx 30005
23 #define MxNum 1000005
24 int BlockSize;
25 int Answer;
26 int Freq[MxNum], Num[Mx];
27 struct info
28 {
29     int L,R,qno;
30     info (int L=0,int R=0,int qno=0):L(L),R(R),qno(qno) {};
31     bool operator<(const info &a) const
32     {
33         if(L/BlockSize!=a.L/BlockSize) return L/BlockSize<a.L/BlockSize;
34         return R<a.R;
35     }
36 } Query[200005];
37 int StoreAnswer[200005];
38 void Add(int indx)
39 {
40     Freq[Num[indx]]++;
41     if (Freq[Num[indx]]==1) Answer++;
42 }
43 void Remove(int indx)
44 {
45     Freq[Num[indx]]--;
46     if (Freq[Num[indx]]==0) Answer--;
47 }
48 int main()
49 {
50     int N;
51     scanf("%d",&N);
52     BlockSize=sqrt(N);
53     for (int i=0;i<N;i++)
54     {
55         scanf("%d",&Num[i]);
56     }
57     int Q;
58     scanf("%d",&Q);
59     for (int i=0;i<Q;i++)
60     {
61         int x,y;
62         scanf("%d %d",&x,&y);
63         Query[i]=info(x-1,y-1,i);
64     }
65     sort(Query,Query+Q);
66     int currentL=0,currentR=0;
67     Answer=0;
68     for (int i=0;i<Q;i++)
69     {
70         int L=Query[i].L;

```

```

68     int R=Query[i].R;
69     while(currentL<L)
70     {
71         Remove(currentL);
72         currentL++;
73     }
74     while(currentL>L)
75     {
76         Add(currentL-1);
77         currentL--;
78     }
79     while(currentR<=R)
80     {
81         Add(currentR);
82         currentR++;
83     }
84     while(currentR>R+1)
85     {
86         Remove(currentR-1);
87         currentR--;
88     }
89     StoreAnswer[Query[i].qno]=Answer;
90 }
91 for(int i=0;i<Q;i++)
92 {
93     printf("%d\n",StoreAnswer[i]);
94 }
95 return 0;
96 }

```

1.2.4 Segment Tree

Lazy Propagation1

```

1  /**
2  **You are given an array of N elements, which are initially all 0. After **that you
   will be given C commands. They are
3  **0 p q v – you have to add v to all numbers in the range **of p to q (inclusive),
   where p and q are two indexes of the array.
4  **1 p q – output a line containing a single integer which is the sum of all **the
   array elements between p and q (inclusive)
5  */
6  #include<bits/stdc++.h>
7  using namespace std;
8  typedef long long LLD;
9  LLD tree[3*100005];
10 LLD lazy[3*100005];
11 void update(int left,int right,int index,int x,int y,int value)
12 {
13     if(x<=left&&y>=right)
14     {
15         tree[index]+=(LLD)(right-left+1)*value;
16         lazy[index]+=value;
17         return;
18     }
19     int mid=(left+right)/2;
20     if(lazy[index]!=0)
21     {
22         tree[2*index]+=(LLD)(mid-left+1)*lazy[index];
23         tree[2*index+1]+=(LLD)(right-mid)*lazy[index];
24         lazy[2*index]+=lazy[index];
25         lazy[2*index+1]+=lazy[index];
26         lazy[index]=0;
27     }
28     if(x<=mid)
29     {
30         update(left,mid,2*index,x,y,value);
31     }
32     if(y>mid)
33     {

```

```

34     update(mid+1,right,2*index+1,x,y,value);
35 }
36 tree[index]=tree[2*index]+tree[2*index+1];
37 }
38 LLD query(int left,int right,int index,int x,int y)
39 {
40     LLD a1=0,a2=0;
41     if(x<=left&&right<=y)
42     {
43         return tree[index];
44     }
45     int mid=(left+right)/2;
46     if(lazy[index]!=0)
47     {
48         tree[2*index]+=(LLD)(mid-left+1)*lazy[index];
49         tree[2*index+1]+=(LLD)(right-mid)*lazy[index];
50         lazy[2*index]+=lazy[index];
51         lazy[2*index+1]+=lazy[index];
52         lazy[index]=0;
53     }
54     if(x<=mid)
55     {
56         a1=query(left,mid,2*index,x,y);
57     }
58     if(y>mid)
59     {
60         a2=query(mid+1,right,2*index+1,x,y);
61     }
62     return (a1+a2);
63 }
64 int main()
65 {
66     int test,t;
67     scanf("%d",&test);
68     for(t=1;t<=test;t++)
69     {
70         memset(tree,0,sizeof(tree));
71         memset(lazy,0,sizeof*lazy);
72         int s,q;
73         scanf("%d %d",&s,&q);
74         while(q--)
75         {
76             int x,y,v,dec;
77             scanf("%d",&dec);
78             if(dec)
79             {
80                 scanf("%d %d",&x,&y);
81                 LLD ans=query(0,s-1,1,x-1,y-1);
82                 printf("%lld\n",ans);
83             }
84             else
85             {
86                 scanf("%d %d %d",&x,&y,&v);
87                 update(0,s-1,1,x-1,y-1,v);
88             }
89         }
90     }
91     return 0;
92 }

```

Lazy Propagation2

```

1  /*
2  **You have an array with n elements which is indexed from 0 to n - 1. **Initially
   all elements are zero. Now you have to deal with two types of **operations
3  **1.Increase the numbers between indices i and j (inclusive) by 1. This **is **
   represented by the command '0 i j'.
4  **2.Answer how many numbers between indices i and j (inclusive) are **divisible by
   3. This is represented by the command '1 i j'.
5  */
6  #include<bits/stdc++.h>

```



```

7 using namespace std;
8 #define Max 100010
9 int Tree[8*Max][4];
10 int lazy[8*Max];
11 int temp[4];
12 void build(int left,int right,int indx)
13 {
14     if(left==right)
15     {
16         Tree[indx][0]=1;
17         Tree[indx][1]=Tree[indx][2]=lazy[indx]=0;
18         return;
19     }
20     int mid=(left+right)/2;
21     build(left,mid,2*indx);
22     build(mid+1,right,2*indx+1);
23     for(int i=0;i<3;i++)
24     {
25         Tree[indx][i]=Tree[2*indx][i]+Tree[2*indx+1][i];
26     }
27 }
28 void update(int left,int right,int indx,int x,int y,int add)
29 {
30     if(lazy[indx])
31     {
32         int lazy_val=lazy[indx];
33         lazy[2*indx]=(lazy[2*indx]+lazy_val)%3;
34         lazy[2*indx+1]=(lazy[2*indx+1]+lazy_val)%3;
35         for(int i=0;i<3;i++)temp[(lazy_val+i)%3]=Tree[indx][i];
36         for(int i=0;i<3;i++)Tree[indx][i]=temp[i];
37         lazy[indx]=0;
38     }
39     if(left>y||right<x)return;
40     if(x<=left&&right<=y)
41     {
42         for(int i=0;i<3;i++)
43         {
44             temp[(i+add)%3]=Tree[indx][i];
45         }
46         for(int i=0;i<3;i++)Tree[indx][i]=temp[i];
47         lazy[2*indx]=(lazy[2*indx]+add)%3;
48         lazy[2*indx+1]=(lazy[2*indx+1]+add)%3;
49         return;
50     }
51     int mid=(left+right)/2;
52     update(left,mid,2*indx,x,y,add);
53     update(mid+1,right,2*indx+1,x,y,add);
54     for(int i=0;i<3;i++)
55     {
56         Tree[indx][i]=Tree[2*indx][i]+Tree[2*indx+1][i];
57     }
58 }
59 int query(int left,int right,int indx,int x,int y)
60 {
61     if(lazy[indx])
62     {
63         int lazy_val=lazy[indx];
64         lazy[2*indx]=(lazy[2*indx]+lazy_val)%3;
65         lazy[2*indx+1]=(lazy[2*indx+1]+lazy_val)%3;
66         for(int i=0;i<3;i++)temp[(lazy_val+i)%3]=Tree[indx][i];
67         for(int i=0;i<3;i++)Tree[indx][i]=temp[i];
68         lazy[indx]=0;
69     }
70     if(left>y||right<x)return 0;
71     if(x<=left&&right<=y)return Tree[indx][0];
72     int mid=(left+right)/2;
73     return query(left,mid,2*indx,x,y)+query(mid+1,right,2*indx+1,x,y);
74 }
75 int main()
76 {

```

```

77     int x,y;
78     int test;
79     scanf("%d",&test);
80     for(int t=1;t<=test;t++)
81     {
82         memset(lazy,0,sizeof(lazy));
83         int N,Q;
84         scanf("%d %d",&N,&Q);
85         build(0,N-1,1);
86         printf("Case %d:\n",t);
87         for(int i=0;i<Q;i++)
88         {
89             int d;
90             scanf("%d %d %d",&d,&x,&y);
91             if(d==0)
92             {
93                 update(0,N-1,1,x,y,1);
94             }
95             else printf("%d\n",query(0,N-1,1,x,y));
96         }
97     }
98     return 0;
99 }

```

Segment Tree Variant 1

```

1  /**
2  **Give a array Of N numbers. Finding Maximum cumulative number frequency in **the
   range.
3  **input:
4  **10 4
5  **1 1 1 3 3 3 3 2 2 2
6  **1 5
7  **1 6
8  **1 7
9  **Output:
10 **3
11 **3
12 **4
13 **2
14 */
15 #include<bits/stdc++.h>
16 using namespace std;
17 typedef long long LLD;
18 #define MAX 50005
19 struct info
20 {
21     int Lcnt,Rcnt,Max,Lnum,Rnum;
22     info(int Lcnt=0,int Rcnt=0,int Max=0,int Lnum=0,int Rnum=0):Lcnt(Lcnt),Rcnt(Rcnt),Max(Max),Lnum(Lnum),Rnum(Rnum){};
23 };
24 info Tree[3*MAX];
25 int arr[MAX];
26 info marge(const info &L,const info &R)
27 {
28     info ret;
29     if(L.Rnum==R.Lnum)
30     {
31         ret.Max=max(L.Rcnt+R.Lcnt,max(L.Max,R.Max));
32     }
33     else ret.Max=max(L.Max,R.Max);
34     ret.Lnum=L.Lnum;
35     ret.Rnum=R.Rnum;
36     if(L.Lnum==R.Lnum)ret.Lcnt=L.Lcnt+R.Lcnt;
37     else ret.Lcnt=L.Lcnt;
38     if(L.Rnum==R.Rnum)ret.Rcnt=L.Rcnt+R.Rcnt;
39     else ret.Rcnt=R.Rcnt;
40     return ret;
41 }
42 void build(int L,int R,int indx)
43 {

```

```

44     if (L==R)
45     {
46         Tree[indx]=info(1,1,1,arr[L],arr[R]);
47         return;
48     }
49     int mid=(L+R)>>1;
50     build(L,mid,2*indx);
51     build(mid+1,R,2*indx+1);
52     Tree[indx]=marge(Tree[2*indx],Tree[2*indx+1]);
53 }
54 info query(int L,int R,int indx,int x,int y)
55 {
56     if (L>=x&&R<=y) return Tree[indx];
57     int mid=(L+R)>>1;
58     info c1,c2;
59     if (x<=mid) c1=query(L,mid,2*indx,x,y);
60     if (y>mid) c2=query(mid+1,R,2*indx+1,x,y);
61     return marge(c1,c2);
62 }
63 int main()
64 {
65     int test;
66     scanf("%d",&test);
67     for(int t=1;t<=test;t++)
68     {
69         int N,C,Q;
70         scanf("%d %d %d",&N,&C,&Q);
71         for(int i=0;i<N;i++)
72         {
73             int x;
74             scanf("%d",&arr[i+1]);
75         }
76         build(1,N,1);
77         printf("Case %d:\n",t);
78         while(Q--)
79         {
80             int x,y;
81             scanf("%d %d",&x,&y);
82             printf("%d\n",query(1,N,1,x,y).Max);
83         }
84     }
85     return 0;
86 }

```

Segment Tree Variant 2

```

1  /**
2  **You are given a sequence A of N (N <= 50000) integers between -10000 and 10000.
3  **On this sequence you have to apply M (M <= 50000) operations:
4  **modify the i-th element in the sequence or for given x y print max{Ai + Ai+1 + ..
   + Aj | x<=i<=j<=y }.
5  **/
6  #include<bits/stdc++.h>
7  using namespace std;
8  typedef long long LLD;
9  template<class T> T MAX3(T a,T b,T c) {return max(a,max(b,c));}
10 LLD Inf=(1ll<<60);
11 #define MN 50005
12 struct info
13 {
14     LLD prefixSum;
15     LLD suffixSum;
16     LLD Total;
17     LLD TotalMax;
18     info(int pre=-Inf,int suff=-Inf,int total=-Inf,int totalmax=-Inf):prefixSum(pre)
19     ,suffixSum(suff),Total(total),TotalMax(totalmax){};
20 };
21 info marge(const info &a,const info &b)
22 {
23     info ret;
24     ret.Total=a.Total+b.Total;

```

```

24     ret.prefixSum=max(a.prefixSum,a.Total+b.prefixSum);
25     ret.suffixSum=max(a.suffixSum+b.Total,b.suffixSum);
26     ret.TotalMax=MAX3(a.TotalMax,b.TotalMax,a.suffixSum+b.prefixSum);
27     return ret;
28 }
29 LLD arr[MN];
30 info Tree[3*MN];
31 void build(int L,int R,int indx)
32 {
33     if(L==R)
34     {
35         Tree[indx]=info(arr[L],arr[L],arr[L],arr[L]);
36         return;
37     }
38     int mid=(L+R)>>1;
39     build(L,mid,2*indx);
40     build(mid+1,R,2*indx+1);
41     Tree[indx]=marge(Tree[2*indx],Tree[2*indx+1]);
42 }
43 void update(int L,int R,int indx,int x,LLD val)
44 {
45     if(L==R)
46     {
47         Tree[indx]=info(val,val,val,val);
48         return;
49     }
50     int mid=(L+R)>>1;
51     if(x<=mid) update(L,mid,2*indx,x,val);
52     else update(mid+1,R,2*indx+1,x,val);
53     Tree[indx]=marge(Tree[2*indx],Tree[2*indx+1]);
54 }
55 info query(int L,int R,int indx,int x,int y)
56 {
57     if(L==x and y==R) return Tree[indx];
58     int mid=(L+R)>>1;
59     if(y<=mid) return query(L,mid,2*indx,x,y);
60     else if(x>mid) return query(mid+1,R,2*indx+1,x,y);
61     return marge(query(L,mid,2*indx,x,mid),query(mid+1,R,2*indx+1,mid+1,y));
62 }
63 int main()
64 {
65     #ifdef _ANICK_
66     //f_input;
67     #endif // _ANICK_
68     int N;
69     scanf("%d",&N);
70     for(int i=1;i<=N;i++)scanf("%lld",&arr[i]);
71     build(1,N,1);
72     int Q;
73     scanf("%d",&Q);
74     while(Q--)
75     {
76         int t,x,y;
77         scanf("%d %d %d",&t,&x,&y);
78         if(t) printf("%lld\n",query(1,N,1,x,y).TotalMax);
79         else update(1,N,1,x,y);
80     }
81     return 0;
82 }

```

Segment Tree Variant 3

```

1  /**
2  **Given a bracket sequence.
3  ** On a bracket word one can do the following operations:
4  **replacement — changes the i-th bracket into the opposite one
5  **check — if the word is a correct bracket expression
6  **/
7  #include<bits/stdc++.h>
8  using namespace std;
9  typedef long long LLD;

```

```

10 #define MAX 50005
11 struct info
12 {
13     int sum,sub;
14     info (int sum=0,int sub=0):sum(sum),sub(sub){};
15 };
16 info Tree[4*MAX];
17 char inp[MAX];
18 info marge(const info &L,const info &R)
19 {
20     info ret;
21     ret.sum= L.sum+R.sum;
22     ret.sub=L.sub;
23     ret.sub=min(ret.sub,L.sum+R.sub);
24     return ret;
25 }
26 void build(int L,int R,int indx)
27 {
28     if(L==R)
29     {
30         int x;
31         if(inp[L]=='(')x=1;
32         else x=-1;
33         Tree[indx]=info(x,x);
34         return;
35     }
36     int mid=(L+R)>>1;
37     build(L,mid,2*indx);
38     build(mid+1,R,2*indx+1);
39     Tree[indx]=marge(Tree[2*indx],Tree[2*indx+1]);
40 }
41 void update(int L,int R,int indx,int x)
42 {
43     if(L==R)
44     {
45         int x;
46         if(inp[L]=='(')x=1;
47         else x=-1;
48         Tree[indx]=info(x,x);
49         return;
50     }
51     int mid=(L+R)>>1;
52     if(x<=mid) update(L,mid,2*indx,x);
53     else update(mid+1,R,2*indx+1,x);
54     Tree[indx]=marge(Tree[2*indx],Tree[2*indx+1]);
55 }
56 info query(int L,int R,int indx,int x,int y)
57 {
58     if(L==x&&R==y) return Tree[indx];
59     int mid=(L+R)>>1;
60     if(y<=mid) return query(L,mid,2*indx,x,y);
61     else if(x>mid) return query(mid+1,R,2*indx+1,x,y);
62     else return marge(query(L,mid,2*indx,x,mid),query(mid+1,R,2*indx+1,mid+1,y));
63 }
64 int main()
65 {
66     int N,t=1;
67     while(scanf("%d",&N)==1)
68     {
69         scanf("%s",inp);
70         build(0,N-1,1);
71         int Q;
72         printf("Test %d:\n",t++);
73         scanf("%d",&Q);
74         while(Q--)
75         {
76             int x;
77             scanf("%d",&x);
78             if(x)
79             {

```

```

80         if(inp[x-1]=='(')inp[x-1]=')';
81         else inp[x-1]='(';
82         update(0,N-1,1,x-1);
83     }
84     else
85     {
86         info y=query(0,N-1,1,0,N-1);
87         if(y.sum==0&&y.sub>=0)printf("YES\n");
88         else printf("NO\n");
89     }
90 }
91 }
92 return 0;
93 }

```

1.2.5 Sliding Window RMQ

```

1  /**
2   * every K size window RMQ
3   * Calculate in O(N+K) time
4   */
5  #include<bits/stdc++.h>
6  using namespace std;
7  vector<int>SlidingRMQ(int *A,int N,int k)
8  {
9      /** Create a Double Ended Queue, Qi that will store indexes of array elements
10       * The queue will store indexes of useful elements in every window and it will
11       * maintain decreasing order of values from front to rear in Qi, i.e.,
12       * arr[Qi.front()] to arr[Qi.rear()] are sorted in increasing order
13       */
14      vector<int>MinWindow;
15      deque<int>Q;
16      int i;
17      /* Process first k (or first window) elements of array */
18      for(i=0;i<k;i++)
19      {
20          /// For very element, the previous largest elements are useless so
21          /// remove them from Qi
22          while(!Q.empty() and A[i]<=A[Q.back()])Q.pop_back();
23          Q.push_back(i);
24      }
25      /// Process rest of the elements, i.e., from arr[k] to arr[n-1]
26      while(i<N)
27      {
28          /// The element at the front of the queue is the smallest element of
29          /// previous window, so insert it result
30          MinWindow.push_back(A[Q.front()]);
31
32          /// Remove the elements which are out of this window
33          while(!Q.empty() and Q.front()<=i-k)Q.pop_front();
34
35          /// Remove all elements larger than the currently
36          /// being added element (remove useless elements)
37          while(!Q.empty() and A[i]<=A[Q.back()])Q.pop_back();
38
39          /// Add current element at the rear of Qi
40          Q.push_back(i);
41          i++;
42      }
43      /// insert the minimum element of last window
44      MinWindow.push_back(A[Q.front()]);
45      return MinWindow;
46  }
47  int main()
48  {
49      int A[]={100,10, -1, 2,-3,-4,10, 1,100,20};
50      vector<int>a=SlidingRMQ(A,10,2);
51      for(int i=0;i<a.size();i++)cout<<a[i]<<" ";
52      return 0;
53  }

```

1.2.6 Sparse Table

```
1  /**
2   Compute sparse table in O(NlogN)
3   query in O(1)
4   Ref link: https://www.topcoder.com/community/data-science/data-science-tutorials/range-minimum-query-and-lowest-common-ancestor/
5  */
6  #include<bits/stdc++.h>
7  using namespace std;
8  #define Max 10000005
9  int rmq[24][Max];
10 int A[Max];
11 void Compute_ST(int N)
12 {
13     for (int i = 0; i < N; ++i)rmq[0][i] = i;
14     for (int k = 1; (1 << k) < N; ++k)
15     {
16         for (int i = 0; i + (1 << k) <= N; i++)
17         {
18             int x = rmq[k - 1][i];
19             int y = rmq[k - 1][i + (1 << k - 1)];
20             rmq[k][i] = A[x] <= A[y] ? x : y;
21         }
22     }
23 }
24
25 int RMQ(int i, int j)
26 {
27     int k = log2(j-i);
28     int x = rmq[k][i];
29     int y = rmq[k][j - (1 << k) + 1];
30     return A[x] <= A[y] ? x : y;
31 }
32
33 int main()
34 {
35
36     return 0;
37 }
```

1.3 Heavy Light Decomposition

```
1  /*
2   Tanvir Hasan Anick
3   University of Asia pacific
4  */
5  /**Header file**/
6  #include<cstdio>
7  #include<iomanip>
8  #include<cstring>
9  #include<cmath>
10 #include<cstdlib>
11 #include<cctype>
12 #include<algorithm>
13 #include<string>
14 #include<vector>
15 #include<queue>
16 #include<map>
17 #include<set>
18 #include<sstream>
19 #include<stack>
20 #include<list>
21 #include<iostream>
22 #include<assert.h>
23
24 /**Define file I/O **/
25 #define f_input freopen("input.txt","r",stdin)
26 #define f_output freopen("output.txt","w",stdout)
```

```

27
28 /**Define memory set function**/
29 #define mem(x,y) memset(x,y,sizeof(x))
30 #define CLEAR(x) memset(x,0,sizeof(x))
31
32 /**Define function and object**/
33 #define pb push_back
34 #define Sort(v) sort(v.begin(),v.end())
35 #define RSort(v) sort(v.rbegin(),v.rend())
36 #define CSort(v,C) sort(v.begin(),v.end(),C)
37 #define all(v) (v).begin(),(v).end()
38 #define sqr(x) ((x)*(x))
39 #define find_dist(a,b) sqrt(sqr(a.x-b.x)+sqr(a.y-b.y))
40
41 /**Define constant value**/
42 #define ERR 1e-9
43 #define pi (2*acos(0))
44 #define PI 3.141592653589793
45
46 /**Define input**/
47 #define scanint(a) scanf("%d",&a)
48 #define scanLLD(a) scanf("%lld",&a)
49 #define scanstr(s) scanf("%s",s)
50 #define scanline(l) scanf("%[^\n]",l);
51
52 /**Define Bitwise operation**/
53 #define check(n, pos) (n & (1<<(pos)))
54 #define biton(n, pos) (n | (1<<(pos)))
55 #define bitoff(n, pos) (n & ~(1<<(pos)))
56
57 /**Define color**/
58 #define WHITE 0
59 #define GREY 1
60 #define BLACK 2
61
62 /**Sync off with stdio**/
63 #define __ cin.sync_with_stdio(false);\
64         cin.tie();
65
66 using namespace std;
67
68 /**Typedef**/
69 typedef vector<int> vint;
70 typedef vector<vint> vint2D;
71 typedef vector<string> vstr;
72 typedef vector<char> vchar;
73 typedef vector<vchar> vchar2D;
74 typedef queue<int> Qi;
75 typedef queue<Qi> Qii;
76 typedef map<int,int> Mii;
77 typedef map<string,int> Msi;
78 typedef map<int,string> Mis;
79 typedef stack<int> stk;
80 typedef pair<int,int> pp;
81 typedef pair<int,pp> ppp;
82 typedef long long int LLD;
83 const int inf=0x7FFFFFFF;
84
85 /**Template & structure**/
86 namespace my{
87 struct point_int{int x,y; point_int(){} point_int(int a,int b){x=a,y=b;}}; //Point
88     for x,y (int) coordinate in 2D space
89 struct point_double{double x,y; point_double(){} point_double(double a,double b){x=a,
90     y=b;}}; //Point for x,y (double) coordinate in 2D space
91 struct Node{int v,w; Node() {} bool operator<(const Node &a) const {return w>a.w;} Node(
92     int _v,int _w){v=_v,w=_w;}}; //Node for Dijkstra
93 template<class T>T gcd(T a,T b){return b==0 ? a : gcd(b, a % b);}
94 template<typename T>T lcm(T a, T b) {return a / gcd(a,b) * b;}
95 template<class T>T big_mod(T n,T p,T m){if(p==0)return (T)1;T x=big_mod(n,p/2,m);x
96     =(x*x)%m; if(p&1)x=(x*n)%m; return x;}

```



```

93 template<class T>T multiplication(T n,T p,T m){if(p==0)return (T)0;T x=
    multiplication(n,p/2,m);x=(x+x)%m;if(p&1)x=(x+n)%m;return x;}
94 template<class T>T my_pow(T n,T p){if(p==0)return 1;T x=my_pow(n,p/2);x=(x*x);if(p
    &1)x=(x*n);return x;} //n to the power p
95 template<class T> double getdist(T a, T b){return sqrt((a.x - b.x) * (a.x - b.x) +
    (a.y - b.y) * (a.y - b.y));} // distance between a & b
96 template<class T> T extract(string s, T ret) {stringstream ss(s); ss >> ret;
    return ret;} // extract words or numbers from a line
97 template<class T> string toString(T n) {stringstream ss; ss << n; return ss.str()
    ;} // convert a number to string
98 template<class T> inline T Mod(T n,T m) {return (n%m+m)%m;} //For Positive
    Negative No.
99 template<class T> T MIN3(T a,T b,T c) {return min(a,min(b,c));} // minimum of 3
    number
100 template<class T> T MAX3(T a,T b,T c) {return max(a,max(b,c));} //maximum of 3
    number
101 template<class T> void print_vector(T &v){int sz=v.size();if(sz)cout<<v[0];for(int
    i = 1; i < sz; i++)cout << ' ' <<v[i];cout<<endl;} // prints all elements in a
    vector
102 bool isVowel(char ch){ ch=toupper(ch); if(ch=='A' || ch=='U' || ch=='I' || ch=='O' || ch=='
    E') return true; return false;}
103 bool isConsonant(char ch){if (isalpha(ch) && !isVowel(ch)) return true; return
    false;}}
104 /**Shortcut input function**/
105 int read_int(){int n;scanf("%d",&n);return n;}
106 int read_LLD(){LLD n;scanf("%lld",&n);return n;}
107 inline int buffer_input() { char inp[1000]; scanf(inp); return atoi(inp); }
108
109 /**Direction**/
110 //int col[8] = {0, 1, 1, 1, 0, -1, -1, -1};int row[8] = {1, 1, 0, -1, -1, -1, 0,
    1}; //8 Direction
111 //int col[4] = {1, 0, -1, 0};int row[4] = {0, 1, 0, -1}; //4 Direction
112 //int dx[]={2,1,-1,-2,-2,-1,1,2};int dy[]={1,2,2,1,-1,-2,-2,-1}; //Knight
    Direction
113 //int dx[]={-1,-1,+0,+1,+1,+0};int dy[]={-1,+1,+2,+1,-1,-2}; //Hexagonal
    Direction
114
115
116 /*****Ajaira Jinish Sesh*****/
117
118 const int Max=10000;
119 struct info
120 {
121     int v, cost;
122     info(int v=0,int cost=0):v(v),cost(cost){};
123 };
124 vector<pp>edges;
125 vector<info>Graph[Max+5];
126 int Tree[5*Max+5],BaseArray[Max+5],SubTreeSize[Max+5];
127 int ChainHead[Max+5],ChainNum[Max+5],PosInBaseArray[Max+5],ChainNo;
128 int Level[Max+5],Parent[Max+5],SparseTable[Max+5][16];
129 int ptr;
130 void init(int N)
131 {
132     for(int i=0;i<=N;i++)
133     {
134         Graph[i].clear(),ChainHead[i]=-1;
135         for(int j=0;j<=15;j++)SparseTable[i][j]=-1;
136     }
137     edges.clear();
138     ptr=ChainNo=0;
139 }
140 void buildSegmentTree(int l,int r,int indx)
141 {
142     if(l==r)
143     {
144         Tree[indx]=BaseArray[l];
145         return;
146     }
147     int mid=(l+r)>>1;

```

```

148     int lindx=indx<<1;
149     int rindx=lindx|1;
150     buildSegmentTree(1,mid,lindx);
151     buildSegmentTree(mid+1,r,rindx);
152     Tree[indx]=max(Tree[lindx],Tree[rindx]);
153 }
154 void updateSegmentTree(int l,int r,int indx,int update_indx,int value)
155 {
156     if(l==r)
157     {
158         Tree[indx]=value;
159         return;
160     }
161     int mid=(l+r)>>1;
162     int lindx=indx<<1;
163     int rindx=lindx|1;
164     if(update_indx<=mid)updateSegmentTree(1,mid,lindx,update_indx,value);
165     else updateSegmentTree(mid+1,r,rindx,update_indx,value);
166     Tree[indx]=max(Tree[lindx],Tree[rindx]);
167 }
168 int querySegmentTree(int l,int r,int indx,int x,int y)
169 {
170     if(l>y||r<x)return 0;
171     if(x<=l&&y>=r)return Tree[indx];
172     int mid=(l+r)>>1;
173     int lindx=indx<<1;
174     int rindx=lindx|1;
175     int c1=0,c2=0;
176     if(x<=mid)c1=querySegmentTree(1,mid,lindx,x,y);
177     if(y>mid)c2=querySegmentTree(mid+1,r,rindx,x,y);
178     return max(c1,c2);
179 }
180 void dfs(int from,int u,int depth)
181 {
182     Level[u]=depth;
183     Parent[u]=from;
184     SubTreeSize[u]=1;
185     int sz=Graph[u].size();
186     for(int i=0;i<sz;i++)
187     {
188         int v=Graph[u][i].v;
189         if(v==from)continue;
190         dfs(u,v,depth+1);
191         SubTreeSize[u]+=SubTreeSize[v];
192     }
193 }
194 void sparseTable(int N)
195 {
196     for(int i=0;i<=N;i++)SparseTable[i][0]=Parent[i];
197     for(int j=1;(1<<j)<=N;j++)
198     {
199         for(int i=0;i<=N;i++)
200         {
201             if(SparseTable[i][j-1]!=-1)
202             {
203                 int a=SparseTable[i][j-1];
204                 SparseTable[i][j]=SparseTable[a][j-1];
205             }
206         }
207     }
208 }
209 int LCA(int p,int q)
210 {
211     if(Level[p]<Level[q])swap(p,q);
212     int Log=log2(Level[p])+1;
213     for(int i=Log;i>=0;i--)
214     {
215         if((Level[p]-(1<<i))>=Level[q])p=SparseTable[p][i];
216     }
217     if(p==q)return p;

```

```

218     for (int i=Log; i>=0; i--)
219     {
220         if (SparseTable[p][i]!=-1 && SparseTable[p][i]!=SparseTable[q][i])
221         {
222             p=SparseTable[p][i], q=SparseTable[q][i];
223         }
224     }
225     return Parent[p];
226 }
227 /**
228  * Actual HL-Decomposition part
229  * Initially all entries of chainHead[] are set to -1.
230  * So when ever a new chain is started, chain head is correctly assigned.
231  * As we add a new node to chain, we will note its position in the baseArray.
232  * In the first for loop we find the child node which has maximum sub-tree size.
233  * The following if condition is failed for leaf nodes.
234  * When the if condition passes, we expand the chain to special child.
235  * In the second for loop we recursively call the function on all normal nodes.
236  * chainNo++ ensures that we are creating a new chain for each normal child.
237  */
238 void heavyLightDecompositon(int from, int curNode, int cost)
239 {
240     if (ChainHead[ChainNo]==-1) ChainHead[ChainNo]=curNode; /// Assign chain head
241     ChainNum[curNode]=ChainNo;
242     PosInBaseArray[curNode]=ptr; /// Position of this node in baseArray which we
243     will use in Segtree
244     BaseArray[ptr++]=cost;
245     int sc=-1, nextCost;
246     int sz=Graph[curNode].size();
247     for (int i=0; i<sz; i++) /// Loop to find special child
248     {
249         int v=Graph[curNode][i].v;
250         if (v==from) continue;
251         if (sc==-1 || SubTreeSize[sc]<SubTreeSize[v])
252         {
253             sc=v;
254             nextCost=Graph[curNode][i].cost;
255         }
256     }
257     if (sc!=-1) heavyLightDecompositon(curNode, sc, nextCost); /// Expand the chain
258     for (int i=0; i<sz; i++)
259     {
260         int v=Graph[curNode][i].v;
261         int cost=Graph[curNode][i].cost;
262         if (v==from || sc==v) continue;
263         ChainNo++;
264         heavyLightDecompositon(curNode, v, cost);
265     }
266 }
267 void updateTree(int ith, int val)
268 {
269     pp a=edges[ith];
270     int u=a.first, v=a.second;
271     int indx=PosInBaseArray[u];
272     if (Level[u]<Level[v]) indx=PosInBaseArray[v];
273     updateSegmentTree(0, ptr-1, 1, indx, val);
274 }
275 /**
276  * query_up:
277  * It takes two nodes u and v, condition is that v is an ancestor of u
278  * We query the chain in which u is present till chain head, then move to next
279  * chain up
280  * We do that way till u and v are in the same chain, we query for that part of
281  * chain and break
282  */
283 int queryUp(int u, int v)
284 {
285     if (u==v) return 0;
286     int uchain, vchain=ChainNum[v], ans=-1;
287     while (true)

```

```

285 {
286     uchain=ChainNum[u];
287     if(uchain==vchain)
288     {
289         if(u==v)          // Both u and v are in the same chain, so we need to
query from u to v, update answer and break.
290             break;        // We break because we came from u up till v, we are
done
291         ans=max(ans, querySegmentTree(0, ptr-1, 1, PosInBaseArray[v]+1,
PosInBaseArray[u]));
292         break;
293     }
294     int uchainhead=ChainHead[uchain];
295     ans=max(ans, querySegmentTree(0, ptr-1, 1, PosInBaseArray[uchainhead],
PosInBaseArray[u]));
296     // Above is call to segment tree query function. We do from
chainHead of u till u. That is the whole chain from
297     u=Parent[uchainhead];
298 }
299 return ans;
300 }
301 int queryTree(int u, int v)
302 {
303     int lca=LCA(u, v);
304     return max(queryUp(u, lca), queryUp(v, lca));
305 }
306 int main()
307 {
308     #ifdef _ANICK_
309     //f_input;
310     #endif // _ANICK_
311     --
312     int test;
313     cin>>test;
314     while(test--)
315     {
316         int N;
317         cin>>N;
318         init(N);
319         for(int i=0; i<N-1; i++)
320         {
321             int u, v, c;
322             cin>>u>>v>>c;
323             u--, v--;
324             Graph[u].pb(info(v, c));
325             Graph[v].pb(info(u, c));
326             edges.pb(pp(u, v));
327         }
328         dfs(-1, 0, 0);
329         sparseTable(N);
330         heavyLightDecompositon(-1, 0, -1);
331         buildSegmentTree(0, ptr-1, 1);
332         string ch;
333         int x, y;
334         while(true)
335         {
336             cin>>ch;
337             if(ch[0]=='D') break;
338             cin>>x>>y;
339             if(ch[0]=='Q') printf("%d\n", queryTree(x-1, y-1));
340             else if(ch[0]=='C') updateTree(x-1, y);
341         }
342     }
343     return 0;
344 }

```

1.4 Ternary Bit Mask

```

1
2 int more_bit[10];

```

```

3 int get_bit(int mask , int pos)
4 {
5     return (mask / more_bit[pos]) % 3;
6 }
7 int set_bit(int mask, int pos , int bit)
8 {
9     int tmp = (mask / more_bit[pos]) % 3;
10    mask -= tmp * more_bit[pos];
11    mask += bit * more_bit[pos];
12    return mask;
13 }
14 void init(void)
15 {
16     more_bit[0] = 3;
17     for(int i = 1; i < 10; i++) more_bit[i] = 3 * more_bit[i - 1];
18 }

```

Chapter 2

Graph Theory

2.1 DFS

2.1.1 Bicoloring

```
1  ///color will be initial with -1
2  int color[20005];
3  bool dfs(int u, int c)
4  {
5      if (color[u]==c) return true;
6      if (color[u]==(1-c)) return false;
7      color[u]=c;
8      bool ret=true;
9      for (auto v: graph[u]) ret&=dfs(v, 1-c);
10     return ret;
11 }
```

2.1.2 Cycle Finding

```
1  int color[20005];
2  bool dfs(int u)
3  {
4      color[u]=GREY;
5      bool no_cycle=true;
6      for (auto v: graph[u])
7      {
8          if (color[v]==WHITE)
9          {
10             no_cycle=dfs(v);
11          }
12          else if (color[v]==GREY) return false;
13      }
14      color[u]=BLACK;
15      return no_cycle;
16 }
```

2.2 Topological Sort

```
1  #include <bits/stdc++.h>
2  using namespace std;
3  #define WHITE 0
4  #define GREY 1
5  #define BLACK 2
6  vector<int> graph[100005];
7  vector<int> ans;
8  int visit[100005];
9  bool dfs(int u)
10 {
11     visit[u]=GREY;
12     bool no_cycle=true;
```

```

13     int sz=graph[u].size();
14     for(int i=0;i<sz;i++)
15     {
16         int v=graph[u][i];
17         if(visit[v]==WHITE)
18         {
19             no_cycle=dfs(v);
20         }
21         else if(visit[v]==GREY) return false;
22     }
23     visit[u]=BLACK;
24     ans.push_back(u);
25     return no_cycle;
26 }
27 bool topsort(int N)
28 {
29     ans.clear();
30     memset(visit, false, sizeof(visit));
31     int no_cycle=true;
32     for(int i=0;i<N;i++)
33     {
34         if(visit[i]==WHITE) no_cycle&=dfs(i);
35     }
36     return no_cycle;
37 }
38 int main()
39 {
40     #ifdef _ANICK_
41     //f_input;
42     #endif // _ANICK_
43     return 0;
44 }

```

2.3 Havel Hakimi

```

1  /**
2   Given N degree d1,d2,d3.....dn. Is it possible to make a graph which have no
3   cycle and
4   different two node will be connected with one Edge?
5   **/
6   #include<stdio.h>
7   #include<queue>
8   #include<vector>
9   using namespace std;
10  int main()
11  {
12      int N;
13      while(scanf("%d",&N) and N)
14      {
15          priority_queue<int>Q;
16          bool Ok=true;
17          int Odd_Node=0;
18          for(int i=0;i<N;i++)
19          {
20              int x;
21              scanf("%d",&x);
22              if(x>=N or x<0)Ok=false;
23              Odd_Node+=(x%2);
24              Q.push(x);
25          }
26          Ok&=(Odd_Node%2==0); //Handshaking Theorem
27          for(int i=0;i<N and Ok;i++)
28          {
29              int k=Q.top();
30              Q.pop();
31              vector<int> v;
32              for(int j=0;j<k and Ok;j++)
33              {
34                  int x=Q.top();

```

```

35         Q.pop();
36         x--;
37         Ok&=(x>=0);
38         v.push_back(x);
39     }
40     for(int j=0;j<k and Ok;j++)
41     {
42         Q.push(v[j]);
43     }
44 }
45 if(Ok)printf("Possible\n");
46 else printf("Not possible\n");
47 }
48 return 0;
49 }

```


Chapter 3

Flow networks/ matching

3.1 Max Flow

```
1  /*
2      Tanvir Hasan Anick
3      University of Asia pacific
4  */
5  /**Header file**/
6  #include<cstdio>
7  #include<iomanip>
8  #include<cstring>
9  #include<cmath>
10 #include<cstdlib>
11 #include<cctype>
12 #include<algorithm>
13 #include<string>
14 #include<vector>
15 #include<queue>
16 #include<map>
17 #include<set>
18 #include<sstream>
19 #include<stack>
20 #include<list>
21 #include<iostream>
22 #include<assert.h>
23
24 /**Define file I/O **/
25 #define f_input freopen("input.txt","r",stdin)
26 #define f_output freopen("output.txt","w",stdout)
27
28 /**Define memory set function**/
29 #define mem(x,y) memset(x,y,sizeof(x))
30 #define CLEAR(x) memset(x,0,sizeof(x))
31
32 /**Define function and object**/
33 #define pb push_back
34 #define Sort(v) sort(v.begin(),v.end())
35 #define RSort(v) sort(v.rbegin(),v.rend())
36 #define CSort(v,C) sort(v.begin(),v.end(),C)
37 #define all(v) (v).begin(),(v).end()
38 #define sqr(x) ((x)*(x))
39 #define find_dist(a,b) sqrt(sqr(a.x-b.x)+sqr(a.y-b.y))
40
41 /**Define constant value**/
42 #define ERR 1e-9
43 #define pi (2*acos(0))
44 #define PI 3.141592653589793
45
46 /**Define input**/
47 #define scanint(a) scanf("%d",&a)
48 #define scanLLD(a) scanf("%lld",&a)
49 #define scanstr(s) scanf("%s",s)
```

```

50 #define scanline(l) scanf("%[^\n]",l);
51
52 /**Define Bitwise operation**/
53 #define check(n, pos) (n & (1<<(pos)))
54 #define biton(n, pos) (n | (1<<(pos)))
55 #define bitoff(n, pos) (n & ~(1<<(pos)))
56
57 /**Define color**/
58 #define WHITE 0
59 #define GREY 1
60 #define BLACK 2
61
62 /**Sync off with stdio**/
63 #define -- cin.sync_with_stdio(false);\
64         cin.tie();
65 /**Debug tools**/
66 #define what_is(x) cerr<<(#x)<<" is "<<x<<endl
67 using namespace std;
68
69 /**Typedef**/
70 typedef vector<int> vint;
71 typedef vector< vint > vint2D;
72 typedef vector<string> vstr;
73 typedef vector<char> vchar;
74 typedef vector< vchar > vchar2D;
75 typedef queue<int> Qi;
76 typedef queue< Qi > Qii;
77 typedef map<int, int> Mii;
78 typedef map<string, int> Msi;
79 typedef map<int, string> Mis;
80 typedef stack<int> stk;
81 typedef pair<int, int> pp;
82 typedef pair<int, pp > ppp;
83 typedef long long int LLD;
84 const int inf=0x7FFFFFFF;
85
86 /**Template & structure**/
87 struct point_int{int x,y; point_int(){} point_int(int a,int b){x=a,y=b;}}; //Point
    for x,y (int) coordinate in 2D space
88 struct point_double{double x,y; point_double(){} point_double(double a,double b){x=a,
    y=b;}}; //Point for x,y (double) coordinate in 2D space
89 struct Node{int v,w; Node() {} bool operator<(const Node &a) const {return w>a.w;} Node(
    int _v, int _w){v=_v,w=_w;}}; //Node for Dijkstra
90 namespace my{
91 template<class T>T gcd(T a,T b){return b == 0 ? a : gcd(b, a % b);}
92 template<typename T>T lcm(T a, T b) {return a / gcd(a,b) * b;}
93 template<class T>T big_mod(T n,T p,T m){if(p==0)return (T)1;T x=big_mod(n,p/2,m);x
    =(x*x)%m;if(p&1)x=(x*n)%m;return x;}
94 template<class T>T multiplication(T n,T p,T m){if(p==0)return (T)0;T x=
    multiplication(n,p/2,m);x=(x+x)%m;if(p&1)x=(x+n)%m;return x;}
95 template<class T>T my_pow(T n,T p){if(p==0)return 1;T x=my_pow(n,p/2);x=(x*x);if(p
    &1)x=(x*n);return x;} //n to the power p
96 template <class T> double getdist(T a, T b){return sqrt((a.x - b.x) * (a.x - b.x) +
    (a.y - b.y) * (a.y - b.y));} // distance between a & b
97 template <class T> T extract(string s, T ret) {stringstream ss(s); ss >> ret;
    return ret;} // extract words or numbers from a line
98 template <class T> string tostring(T n) {stringstream ss; ss << n; return ss.str()
    ;} // convert a number to string
99 template<class T> inline T Mod(T n,T m) {return (n%m+m)%m;} //For Positive
    Negative No.
100 template<class T> T MIN3(T a,T b,T c) {return min(a,min(b,c));} // minimum of 3
    number
101 template<class T> T MAX3(T a,T b,T c) {return max(a,max(b,c));} //maximum of 3
    number
102 template <class T> void print_vector(T &v){int sz=v.size();if(sz)cout<<v[0];for(int
    i = 1; i < sz; i++)cout << ' ' <<v[i];cout<<endl;} // prints all elements in a
    vector
103 bool isVowel(char ch){ ch=toupper(ch); if(ch=='A' || ch=='U' || ch=='I' || ch=='O' || ch=='
    E') return true; return false;}
104 bool isConsonant(char ch){if (isalpha(ch) && !isVowel(ch)) return true; return

```

```

        false;}}
105 /**Shortcut input function**/
106 int read_int(){int n;scanf("%d",&n);return n;}
107 int read_LLD(){LLD n;scanf("%lld",&n);return n;}
108 inline int buffer_input() { char inp[1000]; scanstr(inp); return atoi(inp); }
109
110 /**Direction**/
111 //int col[8] = {0, 1, 1, 1, 0, -1, -1, -1};int row[8] = {1, 1, 0, -1, -1, -1, 0,
112 //1}; //8 Direction
113 //int col[4] = {1, 0, -1, 0};int row[4] = {0, 1, 0, -1}; //4 Direction
114 //int dx[]={2,1,-1,-2,-2,-1,1,2};int dy[]={1,2,2,1,-1,-2,-2,-1};//Knight
115 //Direction
116 //int dx[]={-1,-1,+0,+1,+1,+0};int dy[]={-1,+1,+2,+1,-1,-2}; //Hexagonal
117 //Direction
118
119 /*****Ajaira Jinish Sesh*****/
120 #define MN 1000
121 vint2D graph;
122 int Cost[MN][MN];
123 int parent[MN+5];
124 int flow;
125 void init(int N)
126 {
127     graph=vint2D(N);
128     mem(Cost,0);
129 }
130 void AddEdge(int u,int v,int cost)
131 {
132     graph[u].pb(v);
133     graph[v].pb(u);
134     Cost[u][v]+=cost;
135     Cost[v][u]+=cost;
136 }
137 bool augmenting_path(int source,int sink)
138 {
139     mem(parent,-1);
140     queue<int>Q;
141     Q.push(source);
142     while(!Q.empty())
143     {
144         int u=Q.front();
145         Q.pop();
146         int sz=graph[u].size();
147         for(int i=0;i<sz;i++)
148         {
149             int v=graph[u][i];
150             if(parent[v]==-1 and Cost[u][v]>0)
151             {
152                 parent[v]=u;
153                 Q.push(v);
154                 if(v==sink) return true;
155             }
156         }
157     }
158     return false;
159 }
160 void path(int v,int source)
161 {
162     int u=parent[v];
163     flow=min(flow,Cost[u][v]);
164     if(source!=u)path(u,source);
165     Cost[u][v]-=flow;
166     Cost[v][u]+=flow;
167     return;
168 }
169 int max_flow(int source,int sink)
170 {
171     int ret=0;
172     while(augmenting_path(source,sink))

```

```

171     {
172         flow=inf;
173         path(sink,source);
174         ret+=flow;
175     }
176     return ret;
177 }
178 int main()
179 {
180     #ifdef _ANICK_
181     //f_input;
182     #endif // _ANICK_
183     int test;
184     scanf("%d",&test);
185     while(test--)
186     {
187         int P,S,C,M;
188         scanf("%d %d %d %d",&P,&S,&C,&M);
189         init(P+S+5);
190         int superSource=0,SuperSikn=P+S+1;
191         for(int i=1;i<=P;i++)AddEdge(superSource,i,1);
192         for(int i=1;i<=S;i++)AddEdge(P+1,SuperSikn,C);
193         for(int i=0;i<M;i++)
194         {
195             int x,y;
196             scanf("%d %d",&x,&y);
197             AddEdge(x,P+y,(1<30));
198         }
199         printf("%d\n",max_flow(superSource,SuperSikn));
200     }
201     return 0;
202 }

```

Chapter 4

Dynamic programming

4.1 Edit Distance

```
1  /*
2      Tanvir Hasan Anick
3      University of Asia pacific
4  */
5  /**Header file**/
6  #include<cstdio>
7  #include<iomanip>
8  #include<cstring>
9  #include<cmath>
10 #include<stdlib>
11 #include<cctype>
12 #include<algorithm>
13 #include<string>
14 #include<vector>
15 #include<queue>
16 #include<map>
17 #include<set>
18 #include<sstream>
19 #include<stack>
20 #include<list>
21 #include<iostream>
22 #include<assert.h>
23
24 /**Define file I/O **/
25 #define f_input freopen("input.txt","r",stdin)
26 #define f_output freopen("output.txt","w",stdout)
27
28 /**Define memory set function**/
29 #define mem(x,y) memset(x,y,sizeof(x))
30 #define CLEAR(x) memset(x,0,sizeof(x))
31
32 /**Define function and object**/
33 #define pb push_back
34 #define Sort(v) sort(v.begin(),v.end())
35 #define RSort(v) sort(v.rbegin(),v.rend())
36 #define CSort(v,C) sort(v.begin(),v.end(),C)
37 #define all(v) (v).begin(),(v).end()
38 #define sqr(x) ((x)*(x))
39 #define find_dist(a,b) sqrt(sqr(a.x-b.x)+sqr(a.y-b.y))
40
41 /**Define constant value**/
42 #define ERR 1e-9
43 #define pi (2*acos(0))
44 #define PI 3.141592653589793
45
46 /**Define input**/
47 #define scanint(a) scanf("%d",&a)
48 #define scanLLD(a) scanf("%lld",&a)
49 #define scanstr(s) scanf("%s",s)
```

```

50 #define scanline(l) scanf("%[^\n]",l);
51
52 /**Define Bitwise operation**/
53 #define check(n, pos) (n & (1<<(pos)))
54 #define biton(n, pos) (n | (1<<(pos)))
55 #define bitoff(n, pos) (n & ~(1<<(pos)))
56
57 /**Define color**/
58 #define WHITE 0
59 #define GREY 1
60 #define BLACK 2
61
62 /**Sync off with stdio**/
63 #define -- cin.sync_with_stdio(false);\
64         cin.tie();
65 /**Debug tools**/
66 #define what_is(x) cerr<<(#x)<<" is "<<x<<endl
67 using namespace std;
68
69 /**Typedef**/
70 typedef vector<int> vint;
71 typedef vector< vint > vint2D;
72 typedef vector<string> vstr;
73 typedef vector<char>vchar;
74 typedef vector< vchar >vchar2D;
75 typedef queue<int> Qi;
76 typedef queue< Qi > Qii;
77 typedef map<int, int> Mii;
78 typedef map<string, int> Msi;
79 typedef map<int, string> Mis;
80 typedef stack<int> stk;
81 typedef pair<int, int> pp;
82 typedef pair<int, pp > ppp;
83 typedef long long int LLD;
84 const int inf=0x7FFFFFFF;
85
86 /**Template & structure**/
87 struct point_int{int x,y; point_int(){} point_int(int a,int b){x=a,y=b;}}; //Point
    for x,y (int) coordinate in 2D space
88 struct point_double{double x,y; point_double(){} point_double(double a,double b){x=a,
    y=b;}}; //Point for x,y (double) coordinate in 2D space
89 struct Node{int v,w; Node() {} bool operator<(const Node &a) const {return w>a.w;} Node(
    int _v, int _w){v=_v,w=_w;}}; //Node for Dijkstra
90 namespace my{
91 template<class T>T gcd(T a,T b){return b == 0 ? a : gcd(b, a % b);}
92 template<typename T>T lcm(T a, T b) {return a / gcd(a,b) * b;}
93 template<class T>T big_mod(T n,T p,T m){if(p==0)return (T)1;T x=big_mod(n,p/2,m);x
    =(x*x)%m;if(p&1)x=(x*n)%m;return x;}
94 template<class T>T multiplication(T n,T p,T m){if(p==0)return (T)0;T x=
    multiplication(n,p/2,m);x=(x+x)%m;if(p&1)x=(x+n)%m;return x;}
95 template<class T>T my_pow(T n,T p){if(p==0)return 1;T x=my_pow(n,p/2);x=(x*x);if(p
    &1)x=(x*n);return x;} //n to the power p
96 template <class T> double getdist(T a, T b){return sqrt((a.x - b.x) * (a.x - b.x) +
    (a.y - b.y) * (a.y - b.y));} // distance between a & b
97 template <class T> T extract(string s, T ret) {stringstream ss(s); ss >> ret;
    return ret;} // extract words or numbers from a line
98 template <class T> string tostring(T n) {stringstream ss; ss << n; return ss.str()
    ;} // convert a number to string
99 template<class T> inline T Mod(T n,T m) {return (n%m+m)%m;} //For Positive
    Negative No.
100 template<class T> T MIN3(T a,T b,T c) {return min(a,min(b,c));} // minimum of 3
    number
101 template<class T> T MAX3(T a,T b,T c) {return max(a,max(b,c));} //maximum of 3
    number
102 template <class T> void print_vector(T &v){int sz=v.size();if(sz)cout<<v[0];for(int
    i = 1; i < sz; i++)cout << ' ' <<v[i];cout<<"\n";} // prints all elements in a
    vector
103 bool isVowel(char ch){ ch=toupper(ch); if(ch=='A' || ch=='U' || ch=='I' || ch=='O' || ch=='
    E') return true; return false;}
104 bool isConsonant(char ch){if (isalpha(ch) && !isVowel(ch)) return true; return

```

```

        false;}}
105 /**Shortcut input function**/
106 int read_int(){int n;scanf("%d",&n);return n;}
107 int read_LLD(){LLD n;scanf("%lld",&n);return n;}
108 inline int buffer_input() { char inp[1000]; scanstr(inp); return atoi(inp); }
109
110 /**Direction**/
111 //int col[8] = {0, 1, 1, 1, 0, -1, -1, -1};int row[8] = {1, 1, 0, -1, -1, -1, 0,
112 //1}; //8 Direction
113 //int col[4] = {1, 0, -1, 0};int row[4] = {0, 1, 0, -1}; //4 Direction
114 //int dx[]={2,1,-1,-2,-2,-1,1,2};int dy[]={1,2,2,1,-1,-2,-2,-1};//Knight
115 //Direction
116 //int dx[]={-1,-1,+0,+1,+1,+0};int dy[]={-1,+1,+2,+1,-1,-2}; //Hexagonal
117 //Direction
118
119 /*****Ajaira Jinish Sesh*****/
120 int dp[88][88];
121 int N,M,step;
122 char S1[88],S2[88];
123 int solve(int i,int j)
124 {
125     if(i==N and j==M)return 0;
126     if(i==N)return M-j;
127     if(j==M)return N-i;
128     int &ret=dp[i][j];
129     if(ret!=-1)return ret;
130     ret=(1<<28);
131     if(S1[i]==S2[j]) ret=solve(i+1,j+1);
132     else
133     {
134         ret=min(ret,solve(i,j+1)+1);
135         ret=min(ret,solve(i+1,j)+1);
136         ret=min(ret,solve(i+1,j+1)+1);
137     }
138     return ret;
139 }
140 void pathPrint(int i,int j,int del,int ins,int st)
141 {
142     if(i==N&&j==M) return ;
143     if(i==N)
144     {
145         for(int k=j;k<M;k++,i++)
146         {
147             printf("%d Insert %d,%c\n",st++,i-del+1+ins,S2[k]);
148         }
149         return ;
150     }
151     if(j==M)
152     {
153         for(;i<N;i++)
154         {
155             printf("%d Delete %d\n",st++,i-del+1+ins);
156             del++;
157         }
158         return ;
159     }
160     int ret = solve(i,j);
161     int tmp;
162     if(S1[i]==S2[j])
163     {
164         tmp=solve(i+1,j+1);
165         if(ret==tmp)
166         {
167             pathPrint(i+1,j+1,del,ins,st);
168             return ;
169         }
170     }
171     tmp=solve(i,j+1)+1;
172     if(tmp==ret)

```

```

171 {
172     printf("%d Insert %d,%c\n",st,i-del+1+ins,S2[j]);
173     pathPrint(i,j+1,del,ins+1,st+1);
174     return ;
175 }
176 tmp=solve(i+1,j)+1;
177 if(tmp==ret)
178 {
179     printf("%d Delete %d\n",st,i-del+1+ins);
180     pathPrint(i+1,j,del+1,ins,st+1);
181     return ;
182 }
183 tmp=solve(i+1,j+1)+1;
184 if(tmp==ret)
185 {
186     printf("%d Replace %d,%c\n",st,i-del+1+ins,S2[j]);
187     pathPrint(i+1,j+1,del,ins,st+1);
188     return ;
189 }
190 return ;
191 }
192 int main()
193 {
194     #ifdef _ANICK_
195     //f_input;
196     #endif // _ANICK_
197     bool New=false;
198     while(gets(S1))
199     {
200         gets(S2);
201         if(New) printf("\n");
202         New=true;
203         N=strlen(S1);
204         M=strlen(S2);
205         mem(dp,-1);
206         step=solve(0,0);
207         printf("%d\n",step);
208         pathPrint(0,0,0,0,1);
209     }
210     return 0;
211 }

```


Chapter 5

Strings

5.1 KMP

Tutorial

```
1 #include<bits/stdc++.h>
2 using namespace std;
3 char TXT[10000000], ptr[10000000];
4 vector<int> compute_prefix(const char *p)
5 {
6     int m=strlen(p+1);
7     vector<int> prefix(m+1);
8     prefix[1]=0;
9     int k=0;
10    for(int i=2; i<=m; i++)
11    {
12        while(k>0 and p[k+1]!=p[i]) k=prefix[k];
13        if(p[k+1]==p[i]) k=k+1;
14        prefix[i]=k;
15    }
16    return prefix;
17 }
18 vector<int> KMP_match(const char *txt, const char *ptrn)
19 {
20     int n=strlen(txt+1);
21     int m=strlen(ptrn+1);
22     vector<int> Prefix=compute_prefix(ptrn);
23     vector<int> Match_position;
24     int q=0;
25     for(int i=1; i<=n; i++)
26     {
27         while(q>0 and ptrn[q+1]!=txt[i]) q=Prefix[q];
28         if(ptrn[q+1]==txt[i]) q=q+1;
29         if(q==m)
30         {
31             Match_position.push_back(i-m);
32             q=Prefix[q];
33         }
34     }
35     return Match_position;
36 }
37 int main()
38 {
39     scanf("%s %s", TXT+1, ptr+1);
40     vector<int> Match_position=KMP_match(TXT, ptr);
41     for(int i=0; i<Match_position.size(); i++)
42     {
43         if(!i) printf("%d", Match_position[i]);
44         else printf(" %d", Match_position[i]);
45     }
46     return 0;
47 }
```

5.2 Aho Corasick

5.2.1 Aho Corasick with Dynamic Trie

```
1 #include<bits/stdc++.h>
2 using namespace std;
3 #define Max 26
4 int getID(char c)
5 {
6     return c>='a'?c-'a':c-'A';
7 }
8 char inp[1000005];
9 char text[1000005];
10 int ans[5000];
11 map<string,int>Map;
12 vector<int>v;
13 struct Trie
14 {
15     Trie *next[26],*fail;
16     int stringMap;
17     Trie()
18     {
19         stringMap=0;
20         for(int i=0;i<Max;i++)next[i]=NULL;
21         fail=NULL;
22     }
23 };
24 Trie *root;
25 void Insert(const char *str,int M)
26 {
27     Trie *p=root;
28     for(int i=0;str[i];i++)
29     {
30         int id=getID(str[i]);
31         if(p->next[id]==NULL)p->next[id]=new Trie();
32         p=p->next[id];
33     }
34     p->stringMap=M;
35 }
36 void computeFailure()
37 {
38     Trie *u,*prefix;
39     queue<Trie*>Q;
40     Q.push(root);
41     while(!Q.empty())
42     {
43         u=Q.front(); //Take a new node
44         Q.pop();
45         for(int i=0;i<Max;i++)
46         {
47             if(u->next[i]!=NULL) //select fail position of ith node of parent u
48             {
49                 prefix=u->fail; // Going to u node fail position/ prefix position
50                 while(prefix!=NULL)
51                 {
52                     if(prefix->next[i]!=NULL) //if match found
53                     {
54                         u->next[i]->fail=prefix->next[i];
55                         break;
56                     }
57                     prefix=prefix->fail; // match not found, going to upper child
58                     // prefix position
59                 }
60                 if(prefix==NULL)u->next[i]->fail=root;
61                 Q.push(u->next[i]);
62             }
63         }
64     }
65 }
66 void AhoCorasick(const char *str)
```

```

66 {
67     Trie *p=root;
68     int cnt=0;
69     for (int i=0;str[i];i++)
70     {
71         int id=getID(str[i]);
72         while(p->next[id]==NULL&&p!=root)p=p->fail, cnt++;
73         if(p->next[id]!=NULL)p=p->next[id];
74         Trie *tp=p;
75         while(tp!=root)
76         {
77             cnt++;
78             if(tp->stringMap>0)ans[tp->stringMap]++;
79             tp=tp->fail;
80         }
81     }
82 }
83 void Delete(Trie *u)
84 {
85     if(u==NULL) return;
86     for (int i=0;i<Max;i++)Delete(u->next[i]);
87     delete u;
88 }
89
90 int main()
91 {
92     int test;
93     scanf("%d",&test);
94     for (int t=1;t<=test;t++)
95     {
96         Map.clear();
97         v.clear();
98         memset(ans,0,sizeof(ans));
99         root=new Trie();
100         int N;
101         scanf("%d",&N);
102         scanf("%s",text);
103         int cnt=1;
104         for (int i=0;i<N;i++)
105         {
106             scanf("%s",inp);
107             if(Map.find(inp)==Map.end())Map[inp]=cnt++;
108             Insert(inp,Map[inp]);
109             v.push_back(Map[inp]);
110         }
111         computeFailure();
112         AhoCorasick(text);
113         printf("Case %d:\n",t);
114         for (int i=0;i<N;i++)
115         {
116             printf("%d\n",ans[v[i]]);
117         }
118         Delete(root);
119     }
120     return 0;
121 }

```

5.2.2 Aho Corasick with Static Trie

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define root 0
4 #define NuLL -1
5 #define Max 248878
6 #define MC 26
7 int ans[10000];
8 char text[1000005];
9 char inp[100000];
10 map<string,int>Map;
11 vector<int> v;

```

```

12 int getID(const char c)
13 {
14     return c>='a'?c-'a':c-'A';
15 }
16 struct Trie
17 {
18     struct node
19     {
20         int Next[26], fail;
21         int stringMap;
22         void clear()
23         {
24             memset(Next, -1, sizeof(Next));
25             fail=-1;
26             stringMap=0;
27         }
28     }T[Max];
29     int ptr;
30     void clear()
31     {
32         ptr=1;
33         T[0].clear();
34     }
35     void Insert(char *str, int M)
36     {
37         int p=0;
38         for(int i=0; str[i]; i++)
39         {
40             int id=getID(str[i]);
41             if(T[p].Next[id]==-1)
42             {
43                 T[p].Next[id]=ptr;
44                 T[ptr++].clear();
45             }
46             int q=p;
47             p=T[p].Next[id];
48             if(p<0)
49             {
50                 while(1);
51             }
52         }
53         T[p].stringMap=M;
54     }
55     void ComputeFailure()
56     {
57         queue<int>Q;
58         Q.push(root);
59         int u, prefix;
60         int cnt=0, cnt2=0;
61         while(!Q.empty())
62         {
63             u=Q.front();
64             Q.pop();
65             for(int i=0; i<MC; i++)
66             {
67                 if(T[u].Next[i]!=NULL)
68                 {
69                     int now=T[u].Next[i];
70                     prefix=T[u].fail;
71                     while(prefix!=NULL)
72                     {
73                         cnt2++;
74                         if(T[prefix].Next[i]!=NULL)
75                         {
76                             T[now].fail=T[prefix].Next[i];
77                             break;
78                         }
79                         prefix=T[prefix].fail;
80                     }
81                     if(prefix==NULL)T[now].fail=root;

```

```

82         Q.push(now);
83     }
84 }
85 }
86 }
87 };
88 void AhoCorasick(const Trie &A, const char *str)
89 {
90     int p=root;
91     int cnt1=0,cnt2=0;
92     for(int i=0;str[i];i++)
93     {
94         int id=getID(str[i]);
95         while(A.T[p].Next[id]==NULL&&p!=root)p=A.T[p].fail;
96         if(p!=NULL&&A.T[p].Next[id]!=NULL)p=A.T[p].Next[id];
97         int tp=p;
98         while(tp!=root)
99         {
100             if(A.T[tp].stringMap>0)ans[A.T[tp].stringMap]++;
101             tp=A.T[tp].fail;
102         }
103     }
104 }
105 Trie A;
106 int main()
107 {
108     #ifdef _ANICK_
109         freopen("input.txt","r",stdin);
110     #endif // _ANICK_
111     int test;
112     scanf("%d",&test);
113     for(int t=1;t<=test;t++)
114     {
115         Map.clear();
116         v.clear();
117         memset(ans,0,sizeof(ans));
118         A.clear();
119         int N;
120         scanf("%d",&N);
121         scanf("%s",text);
122         int cnt=1;
123         for(int i=0;i<N;i++)
124         {
125             scanf("%s",inp);
126             if(Map.find(inp)==Map.end())Map[inp]=cnt++;
127             A.Insert(inp,Map[inp]);
128             v.push_back(Map[inp]);
129         }
130         A.ComputeFailure();
131         AhoCorasick(A,text);
132         printf("Case %d:\n",t);
133         for(int i=0;i<N;i++)
134         {
135             printf("%d\n",ans[v[i]]);
136         }
137     }
138     return 0;
139 }

```

5.3 Manacher's Algorithm

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 string s, t;
4 char str[1000005];
5 void prepare_string()
6 {
7     int i;
8     t = "^#";
9     for(i = 0; i < s.size(); i++)

```

```

10     t += s[i], t += "#";
11     t += "$";
12 }
13
14 int manacher()
15 {
16     prepare_string();
17
18     int P[t.size()], c = 0, r = 0, i, i_mirror, n = t.size() - 1;
19
20     for(i = 1; i < n; i++)
21     {
22         i_mirror = (2 * c) - i;
23
24         P[i] = r > i? min(r - i, P[i_mirror]) : 0;
25
26         while(t[i + 1 + P[i]] == t[i - 1 - P[i]])
27             P[i]++;
28
29         if(i + P[i] > r)
30         {
31             c = i;
32             r = i + P[i];
33         }
34     }
35     return *max_element(P + 1, P + n);
36 }
37
38 int main()
39 {
40     int kase = 1;
41     while(scanf("%s", str) && str[0] != 'E')
42     {
43         s = str;
44         printf("Case %d: %d\n", kase++, manacher());
45     }
46     return 0;
47 }

```

Chapter 6

Computational geometry

Chapter 7

Math

7.1 Reduce Ratio

$\left(\frac{A}{B}\right)$ ratio reduce to $\left(\frac{x}{y}\right)$

```
1 int main()
2 {
3     int A,B,x,y;
4     cin>>A>>B>>x>>y;
5     int g=__gcd(x,y);
6     x/=g,y/=g;
7     int t=min(A/x,B/y);
8     cout<<x*t<<" "<<y*t<<endl;
9     return 0;
10 }
```


Chapter 8

Number Theory

8.1 NCR

8.1.1 Lucas Theorem

```
1  /**
2   * Fine NCR % M when N C M are large number.
3   * using Lucas theorem.
4   */
5  #include <bits/stdc++.h>
6  using namespace std;
7  typedef long long LLD;
8  LLD mod=1000003;
9  LLD big_mod(LLD n,LLD p,LLD m)
10 {
11     if (p==0) return (LLD) 1;
12     LLD x=big_mod(n,p/2,m);
13     x=(x*x)%m;
14     if (p&1)x=(x*n)%m;
15     return x;
16 }
17 LLD inverse_modulo(LLD t,LLD m)
18 {
19     return big_mod(t,m-2,m);
20 }
21 LLD combi(LLD n, LLD k,LLD m)
22 {
23     if (n<k)
24         return 0;
25     if (n-k<k)
26         return combi(n,n-k,m);
27     LLD i,p=1,t=1;
28     for (i=n-k+1; i<=n; i++)
29         p=(p*i)%m;
30     for (i=1; i<=k; i++)
31         t=(t*i)%m;
32     return (p*inverse_modulo(t,m))%m;
33 }
34 LLD lucas(LLD n, LLD k, LLD m)
35 {
36     if (n<k)
37         return 0;
38     if (k==0 || n==k)
39         return 1;
40     return (lucas(n/m,k/m,m)*combi(n%m,k%m,m))%m;
41 }
42 int main()
43 {
44     return 0;
45 }
```