### Algorithm Code Book

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## Contents

1	Data Structure	2
2	Graph Theory	3
3	Flow networks/ matching	4
4	Dynamic programming	5
5	Strings         5.1 KMP          5.2 Trie          5.2.1 Static Trie          5.3 Aho Corasick          5.3.1 Aho Corasick with Dynamic Trie          5.3.2 Aho Corasick with Static Trie	6 7 7 8 8 10
6	Computational geometry	14
7	Math	<b>15</b>
8	Number Theory	16

## Data Structure

Graph Theory

Flow networks/ matching

# Dynamic programming

### Strings

### 5.1 KMP

#### Tutorial

```
_{1} #include < bits / stdc++.h>
2 using namespace std;
3 char TXT[10000000], ptr[10000000];
4 vector<int> compute_prefix(const char *p)
6
       int = strlen(p+1);
       vector < int > prefix (m+1);
       prefix[1]=0;
       int k=0;
9
10
       for (int i=2; i \le m; i++)
            while (k>0 \text{ and } p[k+1]!=p[i]) k=prefix[k];
12
            if(p[k+1]==p[i])k=k+1;
13
14
            prefix[i]=k;
15
       return prefix;
16
17 }
vector < int > KMP_match(const char *txt, const char *ptrn)
19
       int n=strlen(txt+1);
20
       int m=strlen(ptrn+1);
21
       vector<int> Prefix=compute_prefix(ptrn);
22
       vector < int > Match_position;
23
24
       int q=0;
       for ( int  i = 1; i <= n; i++)</pre>
25
26
            while (q>0 \text{ and } ptrn[q+1]!=txt[i]) q=Prefix[q];
27
            if(ptrn[q+1]==txt[i])q=q+1;
28
            if(q=m)
30
31
                Match_position.push_back(i-m);
                q=Prefix[q];
32
            }
33
```

```
return Match_position;
35
36 }
37 int main()
38 {
            scanf("%s %s", TXT+1, ptr+1);
39
            vector < int > Match_position = KMP_match(TXT, ptr);
40
            for (int i=0; i<Match_position.size(); i++)</pre>
41
42
                   \begin{array}{ll} \textbf{if} \ (!\,i\,) \ printf \ ("\%d"\,, Match\_position \ [\,i\,]) \ ; \\ \textbf{else} \ \ printf \ ("\%d"\,, Match\_position \ [\,i\,]) \ ; \\ \end{array} 
43
44
45
            return 0;
46
47 }
```

#### **5.2** Trie

#### 5.2.1 Static Trie

```
1 #define Max 10005
2 int getId(char c)
3 {
        return c>='a'?c-'a':c-'A'+26;
4
5 }
6
  struct Trie
7
  {
        struct Tree
8
9
             int Next[52];
10
11
            bool word;
             void clear()
12
13
             {
                  word=false;
14
                  \operatorname{memset}(\operatorname{Next}, -1, \operatorname{sizeof}(\operatorname{Next}));
15
16
        T[Max];
17
18
        int ptr;
        void clear()
19
20
        {
21
             ptr=1;
            T[0].clear();
22
            memset(T[0]. Next, 0, sizeof(T[0]. Next));
23
24
        void Insert(const char *str)
25
26
             int p=0;
27
             for (int i=0; str[i]; i++)
28
29
30
                  int id=getId(str[i]);
31
                  if(T[p].Next[id] \le 0)
32
                       T[p].Next[id]=ptr;
33
                      T[ptr++].clear();
34
35
                  p=T[p].Next[id];
36
```

```
T[p].word=true;
38
39
       bool Search (const char *str)
40
41
            int p=0;
42
            for (int i=0; str[i]; i++)
43
44
                 int id=getId(str[i]);
45
46
                 if(T[p].Next[id]>0)
47
                     p=T[p].Next[id];
48
49
                 else return false;
50
51
            return T[p]. word;
52
53
54
55 Trie A;
```

### 5.3 Aho Corasick

### 5.3.1 Aho Corasick with Dynamic Trie

```
1 #include < bits / stdc++.h>
2 using namespace std;
з #define Max 26
4 int getID(char c)
5 {
       return c>='a'?c-'a':c-'A';
6
7 }
8 char inp[1000005];
9 char text[1000005];
10 int ans [5000];
map<string, int>Map;
vector < int > v;
13 struct Trie
14 {
       Trie *next[26], * fail;
15
       int stringMap;
16
17
       Trie()
18
            stringMap = 0;
19
20
            for (int i=0; i < Max; i++)next[i]=NULL;</pre>
            fail=NULL;
21
23 };
  Trie *root;
24
  void Insert (const char *str, int M)
25
26
       Trie *p=root;
27
       for (int i=0; str[i]; i++)
28
29
            int id=getID(str[i]);
30
            if(p->next[id]==NULL)p->next[id]=new Trie();
31
           p=p->next[id];
32
33
```

```
p−>stringMap=M;
34
35
  }
   void computeFailure()
36
   {
37
         Trie *u, * prefix;
38
        queue<Trie*>Q;
39
40
        Q. push (root);
         while (!Q. empty())
41
42
              u=Q.front(); ///Take a new node
43
             Q. pop();
44
              \begin{array}{ll} \textbf{for} \; (\; \textbf{int} \quad i = 0; i < \!\! \text{Max} \; ; \; i + \!\! +) \end{array}
45
46
                   if (u->next[i]!=NULL) ///select fail position of ith
47
        node of parent u
48
                        prefix=u->fail; /// Going to u node fail position/
49
         prefix position
50
                        while (prefix!=NULL)
                        {
                              if (prefix -> next[i]!=NULL) ///if match found
52
53
                                   u \! - \! > \! n \, ext \, [ \, i \, ] \! - \! > \! f \, a \, i \, l \! = \! p \, r \, e \, f \, i \, x \, - \! > \! n \, ext \, [ \, i \, ] \, ;
55
                                   break;
56
                              prefix=prefix->fail; /// match not found, going
57
          to upper child prefix position
58
                        if (prefix=NULL)u->next[i]->fail=root;
59
                        Q. push (u->next [ i ]);
60
61
              }
62
63
64 }
   void AhoCorasick(const char *str)
65
66
         Trie *p=root;
67
68
         int cnt = 0;
         for (int i=0; str[i]; i++)
69
70
              int id=getID(str[i]);
71
72
              while (p->next [id]==NULL&&p!=root)p=p->fail, cnt++;
              if (p->next [id]!=NULL)p=p->next [id];
73
              Trie *tp=p;
74
              while (tp!=root)
75
76
77
                   if(tp->stringMap>0)ans[tp->stringMap]++;
78
                   tp=tp->fail;
79
80
81
82 }
   void Delete (Trie *u)
83
84 {
         if (u=NULL) return;
85
         for(int i=0; i<Max; i++)Delete(u->next[i]);
86
        delete u;
```

```
88
89
90 int main()
91 {
        int test;
92
        scanf("%d",&test);
93
        for (int t=1; t <= test; t++)
94
95
96
            Map.clear();
97
            v.clear();
            memset(ans,0,sizeof(ans));
98
            root=new Trie();
99
            int N;
100
            scanf("%d",&N);
101
            scanf("%s", text);
            int cnt=1;
103
            for(int i=0; i<\!\!N; i++)
106
                 scanf("%s", inp);
                 if(Map. find(inp)=Map. end())Map[inp]=cnt++;
108
                 Insert(inp,Map[inp]);
                 v.push_back(Map[inp]);
109
111
            computeFailure();
            AhoCorasick(text);
            printf("Case %d:\n",t);
113
            for (int i=0; i< N; i++)
114
115
                 printf("%d\n", ans[v[i]]);
116
117
118
            Delete (root);
119
        return 0;
120
121 }
```

#### 5.3.2 Aho Corasick with Static Trie

```
1 #include < bits / stdc++.h>
2 using namespace std;
з #define root 0
4 #define NuLL −1
5 #define Max 248878
6 #define MC 26
7 int ans[10000];
8 char text[1000005];
9 char inp[100000];
10 map<string , int>Map;
vector \langle int \rangle v;
  int getID(const char c)
12
13 {
       return c>='a'?c-'a':c-'A';
14
15 }
16 struct Trie
17
  {
       struct node
18
19
           int Next[26], fail;
20
```

```
int stringMap;
21
22
            void clear()
            {
23
                 memset(Next, -1, sizeof(Next));
24
                 fail=-1;
25
                 stringMap = 0;
26
27
       T[Max];
28
29
        int ptr;
        void clear()
30
31
32
            ptr=1;
            T[0].clear();
33
34
        void Insert (char *str, int M)
35
36
37
            int p=0;
            for (int i=0; str[i]; i++)
38
39
                 int id=getID(str[i]);
40
41
                 if(T[p].Next[id]==-1)
42
                      T[p].Next[id]=ptr;
43
44
                     T[ptr++].clear();
45
46
                 int q=p;
                 p\!\!=\!\!T[\,p\,] . Next [ id ] ;
47
                 if(p<0)
48
49
                      while (1);
50
51
            T[p].stringMap=M;
53
54
55
        void ComputeFailure()
56
            queue<int>Q;
57
58
            Q. push (root);
            int u, prefix;
59
60
            int cnt=0, cnt2=0;
            while (!Q. empty())
61
62
                 u=Q. front();
63
                 Q. pop();
                 for(int i=0; i < MC; i++)
65
66
                      if(T[u].Next[i]!=NuLL)
67
                      {
68
                           int now=T[u].Next[i];
69
                           prefix=T[u].fail;
70
                           while (prefix!=NuLL)
71
                           {
72
73
                               cnt2++;
                                if (T[prefix].Next[i]!=NuLL)
74
75
                                    T[\,now\,] . fail=T[prefix]. Next[i];
76
```

```
78
79
                               prefix=T[prefix].fail;
80
                           if ( prefix=NuLL)T[now]. fail=root;
81
                          Q. push (now);
82
                      }
83
                 }
84
            }
85
86
87 };
   void AhoCorasick(const Trie &A, const char *str)
88
89
        int p=root;
90
        int cnt1=0, cnt2=0;
91
        for (int i=0; str[i]; i++)
92
93
94
             int id=getID(str[i]);
             while (A.T[p].Next[id]==NuLL\&p!=root)p=A.T[p].fail;
95
96
             if (p!=NuLL&&A.T[p]. Next[id]!=NuLL)p=A.T[p]. Next[id];
            int tp=p;
97
98
             while (tp!=root)
99
                 if (A.T[\,tp\,].\,stringMap > 0) ans [A.T[\,tp\,].\,stringMap] + +;
101
                 tp=A.T[tp].fail;
103
104
   Trie A;
105
106
   int main()
107
108
        #ifdef _ANICK_
            freopen("input.txt","r",stdin);
109
        #endif // _ANICK_
110
111
        int test;
        scanf("%d",&test);
112
113
        for(int t=1;t \le test;t++)
114
115
            Map.clear();
116
            v. clear();
117
            memset(ans,0,sizeof(ans));
            A. clear ();
118
            int N;
119
            scanf("%d",&N);
120
            scanf("%s", text);
121
             int cnt=1;
122
             for(int i=0; i<\!\!N; i++)
124
                 scanf("%s", inp);
125
                 if(Map. find(inp)=Map.end())Map[inp]=cnt++;
126
                 A. Insert (inp, Map[inp]);
127
                 v.push_back(Map[inp]);
128
129
            A. ComputeFailure();
130
            AhoCorasick (A, text);
             printf("Case %d:\n",t);
132
             for (int i=0; i< N; i++)
133
134
```

### 5.4 Manacher's Algorithm

```
1 #include < bits / stdc++.h>
using namespace std;
з string s, t;
4 char str [1000005];
5 void prepare_string()
6 {
       int i;
t = "^#";
8
       for (i = 0; i < s.size(); i++)
9
          t += s[i], t += "#";
10
       t += "$";
11
12 }
13
14 int
      manacher()
15 {
       prepare_string();
16
17
       int P[t.size()], c = 0, r = 0, i, i-mirror, n = t.size() - 1;
18
19
       for(i = 1; i < n; i++)
20
21
           i_{-}mirror = (2 * c) - i;
22
23
           P[i] = r > i? \min(r - i, P[i_mirror]) : 0;
24
25
           while (t[i + 1 + P[i]] = t[i - 1 - P[i]])
26
               P[i]++;
27
28
           if(i + P[i] > r)
29
           {
30
31
                c = i;
               r = i + P[i];
32
33
34
       return *max_element(P + 1, P + n);
35
36 }
37
  int main()
38
39
       int kase = 1;
40
       while (scanf(" %s", str) && str[0] != 'E')
41
42
43
           printf("Case \%d: \%d\n", kase++, manacher());
44
45
       return 0;
46
47 }
```

# Computational geometry

Math

Number Theory