## Algorithm Code Book

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## **Data Structure**

#### 1.1 Trie

#### 1.1.1 Static Trie

```
1 #define Max 10005
2 int getId(char c)
3 {
       return c>='a'?c-'a':c-'A'+26;
4
5 }
6 struct Trie
7
8
       struct Tree
9
            int Next[52];
11
           bool word;
12
           void clear()
           {
13
                word=false;
14
                memset(Next, -1, sizeof(Next));
15
16
       T[Max];
17
       int ptr;
18
       void clear()
19
21
           ptr=1;
           T[0].clear();
22
           memset(T[0].Next,0,sizeof(T[0].Next));
23
24
       void Insert(const char *str)
25
26
           int p=0;
27
           for (int i=0; str [i]; i++)
28
29
                int id=getId(str[i]);
                if(T[p].Next[id] <= 0)
31
32
                    T[p].Next[id]=ptr;
33
                    T[ptr++].clear();
34
35
                p=T[p].Next[id];
36
37
           T[p]. word=true;
38
39
       bool Search (const char *str)
```

```
41
            int p=0;
42
            for ( int i = 0; str [ i ]; i++)
43
44
                 int id=getId(str[i]);
45
                 if (T[p]. Next[id]>0)
                 {
                      p=T[p]. Next[id];
48
49
                 else return false;
50
51
            return T[p].word;
52
53
54 };
55 Trie A;
```

#### 1.2 RMQ

#### 1.2.1 Bit

#### 1D Bit

```
1 #define MaxVal 100000
2 int Bit[MaxVal];
3 /**find sum from 1 to idx**/
4 int read(int idx)
5 {
6
       int sum = 0;
       while (idx > 0)
8
           sum += Bit[idx];
9
           i\,\mathrm{d} x \ -\!\!= \ (\,i\,\mathrm{d} x \ \& \ -i\,\mathrm{d} \, x\,)\;;
10
11
       return sum;
12
13 }
  /**update value ind to MaxVal**/
14
void update(int idx ,int val)
16
       while (idx \le MaxVal)
17
18
19
            Bit[idx] += val;
20
           idx += (idx \& -idx);
21
22
23
  /**Find the value of idx**/
24
  int readSingle(int idx)
25
26
       int sum = Bit[idx]; /// sum will be decreased
27
       if (idx > 0) /// special case
28
29
            int z = idx - (idx & -idx); /// make z first
30
           idx--; /// idx is no important any more, so instead y, you can use
31
      idx
            while (idx != z) /// at some iteration idx (y) will become z
32
33
                sum -= Bit[idx];/// substruct Bit frequency which is between y
34
      and "the same path"
                idx = (idx \& -idx);
35
           }
36
```

```
return sum;
}
```

#### 2D Bit

```
void updatey(int x , int y , int val)
2 {
       while (y \le \max_{y})
3
4
           tree[x][y] += val;
5
6
           y += (y \& -y);
7
8 }
9
  void update(int x , int y , int val)
10 {
       while (x \le \max_{x} x)
11
12
           updatey(x , y , val); // this function should update array tree[x]
13
           x += (x \& -x);
14
15
16 }
```

#### 1.2.2 Square Root Decomposition

```
1 #include < bits / stdc++.h>
2 using namespace std;
3 \text{ const int } sz = 100005;
4 const int inf=(1 < < 28);
5 template < typename t> t MIN3(t a, t b, t c)
6 {
7
       return min(a, min(b, c));
8 }
9 int BLOCK[400];
10 int arr[sz];
  int getId(int indx,int blockSZ)
11
12
13
       return indx/blockSZ;
14 }
void init (int sz)
16
       for (int i=0; i \le sz; i++)BLOCK[i]=inf;
17
18
  void update(int val, int indx, int blockSZ)
19
20 {
       int id=getId(indx, blockSZ);
21
       BLOCK[id]=min(BLOCK[id], val);
22
23 }
24 int query (int L, int R, int blockSZ)
25 {
       int lid=getId(L, blockSZ);
26
       int rid=getId(R, blockSZ);
27
       if(lid=rid)
28
29
            int ret=inf;
30
            for(int i=L; i<=R; i++)ret=min(ret, arr[i]);</pre>
31
            return ret;
32
33
       int ml=inf,m2=inf,m3=inf;
       for (int i=L; i < (lid+1)*blockSZ; i++)m1=min(m1, arr[i]);</pre>
35
       for (int i=lid+1; i<rid; i++)m2=min(m2,BLOCK[i]);</pre>
36
       for (int i=rid*blockSZ; i<=R; i++)m3=min(m3, arr[i]);</pre>
```

```
return MIN3(m1,m2,m3);
38
39 }
40 int main()
41 {
       int N,Q;
42
       scanf ("%d %d",&N,&Q);
43
       int blockSZ=sqrt(N);
44
       init (blockSZ);
45
       for (int i=0; i < N; i++)
46
47
            int x;
48
            scanf("%d",&x);
49
            arr[i]=x;
50
51
            update(x, i, blockSZ);
       }
53
       while (Q--)
55
            int x, y;
            scanf("%d %d",&x,&y);
56
            printf("\%d \ n", query(x,y,blockSZ));
57
58
       return 0;
59
60
```

#### 1.2.3 MO's Algorithm

```
2
      MO's Algorithm
      \verb|problem:| | \texttt{http://www.spoj.com/problems/DQUERY}|
3
4
       MOs algorithm is just an order in which we process the queries.
5
      We were given M queries, we will re-order the queries in a particular
6
      order and then process them.
       Clearly, this is an off-line algorithm. Each query has L and R, we will
      call them opening and closing.
       Let us divide the given input array into Sqrt(N) blocks.
8
       Each block will be N / Sqrt(N) = Sqrt(N) size.
       Each opening has to fall in one of these blocks.
10
       Each closing has to fall in one of these blocks.
11
12
       All the queries are first ordered in ascending order of their block
13
      number (block number is the block in which its opening falls).
       Ties are ordered in ascending order of their R value.
14
15
16 **/
17 #include < bits / stdc++.h>
18 using namespace std;
19 #define Mx 30005
20 #define MxNum 1000005
21 int BlockSize;
22 int Answer;
int Freq[MxNum],Num[Mx];
24 struct info
25 {
26
       int L,R,qno;
       info(int L=0,int R=0,int qno=0):L(L),R(R),qno(qno)\{\};
27
28
       bool operator < (const info &a) const
29
           if (L/BlockSize!=a.L/BlockSize) return L/BlockSize <a.L/BlockSize;</pre>
           return R<a.R;
```

```
33 } Query [200005];
34 int StoreAnswer [200005];
35 void Add(int indx)
36
37
       Freq[Num[indx]]++;
38
       if (Freq [Num[indx]]==1) Answer++;
39
  void Remove(int indx)
40
41 {
       Freq[Num[indx]] - -;
42
       if(Freq[Num[indx]]==0)Answer--;
43
44 }
  int main()
45
46
47
       int N;
       scanf("%d",&N);
48
49
       BlockSize=sqrt(N);
       for (int i=0; i < N; i++)
50
51
            scanf("%d",&Num[i]);
53
       int Q;
54
       scanf("%d",&Q);
55
       for (int i=0; i<Q; i++)
56
57
       {
            int x,y;
58
59
            scanf("%d %d",&x,&y);
            Query [i] = info(x-1,y-1,i);
60
61
       sort(Query,Query+Q);
62
       int currentL=0,currentR=0;
63
       Answer=0;
64
       for (int i=0; i<Q; i++)
65
66
            int L=Query[i].L;
67
            int R=Query[i].R;
68
            while (currentL<L)
69
            {
                Remove(currentL);
                currentL++;
72
73
            while (currentL>L)
74
75
                Add(currentL - 1);
76
                currentL --;
77
            }
78
            while (currentR<=R)
79
            {
                Add(currentR);
81
82
                currentR++;
            }
83
            while (currentR>R+1)
84
            {
85
                Remove (currentR - 1);
86
                currentR --;
87
88
            StoreAnswer [Query [i].qno]=Answer;
89
90
       for (int i=0; i<Q; i++)
91
92
       {
            printf("%d\n", StoreAnswer[i]);
93
```

```
94 }
95 return 0;
96 }
```

#### 1.2.4 Segment Tree

#### Lazy Propagration1

```
1 /**
2 **You are given an array of N elements, which are initially all 0. After **
      that you will be given C commands. They are
  **0 p q v - you have to add v to all numbers in the range **of p to q (
      inclusive), where p and q are two indexes of the array.
  **1 p q - output a line containing a single integer which is the sum of all
      **the array elements between p and q (inclusive)
5 */
6 #include < bits / stdc++.h>
7 using namespace std;
8 typedef long long LLD;
9 LLD tree [3*100005];
10 LLD lazy [3*100005];
  void update(int left, int right, int index, int x, int y, int value)
11
12
  {
13
       if (x<=left&&y>=right)
14
       {
            tree[index] += (LLD)(right - left + 1)*value;
           lazy[index]+=value;
           return;
17
18
       int mid = (left + right)/2;
19
       if (lazy [index]!=0)
20
21
           tree[2*index]+=(LLD)(mid-left+1)*lazy[index];
22
           tree[2*index+1]+=(LLD)(right-mid)*lazy[index];
           lazy [2*index]+=lazy [index];
24
           lazy [2*index+1]+=lazy [index];
25
           lazy[index]=0;
26
27
       if(x \le mid)
28
29
           update(left, mid,2*index,x,y,value);
30
31
       if (y>mid)
32
33
       {
           update(mid+1,right,2*index+1,x,y,value);
34
35
       tree[index] = tree[2*index] + tree[2*index+1];
36
37
38 LLD query(int left, int right, int index, int x, int y)
39
40
      LLD a1=0, a2=0;
       if (x<=left&&y>=right)
41
42
       {
           return tree[index];
43
       int mid = (left + right)/2;
45
       if (lazy [index]!=0)
46
47
           tree[2*index]+=(LLD)(mid-left+1)*lazy[index];
48
           tree[2*index+1]+=(LLD)(right-mid)*lazy[index];
49
           lazy [2*index] += lazy [index];
50
```

```
lazy [2*index+1]+=lazy [index];
51
            lazy[index]=0;
52
53
       if(x \le mid)
54
       {
            a1=query(left, mid, 2*index, x, y);
57
       if (y>mid)
58
59
       {
            a2=query(mid+1, right, 2*index+1, x, y);
60
61
       return (a1+a2);
62
63
64 int main()
65
66
       int test,t;
       scanf("%d",&test);
67
       for (t=1;t \le test;t++)
68
69
            memset(tree, 0, sizeof(tree));
70
            memset(lazy,0,sizeof*lazy);
71
            int s, q;
72
            scanf("%d %d",&s,&q);
73
            while (q--)
74
75
            {
                 int x,y,v,dec;
76
                 scanf("%d",&dec);
                 if (dec)
79
                 {
                      scanf("%d %d",&x,&y);
80
                     LLD ans=query (0, s-1, 1, x-1, y-1);
81
                      printf("%lld\n",ans);
82
                 }
83
                 else
84
                 {
85
                      scanf("%d %d %d",&x,&y,&v);
86
                      update (0, s-1, 1, x-1, y-1, v);
87
89
90
       return 0;
91
92
```

#### Lazy Propagration2

```
13 {
14
        if (left=right)
            Tree [indx][0]=1;
16
            Tree [indx][1] = Tree [indx][2] = lazy[indx] = 0;
17
            return;
18
19
       int mid = (left + right)/2;
20
       build (left, mid, 2*indx);
21
       build (mid+1, right, 2*indx+1);
22
       for (int i=0; i<3; i++)
23
       {
24
            Tree [indx][i] = Tree[2*indx][i] + Tree[2*indx+1][i];
25
26
27
28
   void update(int left, int right, int indx, int x, int y, int add)
29
        if (lazy [indx])
30
31
             int lazy_val=lazy[indx];
32
            lazy [2*indx] = (lazy [2*indx] + lazy_val) \%3;
33
            lazy [2*indx+1]=(lazy [2*indx+1]+lazy_val) %3;
34
            for (int i=0; i<3; i++)temp [(lazy_val+i)%3]=Tree [indx][i];
35
            for (int i=0; i<3; i++)Tree [indx][i]=temp[i];
36
            lazy[indx]=0;
37
38
        if (left >y | | right <x) return;</pre>
39
40
       if(x \le left \&\& right \le y)
41
42
             for (int i = 0; i < 3; i++)
43
            {
                 temp[(i+add)%3]=Tree[indx][i];
44
45
            for (int i = 0; i < 3; i++) Tree [indx] [i] = temp[i];
46
47
            lazy [2*indx] = (lazy [2*indx] + add) \%3;
            lazy [2*indx+1]=(lazy [2*indx+1]+add) \%3;
48
49
            return;
50
        int mid = (left + right)/2;
51
       update(left, mid, 2 * indx, x, y, add);
52
       update(mid+1, right, 2*indx+1, x, y, add);
       for (int i = 0; i < 3; i++)
54
            Tree [indx][i] = Tree[2*indx][i] + Tree[2*indx+1][i];
56
57
58
       query (int left, int right, int indx, int x, int y)
59
  int
60
   {
        if (lazy [indx])
61
       {
62
            int lazy_val=lazy[indx];
63
            lazy [2*indx] = (lazy [2*indx] + lazy_val) \%3;
64
            lazy [2*indx+1]=(lazy [2*indx+1]+lazy_val)%3;
65
            for (int i=0;i<3;i++)temp[(lazy_val+i)%3]=Tree[indx][i];
66
             for (int i=0; i<3; i++) Tree [indx] [i]=temp[i];
67
            lazy[indx]=0;
68
69
       if(left>y||right<x)return 0;
70
        if(x \le left \&\& right \le y) return Tree[indx][0];
71
       int mid = (left + right)/2;
72
       return query(left, mid, 2*indx,x,y)+query(mid+1,right,2*indx+1,x,y);
```

```
74 }
75 int main()
76
        int x,y;
77
        int test;
78
        scanf("%d",&test);
79
80
        for (int t=1; t \le t \in t; t++)
81
            memset(lazy,0, sizeof(lazy));
82
            int N,Q;
83
            scanf("%d %d",&N,&Q);
84
            build(0,N-1,1);
85
             printf("Case \%d: \n",t);
86
87
             for (int i=0; i<Q; i++)
88
             {
89
                 int d;
                 scanf("%d %d %d",&d,&x,&y);
91
                  if(d==0)
92
                      update(0, N-1, 1, x, y, 1);
93
94
                  else printf("%d \setminus n", query(0,N-1,1,x,y));
95
            }
96
97
98
        return 0;
99
```

#### Segment Tree Variant 1

```
1 /**
2 **Give a array Of N numbers. Finding Maximum cumulative number frequency in
      **the range.
3 **input:
4 **10 4
5 **1 1 1 3 3 3 3 2 2 2
6 **1 5
7 **1 6
8 **1 7
9 **Output:
10 **3
11 **3
12 **4
13 **2
14 */
15 #include < bits / stdc++.h>
16 using namespace std;
17 typedef long long LLD;
18 #define MAX 50005
19 struct info
20 {
       int Lcnt, Rcnt, Max, Lnum, Rnum;
21
       info(int Lcnt=0,int Rcnt=0,int Max=0,int Lnum=0,int Rnum=0):Lcnt(Lcnt),
22
      Rcnt(Rcnt), Max(Max), Lnum(Lnum), Rnum(Rnum) {};
23 };
24 info Tree[3*MAX];
25 int arr [MAX];
info marge (const info &L, const info &R)
27
  {
28
       info ret;
       if (L.Rnum=R.Lnum)
29
```

```
ret.Max=max(L.Rcnt+R.Lcnt, max(L.Max, R.Max));
31
32
        }
33
        else ret.Max=max(L.Max,R.Max);
        ret.Lnum=L.Lnum;
34
        ret.Rnum=R.Rnum;
35
        if (L.Lnum=R.Lnum) ret.Lcnt=L.Lcnt+R.Lcnt;
36
37
        else ret.Lcnt=L.Lcnt;
        if (L.Rnum=R.Rnum) ret.Rcnt=L.Rcnt+R.Rcnt;
38
        else ret.Rcnt=R.Rcnt;
39
        return ret;
40
41 }
  void build(int L, int R, int indx)
42
43
44
        if (L=R)
45
        {
46
             Tree [indx] = info (1,1,1,arr [L], arr [R]);
             return;
        int mid=(L+R)>>1;
49
        build (L, mid, 2*indx);
50
        build (mid+1,R,2*indx+1);
        Tree [indx] = marge (Tree [2*indx], Tree [2*indx+1]);
53
  info query (int L, int R, int indx, int x, int y)
54
55
        if (L>=x&&R<=y) return Tree[indx];</pre>
56
57
        int mid=(L+R)>>1;
58
        info c1, c2;
59
        if(x \le mid) c1 = query(L, mid, 2 * indx, x, y);
60
        if(y>mid)c2=query(mid+1,R,2*indx+1,x,y);
61
        return marge(c1,c2);
62
   int main()
63
64
65
        int test;
        scanf("%d",&test);
66
        for (int t=1; t <= test; t++)
67
69
             int N,C,Q;
             scanf("%d %d %d",&N,&C,&Q);
70
             for (int i = 0; i < N; i++)
72
                  int x;
73
                  scanf("%d",&arr[i+1]);
74
75
             build (1,N,1);
76
             printf("Case \%d: \n",t);
             while (Q--)
79
             {
80
                  int x,y;
                  scanf("%d %d",&x,&y);
81
                  p \, \texttt{rintf} \, (\, \texttt{"%d} \backslash \texttt{n"} \, , \texttt{query} \, (\, 1 \, , N, 1 \, , x \, , y \,) \, . \, Max) \, ;
82
             }
83
84
        return 0;
85
86
```

#### Segment Tree Variant 2

```
_{1} /** _{2} **You are given a sequence A of N (N <= 50000) integers between -10000 and
```

```
10000.
3 **On this sequence you have to apply M (M \le 50000) operations:
   **modify the i-th element in the sequence or for given x y print max{Ai + Ai
        +1 + ... + Aj \mid x \le i \le j \le y.
6 \#include < bits / stdc++.h>
7 using namespace std;
8 typedef long long LLD;
9 template < class T> T MAX3(T a,T b,T c) {return max(a,max(b,c));}
10 LLD Inf = (111 << 60);
11 #define MN 50005
12 struct info
13 {
14
        LLD prefixSum;
        LLD suffixSum;
16
        LLD Total;
        LLD TotalMax;
17
        info(int pre=-Inf,int suff=-Inf,int total=-Inf,int totalmax=-Inf):
        prefixSum(pre), suffixSum(suff), Total(total), TotalMax(totalmax) { };
   };
19
   info marge (const info &a, const info &b)
20
21
        info ret;
22
        ret. Total=a. Total+b. Total;
23
        ret.prefixSum=max(a.prefixSum,a.Total+b.prefixSum);
24
        ret.suffixSum=max(a.suffixSum+b.Total,b.suffixSum);
25
        ret . TotalMax=MAX3(a. TotalMax, b. TotalMax, a. suffixSum+b. prefixSum);
        return ret;
27
28
29 LLD arr [MN];
30 info Tree [3*MN];
   void build (int L, int R, int indx)
31
32
         i f (L==R)
33
34
        {
              Tree [indx] = info (arr [L], arr [L], arr [L], arr [L]);
35
              return;
36
        int mid = (L+R) >> 1;
38
        build (L, mid, 2*indx);
39
        build (mid+1,R,2*indx+1);
40
        Tree [indx] = marge (Tree [2*indx], Tree [2*indx+1]);
41
42
   void update(int L, int R, int indx, int x, LLD val)
43
   {
44
        if (L==R)
45
46
        {
              Tree [indx]=info(val, val, val, val);
47
              return;
48
49
        int mid=(L+R)>>1;
50
        if(x \le mid)update(L, mid, 2*indx, x, val);
51
        \textcolor{red}{\textbf{else}} \hspace{0.2cm} \texttt{update} \hspace{0.1cm} (\hspace{0.1cm} \texttt{mid} \hspace{-0.1cm}+\hspace{-0.1cm} 1, \hspace{-0.1cm} R, 2 \hspace{-0.1cm} * \hspace{0.1cm} \texttt{ind} \hspace{0.1cm} x \hspace{-0.1cm}+\hspace{-0.1cm} 1, \hspace{-0.1cm} x \hspace{-0.1cm}, \hspace{0.1cm} \texttt{val} \hspace{0.1cm} ) \hspace{0.1cm} ;
        Tree [indx] = marge(Tree[2*indx], Tree[2*indx+1]);
53
54
   info query (int L, int R, int indx, int x, int y)
55
56
         if (L=x and y=R) return Tree [indx];
57
        int mid = (L+R) >> 1;
58
         if(y \le mid) return query(L, mid, 2 * indx, x, y);
59
        else if (x>mid) return query (mid+1,R,2*indx+1,x,y);
```

```
return marge(query(L, mid, 2*indx, x, mid), query(mid+1, R, 2*indx+1, mid+1, y));
61
62 }
63 int main()
64 {
       #ifdef _ANICK_
65
66
       //f_input;
67
       #endif // _ANICK_
68
       int N;
       scanf("%d",&N);
69
       for (int i=1;i<=N; i++)scanf("%lld",&arr[i]);
70
       build (1,N,1);
71
       int Q;
72
       scanf("%d",&Q);
73
74
       while (Q--)
75
       {
76
            int t, x, y;
            scanf("%d %d %d",&t,&x,&y);
            if (t) printf ("%lld\n", query (1,N,1,x,y). TotalMax);
78
            else update (1, N, 1, x, y);
79
80
       return 0;
81
82
```

#### Segment Tree Variant 3

```
1 /**
2 **Given a bracket sequence.
3 ** On a bracket word one can do the following operations:
4 **replacement -- changes the i-th bracket into the opposite one
5 **check — if the word is a correct bracket expression
6 **/
7 \frac{\text{\#include}}{\text{obits}} / \text{stdc} + + .h >
8 using namespace std;
9 typedef long long LLD;
10 #define MAX 50005
11 struct info
12 {
13
       int sum, sub;
       info(int sum=0, int sub=0): sum(sum), sub(sub) {};
14
15 };
info Tree[4*MAX];
17 char inp [MAX];
info marge(const info &L, const info &R)
19 {
       info ret;
20
       ret.sum= L.sum+R.sum;
21
22
       ret.sub=L.sub;
       ret.sub=min(ret.sub,L.sum+R.sub);
23
24
       return ret;
25 }
26 void build (int L, int R, int indx)
27 {
       if (L=R)
28
29
       {
30
            int x;
            if (inp [L] == '(')x = 1;
31
            else x=-1;
32
            Tree [indx] = info(x,x);
33
34
            return;
35
       int mid=(L+R)>>1;
36
```

```
build (L, mid, 2*indx);
37
38
       build (mid+1,R,2*indx+1);
39
       Tree [indx] = marge (Tree [2*indx], Tree [2*indx+1]);
40
  void update(int L, int R, int indx, int x)
41
42
43
       if (L==R)
44
       {
45
            int x;
            if(inp[L]=='(')x=1;
46
            else x=-1;
47
            Tree [indx] = info(x,x);
48
            return;
49
50
51
       int mid=(L+R)>>1;
52
       if(x \le mid) update(L, mid, 2 * indx, x);
       else update (mid+1,R,2*indx+1,x);
       Tree [indx] = marge (Tree [2*indx], Tree [2*indx+1]);
54
55
  info query (int L, int R, int indx, int x, int y)
56
57
       if (L=x&R=y) return Tree [indx];
58
       int mid = (L+R) >> 1;
59
       if(y \le mid) return query(L, mid, 2 * indx, x, y);
60
       else if (x>mid) return query (mid+1,R,2*indx+1,x,y);
61
       else return marge (query (L, mid, 2*indx, x, mid), query (mid+1, R, 2*indx+1, mid
62
       +1,y));
63
64
  int main()
65
   {
66
       int N, t=1;
       while (scanf("%d",&N)==1)
67
68
            scanf("%s", inp);
69
            build (0, N-1, 1);
70
            int Q;
71
            printf("Test %d:\n",t++);
72
            scanf("%d",&Q);
            while (Q--)
75
76
                 int x;
                 scanf("%d",&x);
                 if(x)
                 {
79
                      if(inp[x-1]=='(')inp[x-1]=')';
80
                      else inp[x-1]='(';
81
                     update(0, N-1, 1, x-1);
82
                 }
84
                 else
85
                 {
                      info y=query(0,N-1,1,0,N-1);
86
                      if(y.sum=0\&\&y.sub>=0)printf("YES\n");
87
                      else printf("NO\n");
88
                 }
89
90
91
       return 0;
92
93
```

#### 1.2.5 Sliding Window RMQ

```
1 /**
2
       every K size window RMQ
       Calculate in O(N+K) time
3
4 **/
5 #include < bits / stdc++.h>
6 using namespace std;
7 vector<int>SlidingRMQ(int *A, int N, int k)
8 {
       /** Create a Double Ended Queue, Qi that will store indexes of array
9
      elements
           The queue will store indexes of useful elements in every window and
10
      it will
           maintain decreasing order of values from front to rear in Qi, i.e.,
11
           arr [Qi.front []] to arr [Qi.rear()] are sorted in increasing order
12
13
14
       vector < int > MinWindow;
       deque < int > Q;
16
       int i;
       /* Process first k (or first window) elements of array */
17
       for (i = 0; i < k; i++)
18
19
           /// For very element, the previous largest elements are useless so
20
           /// remove them from Qi
21
           while (!Q.empty() \text{ and } A[i] \le A[Q.back()])Q.pop_back();
22
           Q. push_back(i);
23
24
       /// Process rest of the elements, i.e., from arr[k] to arr[n-1]
25
       while (i <N)
26
27
           /// The element at the front of the queue is the smallest element of
28
           /// previous window, so insert it result
29
           MinWindow.push_back(A[Q.front()]);
30
31
           /// Remove the elements which are out of this window
32
           while (!Q.empty()) and Q.front() \le i-k)Q.pop_front();
33
34
           /// Remove all elements larger than the currently
35
           /// being added element (remove useless elements)
           while (!Q.empty() \text{ and } A[i] \le A[Q.back()])Q.pop_back();
37
38
           /// Add current element at the rear of Qi
39
           Q. push_back(i);
40
           i++;
41
42
       /// insert the minimum element of last window
43
       MinWindow.push_back(A[Q.front()]);
44
       return MinWindow;
45
46 }
47 int main()
48 {
       int A[] = \{100, 10, -1, 2, -3, -4, 10, 1, 100, 20\};
49
       vector < int > a = SlidingRMQ(A, 10, 2);
50
       for (int i=0; i < a. size(); i++)cout << a[i] << "";
51
       return 0;
52
53 }
```

#### 1.2.6 Sparse Table

```
/**
Compute sparse table in O(NlogN)
query in O(1)
```

```
Ref link: https://www.topcoder.com/community/data-science/data-science-
        tutorials/range-minimum-query-and-lowest-common-ancestor/
5 **/
6 #include < bits / stdc++.h>
7 using namespace std;
8 #define Max 10000005
9 int rmq[24][Max];
10 int A[Max];
void Compute_ST(int N)
12 {
         for (int i = 0; i < N; ++i)rmq[0][i] = i;
13
         for (int k = 1; (1 << k) < N; ++k)
14
               for (int i = 0; i + (1 << k) <= N; i++)
16
17
              {
                    \begin{array}{ll} \mbox{int} & x \, = \, rmq \, [\, k \, - \, 1\,] \, [\, i\, ]\,; \\ \mbox{int} & y \, = \, rmq \, [\, k \, - \, 1\,] \, [\, i \, + \, (\, 1 \, << \, k \, - \, 1) \, ]\,; \end{array}
18
19
                    rmq[k][i] = A[x] \le A[y] ? x : y;
20
              }
21
         }
22
23
24
   int RMQ(int i, int j)
25
26
         int k = log2(j-i);
27
         int x = rmq[k][i];
28
         29
30
         \mathbf{return} \ \mathbf{A}[\mathbf{x}] \iff \mathbf{A}[\mathbf{y}] \ ? \ \mathbf{x} : \mathbf{y};
31
32
33
   int main()
34 {
35
36
         return 0;
37 }
```

#### 1.3 Heavy Light Decomposition

```
1 #include < bits / stdc++.h>
2 using namespace std;
3 #define pp pair<int,int>
4 #define pb push_back
5 const int Max=10000;
6 struct info
7
  {
8
        int v, cost;
9
        info(int v=0,int cost=0):v(v),cost(cost)\{\};
10 };
vector<pp>edges;
vector <info>Graph [Max+5];
  int Tree[5*Max+5], BaseArray[Max+5], SubTreeSize[Max+5];
14 int ChainHead [Max+5], ChainNum [Max+5], PosInBaseArray [Max+5], ChainNo;
\begin{array}{ll} \text{int} & Level\left[\text{Max}+5\right], Parent\left[\text{Max}+5\right], SparseTable\left[\text{Max}+5\right][16]; \end{array}
16 int ptr;
17
  void init (int N)
18
   {
        for(int i=0; i \le N; i++)
19
20
        {
             Graph[i].clear(), ChainHead[i]=-1;
21
             for (int j=0; j <=15; j++)SparseTable[i][j]=-1;
22
```

```
23
24
       edges.clear();
25
       ptr=ChainNo=0;
26
  void buildSegmentTree(int 1, int r, int indx)
27
  {
28
29
       if ( l==r )
30
       {
            Tree [indx]=BaseArray[l];
31
32
            return;
33
       int mid = (l+r) >> 1;
34
       int lindx=indx << 1;
35
       int rindx=lindx | 1;
36
       buildSegmentTree(l,mid,lindx);
37
38
       buildSegmentTree(mid+1,r,rindx);
       Tree [indx] = max(Tree [lindx], Tree [rindx]);
39
40
   void updateSegmentTree(int l, int r, int indx, int update_indx, int value)
41
42
       if ( l==r )
43
       {
44
            Tree [indx]=value;
45
            return;
46
       }
47
       int mid=(l+r)>>1;
48
       int \lim dx = \inf dx <<1;
49
50
       int rindx=lindx | 1;
51
       if (update_indx <= mid) updateSegmentTree(l, mid, lindx, update_indx, value);</pre>
       else updateSegmentTree(mid+1,r,rindx,update_indx,value);
       Tree [indx] = max(Tree [lindx], Tree [rindx]);
53
54
  int querySegmentTree(int l, int r, int indx, int x, int y)
55
56
       if (1>y | | r<x) return 0;
57
       if (x<=l&&y>=r) return Tree[indx];
58
       int mid=(l+r)>>1;
59
       int \lim dx = \inf dx <<1;
60
       int rindx=lindx | 1;
61
       int c1=0, c2=0;
62
       if (x<=mid) c1=querySegmentTree(l, mid, lindx, x, y);</pre>
63
       if (y>mid) c2=querySegmentTree(mid+1,r,rindx,x,y);
64
       return \max(c1, c2);
65
66
   void dfs (int from, int u, int depth)
67
68
       Level [u]=depth;
69
       Parent [u]=from;
70
71
       SubTreeSize[u]=1;
72
       int sz=Graph[u].size();
       for (int i = 0; i < sz; i++)
73
74
       {
            int v=Graph[u][i].v;
75
            if (v==from)continue;
76
            dfs(u,v,depth+1);
77
            SubTreeSize[u]+=SubTreeSize[v];
78
79
80
   void sparseTable(int N)
81
82
       for (int i=0; i \le N; i++) Sparse Table [i][0] = Parent[i];
```

```
for (int j=1;(1<< j)<=N; j++)
84
85
       {
            for (int i = 0; i <= N; i++)
86
87
            {
                if (SparseTable [i] [j-1]!=-1)
88
                {
                     int a=SparseTable[i][j-1];
90
                     SparseTable[i][j]=SparseTable[a][j-1];
91
92
                }
            }
93
       }
94
95
   int LCA(int p, int q)
96
97
98
       if(Level[p] < Level[q]) swap(p,q);
99
       int Log=log 2 (Level[p]) + 1;
100
       for (int i=Log; i>=0; i--)
101
            if ((Level[p]-(1<<i))>=Level[q])p=SparseTable[p][i];
102
103
       if(p=q)return p;
104
       for (int i=Log; i>=0; i--)
106
            if (SparseTable [p][i]!=-1&&SparseTable [p][i]!=SparseTable [q][i])
107
            {
108
                p=SparseTable[p][i],q=SparseTable[q][i];
111
       return Parent[p];
112
113
114
    * Actual HL-Decomposition part
115
    * Initially all entries of chainHead[] are set to -1.
116
    * So when ever a new chain is started, chain head is correctly assigned.
117
    * As we add a new node to chain, we will note its position in the baseArray
118
    * In the first for loop we find the child node which has maximum sub-tree
119
       size.
    * The following if condition is failed for leaf nodes.
120
    * When the if condition passes, we expand the chain to special child.
121
    * In the second for loop we recursively call the function on all normal
       nodes.
    * chainNo++ ensures that we are creating a new chain for each normal child.
123
    **/
124
   void heavyLightDecompositon(int from, int curNode, int cost)
125
126
       if (ChainHead [ChainNo]==-1)ChainHead [ChainNo]=curNode; /// Assign chain
127
       head
       ChainNum [curNode]=ChainNo;
128
       PosInBaseArray [curNode] = ptr; /// Position of this node in baseArray
       which we will use in Segtree
       BaseArray [ ptr++]=cost;
130
       int sc=-1, nextCost;
131
       int sz=Graph[curNode].size();
       for (int i=0; i < sz; i++) /// Loop to find special child
134
       {
            int v=Graph[curNode][i].v;
135
            if (v==from)continue;
136
            if(sc == -1 || SubTreeSize[sc] < SubTreeSize[v])
137
            {
138
139
                sc=v;
```

```
nextCost=Graph[curNode][i].cost;
140
141
            }
       if (sc!=-1)heavyLightDecompositon(curNode, sc, nextCost); /// Expand the
143
       chain
       for (int i=0; i < sz; i++)
144
145
       {
            int v=Graph[curNode][i].v;
146
            int cost=Graph[curNode][i].cost;
147
            if (v=from | | sc=v) continue;
148
            ChainNo++;
149
            heavyLightDecompositon(curNode, v, cost);
152
153
   void updateTree(int ith, int val)
154
       pp a=edges[ith];
156
       int u=a.first ,v=a.second;
       int indx=PosInBaseArray[u];
157
       if (Level[u] < Level[v]) indx=PosInBaseArray[v];</pre>
158
       updateSegmentTree(0, ptr-1, 1, indx, val);
159
160
161
   * query_up:
162
    * It takes two nodes u and v, condition is that v is an ancestor of u
163
    * We query the chain in which u is present till chain head, then move to
164
       next chain up
    * We do that way till u and v are in the same chain, we query for that part
165
        of chain and break
166
   int queryUp(int u, int v)
167
168
       if(u=v)return 0;
169
       int uchain, vchain=ChainNum[v], ans=-1;
170
       while (true)
171
172
       {
            uchain=ChainNum[u];
173
            if (uchain=vchain)
                if (u==v)
                                  /// Both u and v are in the same chain, so we
       need to query from u to v, update answer and break.
                                  /// We break because we came from u up till v,
                     break;
       we are done
                ans=max(ans, querySegmentTree(0, ptr-1, 1, PosInBaseArray[v]+1,
178
       PosInBaseArray[u]));
                break;
179
180
            int uchainhead=ChainHead[uchain];
181
            ans=max(ans, querySegmentTree(0, ptr-1,1, PosInBaseArray[uchainhead],
182
       PosInBaseArray[u]));
                         /// Above is call to segment tree query function. We do
183
       from chainHead of u till u. That is the whole chain from
           u=Parent [uchainhead];
184
185
       return ans;
186
187
       queryTree(int u, int v)
188
   int
189
       int lca=LCA(u,v);
       return max(queryUp(u,lca),queryUp(v,lca));
191
192
```

```
int main()
194 {
195
        int test;
        cin>>test;
196
        while (test --)
197
198
199
             int N;
200
             cin >> N;
             init(N);
201
             for (int i=0; i< N-1; i++)
202
             {
203
                 int u, v, c;
204
                 cin>>u>>v>>c;
205
                 u--,v--;
206
207
                 Graph[u].pb(info(v,c));
208
                 Graph[v].pb(info(u,c));
                 edges.pb(pp(u,v));
210
             dfs(-1,0,0);
211
             sparseTable(N);
212
             heavyLightDecomposition (-1,0,-1);
213
             buildSegmentTree(0,ptr-1,1);
214
             string ch;
215
             int x, y;
216
             while (true)
217
218
             {
219
                  cin >> ch;
                  if(ch[0]=='D')break;
220
221
                 cin>>x>>y;
                  if(ch[0]=='Q')printf("%d\n",queryTree(x-1,y-1));
222
                  else if (ch[0] == 'C') updateTree (x-1,y);
223
224
225
        return 0;
226
227 }
```

#### 1.4 Ternary Bit Mask

```
1
1 int more_bit [10];
3 int get_bit(int mask, int pos)
4 {
5
      return (mask / more_bit[pos]) % 3;
6 }
  int set_bit(int mask, int pos , int bit)
7
8
      int tmp = (mask / more_bit[pos]) % 3;
9
      mask -= tmp * more_bit[pos];
10
      mask += bit * more_bit[pos];
11
      return mask;
12
13 }
14 void init (void)
15 {
16
      more_bit[0] = 3;
17
      for(int i = 1; i < 10; i++) more_bit[i] = 3 * more_bit[i - 1];
18 }
```

# Graph Theory

#### 2.1 DFS

#### 2.1.1 Bicoloring

```
///color will be initial with -1
int color[20005];
bool dfs(int u,int c)

{
    if(color[u]==c)return true;
    if(color[u]==(1-c))return false;
    color[u]=c;
    bool ret=true;
    for(auto v:graph[u])ret&=dfs(v,1-c);
    return ret;
}
```

#### 2.1.2 Cycle Finding

```
int color [20005];
2 bool dfs(int u)
3 {
       color [u]=GREY;
4
5
       bool no_cycle=true;
6
       for (auto v:graph[u])
           if ( color [ v]==WHITE)
           {
9
                no_cycle=dfs(v);
10
11
           else if(color[v]==GREY)return false;
12
13
       color [u]=BLACK;
14
       return no_cycle;
15
16 }
```

#### 2.2 Topological Sort

```
#include < bits / stdc ++.h>
using namespace std;
#define WHITE 0
#define GREY 1
#define BLACK 2
vector < int > graph [100005];
```

```
7 vector<int> ans;
8 int visit [100005];
9 bool dfs(int u)
10 {
11
       visit[u]=GREY;
12
       bool no_cycle=true;
13
       int sz=graph[u].size();
       for (int i = 0; i < sz; i++)
14
15
            int v=graph[u][i];
16
            if ( visit [v]==WHITE)
17
            {
18
                 no_cycle=dfs(v);
19
20
            }
21
            else if(visit[v]==GREY)return false;
22
       visit[u]=BLACK;
23
24
       ans.push_back(u);
       return no_cycle;
25
26
  bool topsort (int N)
27
  {
28
       ans.clear();
29
       memset(visit, false, sizeof(visit));
30
       int no_cycle=true;
31
       for (int i = 0; i < N; i++)
32
33
       {
            if ( visit [ i]==WHITE) no_cycle&=dfs(i);
34
35
36
       return no_cycle;
37 }
38 int main()
39
40
       return 0;
41 }
```

#### 2.3 Havel Hakimi

```
1 /**
       Given N degree d1, d2, d3....dn. Is it possible to make a graph which
2
      have no cycle and
       different two node will be connected with one Edge?
3
4
5 **/
6 #include < stdio.h>
7 #include <queue>
8 #include < vector >
9 using namespace std;
10 int main()
11
       int N;
       while (scanf("%d",&N) and N)
13
14
15
            priority_queue <int>Q;
16
            bool Ok=true;
17
            int Odd_Node=0;
            for (int i=0; i < N; i++)
            {
19
20
                int x;
                \operatorname{scanf}("%d",\&x);
21
```

```
if(x>=N or x<0)Ok&=false;
22
                 Odd_Node = (x\%2);
23
                 Q. push(x);
24
25
            Ok&=(Odd_Node%2==0); ///Handshaking Theorem
26
            for (int i=0; i \le N and Ok; i++)
            {
29
                 int k=Q. top();
                 Q. pop();
30
                 vector < int > v;
31
                 for (int j=0; j < k and Ok; j++)
32
33
                      int x=Q.top();
34
                      Q. pop();
35
36
37
                      Ok\&=(x>=0);
                      v.push_back(x);
39
                 for (int j=0; j < k \text{ and } Ok; j++)
40
41
                      Q. push (v[j]);
42
43
44
             if (Ok) printf("Possible\n");
45
            else printf("Not possible\n");
46
47
        return 0;
49
```

#### 2.4 Articulation Point/Bridge

#### 2.4.1 Find Articulation Point:

```
vector < int > Graph [10000];
2 bool visit [10000];
3 int arti[100000];
4 int discover [100000], Back [100000];
5 int predfn;
6 int source;
7 int child_of_root;
8 int cnt = 0;
9 void reset()
10
       memset(visit, false, sizeof(visit));
11
       memset(arti, false, sizeof(arti));
12
       predfn=child_of_root=0;
13
14 }
  void articulation (int v)
15
16
       visit[v] = true;
17
       predfn++;
18
       discover [v]=Back[v]=predfn;
19
       for (int i=0; i < Graph [v]. size (); i++)
20
           int w=Graph[v][i];
22
           if (! visit [w])
24
                articulation (w);
25
                Back[v] = min(Back[v], Back[w]);
26
                if (Back [w]>=discover [v]&&v!=source)
27
```

```
arti[v] = true;
29
                  }
30
31
                  else if (v=source)
                  {
32
                       child_of_root++;
33
34
                       if (child_of_root == 2)
35
                            arti[v] = true;
36
37
                  }
38
             }
39
             else
40
             {
41
42
                  Back[v]=min(Back[v], discover[w]);
43
44
        }
45
```

#### 2.4.2 Find Bridge version 1:

```
_{1} \text{ vector} < \frac{\text{int}}{\text{Graph}} [200];
2 int Back[205], Discover[205];
з bool visit [205];
4 bool bridge [205][205];
5 int brcount;
6 void reset (int n)
7 {
8
       for (int i=0; i \le n; i++)Graph[i].clear();
9
       memset(visit, false, sizeof(visit));
10
       memset(bridge, false, sizeof(false));
       brcount=0;
11
12 }
  void find_bridge(int u, int parent, int depth)
13
14
        visit[u] = true;
15
       Discover [u] = Back [u] = depth;
16
17
       for (int i=0 ; i<Graph[u].size() ; i++)</pre>
18
19
            int v = Graph[u][i];
20
21
            if (visit[v] && v!=parent)
22
23
                 Back[u] = min(Back[u], Discover[v]);
24
25
                (! visit [v])
26
27
            {
                 find_bridge(v, u, depth+1);
                 Back[u] = min(Back[u], Back[v]);
                 if (Back[v]>Discover[u])
30
31
                      brcount++;
32
                      bridge[u][v] = bridge[v][u] = true;
33
                 }
34
            }
35
36
       }
37
38
```

#### 2.4.3 Find Bridge version 2:

```
void find_bridge(int node, int parent)
2 {
3
       discovery_time[node] = bedge[node] = ++T;
       int to, i, connected = adj[node].size();
4
       for (i = 0; i < connected; i++)
5
6
            to = adj [node][i];
            if(to == parent) continue;
8
            if (!discovery_time[to])
9
10
                 \begin{array}{ll} printf(\mbox{"\%d \%d} \mbox{$\backslash$n"$}, \ node\,, \ to\,)\,; \\ find\_bridge(\mbox{$to$}, \ node)\,; \end{array} 
11
12
                13
14
15
            else if(discovery_time[node] > discovery_time[to])
16
17
                 printf("%d %d\n", node, to);
18
                bedge[node] = min(bedge[node], discovery_time[to]);
19
            }
20
       }
21
22 }
```

# Flow networks/ matching

#### 3.1 Max Flow

```
1 #include < bits / stdc++.h>
2 using namespace std;
3 #define pb push_back
4 #define MN 1000
5 typedef vector < vector <int> > vint2D;
6 const int inf=(1 < < 29);
7 vint2D graph;
8 int Cost [MN] [MN];
9 int parent [MN+5];
10 int flow;
void init (int N)
12 {
       graph=vint2D(N);
13
       memset (Cost, 0, size of (Cost));
14
15 }
  void AddEdge(int u, int v, int cost)
17 {
18
       graph[u].pb(v);
19
       graph[v].pb(u);
       Cost[u][v]+=cost;
20
       Cost[v][u]+=cost;
21
22 }
  bool augmenting_path(int source, int sink)
23
24
       memset (parent, -1, size of (parent));
26
       queue<int>Q;
       Q. push (source);
       while (!Q. empty())
28
20
           int u=Q. front();
30
           Q. pop();
31
           int sz=graph[u].size();
32
            for (int i=0; i < sz; i++)
33
34
                int v=graph[u][i];
35
                if (parent[v]==-1 \text{ and } Cost[u][v]>0)
37
                {
                     parent [v]=u;
38
                     Q. push(v);
39
                     if (v==sink)return true;
40
                }
41
```

```
43
        return false;
44
45 }
  void path(int v,int source)
46
47 {
        int u=parent[v];
48
        flow=min(flow, Cost[u][v]);
49
        if (source!=u) path(u, source);
50
        Cost[u][v]-=flow;
51
        Cost\left[\,v\,\right]\left[\,u\right] += flow\;;
        return;
53
54 }
int max_flow(int source, int sink)
56
57
        int ret = 0;
58
        while (augmenting_path (source, sink))
59
        {
              flow=inf;
60
             path(sink, source);
61
             ret+=flow;
62
63
        return ret;
64
  }
65
   int main()
66
67
   {
68
        int test;
69
        scanf("%d",&test);
70
        while (test --)
71
              int P,S,C,M;
72
             scanf ("%d %d %d %d",&P,&S,&C,&M);
73
             init(P+S+5);
74
              int superSource=0,SuperSikn=P+S+1;
75
              for (int i=1;i<=P;i++)AddEdge(superSource,i,1);</pre>
76
              for(int i=1; i \le S; i++)AddEdge(P+1, SuperSikn, C);
77
              for (int i=0; i \triangleleft M; i++)
78
79
                   int x, y;
80
                   scanf("%d %d",&x,&y);
                   \operatorname{AddEdge}\left(\left.x\right.,P\!\!+\!\!y\left.,\left(1\!<\!<\!30\right)\right.\right);
82
83
             printf("%d\n", max_flow(superSource, SuperSikn));
84
85
        return 0;
86
87 }
```

# Dynamic programming

#### 4.1 Edit Distance

```
1 #include < bits / stdc++.h>
2 using namespace std;
3 int dp[88][88];
4 int N,M, step;
5 char S1[88], S2[88];
6 int solve(int i, int j)
7
        if (i \longrightarrow N \text{ and } j \longrightarrow M) \text{ return } 0;
8
        if(i=N) return M-j;
9
        if (j=M) return N-i;
        int &ret=dp[i][j];
11
        if(ret!=-1)return ret;
12
        ret = (1 < < 28);
13
        if(S1[i]==S2[j]) ret=solve(i+1,j+1);
14
        else
16
       {
             ret=min(ret, solve(i, j+1)+1);
17
18
            ret=min(ret, solve(i+1,j)+1);
            ret=min(ret, solve(i+1, j+1)+1);
19
20
        return ret;
21
22 }
  void pathPrint(int i, int j, int del, int ins, int st)
23
24
        if (i=N&&j=M) return ;
25
26
        if (i=N)
             for (int k=j; k < M; k++, i++)
29
                  printf("%d Insert %d,%c\n", st++,i-del+1+ins, S2[k]);
30
            }
31
            return ;
32
33
        if ( j==M)
34
35
             for (; i < N; i++)
37
                  printf("%d Delete %d\n", st++,i-del+1+ins);
38
                 del++;
39
40
            return ;
41
```

```
int ret = solve(i,j);
43
       int tmp;
44
       if (S1[i]==S2[j])
45
46
            tmp = solve(i+1,j+1);
47
48
            if(ret = tmp)
49
            {
                 pathPrint(i+1,j+1,del,ins,st);
50
                 return ;
51
            }
52
53
       tmp=solve(i,j+1)+1;
54
       if (tmp=ret)
56
            printf("%d Insert %d,%c\n",st,i-del+1+ins,S2[j]);
57
58
            pathPrint(i, j+1, del, ins+1, st+1);
59
            return ;
60
       tmp = solve(i+1, j)+1;
61
       if (tmp=ret)
62
63
            printf("%d Delete %d\n",st,i-del+1+ins);
64
            pathPrint\left(\,i+1,j\,\,,d\,e\,l+1,i\,n\,s\,\,,\,s\,t\,+1\right);
65
            return ;
66
67
       tmp = solve(i+1, j+1)+1;
68
69
       if (tmp=ret)
70
       {
            printf("%d Replace %d,%c\n",st,i-del+1+ins,S2[j]);
71
            pathPrint(i+1,j+1,del,ins,st+1);
72
73
            return ;
74
       return ;
75
76
  int main()
77
78
       bool New=false;
79
       while (gets (S1))
80
            gets(S2);
82
            if (New) printf("\n");
83
            New=true;
84
            N=strlen(S1);
85
            M≡strlen(S2);
86
            memset(dp, -1, sizeof(dp));
87
            step=solve(0,0);
88
            printf("%d\n", step);
89
            pathPrint(0,0,0,0,1);
90
91
92
       return 0;
93 }
```

# Strings

#### 5.1 KMP

#### **Tutorial**

```
1 #include < bits / stdc++.h>
using namespace std;
3 char TXT[10000000], ptr [10000000];
4 vector<int> compute_prefix(const char *p)
5
6
       int m=strlen(p+1);
       vector < int > prefix (m+1);
        prefix[1]=0;
       int k=0;
       for (int i=2; i \leqslant m; i++)
11
            while (k>0 \text{ and } p[k+1]!=p[i]) k=prefix[k];
            if(p[k+1]==p[i])k=k+1;
13
            prefix[i]=k;
14
15
       return prefix;
16
17 }
  vector <int > KMP_match(const char *txt, const char *ptrn)
18
19
20
       int n=strlen(txt+1);
21
       int m=strlen(ptrn+1);
22
       vector<int> Prefix=compute_prefix(ptrn);
23
       vector<int>Match_position;
24
       int q=0;
       for(int i=1; i \le n; i++)
25
26
            while (q>0 \text{ and } ptrn[q+1]!=txt[i]) q=Prefix[q];
27
            if(ptrn[q+1]==txt[i])q=q+1;
28
            i f ( q==m)
            {
30
                 Match_position.push_back(i-m);
32
                 q=Prefix[q];
33
34
       return Match_position;
35
36
  int main()
37
38
  {
       \operatorname{scanf}(\text{"%s \%s"},\operatorname{TXT+1},\operatorname{ptr+1});
39
       vector <int > Match_position=KMP_match(TXT, ptr);
40
       for (int i=0; i<Match_position.size(); i++)
```

#### 5.2 Aho Corasick

#### 5.2.1 Aho Corasick with Dynamic Trie

```
1 #include < bits / stdc++.h>
2 using namespace std;
з #define Max 26
4 int getID (char c)
5 {
6
       return c>='a'?c-'a':c-'A';
7 }
8 char inp[1000005];
9 char text[1000005];
10 int ans [5000];
map<string , int >Map;
vector <int>v;
  struct Trie
13
14
       Trie *next[26], * fail;
       int stringMap;
16
       Trie()
17
18
       {
            stringMap = 0;
19
20
            for (int i=0; i<Max; i++)next[i]=NULL;
21
            fail=NULL;
22
23 };
24 Trie *root;
  void Insert (const char *str, int M)
25
26
       Trie *p=root;
27
       for (int i=0; str [i]; i++)
28
29
            int id=getID(str[i]);
            if (p->next[id]==NULL)p->next[id]=new Trie();
            p=p->next[id];
32
33
       p{\longrightarrow} stringMap{=}\!\!M;
34
  }
35
  void computeFailure()
36
37
       Trie *u, * prefix;
38
       queue<Trie*>Q;
39
       Q. push (root);
40
41
       while (!Q. empty())
42
            u=Q. front(); ///Take a new node
43
            Q. pop();
44
            for (int i=0; i<Max; i++)
45
46
47
                 if(u->next[i]!=NULL) ///select fail position of ith node of
       parent u
```

```
48
                       prefix=u->fail; /// Going to u node fail position/ prefix
49
        position
                       while (prefix!=NULL)
50
                      {
51
                           if (prefix ->next[i]!=NULL) ///if match found
52
53
                           {
                                u->next[i]->fail=prefix->next[i];
54
                                break;
55
56
                           prefix=prefix->fail; /// match not found, going to upper
57
         child prefix position
58
                      if (prefix=NULL)u->next[i]->fail=root;
59
60
                      Q. push(u->next[i]);
61
                 }
             }
62
63
64
   void AhoCorasick(const char *str)
65
66
        Trie *p=root;
67
        for ( int i = 0; str [ i ]; i++)
68
69
             int id=getID(str[i]);
70
             while (p->next[id]==NULL&&p!=root)p=p->fail;
71
72
             if(p\rightarrow next[id]!=NULL)p=p\rightarrow next[id];
73
             Trie *tp=p;
74
             while (tp!=root)
75
             {
                  if (tp->stringMap >0) ans [tp->stringMap]++;
76
                  tp=tp->fail;
77
78
79
80
   void Delete (Trie *u)
81
82
83
        if (u=NULL) return;
        for (int i=0; i \le Max; i++) Delete(u->next[i]);
84
        delete u;
85
86
87
   int main()
88
89
90
        int test;
        scanf("%d",&test);
91
        for (int t=1; t \le test; t++)
92
93
        {
94
            Map. clear();
95
             v. clear();
             memset(ans, 0, sizeof(ans));
96
             root=new Trie();
97
             int N;
98
             \operatorname{scanf}("%d",&N);
99
             scanf("%s", text);
100
             int cnt=1;
101
             for (int i=0; i< N; i++)
102
103
                  scanf("%s", inp);
                  if (Map. find (inp) = Map. end ()) Map [inp] = cnt ++;
105
                  Insert(inp,Map[inp]);
106
```

```
v.push_back(Map[inp]);
107
             }
108
             computeFailure();
             AhoCorasick(text);
110
             printf("Case %d:\n",t);
111
112
             for (int i=0; i < N; i++)
113
             {
                  printf("%d\n", ans[v[i]]);
114
115
             Delete (root);
117
        return 0;
118
119
```

#### 5.2.2 Aho Corasick with Static Trie

```
1 #include < bits / stdc++.h>
2 using namespace std;
з #define root 0
4 #define NuLL −1
5 #define Max 248878
6 #define MC 26
7 int ans[10000];
8 char text[1000005];
9 char inp[100000];
10 map<string , int>Map;
11 vector < int > v;
12 int getID (const char c)
13 {
       return c>='a'?c-'a':c-'A';
14
15 }
16 struct Trie
17
       struct node
18
19
            int Next[26], fail;
20
            int stringMap;
21
22
            void clear()
23
                memset(Next, -1, sizeof(Next));
                fail=-1;
25
                stringMap = 0;
26
27
       T[Max];
28
       int ptr;
29
       void clear()
30
31
       {
32
           ptr=1;
33
           T[0]. clear();
34
       void Insert(char *str, int M)
35
       {
36
            int p=0;
37
            for (int i=0; str [i]; i++)
38
39
                int id=getID(str[i]);
40
                if(T[p].Next[id]==-1)
41
42
                {
                     T[p]. Next[id] = ptr;
43
                     T[ptr++].clear();
44
45
```

```
<u>int</u> q=p;
46
47
                 p=T[p]. Next[id];
48
            T[p].stringMap=M;
49
50
51
        void ComputeFailure()
52
        {
53
            queue<int>Q;
            Q. push (root);
54
            int u, prefix;
             while (!Q. empty())
56
57
                 u=Q. front();
58
                 Q. pop();
59
60
                 for (int i=0; i < MC; i++)
61
                      if (T[u]. Next[i]!=NuLL)
63
                           int now=T[u].Next[i];
64
                           prefix=T[u].fail;
65
                           while (prefix!=NuLL)
66
67
                                if(T[prefix].Next[i]!=NuLL)
68
69
                                    T[now]. fail=T[prefix]. Next[i];
70
                                    break;
71
72
                                }
73
                                prefix=T[prefix].fail;
74
                           if ( prefix=NuLL)T[now ]. fail=root;
75
                           Q. push (now);
76
                      }
77
                 }
78
            }
79
80
81
   };
   void AhoCorasick (const Trie &A, const char *str)
82
83
84
        int p=root;
        for (int i=0; str[i]; i++)
85
86
             int id=getID(str[i]);
87
             while (A.T[p].Next[id] == NuLL & p! = root) p = A.T[p].fail;
88
             if (p!=NuLL&&A.T[p]. Next[id]!=NuLL)p=A.T[p]. Next[id];
89
            int tp=p;
90
            while (tp!=root)
91
92
                 if (A.T[tp].stringMap>0)ans[A.T[tp].stringMap]++;
93
94
                 tp=A.T[tp].fail;
            }
95
        }
96
97
   Trie A;
98
   int main()
99
100
       #ifdef _ANICK_
101
            freopen ("input.txt", "r", stdin);
102
       #endif // _ANICK_
103
        int test;
        scanf("%d",&test);
        for (int t=1; t \le test; t++)
106
```

```
107
                  Map. clear();
108
                  v.clear();
                  memset(ans,0,sizeof(ans));
110
                  A. clear();
111
112
                  int N;
                  scanf("%d",&N);
113
                  scanf("%s", text);
114
                  int cnt=1;
115
                  for (int i=0; i< N; i++)
117
                         scanf("%s", inp);
118
                         \label{eq:map:end} \begin{array}{l} \text{if } (\operatorname{Map.\,find}\,(\operatorname{inp}) \!\!=\!\!\!-\!\!\!\operatorname{Map.\,end}\,()\,) \operatorname{Map}[\operatorname{inp}] \!\!=\! \operatorname{cnt} \!+\!+; \end{array}
119
                        A. Insert (inp , Map[inp]);
120
121
                        v.push_back(Map[inp]);
122
                  A. ComputeFailure();
124
                  AhoCorasick(A, text);
                  printf("Case %d:\n",t);
125
                  for (int i = 0; i < N; i++)
126
127
                         printf("%d\n", ans[v[i]]);
128
129
130
131
           return 0;
132
```

#### 5.3 Manacher's Algorithm

```
1 #include < bits / stdc++.h>
2 using namespace std;
3 string s, t;
4 char str [1000005];
5 void prepare_string()
6 {
7
        int i;
        t{=}"\,\hat{}\#"\;;
8
        for (i=0; i < s. size(); i++)
9
             t+=s [ i ] , t+="#";
10
        t+="$";
11
12 }
13
14
   int manacher()
15
        prepare_string();
16
        int P[t.size()], c=0, r=0, i, i\_mirror, n=t.size()-1;
17
        for (i=1; i < n; i++)
19
             i_m i r r o r = (2*c)-i;
20
             P[i]=r>i?min(r-i,P[i-mirror]):0;
21
             while (t[i+1+P[i]]==t[i-1-P[i]]) P[i]++;
22
             _{i\,f}\left(\,i+\!\!P\left[\,i\,\right]\!>\!r\,\right)
23
             {
24
25
26
                  r=i+P[i];
27
28
        return *max_element(P+1,P+n);
29
30 }
31 int main()
```

```
32 {
    int kase=1;
    while(scanf(" %s", str)&&str[0]!= 'E')
    {
        s=str;
        printf("Case %d: %d\n", kase++, manacher());
    }
    return 0;
}
```

### Math

#### 6.1 Reduce Ratio

#### 6.2 Floyd's Cycle Finding algorithm

```
1 #include < bits / stdc++.h>
2 using namespace std;
3 #define pp pair <int, int>
_{4} int Z,L,M,I;
5 int f(int L)
6 {
7
       return (Z*L+I)%M;
8
9 pp CycleFinding()
10
       ///L here initial seed
11
       int hare, tortoise, lambda, meu;
12
       bool cyclefind=false;
13
       hare=tortoise=L;
14
       while (!cyclefind)
15
16
           tortoise=f(tortoise);
17
           hare=f(hare);
18
           hare=f(hare);
19
20
           if (hare==tortoise) cyclefind=true;
21
22
       hare=L;
       meu=0;
23
       while (hare!=tortoise)
24
```

```
meu++;
26
          hare=f(hare);
27
          tortoise=f(tortoise);
28
29
      int i=0;
30
      hare=L;
31
      while (i<=meu)
32
33
      {
          i++;
34
          hare=f(hare);
35
36
      tortoise=f(hare);
37
      lambda=1;
38
39
      while (hare!=tortoise)
40
      {
          tortoise=f(tortoise);
41
          lambda++;
42
43
      return {meu, lambda}; ///meu is starting index and lambda is cycle length
44
45
  int main()
46
  {
47
      int t=1;
48
      49
50
51
          pp a=CycleFinding();
          cout << "Cycle starts from index "<<a.first << "\nCycle length is "<<a.
52
      second << endl;
53
54
      return 0;
55 }
```

# Number Theory

#### 7.1 NCR

#### 7.1.1 Lucas Theorem

```
Fine NCR % M when N C M are large number.
2
       using Lucas theorem.
3
5 #include < bits / stdc++.h>
6 using namespace std;
7 typedef long long LLD;
8 LLD mod=1000003;
9 LLD big_mod(LLD n,LLD p,LLD m)
11
       if(p==0)return (LLD) 1;
      LLD x=big_mod(n,p/2,m);
12
       x=(x*x)\%m;
13
       if(p&1)x=(x*n)\%m;
14
       return x;
15
16
17 LLD inverse_modulo(LLD t,LLD m)
18
       return big_mod(t,m-2,m);
19
20
  LLD combi(LLD n, LLD k, LLD m)
21
22
       if (n<k)
23
           return 0;
24
       if (n-k<k)
25
           return combi(n, n-k,m);
26
      LLD~i~,p\!=\!1,t\!=\!1;
27
       for (i=n-k+1; i \le n; i++)
28
           p=(p*i)m;
       for (i=1; i \le k; i++)
           t = (t * i) \%m;
31
       return (p*inverse_modulo(t,m))%m;
32
33 }
34 LLD lucas (LLD n, LLD k, LLD m)
35 {
       if (n<k)
36
37
           return 0;
       if (k==0 || n==k)
38
           return 1;
39
       return (lucas(n/m, k/m,m)*combi(n\%m, k\%m,m))\%m;
```

```
41 }
42 int main()
43 {
44 return 0;
45 }
```

# Computational geometry