

→ Two event: A, B

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \dots \textcircled{i}$$

Example: two die D_1, D_2

$$\text{sample} = \{(1,1), (1,2) \dots (6,6)\}$$

$\textcircled{36}$

so,

$$P(A=5) = \frac{1}{6}$$

2) $D_1 + D_2 \leq 10$?

$$\therefore P(D_1 + D_2 \leq 10) = \frac{33}{36}$$

Now, $P(D_1 = 5)$ give $D_1 + D_2 \leq 10$?

$$P(D_1 = 5 \mid D_1 + D_2 \leq 10)$$

$$\therefore P(A|B) = \frac{5}{33} \quad \checkmark \checkmark$$

Now back to the formula:

$$A = \{D_1 = 5\}, B = \{D_1 + D_2 \leq 10\}$$

$$P(A \cap B) = \frac{5}{36}$$

$$\begin{aligned} \therefore P(A|B) &= \frac{\frac{5}{36}}{\frac{33}{36}} \\ &= \frac{5}{33} \quad \checkmark \checkmark \end{aligned}$$

