



# ACM Amman Collegiate Programming Contest

## Problem Set

4<sup>th</sup> of July, 2015

### A. Who Is The Winner?

Bahosain is a judge in one of the programming contests. The winner of this contest will be the team that solves the maximum number of problems. If more than one team solves the maximum number of problems, then the one with the minimum penalty will be the winner.

Given the number of problems solved by each team and the penalty, can you help Bahosain by determining the winner of the contest?

#### Input

The first line of input contains an integer  $T$  ( $1 \leq T \leq 128$ ) that represents the number of test cases.

The first line of each test case contains one integer  $N$  ( $1 \leq N \leq 100$ ) that represents the number of teams in the contest.

Each of the next  $N$  lines contains a string **name** followed by two integers  $S$  and  $P$ , where **name** represents the name of the team and contains at most 20 lowercase letters,  $S$  ( $0 \leq S \leq 16$ ) represents the number of problems solved by this team, and  $P$  ( $0 \leq P \leq 1500$ ) represents the penalty of the team.

It is guaranteed that there is only one winner in the contest.

#### Output

For each test case, print a single line with the name of the team who won.

| Sample Input  | Sample Output           |
|---|-------------------------|
| 2<br>3<br>tourist 13 567<br>petr 13 600<br>endagorion 14 419<br>2<br>tourist 7 512<br>bayashout 7 477 | endagorion<br>bayashout |

## B. Rock-Paper-Scissors

Rock-Paper-Scissors is a two-player game, where each player chooses one of Rock, Paper, or Scissors. Here are the three cases in which a player gets one point:

- Choosing Rock wins over a player choosing scissors.
- Choosing Scissors wins over a player choosing Paper.
- Choosing Paper wins over a player choosing Rock.

In all other cases, the player doesn't get any points.

Bahosain and his friend Bayashout played  $N$  rounds of this game. Unlike Bayashout, Bahosain was too lazy to decide what to play next for each round, so before starting to play, he chose three integers  $X$   $Y$   $Z$  such that  $X+Y+Z = N$  and  $X, Y, Z \geq 0$ , and then played Rock for the first  $X$  rounds, Paper for the next  $Y$  rounds, and Scissors for the last  $Z$  rounds.

Bayashout got more points in the  $N$  rounds and won. Given the moves played by Bayashout in each round, Bahosain wants to know the number of ways in which he could have chosen  $X$ ,  $Y$  and  $Z$  such that he wins in the  $N$  rounds.

The winner of the  $N$  rounds is the player that gets more total points in the  $N$  rounds.

### Input

The first line of input contains  $T$  ( $1 \leq T \leq 64$ ), where  $T$  is the number of test cases.

The first line of each test case contains an integer  $N$  ( $1 \leq N \leq 1000$ ) that represents the number of rounds.

The next line contains a string of  $N$  uppercase letters, the first letter represents the choice of Bayashout for the first round, the second letter represents his choice for the second round, and so on.

Each letter in the string is one of the following: **R** (Rock), **P** (Paper), or **S** (Scissors).

### Output

For each test case, print a single line with the number of ways in which Bahosain could have won.

| Sample Input | Sample Output |
|--------------|---------------|
| 4            | 3             |
| 3            | 1             |
| RPS          | 1             |
| 1            | 5             |
| R            |               |
| 5            |               |
| PPRSR        |               |
| 5            |               |
| RPSPR        |               |

### C. Street Lamps

Bahosain is walking in a street of  $N$  blocks. Each block is either empty or has one lamp. If there is a lamp in a block, it will light it's block and the direct adjacent blocks. For example, if there is a lamp at block 3, it will light the blocks 2, 3, and 4.

Given the state of the street, determine the minimum number of lamps to be installed such that each block is lit.

#### Input

The first line of input contains an integer  $T$  ( $1 \leq T \leq 1025$ ) that represents the number of test cases.

The first line of each test case contains one integer  $N$  ( $1 \leq N \leq 100$ ) that represents the number of blocks in the street.

The next line contains  $N$  characters, each is either a dot '.' or an asterisk '\*'.

A dot represents an empty block, while an asterisk represents a block with a lamp installed in it.

#### Output

For each test case, print a single line with the minimum number of lamps that have to be installed so that all blocks are lit.

| Sample Input | Sample Output |
|--------------|---------------|
| 3            | 2             |
| 6            | 0             |
| .....        | 1             |
| 3            |               |
| *.*          |               |
| 8            |               |
| .*. . . . *  |               |

### D. Alternating Strings

Bahosain has a strange habit. He writes his daily notes in binary! His little brother also has a strange habit. He hates seeing alternating patterns of 0s and 1s or strings longer than  $K$ . Therefore, whenever Bahosain writes a binary note on a paper, his little brother cuts it at night with scissors in order to make each part of it not longer than  $K$  and not alternating.

After several years of suffering from cutting binary notes with scissors, Bahosain decided to cut his notes in such a way that his brother won't touch them.

Given a binary string of length  $N$ , find the minimum number of cuts Bahosain has to make such that each of the resulting strings are NOT alternating and contains no more than  $K$  bits.

A binary string is considered alternating only if each bit after the first one is different from the one before it.

For example: strings 110, 0110 and 010100 are not alternating, while 101 and 01 are alternating strings.

A string with one character is not an alternating string.

#### Input

The first line of input contains  $T$  ( $1 \leq T \leq 64$ ) that represents the number of test cases.

The first line of each test case contains two integers:  $N$  and  $K$  ( $1 \leq K \leq N \leq 1000$ ), where  $N$  is the length of the string and  $K$  is the maximum length of a resulting string.

The next line contains a string of  $N$  bits (0 or 1).

#### Output

For each test case, print a single line with the minimum number of cuts.

| Sample Input | Sample Output |
|--------------|---------------|
| 4            | 1             |
| 6 3          | 3             |
| 111000       | 0             |
| 5 2          | 2             |
| 11010        |               |
| 3 3          |               |
| 110          |               |
| 3 3          |               |
| 101          |               |

### E. Epic Professor

Dr. Bahosain works as a professor of Computer Science at HU (Hadramout University).

After grading his programming exam, he noticed that most of the students have failed. Since this is the last semester for him teaching in Yemen, Dr. Bahosain decided to give bonus marks to all students in a fair way. He decided to give the same bonus marks to all students without making the mark of any student exceed **100**.

Help Dr. Bahosain by finding the maximum possible number of students that will pass the course after adding the bonus marks.

A student will pass the course if his mark after adding the bonus marks is more than or equal to **50**.

#### Input

The first line of input contains an integer  **$T$  ( $1 \leq T \leq 1024$ )** that represents the number of test cases.

The first line of each test case contains one integer  **$N$  ( $1 \leq N \leq 100$ )** that represents the number of students in Dr. Bahosain's class.

The next line contains  **$N$**  space-separated integers between **0** and **100**, each representing the initial mark of a student.

#### Output

For each test case, print a single line with the maximum number of students that will pass the course.

| Sample Input         | Sample Output |
|----------------------|---------------|
| 2                    | 3             |
| 5                    | 4             |
| 0 21 83 45 64        |               |
| 7                    |               |
| 99 50 46 47 48 49 98 |               |

## F. Travelling Salesman

After leaving Yemen, Bahosain now works as a salesman in Jordan. He spends most of his time travelling between different cities. He decided to buy a new car to help him in his job, but he has to decide about the capacity of the fuel tank. The new car consumes one liter of fuel for each kilometer.

Each city has at least one gas station where Bahosain can refill the tank, but there are no stations on the roads between cities.

Given the description of cities and the roads between them, find the minimum capacity for the fuel tank needed so that Bahosain can travel between any pair of cities in at least one way.

### Input

The first line of input contains  $T$  ( $1 \leq T \leq 64$ ) that represents the number of test cases.

The first line of each test case contains two integers:  $N$  ( $3 \leq N \leq 100,000$ ) and  $M$  ( $N-1 \leq M \leq 100,000$ ), where  $N$  is the number of cities, and  $M$  is the number of roads.

Each of the following  $M$  lines contains three integers:  $X Y C$  ( $1 \leq X, Y \leq N$ )( $X \neq Y$ )( $1 \leq C \leq 100,000$ ), where  $C$  is the length in kilometers between city  $X$  and city  $Y$ . Roads can be used in both ways.

It is guaranteed that each pair of cities is connected by at most one road, and one can travel between any pair of cities using the given roads.

### Output

For each test case, print a single line with the minimum needed capacity for the fuel tank.

| Sample Input  | Sample Output |
|---|---------------|
| 2<br>6 7<br>1 2 3<br>2 3 3<br>3 1 5<br>3 4 4<br>4 5 4<br>4 6 3<br>6 5 5<br><br>3 3<br>1 2 1<br>2 3 2<br>3 1 3 | 4<br>2        |

## G. Heavy Coins

Bahosain has a lot of coins in his pocket. These coins are really heavy, so he always tries to get rid of some of the coins by using them when paying for the taxi.

Whenever Bahosain has to pay **S** pennies for the taxi driver, he tries to choose the *maximum* number of coin pieces to pay. The driver will accept receiving more than **S** pennies only if he can't remove one or more of the given coins and still has **S** or more pennies.

For example, if Bahosain uses the coins of the following values: **2**, **7** and **5** to pay **11** pennies, the taxi driver will not accept this because the coin of value 2 can be removed. On the other hand, when Bahosain uses coins of **7** and **5** to pay **11** pennies, the driver will accept it.

Note that the driver won't give Bahosain any change back if he receives more than **S** pennies, and Bahosain doesn't care!

### Input

The first line of input contains **T** ( $1 \leq T \leq 1001$ ), the number of test cases.

The first line of each test case contains two integers: **N** ( $1 \leq N \leq 10$ ) and **S** ( $1 \leq S \leq 1000$ ), where **N** is the number of coins in Bahosain's pocket and **S** is the amount (in pennies) Bahosain has to pay for the taxi driver.

The next line contains **N** space-separated integers between **1** and **100** that represent the values (in pennies) of the coins in Bahosain's pocket.

### Output

For each test case, print a single line with the maximum number of coins Bahosain can use to pay for the driver.

| Sample Input   | Sample Output |
|----------------|---------------|
| 2              | 3             |
| 5 9            | 6             |
| 4 1 3 5 4      |               |
| 7 37           |               |
| 7 5 8 8 5 10 4 |               |

### Note

In the first test case, Bahosain can pay in any of the following ways: **(1, 3, 5)**, **(3, 4, 4)** or **(1, 4, 4)**.



## H. Bridges

An edge in an undirected graph is a **bridge** if after removing it the graph will be disconnected.

Given an undirected connected graph, you are allowed to add one edge between any pair of nodes so that the total number of bridges in the graph is minimized.

### Input

The first line of input contains  $T$  ( $1 \leq T \leq 64$ ) that represents the number of test cases.

The first line of each test case contains two integers:  $N$  ( $3 \leq N \leq 100,000$ ) and  $M$  ( $N-1 \leq M \leq 100,000$ ), where  $N$  is the number of nodes, and  $M$  is the number of edges.

Each of the following  $M$  lines contains two space-separated integers:  $X Y$  ( $1 \leq X, Y \leq N$ )( $X \neq Y$ ), which means that there is an edge between node  $X$  and node  $Y$ .

It is guaranteed that each pair of nodes is connected by at most one edge.

Test cases are separated by a blank line.

### Output

For each test case, print a single line with the minimum possible number of bridges after adding one edge.

| Sample Input  | Sample Output |
|---|---------------|
| 2<br>7 7<br>1 2<br>2 3<br>3 1<br>3 4<br>4 5<br>4 6<br>6 7<br><br>3 3<br>1 2<br>2 3<br>3 1 | 1<br>0        |

## I. Bahosain and Digits

Bahosain has a string of digits. He is going to perform the following operation on the string as many times as needed to make all digits in the string the same.

In one move, he can choose a substring of length  $K$  and change each digit in this substring to its next digit, the digit that goes after '9' is '0'.

For example, applying the operation on the string **905** will change it to **016**.

Your task is to determine the maximum  $K$  such that it is possible to make all digits in the string equal using the described operation.

### Input

The first line of input contains an integer  $N$  ( $1 \leq T \leq 128$ ) that represents the number of test cases.

Each test case contains a string of no more than **250** digits (**0 - 9**).

Each string contains at least two different digits.

### Output

For each test case print a single line with the maximum possible  $K$ .

| Sample Input | Sample Output |
|--------------|---------------|
| 3            | 1             |
| 04           | 2             |
| 651          | 3             |
| 0552         |               |

### Note

In the last test case, when  $K = 3$ , Bahosain can perform the operation on the substring **552** five times to get the string **0007**, then perform the operation again on the substring **000** seven times to get **7777**.

## J. Candy

Bahosain went back for teaching but now in a primary school. His classes, which contain a total of  $N$  students, went to a school trip. Bahosain has  $M$  packets of candies; each packet contains one or more candies.

Students think that a distribution of packets is fair if all students from the same age get the same number of candies, and older students get more candies than the younger students.

Given the age of each student, and the number of candies in each packet, determine if it is possible to distribute the packets so that every student gets *exactly one packet* and the distribution is fair according to the students.

### Input

The first line of input contains  $T$  ( $1 \leq T \leq 128$ ), the number of test cases.

The first line of each test case contains two integers:  $N$  ( $1 \leq N \leq 100$ ) and  $M$  ( $N \leq M \leq 200$ ), which represent the number of students and the number of candy packets respectively.

The next line contains  $N$  space-separated integers between 5 and 15, each representing the age of one student.

The next line contains  $M$  space-separated integers between 1 and 50, each representing the amount of candies in one of the packets.

### Output

For each test case print a single line with "YES" if it is possible to distribute the packets according to the problem statement, otherwise print "NO".

| Sample Input | Sample Output |
|--------------|---------------|
| 3            | YES           |
| 3 6          | NO            |
| 5 15 10      | NO            |
| 2 2 2 3 3 4  |               |
| 4 4          |               |
| 5 5 6 7      |               |
| 5 4 6 6      |               |
| 5 6          |               |
| 8 6 7 5 5    |               |
| 1 2 1 3 1 2  |               |

### K. Runtime Error

Bahosain was trying to solve this simple problem, but he got a Runtime Error on one of the test cases, can you help him by solving it?

Given an array of  $N$  non-negative integers and an integer  $K$ , your task is to find two integers  $X$  and  $Y$  from the given array such that  $X \times Y = K$ .

The chosen numbers must have different indices in the array.

#### Input

The first line of input contains  $T$  ( $1 \leq T \leq 128$ ), the number of test cases.

The first line of each test case contains two integers:  $N$  ( $2 \leq N \leq 100,000$ ) and  $K$  ( $1 \leq K \leq 100,000$ ).

The next line contains  $N$  space-separated integers, each between  $0$  and  $100,000$ .

#### Output

For each test case, if there is no solution, print  $-1$  on a single line. Otherwise print a single line with two space-separated integers  $X\ Y$  ( $X \leq Y$ ), where  $X$  and  $Y$  are two numbers from the given array and  $X \times Y = K$ .

If there is more than one possible solution, print the one with the minimum  $X$ .

| Sample Input | Sample Output |
|--------------|---------------|
| 4            | 2 6           |
| 6 12         | -1            |
| 3 6 2 4 2 9  | 3 12          |
| 2 1          | 1 12          |
| 1 2          |               |
| 4 36         |               |
| 12 18 3 36   |               |
| 4 12         |               |
| 1 2 6 12     |               |

## L. Alternating Strings II

*This problem is the same as problem D but with different constraints!*

Bahosain has a strange habit. He writes his daily notes in binary! His little brother also has a strange habit. He hates seeing alternating patterns of 0s and 1s or strings longer than  $K$ . Therefore, whenever Bahosain writes a binary note on a paper, his little brother cuts it at night with scissors in order to make each part of it not longer than  $K$  and not alternating.

After several years of suffering from cutting binary notes with scissors, Bahosain decided to cut his notes in such a way that his brother won't touch them.

Given a binary string of length  $N$ , find the minimum number of cuts Bahosain has to make such that each of the resulting strings are NOT alternating and contains no more than  $K$  bits.

A binary string is considered alternating only if each bit after the first one is different from the one before it.

For example: strings 110, 0110 and 010100 are not alternating, while 101 and 01 are alternating strings.

A string with one character is not an alternating string.

### Input

The first line of input contains  $T$  ( $1 \leq T \leq 128$ ) that represents the number of test cases.

The first line of each test case contains two integers:  $N$  and  $K$  ( $1 \leq K \leq N \leq 100,000$ ), where  $N$  is the length of the string and  $K$  is the maximum length of a resulting string.

The next line contains a string of  $N$  bits (0 or 1).

### Output

For each test case, print a single line with the minimum number of cuts.

| Sample Input | Sample Output |
|--------------|---------------|
| 4            | 1             |
| 6 3          | 3             |
| 111000       | 0             |
| 5 2          | 2             |
| 11010        |               |
| 3 3          |               |
| 110          |               |
| 3 3          |               |
| 101          |               |