

ICT2213 Applied Cryptography

Topic 1.3: Classical Cryptography (Poly-alphabetic ciphers)



Learning outcomes

- Explain how classical poly-alphabetic ciphers, such as the Vigenère and one-time pad ciphers, work
- Cryptanalyze the Vigenère cipher

The one-time pad (OTP) cipher (aka Vernam cipher)

Operation

- The key is a large **non-repeating** set of **truly random** letters
- The sender uses each key letter on the pad to encrypt **exactly one** plaintext character
- Encryption is the same as in the shift cipher
- The receiver has an identical key to decrypt the ciphertext

Example

- Assume the plaintext is **onetimepad**
- Assume the key sequence is **tbfrgfarfm**
- The resulting ciphertext is **HOJKOREGFP**
- The first key letter is t, which corresponds to number 19
- Therefore, character o is shifted 19 positions and wraps around to H

Properties of the OTP cipher

Poly-alphabetic cipher

- The OTP cipher is a **poly-alphabetic** cipher
- Each character of the plaintext can be mapped to any character of the alphabet
- This is because the shift value depends on the letter that is next on the key sequence

Unconditionally secure

- The OTP cipher is the only known **provably secure** cipher
- If used correctly, it cannot be broken
- The reason is that a given ciphertext is **equally likely** to correspond to any plaintext of equal size
- Because all keys are **equally** possible
- However, it is nearly impossible to use OTP correctly

The Vigenère cipher

- The Vigenère cipher is an OTP with a **periodic** key
- The key for Vigenère is a string of characters which is **repeated** until the string of copies is as long as the message
- Encryption is identical to the OTP cipher
- An example can be seen below, where the key is the word **dog**
- In this example
 - The 0th, 3rd, 6th, 9th, . . . characters are shifted by 3
 - The 1st, 4th, 7th, 10th, . . . characters are shifted by 14
 - The 2nd, 5th, 8th, 11th, . . . characters are shifted by 6

Plaintext:	helloworldoutthere
Key:	dogdogdogdogdogdog
Ciphertext:	KSROCCRFRCAGWHNHF

Properties of the Vigenère cipher

Poly-alphabetic cipher

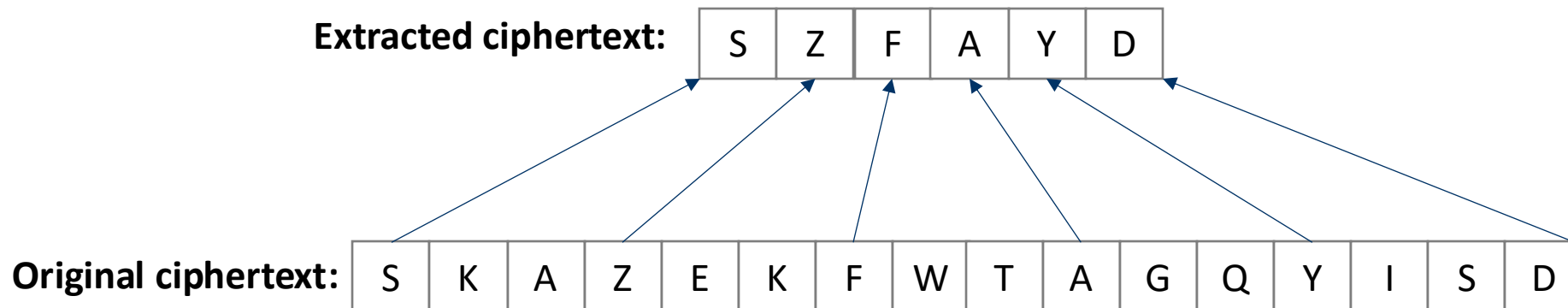
- The Vigenère cipher is a **poly-alphabetic** cipher
- A given letter of the plaintext can be encrypted in **different** ways, depending on where it falls in the message
- This messes up inter-letter statistics, and also flattens single-letter frequency statistics

Completely broken

- Despite its poly-alphabetic nature, the Vigenère cipher is very easy to break.
- The main drawback is the periodic structure of the key
- Once the length of the key is known, Vigenère is as secure as a simple shift cipher

Cryptanalysis of the Vigenère cipher

- Assume that the key length is T (sometimes called the **period**)
- Then, the ciphertext can be divided into T parts
- Each part can be viewed as being encrypted using a **single** instance of the shift cipher
- In the example below, assume that the key length is 3 (maybe an incorrect assumption)
- Then, if we extract the 0th, 3rd, 6th, 9th, 12th, and 15th characters, they are all supposed to be encrypted under the same key (shift cipher)
- In other words, the IOC for the **extracted** ciphertext should be ≈ 0.065



Determining the key length

- For period $T = 1, 2, 3, \dots$, up to a large enough value, extract the sequence of ciphertext characters at positions $0, T, 2T, 3T, \dots$
- Compute the **probability vector q** for the individual ciphertext letters of the **extracted** sequence
- Compute the IOC for vector q (sum of q_i squared)
- Once you have all the IOCs for different values of period T , look for a **pattern**
- When $T = s, 2s, 3s, \dots$, where s is the **actual** key length, we expect the IOCs to be ≈ 0.065 (or be slightly larger than the values around them)
- Once the key length s is established, decrypt the ciphertext by using s instances of the shift cipher decryption module