

1. First, creating a class Node to initialize nodes with a singly linked list:

```
class Node:
```

```
    def __init__(self, value):
```

```
        self.value = value
```

```
        self.next = None
```

Next, a function should be created with node parameter (to take in a node from the list), x, and y:

```
def verify_values(node, x, y):
```

Then, node, x, and y need to be checked, along with checking if x and y are the same:

```
    if not node or x is None or y is None:
```

```
        return False
```

```
    if x == y:
```

```
        return True
```

Next, pointers and variables to verify if x and y are in the list:

```
    verify_x = False
```

```
    verify_y = False
```

```
    current = node
```

Next, a while loop can be used to traverse and check for x and y:

```
    while True:
```

```
        if current.value == x:
```

```
            verify_x = True
```

```
        if current.value == y:
```

```
            verify_y = True
```

```
        if verify_x == verify_y:
```

```
            return True
```

```
        current = current.next # updates current by moving forward
```

```
    if current == None: # if link is traversed without x and y,
```

```
        break
```

function stops

```
    return False
```

This program works to traverse the circular linked list and check if  $x$  and  $y$  are both in the list. It has a time complexity of  $O(n)$  because the function potentially needs to traverse the entire list once to determine if both  $x$  and  $y$  exist.

2) To switch  $x$  and  $y$  values in a singly linked list, the previous node to  $x$  and  $y$  can be stored to later find and switch. First, the Node class needs to be constructed:

class Node:

def \_\_init\_\_(self, value):

self.value = value

self.next = None

Second, a function needs to be defined with the list's head,  $x$ , and  $y$ . A check should also be placed for  $x$  and  $y$ .

def swap\_nodes(head, x, y):

if  $x == y$ :

return head

Third, variables can be set for  $x$ ,  $y$ , and their previous nodes

prev\_x = None

prev\_y = None

x\_node = head

y\_node = head

Next, a while loop tracking the current  $x$  node can be used to find prev\_x

while x\_node and x\_node.value != x:

prev\_x = x\_node

x\_node = x\_node.next

The same needs to be repeated for  $y$

while y\_node and y\_node.value != y:

prev\_y = y\_node

y\_node = y\_node.next

Next, a check can be used if the values are not in the list

if not x\_node or not y\_node:

return 'x and y values not in list'



Next, if/else statements can be used can be used in case x or y are the list's head

```
if prev-x:  
    prev-x.next = x-node  
else:  
    head = y-node
```

```
if prev-y:  
    prev-y.next = y-node  
else:  
    head = x-node
```

Finally, the pointers can be swapped to swap the x and y-values  
x-node.next, y-node.next = y-node.next, x-node.next  
return head

To swap x and y in a doubly linked list, similarly to the singly linked list, the previous and next pointers can be used. First, a class Node needs to be made.

```
class Node:  
    def __init__(self, value):  
        self.value = value  
        self.next = None  
        self.prev = None
```

Next, the function to swap nodes can be defined with head, x, and y parameters. The x and y nodes also need to be checked  
def swap-nodes(head, x, y):

```
    if x == y:  
        return head
```

Next, the next pointers for  $x$  and  $y$  need to be swapped with a temp variable

$temp = x.next$

$x.next = y.next$

$y.next = temp$

Then, the previous pointers also need to be swapped similar to next

$temp = x.prev$

$x.prev = y.prev$

$y.prev = temp$

Next,  $x$  and  $y$ 's next and prev need to be changed if they are not tails

if  $x.next$ :

$x.next.prev = x$

if  $y.next$ :

$y.next.prev = y$

Then, the cases where  $x$  or  $y$  are the head are addressed with if/else statements

if  $x.prev$  is None:

$head = y$

elif  $y.prev$  is None:

$head = x$

return head

The time complexity for the singly linked list is  $O(n)$  because it depends on the number of nodes. The time complexity for the doubly linked list is  $O(1)$  because  $x$  and  $y$  can update pointers faster without the list.

- 3) Using Euler Tour Traversal's depth-first traversal to visit each node of a binary tree as before visiting children, between children, and after visiting children. It will start at the root, go to all children, and goes back to the root. First, the Node class needs to be programmed with a counter
- class Node:

def \_\_init\_\_(self, value):

self.value = value

self.left = None

self.right = None

self.count = 0



Next, a function to count descendants needs to be defined and check for node's existence

def count\_descendants(node):

if not node:

return 0

Then, recursion can be used to count the subtrees and nodes

left\_subtrees = count\_descendants(node.left)

right\_subtrees = count\_descendants(node.right)

Next, the numbers can be added to get the total count

node\_descendants = right\_subtrees + left\_subtrees

Finally the count can be returned by adding one because the count started at 0

return node\_descendants + 1