

Tanya Gyanmote

[tgyanmot@ucsc.edu](mailto:tgyanmot@ucsc.edu)

Fall 2022

## CSE13S Assignment 2 - A Small Numerical Library

### Programming Analysis:

This program implements functions, created in mathlib.c which is small numerical library and has a corresponding test harness. The functions in mathlib.c,  $\sin$ ,  $\cos$ ,  $\sin^{-1}$  (arcsin),  $\cos^{-1}$  (arccos),  $\tan^{-1}$  (arctan) of the taylor series expansion near some point  $f(a)$ . The program takes certain command line arguments like -a, -s, and etc;

### Sin(x)

| x      | sin          | Library      | Difference      |
|--------|--------------|--------------|-----------------|
| 0.0000 | 0.0000000000 | 0.0000000000 | 0.000000000000  |
| 0.1571 | 0.156434465  | 0.156434465  | 0.000000000000  |
| 0.3142 | 0.309016994  | 0.309016994  | 0.000000000000  |
| 0.4712 | 0.453990500  | 0.453990500  | -0.000000000000 |
| 0.6283 | 0.587785252  | 0.587785252  | 0.000000000000  |
| 0.7854 | 0.707106781  | 0.707106781  | 0.000000000000  |
| 0.9425 | 0.809016994  | 0.809016994  | 0.000000000000  |
| 1.0996 | 0.891006524  | 0.891006524  | -0.000000000000 |
| 1.2566 | 0.951056516  | 0.951056516  | -0.000000000000 |
| 1.4137 | 0.987688341  | 0.987688341  | 0.000000000000  |
| 1.5708 | 1.000000000  | 1.000000000  | 0.000000000000  |
| 1.7279 | 0.987688341  | 0.987688341  | 0.000000000000  |
| 1.8850 | 0.951056516  | 0.951056516  | -0.000000000000 |
| 2.0420 | 0.891006524  | 0.891006524  | -0.000000000000 |
| 2.1991 | 0.809016994  | 0.809016994  | -0.000000000000 |
| 2.3562 | 0.707106781  | 0.707106781  | -0.000000000001 |
| 2.5133 | 0.587785252  | 0.587785252  | 0.000000000000  |
| 2.6704 | 0.453990500  | 0.453990500  | 0.000000000000  |
| 2.8274 | 0.309016994  | 0.309016994  | 0.000000000001  |
| 2.9845 | 0.156434465  | 0.156434465  | -0.000000000000 |
| 3.1416 | -0.000000000 | 0.000000000  | -0.000000000000 |
| 3.2987 | -0.156434465 | -0.156434465 | -0.000000000001 |
| 3.4558 | -0.309016994 | -0.309016994 | -0.000000000002 |
| 3.6128 | -0.453990500 | -0.453990500 | 0.000000000000  |
| 3.7699 | -0.587785252 | -0.587785252 | 0.000000000000  |
| 3.9270 | -0.707106781 | -0.707106781 | 0.000000000001  |
| 4.0841 | -0.809016994 | -0.809016994 | -0.000000000000 |
| 4.2412 | -0.891006524 | -0.891006524 | -0.000000000000 |
| 4.3982 | -0.951056516 | -0.951056516 | -0.000000000001 |
| 4.5553 | -0.987688341 | -0.987688341 | -0.000000000001 |
| 4.7124 | -1.000000000 | -1.000000000 | 0.000000000000  |
| 4.8695 | -0.987688341 | -0.987688341 | 0.000000000000  |
| 5.0265 | -0.951056516 | -0.951056516 | 0.000000000001  |
| 5.1836 | -0.891006524 | -0.891006524 | 0.000000000002  |
| 5.3407 | -0.809016994 | -0.809016994 | -0.000000000000 |
| 5.4978 | -0.707106781 | -0.707106781 | -0.000000000000 |
| 5.6549 | -0.587785252 | -0.587785252 | -0.000000000001 |
| 5.8119 | -0.453990500 | -0.453990500 | -0.000000000002 |
| 5.9690 | -0.309016994 | -0.309016994 | 0.000000000000  |
| 6.1261 | -0.156434465 | -0.156434465 | 0.000000000000  |

my\_sin(x) I created has a similar output to the library sin(x) with an acceptable difference. I created my\_sin(x) using the pseudocode I had mentioned in my Design Document.

## Cos(x)

| x      | cos          | Library      | Difference      |
|--------|--------------|--------------|-----------------|
| 0.0000 | 1.000000000  | 1.000000000  | 0.000000000000  |
| 0.1571 | 0.987688341  | 0.987688341  | 0.000000000000  |
| 0.3142 | 0.951056516  | 0.951056516  | -0.000000000000 |
| 0.4712 | 0.891006524  | 0.891006524  | -0.000000000000 |
| 0.6283 | 0.809016994  | 0.809016994  | 0.000000000000  |
| 0.7854 | 0.707106781  | 0.707106781  | 0.000000000000  |
| 0.9425 | 0.587785252  | 0.587785252  | 0.000000000000  |
| 1.0996 | 0.453990500  | 0.453990500  | -0.000000000000 |
| 1.2566 | 0.309016994  | 0.309016994  | 0.000000000000  |
| 1.4137 | 0.156434465  | 0.156434465  | -0.000000000000 |
| 1.5708 | 0.000000000  | 0.000000000  | -0.000000000000 |
| 1.7279 | -0.156434465 | -0.156434465 | -0.000000000000 |
| 1.8850 | -0.309016994 | -0.309016994 | -0.000000000000 |
| 2.0420 | -0.453990500 | -0.453990500 | 0.000000000000  |
| 2.1991 | -0.587785252 | -0.587785252 | -0.000000000000 |
| 2.3562 | -0.707106781 | -0.707106781 | -0.000000000000 |
| 2.5133 | -0.809016994 | -0.809016994 | -0.000000000000 |
| 2.6704 | -0.891006524 | -0.891006524 | 0.000000000000  |
| 2.8274 | -0.951056516 | -0.951056516 | 0.000000000000  |
| 2.9845 | -0.987688341 | -0.987688341 | -0.000000000000 |
| 3.1416 | -1.000000000 | -1.000000000 | -0.000000000000 |
| 3.2987 | -0.987688341 | -0.987688341 | -0.000000000000 |
| 3.4558 | -0.951056516 | -0.951056516 | 0.000000000000  |
| 3.6128 | -0.891006524 | -0.891006524 | 0.000000000000  |
| 3.7699 | -0.809016994 | -0.809016994 | 0.000000000000  |
| 3.9270 | -0.707106781 | -0.707106781 | 0.000000000001  |
| 4.0841 | -0.587785252 | -0.587785252 | -0.000000000000 |
| 4.2412 | -0.453990500 | -0.453990500 | -0.000000000000 |
| 4.3982 | -0.309016994 | -0.309016994 | -0.000000000001 |
| 4.5553 | -0.156434465 | -0.156434465 | 0.000000000000  |
| 4.7124 | 0.000000000  | -0.000000000 | 0.000000000000  |
| 4.8695 | 0.156434465  | 0.156434465  | 0.000000000001  |
| 5.0265 | 0.309016994  | 0.309016994  | 0.000000000002  |
| 5.1836 | 0.453990500  | 0.453990500  | -0.000000000000 |
| 5.3407 | 0.587785252  | 0.587785252  | -0.000000000000 |
| 5.4978 | 0.707106781  | 0.707106781  | -0.000000000001 |
| 5.6549 | 0.809016994  | 0.809016994  | 0.000000000000  |
| 5.8119 | 0.891006524  | 0.891006524  | 0.000000000000  |
| 5.9690 | 0.951056516  | 0.951056516  | 0.000000000001  |
| 6.1261 | 0.987688341  | 0.987688341  | 0.000000000001  |

my\_cos(x) I created has a similar output to the library cos(x) with an acceptable difference. I created my\_cos(x) using the pseudocode I had mentioned in my Design Document.

## Arcsin(x)

| x       | arccos      | Library     | Difference      |
|---------|-------------|-------------|-----------------|
| -1.0000 | 3.141592358 | 3.141592654 | -0.000000295286 |
| -0.9500 | 2.824032224 | 2.824032224 | 0.000000000000  |
| -0.9000 | 2.690565842 | 2.690565842 | 0.000000000000  |
| -0.8500 | 2.586781621 | 2.586781621 | 0.000000000000  |
| -0.8000 | 2.498091545 | 2.498091545 | -0.000000000000 |
| -0.7500 | 2.418858406 | 2.418858406 | -0.000000000000 |
| -0.7000 | 2.346193823 | 2.346193823 | -0.000000000000 |
| -0.6500 | 2.278380764 | 2.278380764 | -0.000000000000 |
| -0.6000 | 2.214297436 | 2.214297436 | -0.000000000000 |
| -0.5500 | 2.153160565 | 2.153160565 | 0.000000000000  |
| -0.5000 | 2.094395102 | 2.094395102 | 0.000000000000  |
| -0.4500 | 2.037561666 | 2.037561666 | 0.000000000000  |
| -0.4000 | 1.982313173 | 1.982313173 | 0.000000000000  |
| -0.3500 | 1.928367430 | 1.928367430 | 0.000000000000  |
| -0.3000 | 1.875488981 | 1.875488981 | -0.000000000000 |
| -0.2500 | 1.823476582 | 1.823476582 | -0.000000000000 |
| -0.2000 | 1.772154248 | 1.772154248 | -0.000000000000 |
| -0.1500 | 1.721364600 | 1.721364600 | 0.000000000000  |
| -0.1000 | 1.670963748 | 1.670963748 | 0.000000000000  |
| -0.0500 | 1.620817184 | 1.620817184 | -0.000000000000 |
| 0.0000  | 1.570796327 | 1.570796327 | 0.000000000000  |
| 0.0500  | 1.520775470 | 1.520775470 | 0.000000000000  |
| 0.1000  | 1.470628906 | 1.470628906 | -0.000000000000 |
| 0.1500  | 1.420228054 | 1.420228054 | 0.000000000000  |
| 0.2000  | 1.369438406 | 1.369438406 | 0.000000000000  |
| 0.2500  | 1.318116072 | 1.318116072 | 0.000000000000  |
| 0.3000  | 1.266103673 | 1.266103673 | 0.000000000000  |
| 0.3500  | 1.213225223 | 1.213225223 | -0.000000000000 |
| 0.4000  | 1.159279481 | 1.159279481 | -0.000000000000 |
| 0.4500  | 1.104030988 | 1.104030988 | -0.000000000000 |
| 0.5000  | 1.047197551 | 1.047197551 | -0.000000000000 |
| 0.5500  | 0.988432089 | 0.988432089 | -0.000000000000 |
| 0.6000  | 0.927295218 | 0.927295218 | 0.000000000000  |
| 0.6500  | 0.863211890 | 0.863211890 | 0.000000000000  |
| 0.7000  | 0.795398830 | 0.795398830 | 0.000000000000  |
| 0.7500  | 0.722734248 | 0.722734248 | 0.000000000000  |
| 0.8000  | 0.643501109 | 0.643501109 | 0.000000000000  |
| 0.8500  | 0.554811033 | 0.554811033 | -0.000000000000 |
| 0.9000  | 0.451026812 | 0.451026812 | -0.000000000000 |
| 0.9500  | 0.317560429 | 0.317560429 | -0.000000000000 |

my\_cos(x) I created has a similar output to the library cos(x) with an acceptable difference. I created my\_cos(x) using the pseudocode I had mentioned in my Design Document.

## Arccos(x)

| x       | arccos      | Library     | Difference      |
|---------|-------------|-------------|-----------------|
| -1.0000 | 3.141592358 | 3.141592654 | -0.000000295286 |
| -0.9500 | 2.824032224 | 2.824032224 | 0.000000000000  |
| -0.9000 | 2.690565842 | 2.690565842 | 0.000000000000  |
| -0.8500 | 2.586781621 | 2.586781621 | 0.000000000000  |
| -0.8000 | 2.498091545 | 2.498091545 | -0.000000000000 |
| -0.7500 | 2.418858406 | 2.418858406 | -0.000000000000 |
| -0.7000 | 2.346193823 | 2.346193823 | -0.000000000000 |
| -0.6500 | 2.278380764 | 2.278380764 | -0.000000000000 |
| -0.6000 | 2.214297436 | 2.214297436 | -0.000000000000 |
| -0.5500 | 2.153160565 | 2.153160565 | 0.000000000000  |
| -0.5000 | 2.094395102 | 2.094395102 | 0.000000000000  |
| -0.4500 | 2.037561666 | 2.037561666 | 0.000000000000  |
| -0.4000 | 1.982313173 | 1.982313173 | 0.000000000000  |
| -0.3500 | 1.928367430 | 1.928367430 | 0.000000000000  |
| -0.3000 | 1.875488981 | 1.875488981 | -0.000000000000 |
| -0.2500 | 1.823476582 | 1.823476582 | -0.000000000000 |
| -0.2000 | 1.772154248 | 1.772154248 | -0.000000000000 |
| -0.1500 | 1.721364600 | 1.721364600 | 0.000000000000  |
| -0.1000 | 1.670963748 | 1.670963748 | 0.000000000000  |
| -0.0500 | 1.620817184 | 1.620817184 | -0.000000000000 |
| 0.0000  | 1.570796327 | 1.570796327 | 0.000000000000  |
| 0.0500  | 1.520775470 | 1.520775470 | 0.000000000000  |
| 0.1000  | 1.470628906 | 1.470628906 | -0.000000000000 |
| 0.1500  | 1.420228054 | 1.420228054 | 0.000000000000  |
| 0.2000  | 1.369438406 | 1.369438406 | 0.000000000000  |
| 0.2500  | 1.318116072 | 1.318116072 | 0.000000000000  |
| 0.3000  | 1.266103673 | 1.266103673 | 0.000000000000  |
| 0.3500  | 1.213225223 | 1.213225223 | -0.000000000000 |
| 0.4000  | 1.159279481 | 1.159279481 | -0.000000000000 |
| 0.4500  | 1.104030988 | 1.104030988 | -0.000000000000 |
| 0.5000  | 1.047197551 | 1.047197551 | -0.000000000000 |
| 0.5500  | 0.988432089 | 0.988432089 | -0.000000000000 |
| 0.6000  | 0.927295218 | 0.927295218 | 0.000000000000  |
| 0.6500  | 0.863211890 | 0.863211890 | 0.000000000000  |
| 0.7000  | 0.795398830 | 0.795398830 | 0.000000000000  |
| 0.7500  | 0.722734248 | 0.722734248 | 0.000000000000  |
| 0.8000  | 0.643501109 | 0.643501109 | 0.000000000000  |
| 0.8500  | 0.554811033 | 0.554811033 | -0.000000000000 |
| 0.9000  | 0.451026812 | 0.451026812 | -0.000000000000 |
| 0.9500  | 0.317560429 | 0.317560429 | -0.000000000000 |

my\_arccos(x) I created has a similar output to the library acos(x) with an acceptable difference. I created my\_arccos(x) using the pseudocode I had mentioned in my Design Document.

## Arctan(x)

| x      | arctan      | Library     | Difference      |
|--------|-------------|-------------|-----------------|
| 1.0000 | 0.785398163 | 0.785398163 | 0.000000000033  |
| 1.0500 | 0.809783573 | 0.809783573 | -0.000000000032 |
| 1.1000 | 0.832981267 | 0.832981267 | -0.000000000001 |
| 1.1500 | 0.855052737 | 0.855052737 | 0.000000000024  |
| 1.2000 | 0.876058051 | 0.876058051 | 0.000000000041  |
| 1.2500 | 0.896055385 | 0.896055385 | 0.000000000044  |
| 1.3000 | 0.915100701 | 0.915100701 | -0.000000000003 |
| 1.3500 | 0.933247529 | 0.933247529 | -0.000000000005 |
| 1.4000 | 0.950546841 | 0.950546841 | 0.000000000047  |
| 1.4500 | 0.967046993 | 0.967046993 | -0.000000000052 |
| 1.5000 | 0.982793723 | 0.982793723 | -0.000000000002 |
| 1.5500 | 0.997830184 | 0.997830184 | 0.000000000029  |
| 1.6000 | 1.012197011 | 1.012197011 | 0.000000000029  |
| 1.6500 | 1.025932411 | 1.025932411 | 0.000000000014  |
| 1.7000 | 1.039072259 | 1.039072260 | -0.000000000046 |
| 1.7500 | 1.051650213 | 1.051650213 | -0.000000000039 |
| 1.8000 | 1.063697822 | 1.063697822 | 0.000000000007  |
| 1.8500 | 1.075244653 | 1.075244653 | -0.000000000020 |
| 1.9000 | 1.086318398 | 1.086318398 | 0.000000000054  |
| 1.9500 | 1.096944990 | 1.096944990 | -0.000000000016 |
| 2.0000 | 1.107148718 | 1.107148718 | 0.000000000064  |
| 2.0500 | 1.116952325 | 1.116952325 | 0.000000000014  |
| 2.1000 | 1.126377117 | 1.126377117 | 0.000000000057  |
| 2.1500 | 1.135443052 | 1.135443052 | 0.000000000069  |
| 2.2000 | 1.144168834 | 1.144168834 | -0.000000000062 |
| 2.2500 | 1.152571997 | 1.152571997 | 0.000000000045  |
| 2.3000 | 1.160668986 | 1.160668986 | 0.000000000032  |
| 2.3500 | 1.168475229 | 1.168475229 | -0.000000000083 |
| 2.4000 | 1.176005207 | 1.176005207 | 0.000000000035  |

my\_arctan(x) I created has a similar output to the library atan(x) with an acceptable difference. I created my\_arctan(x) using the pseudocode I had mentioned in my Design Document.

## Log(x)

| x      | log          | Library      | Difference     |
|--------|--------------|--------------|----------------|
| 1.0000 | 0.0000000000 | 0.0000000000 | 0.000000000000 |
| 1.0500 | 0.048790164  | 0.048790164  | 0.000000000000 |
| 1.1000 | 0.095310180  | 0.095310180  | 0.000000000000 |
| 1.1500 | 0.139761942  | 0.139761942  | 0.000000000000 |
| 1.2000 | 0.182321557  | 0.182321557  | 0.000000000001 |
| 1.2500 | 0.223143551  | 0.223143551  | 0.000000000000 |
| 1.3000 | 0.262364264  | 0.262364264  | 0.000000000000 |
| 1.3500 | 0.300104592  | 0.300104592  | 0.000000000001 |
| 1.4000 | 0.336472237  | 0.336472237  | 0.000000000000 |
| 1.4500 | 0.371563556  | 0.371563556  | 0.000000000000 |
| 1.5000 | 0.405465108  | 0.405465108  | 0.000000000001 |
| 1.5500 | 0.438254931  | 0.438254931  | 0.000000000002 |
| 1.6000 | 0.470003629  | 0.470003629  | 0.000000000000 |
| 1.6500 | 0.500775288  | 0.500775288  | 0.000000000000 |
| 1.7000 | 0.530628251  | 0.530628251  | 0.000000000001 |
| 1.7500 | 0.559615788  | 0.559615788  | 0.000000000001 |
| 1.8000 | 0.587786665  | 0.587786665  | 0.000000000002 |
| 1.8500 | 0.615185639  | 0.615185639  | 0.000000000000 |
| 1.9000 | 0.641853886  | 0.641853886  | 0.000000000000 |
| 1.9500 | 0.667829373  | 0.667829373  | 0.000000000000 |
| 2.0000 | 0.693147181  | 0.693147181  | 0.000000000001 |
| 2.0500 | 0.717839793  | 0.717839793  | 0.000000000001 |
| 2.1000 | 0.741937345  | 0.741937345  | 0.000000000002 |
| 2.1500 | 0.765467842  | 0.765467842  | 0.000000000002 |
| 2.2000 | 0.788457360  | 0.788457360  | 0.000000000000 |
| 2.2500 | 0.810930216  | 0.810930216  | 0.000000000000 |
| 2.3000 | 0.832909123  | 0.832909123  | 0.000000000000 |
| 2.3500 | 0.854415328  | 0.854415328  | 0.000000000001 |
| 2.4000 | 0.875468737  | 0.875468737  | 0.000000000001 |
| 2.4500 | 0.896088025  | 0.896088025  | 0.000000000001 |
| 2.5000 | 0.916290732  | 0.916290732  | 0.000000000001 |
| 2.5500 | 0.936093359  | 0.936093359  | 0.000000000002 |
| 2.6000 | 0.955511445  | 0.955511445  | 0.000000000002 |
| 2.6500 | 0.974559640  | 0.974559640  | 0.000000000000 |

my\_log(x) I created has a similar output to the library log(x) with an acceptable difference. I created my\_log(x) using the pseudocode I had mentioned in my Design Document.

