## High Performance Computing Project #2 due 2022 APR 29, 3:00 p.m.

## 1 The Assignment

- (A) (50 points) Section 9.5.1 in the notes.
- (B) (30 points) Repeat Section 9.5.1 in the notes to solve the two-dimensional Poisson equation in Definition 7.4 on  $\Omega=(0,1)^2$  by a straightforward generalization of the one-dimensional multigrid method. In addition to errors and convergence rates, you should also compare the CPU time between your multigrid implementation and your LU-factorization implementation in Project 1.
- (C) (10 points) Use template programming throughout your package with int dim as the template parameter so that the main program and the unit tests are the only places where dim, the dimensionality of the domain, is specialized to 1 and 2.
- (D) (20 points) Give a complete and coherent presentation of the theory to analyze the convergence of your two-dimensional multigrid method on  $\Omega = (0,1)^2$ . Your report must be written in LATEX and must follow the style of the notes. (hint: use Kronecker product in Section 7.6.1)

Extra credits:

(a) (50 points) Change the problem domain  $\Omega=(0,1)^2$  to  $\tilde{\Omega}$ , which is the same boundary as  $\Omega$  except that the lower boundary is changed to

$$\{(x,y): y = \sin(\pi x); x \in [0,1]\}.$$

Design a two-dimensional multigrid method for simply-connected irregular domains and carry out (B) and (b) for your method.

To get any extra credit for (a), your report must hit at least half of the main points on the answer sheet.

Additional 10% credits will be given to you if you type-set your report in IATEX.

## 2 How to submit

Send to 3150104952@zju.edu.cn your report, your C++ package, and other documentation in a single gzipped tar ball named as YourName\_Project2.tar.gz.