

**Econ 7710**  
**Assignment 6**

**Due November 10th**

1. You have  $n$  i.i.d. draws from the uniform distribution on  $[0, \theta]$ .
  - (a) Construct the maximum likelihood estimator for parameter  $\theta$
  - (b) Derive the exact distribution of your estimator and compute its “small sample” bias, i.e.  $E[\hat{\theta}_{MLE}] - \theta$
  - (c) Find the variance of your estimator, find the rate  $r_n$  (as a function of  $n$ ) at which the standard deviation of your estimator converges to 0 and show that your estimator is consistent
  - (d) Find the asymptotic distribution of your estimator, i.e. the distribution limit of the sequence of random variables  $r_n(\hat{\theta}_{MLE} - \theta)$