

# Multi-dimensional Array

# Before That, Let's Introduce Numpy

- A convenient package
- You can get around with “normal” Python method but Numpy can shorten your code a lot
- For example, if you want to create a list of numbers from 0 to  $\pi$  without Numpy you have to:

`x = [i/100 for i in range(0, 314)]`



# With Numpy

```
>>> import numpy as np
>>> x1 = np.arange(0, 3.14, 0.1)
>>> x1
array([ 0. ,  0.1,  0.2,  0.3,  0.4,
        0.5,  0.6,  0.7,  0.8,  0.9,  1. ,
        1.1,  1.2,  1.3,  1.4,  1.5,
        1.6,  1.7,  1.8,  1.9,  2. ,  2.1,
        2.2,  2.3,  2.4,  2.5,  2.6,
        2.7,  2.8,  2.9,  3. ,  3.1])
>>> len(x1)
32
```

Be Careful!!!

This is not “arrange”  
but “arange”

# Another Way

Be Careful!!!

This is not  
"linespace" but  
"linspace"

```
>>> x2 = np.linspace(0, 3.14, 100)
>>> x2
array([ 0.          ,  0.03171717,  0.063
43434,  0.09515152,  0.12686869,
        0.15858586,  0.19030303,  0.222
0202 ,  0.25373737,  0.28545455,
        0.31717172,  0.34888889,  0.380
.
.
.
        2.6959596 ,  2.72767677,  2.759
39394,  2.79111111,  2.82282828,
        2.85454545,  2.88626263,  2.917
9798 ,  2.94969697,  2.98141414,
        3.01313131,  3.04484848,  3.076
56566,  3.10828283,  3.14          ])
>>> len(x2)
100
```

# Remember Numpy?

- So far, we have learned that Numpy can create an array that is like a list

```
>>> import numpy as np
>>> a = np.array([1,2,3])
>>> a
array([1, 2, 3])
>>> a[0]=999
>>> a
array([999,  2,  3])
>>> type(a)
<class 'numpy.ndarray'>
>>> l = [1,2,3]
>>> type(l)
<class 'list'>
```

# Broadcasting



# Array Broadcasting

```
>>> a = np.array([1,2,3,4,5])
>>> a + 1  ←————— “Broadcasting”
array([2, 3, 4, 5, 6])
>>> a * 3  ←————— Different from LIST
array([ 3,  6,  9, 12, 15])
>>> a > 5
array([False, False, False, False, False], dtype=bool)
```

← Create another array with the Boolean results

# Array Broadcasting

```
>>> a = np.array([1,2,3,4,5])
>>> a + 1
array([2, 3, 4, 5, 6])
>>> a * 3
array([ 3,  6,  9, 12, 15])
>>> a > 5
array([False, False, False, False, False], dtype=bool)
```

The diagram illustrates the broadcasting of the scalar value 1 to each element of the array [1, 2, 3, 4, 5]. A blue arrow originates from the number 1 in the expression 'a + 1' and branches out to point to each of the five elements (1, 2, 3, 4, 5) in the array, demonstrating how the single value is applied to every element.

- A single operator with a single number at the right side
  - Apply that operation to every single entry of the array



# Array Math

```
>>> v1 = np.array([1,2,3])
>>> v2 = np.array([4,9,16])
```

```
>>> print(v1+v2) ←—————
```

Different  
from list !!!!

```
[ 5 11 19]
>>> print(v1*v2)
[ 4 18 48]
```

```
>>> np.sqrt(v2) ←—————
array([ 2.,  3.,  4.])
```

Directly apply on  
EVERY element in the  
array

```
>>> v1.dot(v2) ←————— Dot product
70
```

```
>>> v2.sum()
29
```

More of these functions:

<https://docs.scipy.org/doc/numpy-1.13.0/reference/routines.math.html>

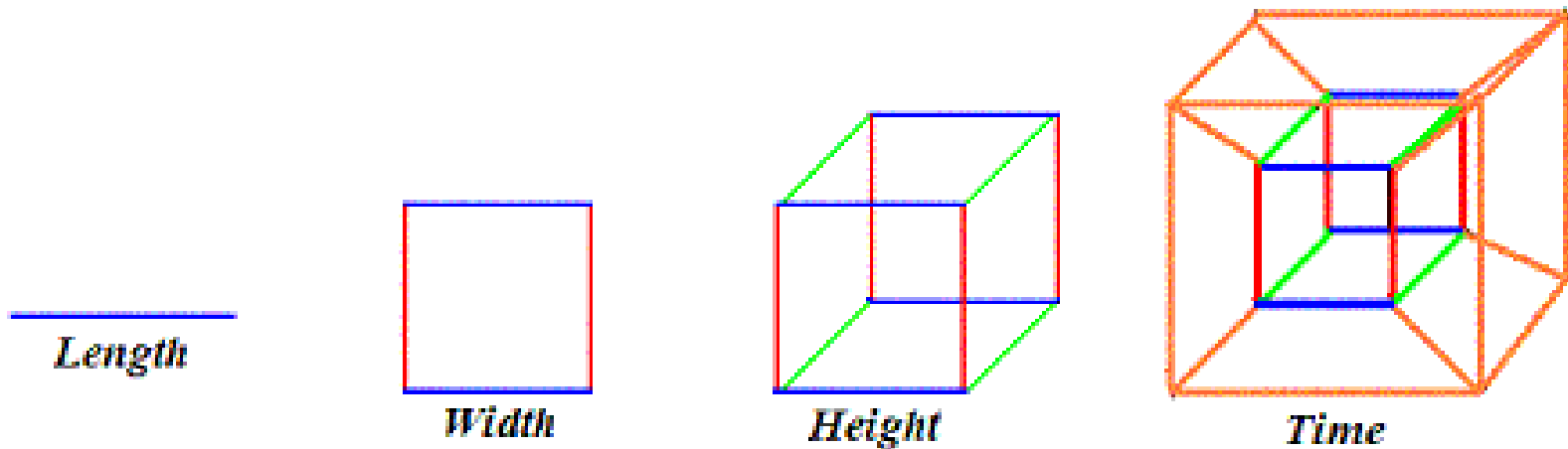
# Two-dimensional Array

# Dimensions

- Are we living in a three dimensional space?

## *The Four Dimensions*

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[The xkcd guide to the fourth dimension](#)

# Motel in US



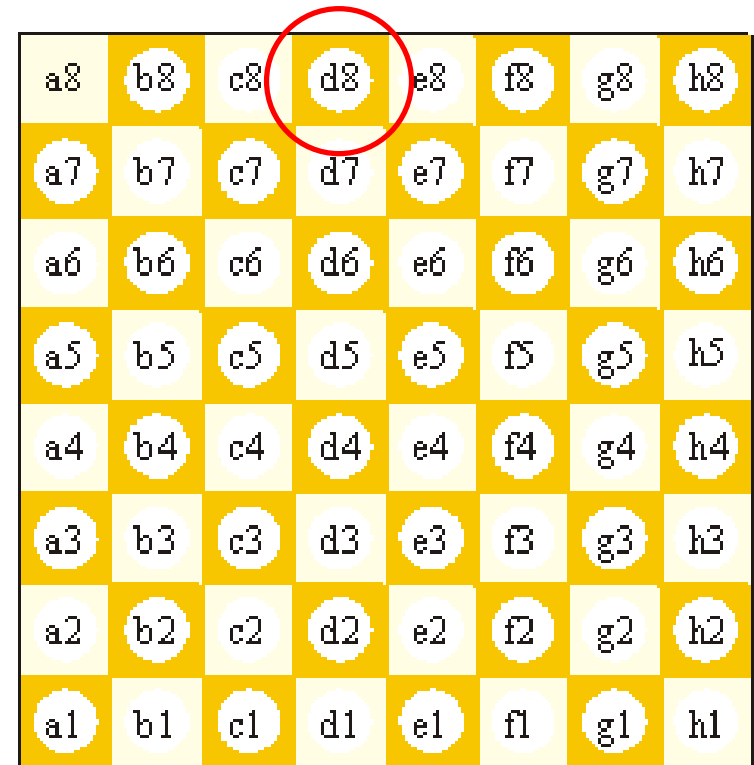
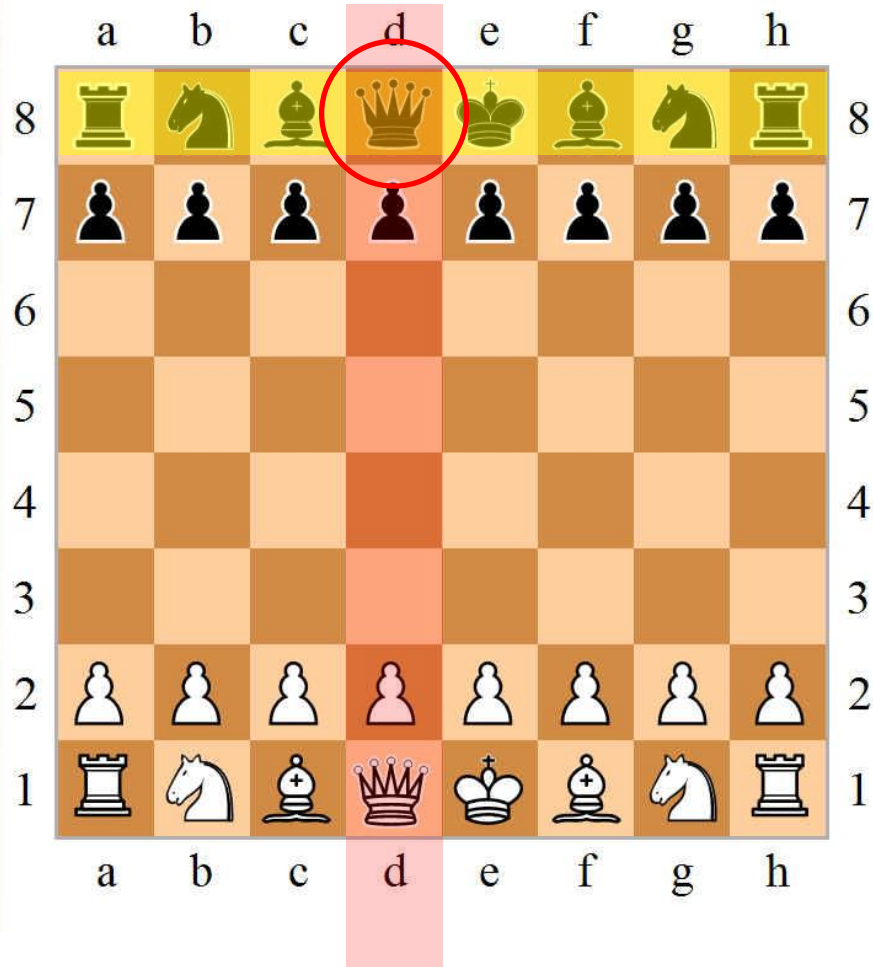
One Dimension

# Hotel

My room is 02-05



# Chess Position





- Row 8
- Col B
- So, B8

crude-... Search Sheet

Home Insert Page Layout Formulas Data Review View

Normal Page Layout Custom Views Show Zoom 150% Zoom to 100% Freeze Panes View Macros Record Macro

B8  $\times$   $\checkmark$   $fx$  Crude Birth Rate

	A	B	C	D
1	year	level_1	value	
2	1960	Crude Birth Rate	37.5	
3	1961	Crude Birth Rate	35.2	
4	1962	Crude Birth Rate	33.7	
5	1963	Crude Birth Rate	33.2	
6	1964	Crude Birth Rate	31.6	
7	1965	Crude Birth Rate	29.5	
8	1966	Crude Birth Rate	28.3	
9	1967	Crude Birth Rate	25.6	
10	1968	Crude Birth Rate	23.5	
11	1969	Crude Birth Rate	21.8	
12	1970	Crude Birth Rate	22.1	
13	1971	Crude Birth Rate	22.3	
14	1972	Crude Birth Rate	23.1	

crude-birth-rate +

Ready

# Dimensions

One Dimensional Array, A

Index	Contents
0	'Apple'
1	'John'
2	'Eve'
3	'Mary'
4	'Ian'
5	'Smith'
6	'Kelvin'

A[5] = 'Smith'

Two Dimensional Array, M

	0	1	2	3
0	'Apple'	'Lah'	'Cat'	'Eve'
1	'Hello'	'Pay'	'TV'	'Carl'
2	'What'	'Bank'	'Radio'	'Ada'
3	'Frog'	'Peter'	'Sea'	'Eat'
4	'Job'	'Fry'	'Gym'	'Wow'
5	'Walk'	'Fly'	'Cook'	'Look'

M[4][1] = 'Fry'



# Locating an Entry

- Creating a 3x5 array with all zeros

```
>>> c = np.zeros((3,5))
```

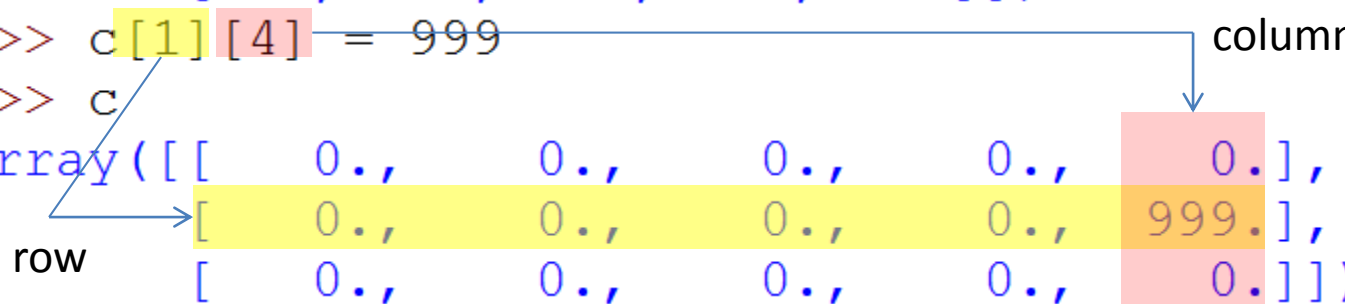
```
>>> c
```

```
array([[ 0.,  0.,  0.,  0.,  0.],  
       [ 0.,  0.,  0.,  0.,  0.],  
       [ 0.,  0.,  0.,  0.,  0.]])
```

```
>>> c[1][4] = 999
```

```
>>> c
```

```
array([[ 0.,  0.,  0.,  0.,  0.,  0.],  
       [ 0.,  0.,  0.,  0.,  0., 999.],  
       [ 0.,  0.,  0.,  0.,  0.,  0.]])
```



```
>>> c[1][4]
```

```
999.0
```

```
>>> c[1,4]
```

```
999.0
```

# Sub-array (Sub-matrix)

```
>>> a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
```

```
>>> a
```

```
array([[ 1,  2,  3,  4],  
       [ 5,  6,  7,  8],  
       [ 9, 10, 11, 12]])
```

```
>>> a[1:3,2:4]
```

```
array([[ 7,  8],  
       [11, 12]])
```

```
>>> a[0:2,2:]
```

```
array([[3, 4],  
       [7, 8]])
```

```
>>> a[:,0::2]
```

```
array([[ 1,  3],  
       [ 5,  7],  
       [ 9, 11]])
```

```
array([[ 1,  2,  3,  4],  
       [ 5,  6,  7,  8],  
       [ 9, 10, 11, 12]])
```

```
array([[ 1,  2,  3,  4],  
       [ 5,  6,  7,  8],  
       [ 9, 10, 11, 12]])
```

```
array([[ 1,  2,  3,  4],  
       [ 5,  6,  7,  8],  
       [ 9, 10, 11, 12]])
```

# Matrix Multiplication

```
>>> m1 = np.array([[2,1],[3,10]])
```

```
>>> m2 = np.array([[4,0],[0,3]])
```

```
>>> m1
```

```
array([[ 2,  1],  
       [ 3, 10]])
```

```
>>> m2
```

```
array([[4, 0],  
       [0, 3]])
```

```
>>> np.matmul(m1,m2)
```

```
array([[ 8,  3],  
       [12, 30]])
```

```
>>> m3 = np.array([[1,2,3,4,5]])
```

```
>>> np.matmul(m1,m3)
```

```
Traceback (most recent call last):
```

```
  File "<pyshell#119>", line 1, in <module>
```

```
    np.matmul(m1,m3)
```

```
ValueError: shapes (2,2) and (1,5) not aligned: 2 (dim 1)  
!= 1 (dim 0)
```

# Boolean Array Indexing


```
>>> a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
>>> a
array([[ 1,  2,  3,  4],
       [ 5,  6,  7,  8],
       [ 9, 10, 11, 12]])

>>> bool_idx = (a > 5)
>>> print(bool_idx)
[[False False False False]
 [False  True  True  True]
 [ True  True  True  True]]
>>> print(a[bool_idx])
[ 6  7  8  9 10 11 12]
>>> print(a[a>10])
[11 12]
```

# Multi-dimensional Array

# Dimensions



One Dimensional Array, A



Index	Contents
0	'Apple'
1	'John'
2	'Eve'
3	'Mary'
4	'Ian'
5	'Smith'
6	'Kelvin'

A[5] = 'Smith'

Two Dimensional Array, M

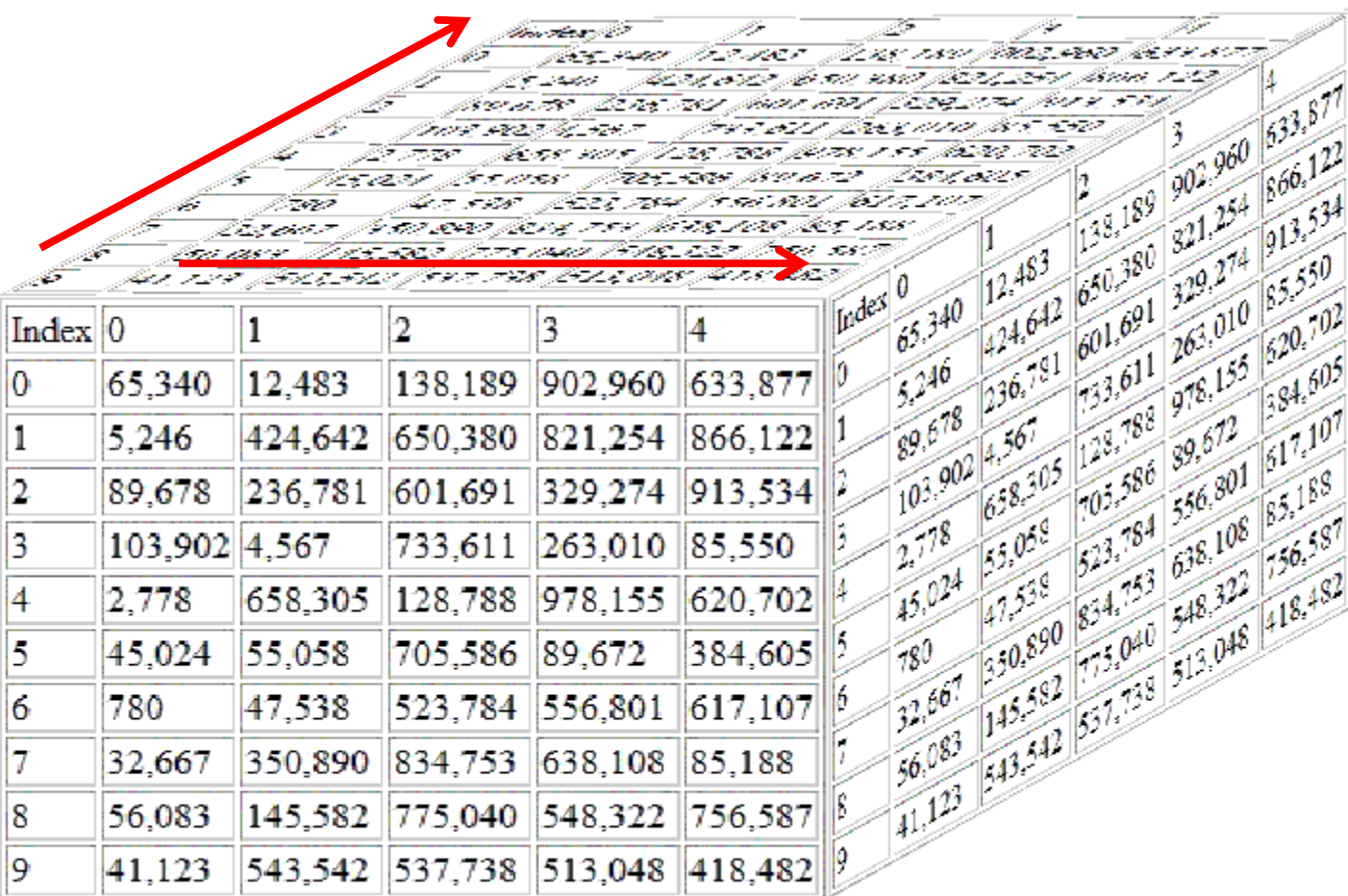


	0	1	2	3
0	'Apple'	'Lah'	'Cat'	'Eve'
1	'Hello'	'Pay'	'TV'	'Carl'
2	'What'	'Bank'	'Radio'	'Ada'
3	'Frog'	'Peter'	'Sea'	'Eat'
4	'Job'	'Fry'	'Gym'	'Wow'
5	'Walk'	'Fly'	'Cook'	'Look'

M[4][1] = 'Fry'

# Multi-Dimensional Array

- A **three** dimensional array



The image illustrates a 3D array as a stack of 10 5x5 matrices. The matrices are indexed from 0 to 9 along the depth axis (vertical arrow). Each matrix has rows indexed 0 to 4 and columns indexed 0 to 4. The values in the matrices are as follows:

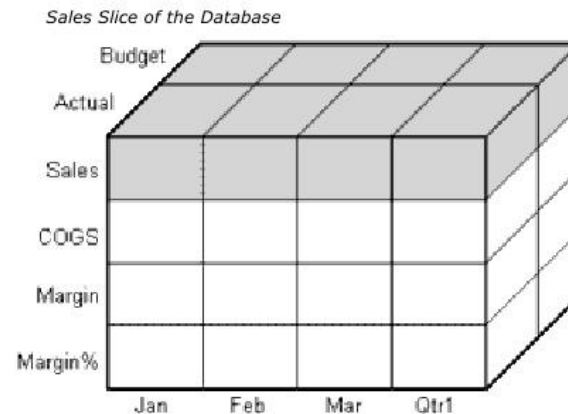
Index	0	1	2	3	4
0	65,340	12,483	138,189	902,960	633,877
1	5,246	424,642	650,380	821,254	866,122
2	89,678	236,781	601,691	329,274	913,534
3	103,902	4,567	733,611	263,010	85,550
4	2,778	658,305	128,788	978,155	620,702
5	45,024	55,058	705,586	89,672	384,605
6	780	47,538	523,784	556,801	617,107
7	32,667	350,890	834,753	638,108	85,188
8	56,083	145,582	775,040	548,322	756,587
9	41,123	543,542	537,738	513,048	418,482

# Fancy Terminology in Business

- Multidimensional Data Model
- Multidimensional Analysis

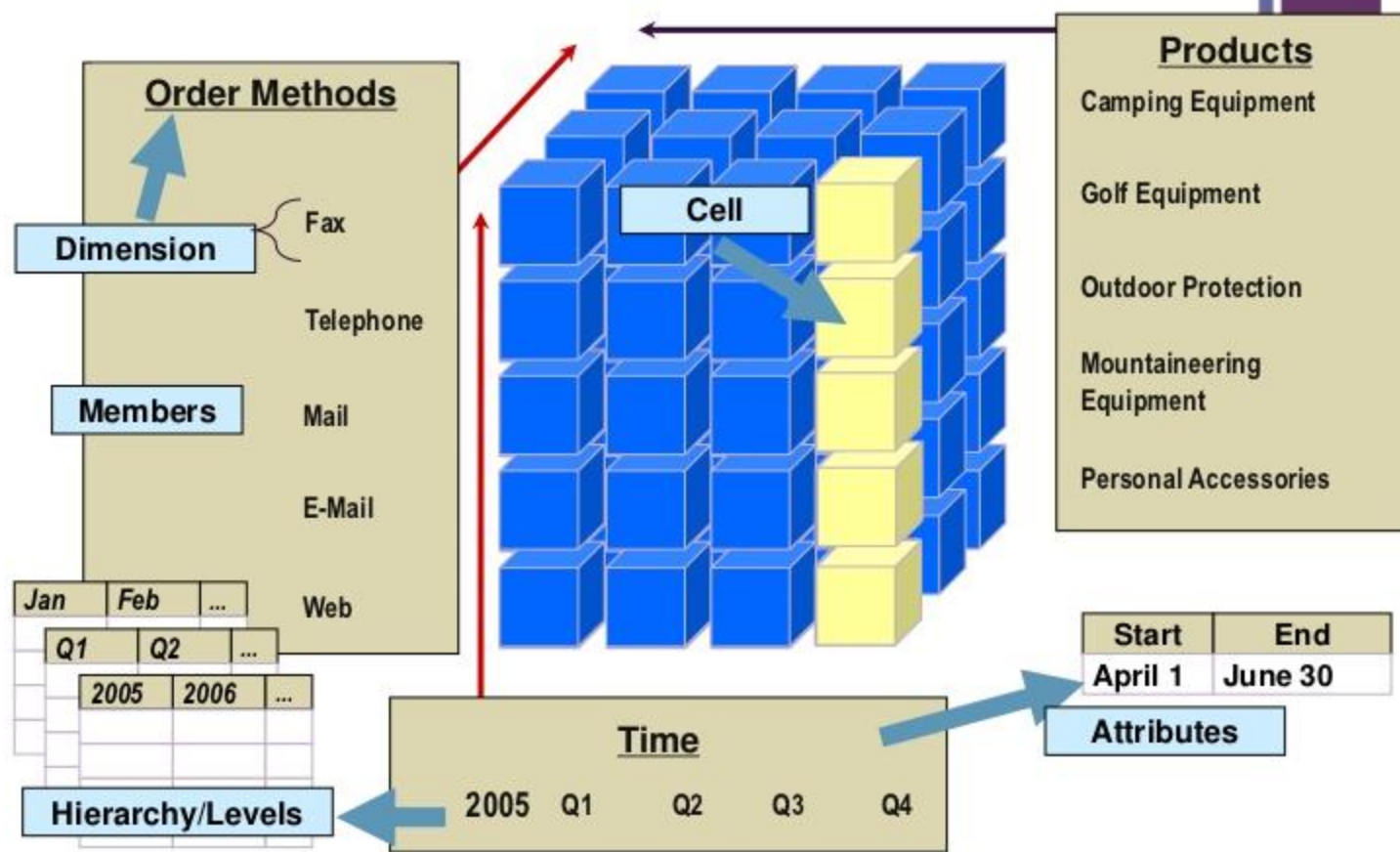


The shaded cells is called a slice illustrate that, when you refer to Sales, you are referring to the portion of the database containing eight Sales values.



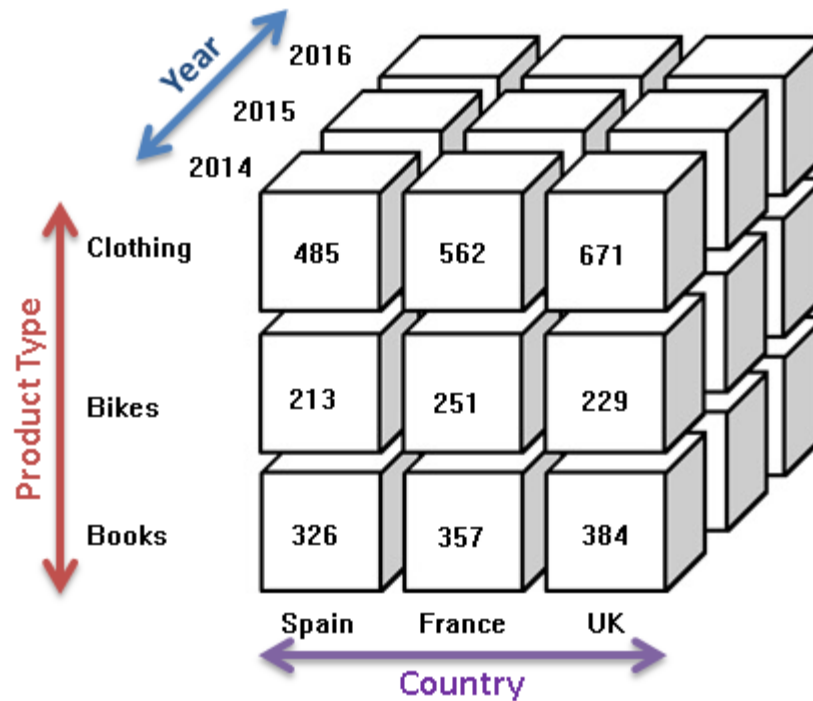


## + What's a "Cube"?



# Sales Cube

- Product Type x Year x Country



- 4<sup>th</sup> Dimensional Sales Cube:
  - Product Type x Year x Country x {Predicted vs actual}

# Multi-Dimensional Array

- A **three** dimensional array
  - E.g. a picture:
    - N x M pixels, and each pixel is an array of three colors, (R, G, B) (Dimensions = N x M x 3)
  - Next Week:

```
from scipy import misc, ndimage
import matplotlib.pyplot as plt

cat_pic = misc.imread('cute cat.jpg')
cat_pic2 = 255 - cat_pic
plt.figure(1)
plt.imshow(cat_pic)
plt.figure(2)
plt.imshow(cat_pic2)
plt.show()
```

# Image Processing

- Original Picture

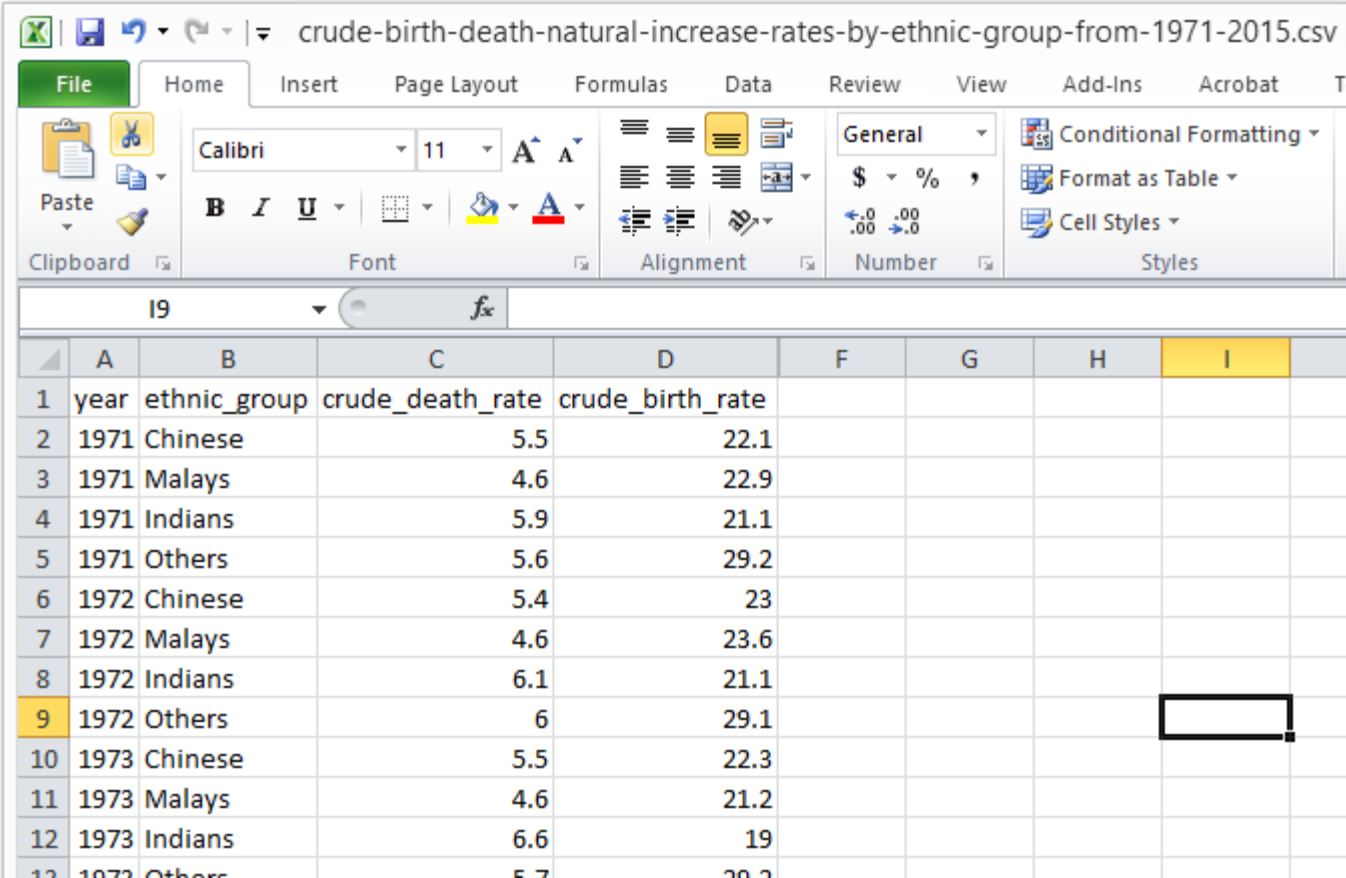


- Negative Image



# Multi-Dimensional Array

- Year x Ethnic Group x {death/birth}

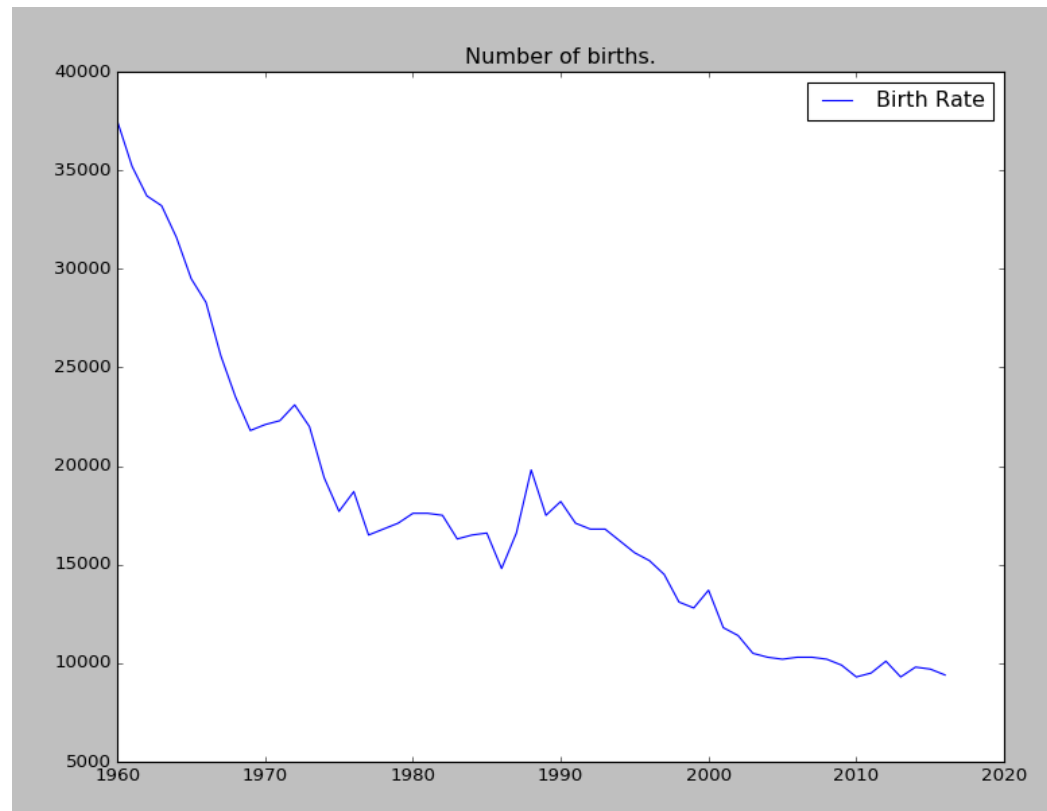


The screenshot shows an Excel spreadsheet titled "crude-birth-death-natural-increase-rates-by-ethnic-group-from-1971-2015.csv". The spreadsheet contains a table with 5 columns: "year", "ethnic\_group", "crude\_death\_rate", and "crude\_birth\_rate". The data is organized by year (1971, 1972, 1973) and ethnic group (Chinese, Malays, Indians, Others). The "crude\_death\_rate" and "crude\_birth\_rate" columns contain numerical values. The spreadsheet interface includes the ribbon with tabs for File, Home, Insert, Page Layout, Formulas, Data, Review, View, Add-Ins, Acrobat, and Tools. The Home tab is active, showing options for Clipboard, Font, Alignment, Number, and Styles. The formula bar shows "I9".

	A	B	C	D	F	G	H	I
1	year	ethnic_group	crude_death_rate	crude_birth_rate				
2	1971	Chinese	5.5	22.1				
3	1971	Malays	4.6	22.9				
4	1971	Indians	5.9	21.1				
5	1971	Others	5.6	29.2				
6	1972	Chinese	5.4	23				
7	1972	Malays	4.6	23.6				
8	1972	Indians	6.1	21.1				
9	1972	Others	6	29.1				
10	1973	Chinese	5.5	22.3				
11	1973	Malays	4.6	21.2				
12	1973	Indians	6.6	19				
13	1973	Others	5.7	20.2				

# 2D Array x CSV

- Remember last week, we plotted the Singapore birth rate with the data in a CSV file



```
import matplotlib.pyplot as plt
```

```
def plot_birth_rate():
```

```
    with open('crude-birth-rate.csv') as f:
```

```
        f.readline()
```

```
        year = []
```

```
        num_birth = []
```

```
        for line in f:
```

```
            list_form = line.rstrip('\n').split(',')
```

```
            year.append(int(list_form[0]))
```

```
            num_birth.append(float(list_form[2])*1000)
```

```
plt.plot(year,num_birth,label="Birth Rate")
```

```
plt.legend(loc="upper right")
```

```
plt.title('Number of births.')
```

```
plt.show()
```

```
plot_birth_rate()
```

Are you  
pulling  
my leg?





# Reading CSV File

Create a CSV File  
Reader

Read in a  
CSV file  
into a list

```
>>> import csv
>>> birth_file = open('crude-birth-rate.csv')
>>> birth_file_reader = csv.reader(birth_file)
>>> data_in_list = list(birth_file_reader)
>>> print(data_in_list)
[['year', 'level_1', 'value'], ['1960', 'Crude Birth Rate', '37.5'], ['1961', 'Crude Birth Rate', '35.2'], ['1962', 'Crude Birth Rate', '33.7'], ['1963', 'Crude Birth Rate', '33.2'], ['1964', 'Crude Birth Rate', '31.6'], ['1965', 'Crude Birth Rate', '29.5'], ['1966', 'Crude Birth Rate', '28.3'], ['1967', 'Crude Birth Rate', '25.6'], ['1968', 'Crude Birth Rate', '23.5']]
```

```
import matplotlib.pyplot as plt
import numpy as np
import csv
```

```
def plot_birth_rate():
    birth_file = open('crude-birth-rate.csv')
    birth_file_reader = csv.reader(birth_file)

    birth_data = np.array(list(birth_file_reader))
    year = birth_data[1:,0]
    num_birth = birth_data[1:,2]
    birth_file.close()

    plt.plot(year, num_birth, label="Birth Rate")
    plt.legend(loc="upper right")
    plt.title('Number of births.')
    plt.show()
```

Because we want  
these cool Numpy  
features

```
plot_birth_rate()
```

Actually we should close  
the file always. But the  
“for” loop with file close  
it for you automatically

Number of births.

