

Date: \_\_\_\_\_

Day:

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04071913026

IML - Assignment #3

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Regression Tree (Karachi House Price Prediction)

$$\rightarrow \text{Var}(S) = 0.66$$

(i) Type :- (Flat, House)

$$\text{var(Flat)} = 0.67$$

$$\text{var(House)} = 0.65$$

$$\text{Gain} = 0.0$$

(ii) Bedrooms :- (2, 3) :-

$$\text{Var(Bedrooms-2)} = 0.2$$

$$\text{var(Bedrooms-3)} = 0.66$$

$$\text{Gain} = 0.15$$

(iii) Bathroom :- (2, 3)

$$\text{var(Bathroom-2)} = 0.2$$

$$\text{var(Bathroom-3)} = 0.66$$

$$\text{Gain} = 0.15$$

(iv) Location (DHA, Bahria) :-

$$\text{var(Bahria)} = 0.58$$

$$\text{var(DHA)} = 0.73$$

$$\text{Gain} = 0.02$$

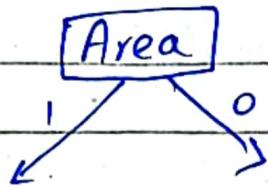
(v) Area (1, 0) OR ( $\leq 236$ ,  $> 236$ )

$$\text{var}(\leq 236) = 0.43$$

$$\text{var}(> 236) = 0$$

$$\text{Gain} = 0.26$$

Max - Gain = 0.26 (Area)



$$\rightarrow \text{Var}(S) = 0.43$$

(i) Type:-

$$\text{var(Flat)} = 0.67$$

$$\text{var(House)} = 0.04$$

$$\text{Gain} = 0.03$$

(ii) Bedrooms:-

$$\text{var(Bedrooms-2)} = 0.2$$

$$\text{var(Bedrooms-3)} = 0.41$$

$$\text{Gain} = 0.09$$

(iii) Bathroom:-

$$\text{var(Bathroom-2)} = 0.2$$

$$\text{var(Bathroom-3)} = 0.41$$

$$\text{Gain} = 0.09$$

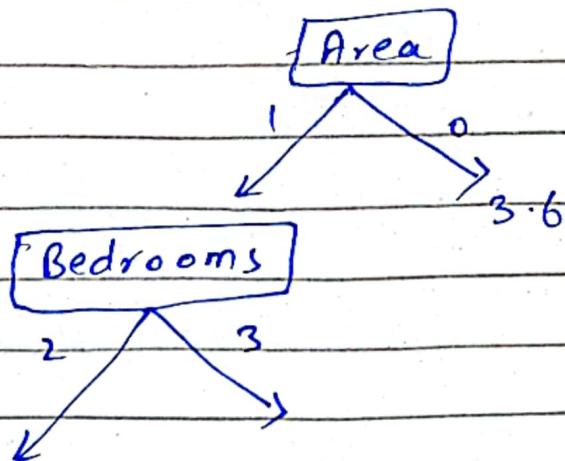
(iv) Location:-

$$\text{var(Bahria)} = 0.09$$

$$\text{var(DHA)} = 0.73$$

$$\text{Gain} = 0.07$$

$$\text{Max - Gain} = 0.09 \text{ (Bedrooms, Bathroom)}$$



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$$\rightarrow \text{Var}(S) = 0.2$$

(i) Type:-

$$\text{var(Flat)} = 0.0$$

$$\text{var(House)} = 0.0$$

$$\text{Gain} = 0.0$$

(ii) Bedrooms:-

$$\text{var(Bedrooms-2)} = 0.0$$

$$\text{var(Bedrooms-3)} = 0.0$$

$$\text{Gain} = 0.0$$

(iii) Bathroom,

$$\text{var(Bathroom-2)} = 0.0$$

$$\text{var(Bathroom-3)} = 0.0$$

$$\text{Gain} = 0.0$$

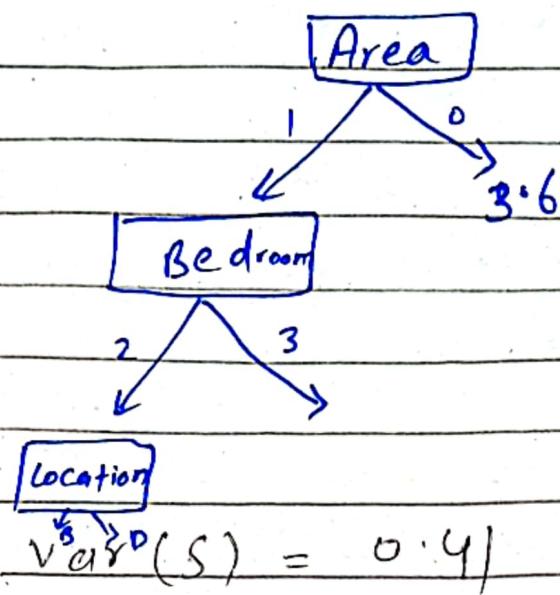
(iv) Location:-

$$\text{var(Bahria)} = 0.23$$

$$\text{var(DHA)} = 0.15$$

$$\text{Gain} = 0.02$$

$$\text{Max-Gain} = 0.02 \text{ (Location)}$$



(i) Type :-

$$\text{var(Flat)} = 0.03$$

$$\text{var(House)} = 0.04$$

$$\text{Grain} = 0.37$$

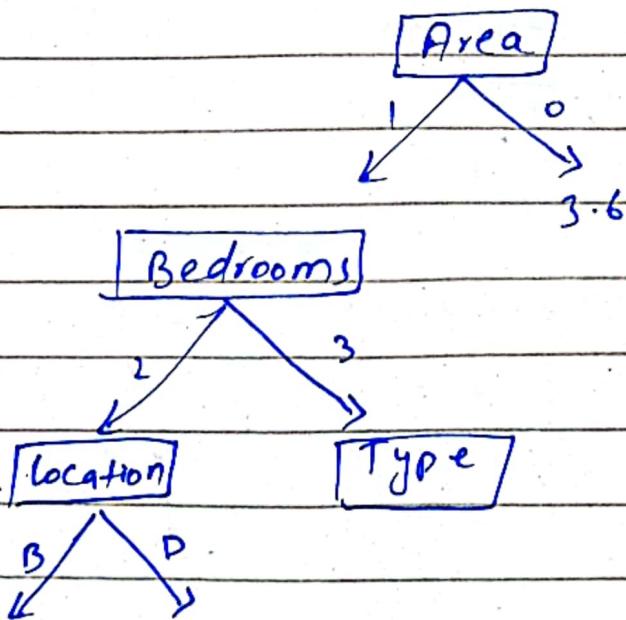
(ii) Bathroom :

$$\text{var(Bathroom-2)} = 0.0$$

$$\text{var(Bathroom-3)} = 0.0$$

$$\text{Grain} = 0.0$$

$$\text{Max-Grain} = 0.37 \text{ (Type)}$$



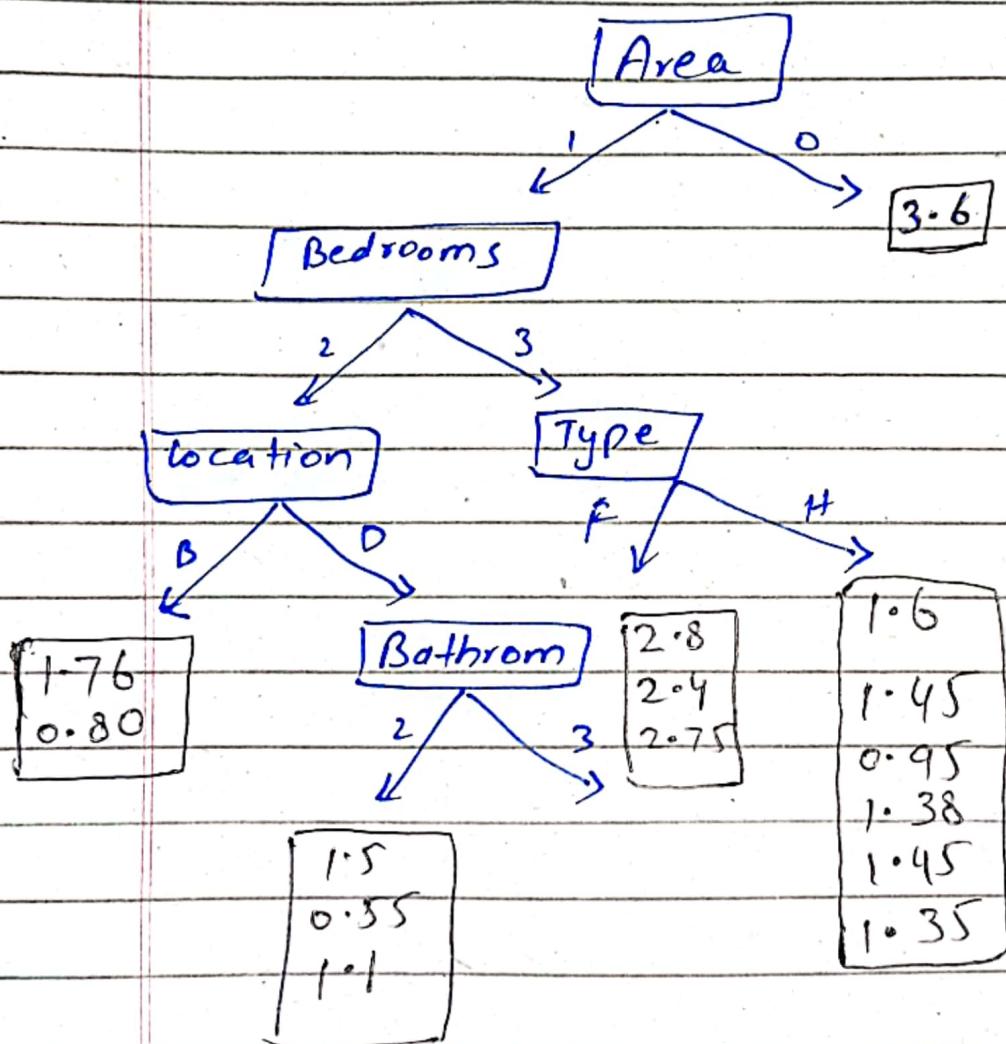
→ var(S) 0.23

(i) Bedroom:-

$$\text{var}(\text{Bathroom-2}) = 0.15$$

$$\text{var}(\text{Bathroom-3}) = 0.03$$

$$\text{Gain} = 0.64$$



→ Random Forest Tree - 1

$$\rightarrow \text{var}(S) = 0.73558$$

(i) Bedrooms:

$$V(\text{Bedrooms-2}) = 0.3000$$

$$V(\text{Bedrooms-3}) = 0.6827$$

$$\text{Gain} = 0.1549$$

(ii) Bathroom:

$$V(\text{Bathroom-2}) = 0.3000$$

$$V(\text{Bathroom-3}) = 0.6827$$

$$\text{Gain} = 0.1549$$

(iii) Type:

$$V(\text{Flat}) = 0.7400$$

$$V(\text{House}) = 0.7048$$

$$\text{Gain} = 0.0119$$

(iv) Location:

$$V(\text{Babria}) = 0.6186$$

$$V(\text{DHA}) = 0.8445$$

$$\text{Gain} = 0.0146$$

(v) Area:

$$V(\leq 236) = 0.5241$$

$$V(>236) = 0$$

$$\text{Gain} = 0.2464$$

$$\text{Max-Gain} = 0.2464 \text{ (Area)}$$



$$\rightarrow \text{Var}(S) = 0.5241$$

(i) Bedrooms:

$$V(\text{Bedrooms} - 2) = 0.3000$$

$$V(\text{Bedrooms} - 3) = 0.4623$$

$$\text{Gain} = 0.1188$$

(ii) Bathroom:

$$V(\text{Bathroom} - 2) = 0.3000$$

$$V(\text{Bathroom} - 3) = 0.4623$$

$$\text{Gain} = 0.1188$$

(iii) Type:

$$V(\text{Flat}) = 0.7400$$

$$V(\text{House}) = 0.6643$$

$$\text{Gain} = 0.0736$$

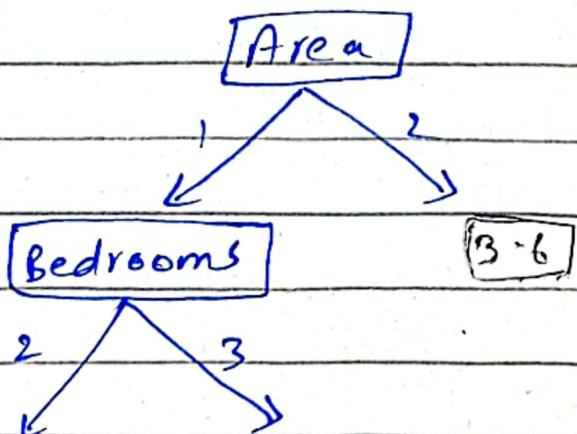
(iv) Location:-

$$V(\text{Bahria}) = 0.0814$$

$$V(\text{DHA}) = 0.8445$$

$$\text{Gain} = 0.0995$$

$$\text{Max - Gain} = 0.1188 \text{ (Bedrooms, Bathroom)}$$



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$$\rightarrow \text{Var}(S) = 0.3000$$

(i) Bathroom:

$$v(\text{Bathroom-2}) = 0.3000$$

$$v(\text{Bathroom-3}) = 0$$

$$\text{Gain} = 0$$

(ii) Type:-

$$v(\text{Flat}) = 0.3000$$

$$v(\text{House}) = 0$$

$$\text{Gain} = 0$$

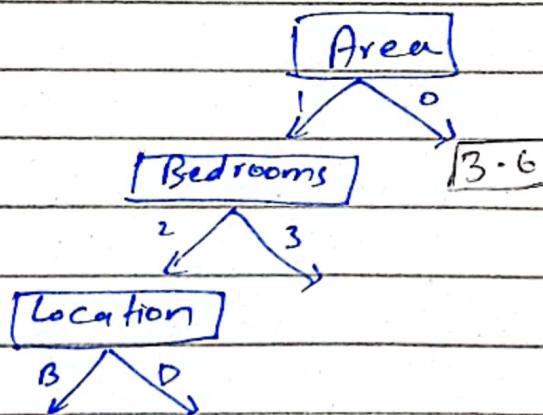
(iii) Location = 0

$$v(\text{Bahria}) = 0.200$$

$$v(\text{DHA}) = 0.2005$$

$$\text{Gain} = 0.1496$$

$$\text{Max-Gain} = 0.1496 \text{ (Location)}$$



$$\rightarrow \text{Var}(S) = 0.4623$$

(i) Bathroom:

$$v(\text{Bathroom-2}) = 0$$

$$v(\text{Bathroom-3}) = 0.4623$$

$$\text{Gain} = 0$$

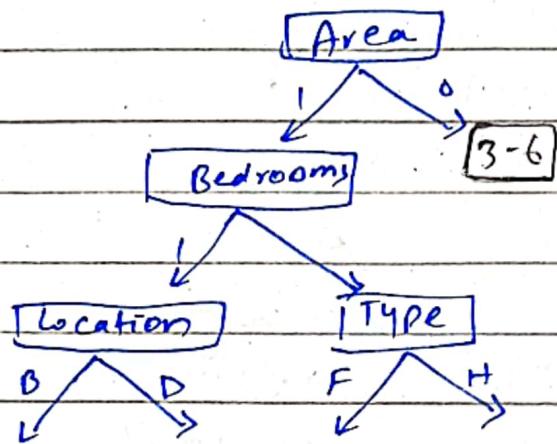
(ii) Type:

$$V(\text{Flat}) = 0.04$$

$$V(\text{House}) = 0.0643$$

$$\text{Grain} = 0.4076$$

$$\text{Max-Grain} = 0.4076 \text{ (Type)}$$



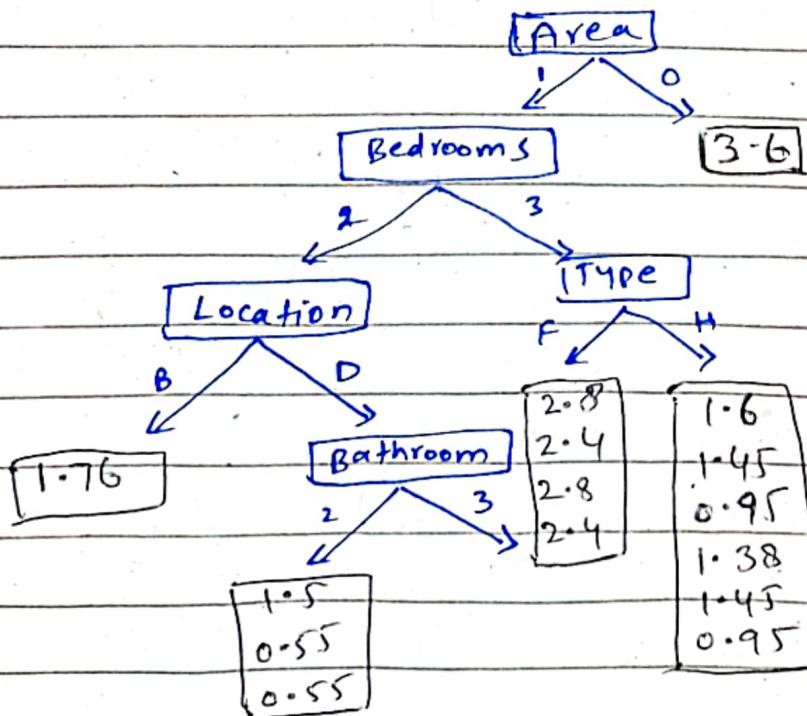
$$\rightarrow \text{Var}(s) = 0.08445$$

(i) Bathroom:

$$V(\text{Bathroom-2}) = 0.2005$$

$$V(\text{Bathr oom-3}) = 0.04$$

$$\text{Grain} = 0.7357$$



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$\Rightarrow$  Random Forest Tree II :-

$$\rightarrow \text{Var}(S) = 0.8207$$

(i) Bedrooms:-

$$V(\text{Bedrooms-2}) = 0.2704$$

$$V(\text{Bedrooms-3}) = 0.8371$$

$$\text{Gain} = 0.01759$$

(ii) Bathroom:-

$$V(\text{Bathroom-2}) = 0.2704$$

$$V(\text{Bathroom-3}) = 0.8371$$

$$\text{Gain} = 0.01759$$

(iii) Type:-

$$V(\text{Flat}) = 0.680$$

$$V(\text{House}) = 0.7898$$

$$\text{Gain} = 0.01969$$

(iv) Location:-

$$V(\text{Bahria}) = 0.841644$$

$$V(\text{DHA}) = 0.7584$$

$$\text{Gain} = 0.0068$$

(v) Area:-

$$V(<236) = 0.6563$$

$$V(>236) = 0$$

$$\text{Gain} = 0.0437$$

Max-Gain = 0.0437 (Area)



$$\rightarrow \text{var}(S) = 0.6563$$

(i) Bedrooms:

Date: \_\_\_\_\_

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$$\text{var}(\text{Bedrooms}-2) = 0.2704$$

$$\text{var}(\text{Bedroom}-3) = 0.6745$$

$$\text{Gain} = 0.0320$$

(ii) Bathroom:-

$$v(\text{Bathroom}-2) = 0.2704$$

$$v(\text{Bathroom}-3) = 0.6745$$

$$\text{Gain} = 0.0320$$

(iii) Type:-

$$v(\text{Flat}) = 0.6406$$

$$v(\text{House}) = 0.6167$$

$$\text{Gain} = 0.02929$$

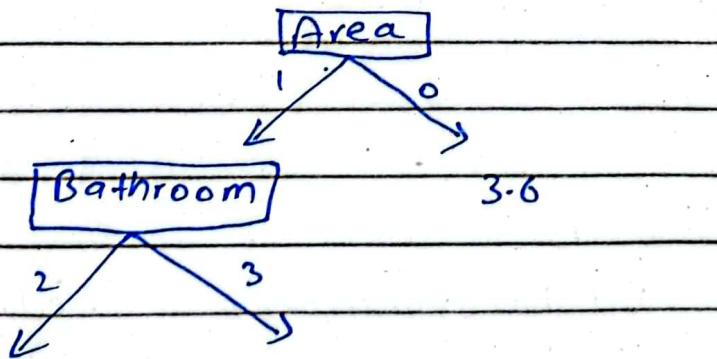
(iv) Location:-

$$v(\text{Bahria}) = 0.5501$$

$$v(\text{DHA}) = 0.7584$$

$$\text{Gain} = 0.03181$$

Max-Gain:- 0.0320 (Bathroom, Bedroom)



$$\rightarrow \text{var}(S) = 0.2704$$

(i) Bedrooms:-

$$\text{var}(\text{Bedroom}-2) = 0.270$$

$$\text{var}(\text{Bedroom}-3) = 0$$

$$\text{Gain} = 0$$

Date: \_\_\_\_\_

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(ii) Type:-

$$v(\text{Flat}) = 0.2704$$

$$v(\text{House}) = 0$$

$$\text{Gain} = 0$$

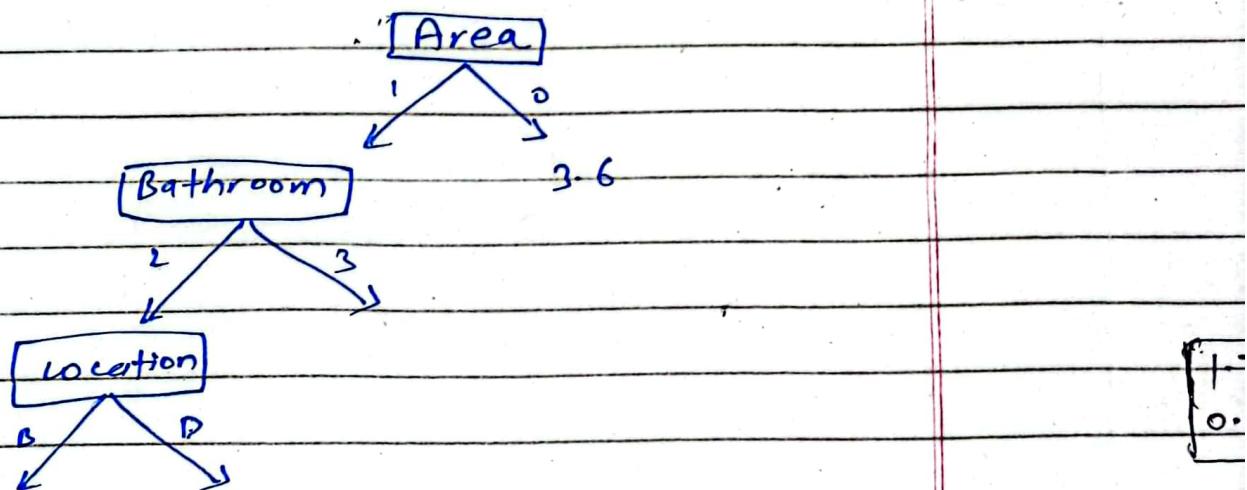
(iii) Location:-

$$v(\text{Bahria}) = 0$$

$$v(\text{DHA}) = 0.2256$$

$$\text{Gain} = 0.1200$$

$$\text{Max-Gain} = 0.1200 \text{ (Location)}$$



$$\rightarrow \text{var}(S) = 0.5501$$

(i) Bedrooms:-

$$v(\text{Bedroom-2}) = 0$$

$$v(\text{Bedroom-3}) = 0.6167$$

$$\text{Gain} = 0.0018$$

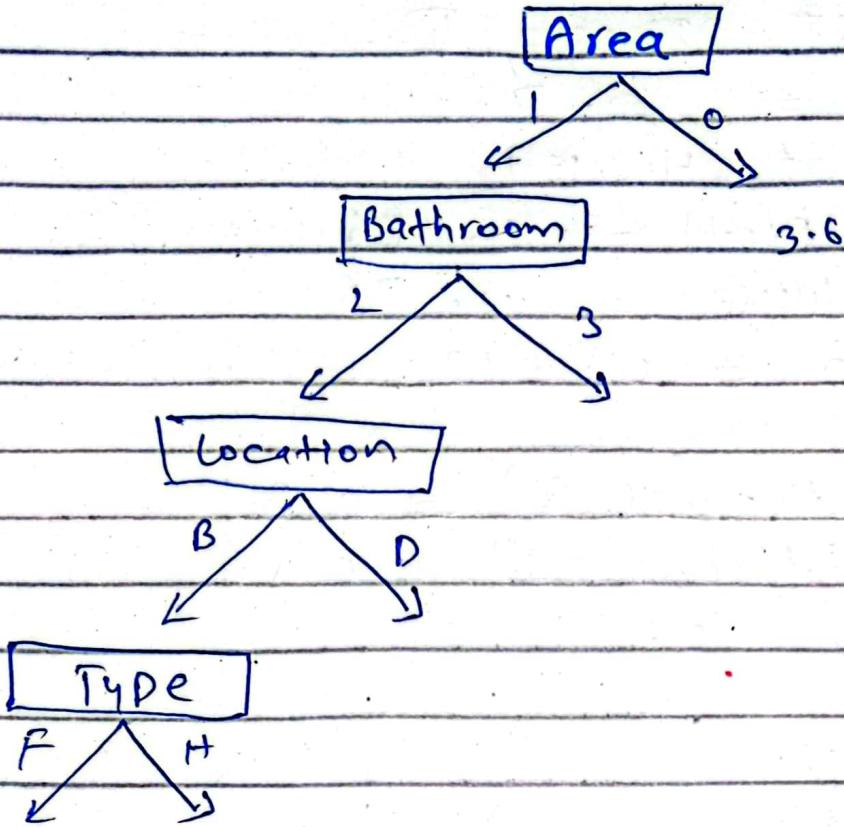
(ii) Type:-

$$v(\text{Flat}) = 0$$

$$v(\text{House}) = 0.6167$$

$$\text{Gain} = 0.0018$$

$$\text{Max-Gain} = 0.0018 \text{ (Bedrooms, Type)}$$



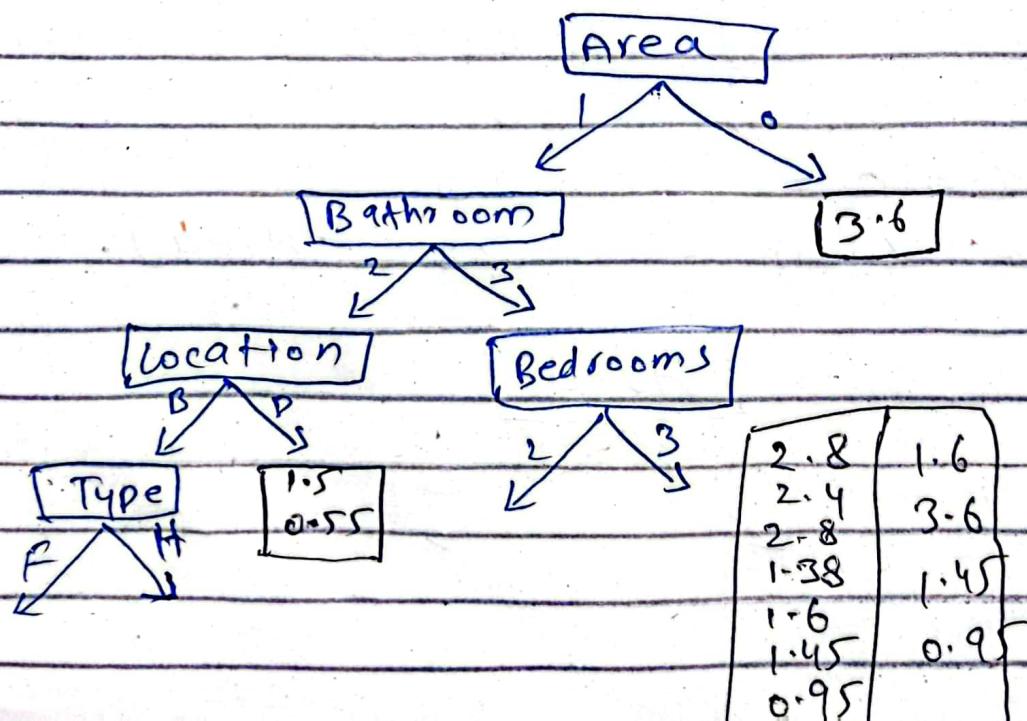
$$\Rightarrow \text{Var}(S) = 0.6745$$

(i) Bedrooms :-

$$v(\text{Bedroom-2}) = 0$$

$$v(\text{Bedroom-3}) = 0.6745$$

$$\text{Grain} = 0$$



$\Rightarrow$  XG BOOST Tree - I

$$\rightarrow \text{Var}(S) = 0.73558$$

(i) Bedrooms:

$$V(\text{Bedrooms-2}) = 0.3000$$

$$V(\text{Bedrooms-3}) = 0.6827$$

$$\text{Gain} = 0.1549$$

(ii) Bathroom:

$$V(\text{Bathroom-2}) = 0.3000$$

$$V(\text{Bathroom-3}) = 0.6827$$

$$\text{Gain} = 0.1549$$

(iii) Type:

$$V(\text{Flat}) = 0.7400$$

$$V(\text{House}) = 0.7048$$

$$\text{Gain} = 0.0119$$

(iv) Location:-

$$V(\text{Babria}) = 0.6186$$

$$V(\text{DHA}) = 0.8445$$

$$\text{Gain} = 0.01146$$

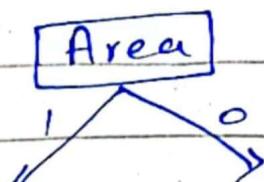
(v) Area:

$$V(\leq 236) = 0.5241$$

$$V(>236) = 0$$

$$\text{Gain} = 0.2464$$

$$\text{Max-Gain} = 0.2464 \text{ (Area)}$$



$$\rightarrow \text{var}(S) = 0.5241$$

(i) Bedrooms:

$$V(\text{Bedrooms-2}) = 0.3000$$

$$V(\text{Bedrooms-3}) = 0.4623$$

$$\text{Gain} = 0.1188$$

(ii) Bathroom:

$$V(\text{Bathroom-2}) = 0.3000$$

$$V(\text{Bathroom-3}) = 0.4623$$

$$\text{Gain} = 0.1188$$

(iii) Type:

$$V(\text{Flat}) = 0.7400$$

$$V(\text{House}) = 0.6643$$

$$\text{Gain} = 0.0736$$

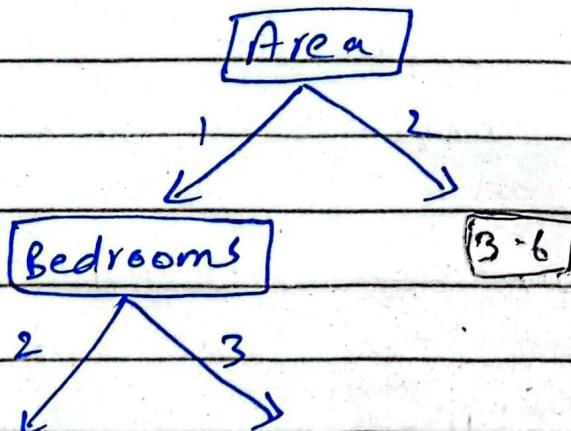
(iv) Location:-

$$V(\text{Bahria}) = 0.0814$$

$$V(\text{DHA}) = 0.8445$$

$$\text{Gain} = 0.0995$$

Max - Gain = 0.1188 (Bedrooms,  
Bathroom)



$$\rightarrow \text{Var}(S) = 0.3000$$

(i) Bathroom:

$$V(\text{Bathroom-2}) = 0.3000$$

$$V(\text{Bathroom-3}) = 0$$

$$\text{Gain} = 0$$

(ii) Type:-

$$V(\text{Flat}) = 0.3000$$

$$V(\text{House}) = 0$$

$$\text{Gain} = 0$$

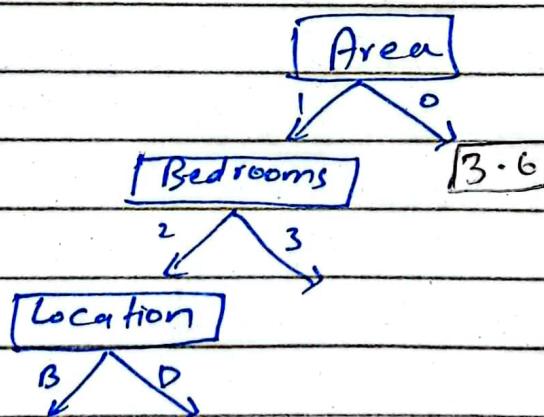
(iii) Location =

$$V(\text{Bahria}) = 0.200$$

$$V(\text{DHA}) = 0.2005$$

$$\text{Gain} = 0.1496$$

$$\text{Max-Gain} = 0.1496 \text{ (Location)}$$



$$\rightarrow \text{Var}(S) = 0.4623$$

(i) Bathroom:

$$V(\text{Bathroom-2}) = 0$$

$$V(\text{Bathroom-3}) = 0.4623$$

$$\text{Gain} = 0$$

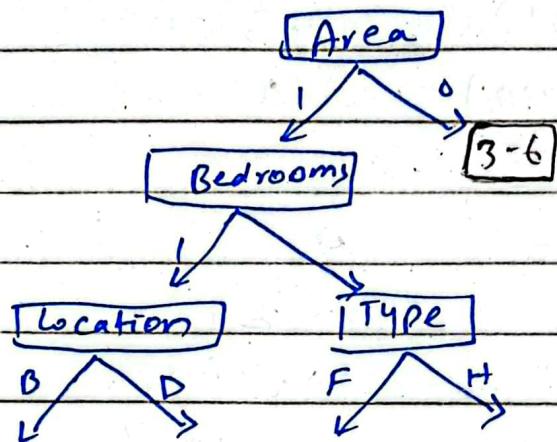
(ii) Type:

$$V(\text{Flat}) = 0.04$$

$$V(\text{House}) = 0.0643$$

$$\text{Grain} = 0.4076$$

$$\text{Max-Grain} = 0.4076 \text{ (Type)}$$



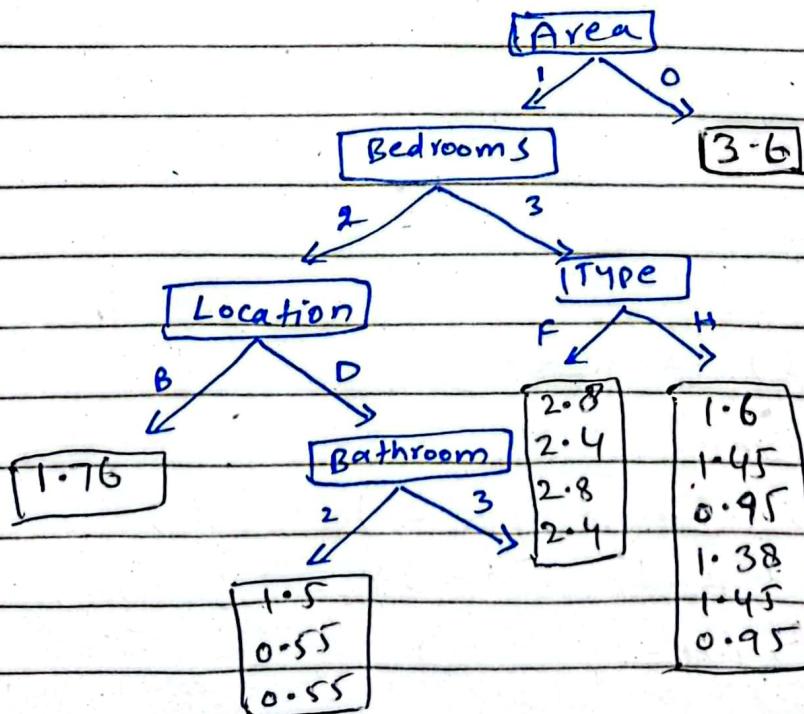
$$\rightarrow V_{\text{var}}(S) = 0.08445$$

(i) Bathroom:

$$V(\text{Bathroom-2}) = 0.2005$$

$$V(\text{Bathr oom-3}) = 0.04$$

$$\text{Grain} = 0.7357$$



$\Rightarrow$  XG BOOST Tree II:-

$$\rightarrow \text{Var}(s) = 0.78$$

(i) Type :- (Flat, House)

$$\text{var(Flat)} = 0.56$$

$$v(\text{House}) = 0.76$$

$$\text{Gain} = 0.012$$

(ii) Bedrooms :-

$$v(\text{Bedrooms-2}) = 0.3$$

$$v(\text{Bedrooms-3}) = 0.56$$

$$\text{Gain} = 0.18$$

(iii) Bathroom :-

$$v(\text{Bathroom-2}) = 0.3$$

$$v(\text{Bathroom-3}) = 0.56$$

$$\text{Gain} =$$

(iv) Location :-

$$v(\text{Babria}) = 0.72$$

$$v(\text{DHA}) = 0.63$$

$$\text{Gain} = 0.03$$

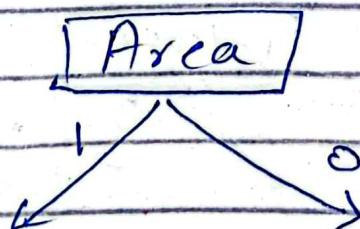
(v) Area :

$$v(\leq 236) = 0.53$$

$$v(> 236) = 0$$

$$\text{Gain} = 0.28$$

$$\text{Max-Gain} = 0.28 \text{ (Area).}$$



$$\rightarrow \text{var}(S) = 0.56$$

(i) Type:-

$$v(\text{Flat}) = 0.76$$

$$v(\text{House}) = 0.06$$

$$\text{Gain} = 0.05$$

(ii) Bedrooms:-

$$v(\text{Bedrooms-2}) = 0.4$$

$$v(\text{Bedrooms-3}) = 0.31$$

$$\text{Gain} = 0.10$$

(iii) Bathroom:-

$$v(\text{Bathroom-2}) = 0.4$$

$$v(\text{Bathroom-3}) = 0.31$$

$$\text{Gain} = 0.10$$

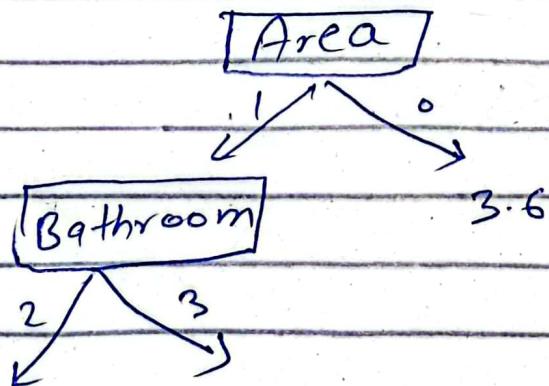
(iv) Location:-

$$v(\text{Bahria}) = 0.10$$

$$v(\text{DHA}) = 0.64$$

$$\text{Gain} = 0.06$$

$$\text{Max - Gain} = 0.10 \quad (\text{Bedrooms, } \text{Bathroom})$$



$$\rightarrow \text{Var}(S) = 0.32$$

(i) Type:

$$v(\text{Flat}) = 0.0$$

$$v(\text{House}) = 0.0$$

$$\text{Gain} = 0.0$$

(ii) Bedrooms:

$$v(\text{Bedrooms}-2) = 0.0$$

$$v(\text{Bedrooms}-3) = 0.0$$

$$\text{Gain} = 0.0$$

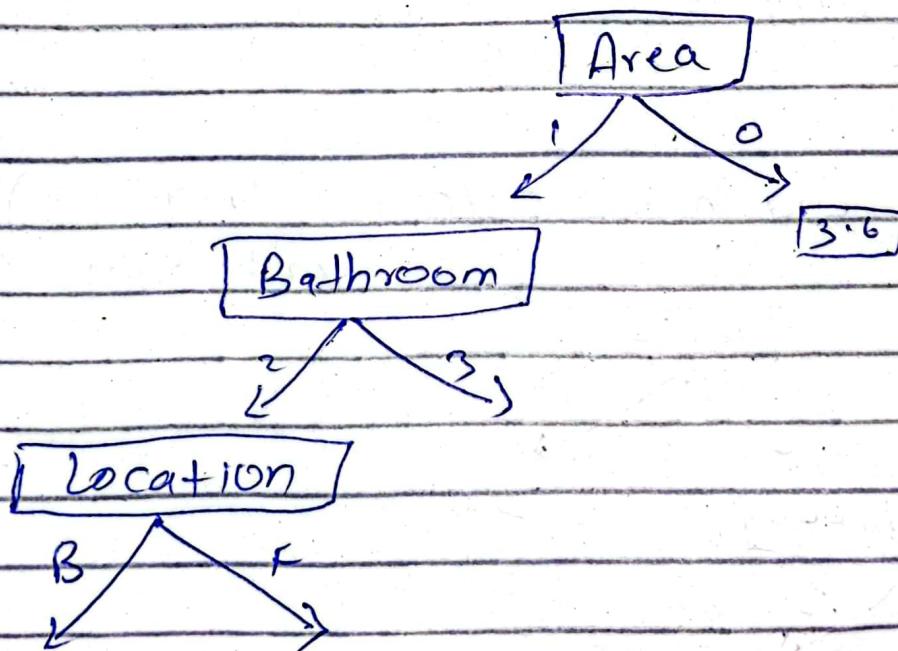
(iii) Location:

$$v(\text{Bahrain}) = 0.34$$

$$v(\text{DHA}) = 0.05$$

$$\text{Gain} = 0.04$$

$$\text{Max - Gain} = 0.04 \text{ (Location)}$$



$$\rightarrow \text{var}(S) = 0.31$$

(i) Type:-

$$v(\text{Flat}) = 0.01$$

$$v(\text{House}) = 0.03$$

$$\text{Gain} = 0.29$$

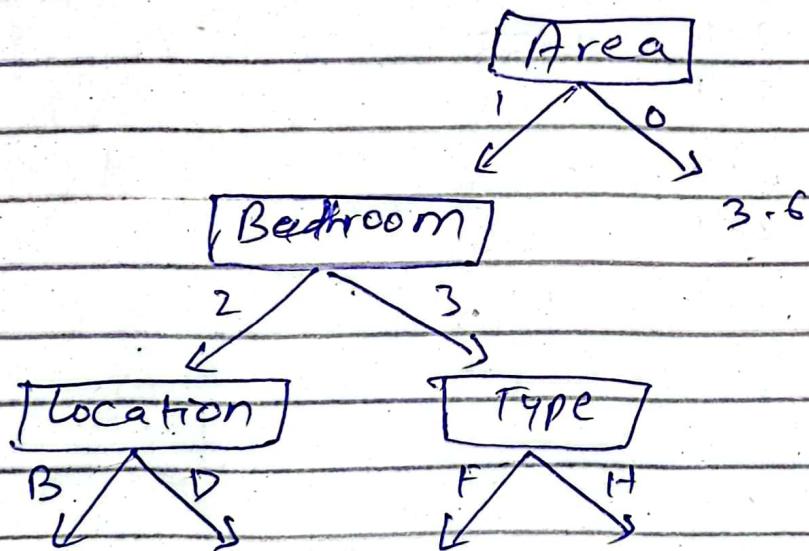
(ii) Bedroom:

$$v(\text{Bedroom-2}) = 0.0$$

$$v(\text{Bedroom-3}) = 0.0$$

$$\text{Gain} = 0.0$$

$$\text{Max - Gain} = 0.29 \text{ (Type)}.$$



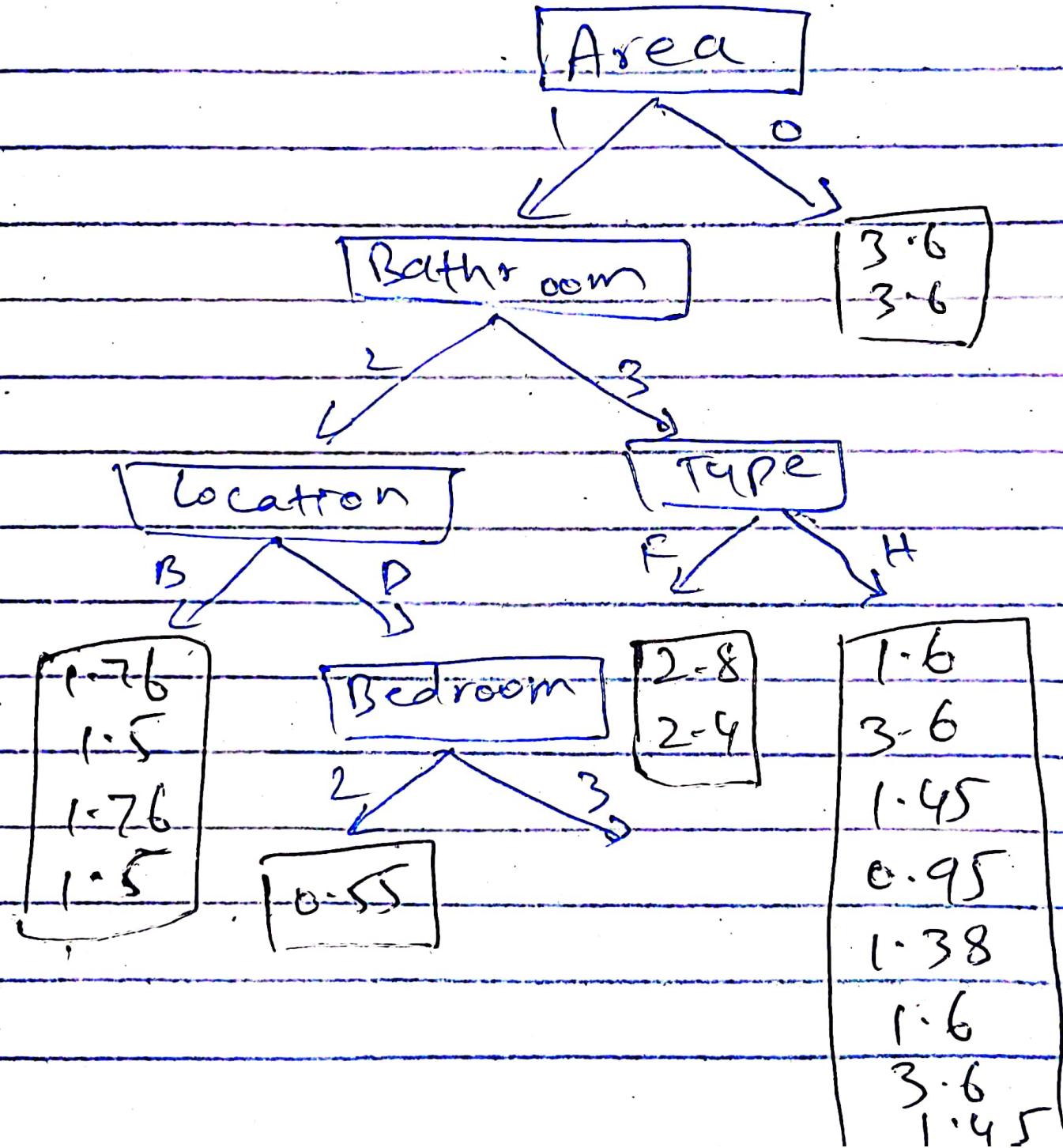
$$\rightarrow \text{var}(S) = 0.31$$

(i) Bedrooms:-

$$v(\text{Bedrooms-2}) = 0.45$$

$$v(\text{Bedrooms-3}) = 0.02$$

$$\text{Gain} = 0.55$$



⇒ Mean Squared Error (Regression Tree)

→ Training Data:

Actual Price	Predicted Price
1.76	1.28
1.5	1.05
1.6	1.363
3.6	3.6
1.45	1.363
0.95	1.363
2.8	2.65
2.4	2.65
0.55	1.05
1.38	1.363
1.1	1.363
1.45	1.05
1.35	1.363
2.75	2.65
0.80	1.28

⇒ Test Data:

Actual price	Predicted Price
0.77	1.28
0.70	1.28
0.81	1.28
1.8	1.28
3.35	2.65

$$MSE_{test} = 0.31556$$

$$MSE_{train} = 0.09815$$

As  $MSE_{train} < MSE_{test}$  so,  
the model is High variance.

⇒ Mean Squared Error (Random Forest)

⇒ Training Data:-

Actual price

1.76

1.5

1.6

3.6

1.45

0.95

2.8

2.4

0.55

1.38

1.45

0.95

2.8

2.4

0.55

Tree - I

Predicted price

1.76

0.86

1.29

3.6

1.29

1.29

2.6

2.6

0.86

1.29

1.29

1.29

2.6

2.6

0.86

⇒ Test Data

Actual Price

0.77

0.76

0.81

1.8

3.35

Predicted Price

1.29

1.29

1.29

1.29

2.6

$$MSE_{Train} = 0.07656$$

$$MSE_{Test} = 0.33430$$

As  $MSE_{Train} < MSE_{Test}$  the model is High variance.

⇒ Mean Square Error (Random Forest Tree II)

→ Training Data

Actual Price	Predicted Price
1.76	1.8
1.5	1.02
1.6	1.8
3.6	3.6
1.45	1.8
0.95	1.8
2.8	1.8
2.4	1.8
0.55	1.02
1.38	1.8
1.6	1.8
3.6	1.8
1.45	1.8
0.95	1.8
2.8	1.8

$\Rightarrow$  Test Data :-

Actual Data

0.77

0.70

0.81

1.8

3.35

Predicted Data

1.8

1.8

1.8

1.8

1.8

$$MSE_{train} = 0.53329$$

$$MSE_{test} = 1.13070$$

As  $MSE_{train} < MSE_{test}$  then  
the model is High variance.

As  $MSE_{train} < MSE_{test}$  so,  
the model is High variance.

→ Mean Squared Error (XG BOOST)  
⇒ Training Data:- Tree - I

Actual price	Predicted price
1.76	1.76
1.5	0.86
1.6	1.29
3.6	3.6
1.45	1.29
0.95	1.29
2.8	2.6
2.4	2.6
0.55	0.86
1.38	1.29
1.45	1.29
0.95	1.29
2.8	2.6
2.4	2.6
0.55	0.86

→ Test Data

Actual Price	Predicted Price
0.77	1.29
0.76	1.29
0.81	1.29
1.8	1.29
3.35	2.6

$$MSE_{\text{train}} = 0.07656$$

$$MSE_{\text{test}} = 0.33430$$

As  $MSE_{\text{train}} < MSE_{\text{test}}$  the model  
is high variance.

→ Mean Squared Error (XG BOOST  
Tree - II)

→ Training Data

Actual price

1.76

1.5

1.6

~~1.75~~

3.6

1.45

0.95

2.8

2.4

0.55

1.38

1.76

1.5

1.6

3.6

1.45

Predicted Price

1.63

1.63

1.95

~~1.75~~

3.6

1.95

1.95

2.6

2.6

0.55

1.95

1.63

1.63

1.95

3.6

1.95

⇒ Test Data :-

Actual Price

0.77

0.70

0.81

01.8

3.35

Predicted price

1.95

1.95

1.95

1.95

3.6

$$MSE_{\text{train}} = 0.14783$$

$$MSE_{\text{test}} = 0.86790$$

As  $MSE_{\text{train}} < MSE_{\text{test}}$  then  
the model is High variant.