CSC384 – Assignment 2 Report Tanzeem Chowdhury - 997574726

\* Notes About Code:

In addition to SudokuSolver.py, two additional files have been submitted:

* SudokuHelpers.py – contains helper methods for SudokuSolver.py
* SudokuIO.py - contains methods to read/write to files, and outputting to the screen

SudokuSolver contains the main algorithms and main. **Without the two additional files, the program won’t compile/run, so please download them aswell.**

**Brute Force Algorithm**

This implementation attempts to solve the sudoku puzzle using an exhaustive search method. Initially, scan the puzzle for a coordinates list of all empty cells (by row and column). Since we are brute forcing, we need every single permutation of possible values we can insert into empty cell values. Retrieving all possible blanks was retrieved using the itertools module’s product method, which provided permutative lists of size of the number of blank cells found. Starting with the first permutation (e.g. (1, 1, 1, ...) ), iterate through all possibilities, and check if it applying the permuation to the puzzle results in a goal state, until a permuation is found that solves the puzzle.

**Back Tracking Algorithm**

This implementation attempts to solve the sudoku puzzle using the back-tracking constraint satisfaction problem method, using recursion to back-track if a path leads to a situation where a legal placement of a value is not possible. The algorithm was adapted from pseudo code in slide 24 of CSP lecture. As a base case to the recursion, check if puzzle is in goal state and return true if so. Else, get the first empty cell. For each value that can be put in the empty cell (1-9), assign the value to the empty cell. Check if this creates conflicts, and choose the next value if it does and so on. If constraints are ok, modify puzzle with the value and then recurse this function with the rest of the empty cells, returning true with each successful placement. If this value doesn't lead to the solution, the recursive call will eventually return false, then try the next value if one exists**.** Check constraints before assigning the value, or else it'll accidentally find itself as duplicate. If all values are tried in the cell, and a legal placement is not possible, reset the cell to an empty cell as we have tried all values without success, and return false. The recursive function will then backtrack to an earlier placed space to try a different state.

**Forward Checking + MRV Algorithm**

This implementation extends back tracking, and attempts to solve the puzzle using a mininum remaining values heuristics method, using recursion to back-track if path leads to inability to place values legally**.** As a base case to the recursion, check if puzzle is in goal state and return true if so. Else, get list of all empty cells, and the legal values they can currently take, sorted by minimum restricted values, i.e. the cells which have the fewest legal options. For each value that can legally be put in the chosen empty cell, modify the puzzle by placing value in empty cell. Then recurse this function with the rest of the empty cells, re-evaluating the mrv cells. If this value doesn't lead to the solution, the recursive call with eventually return false, then try the next legal value if one exists. If all legal values have been tried in the cell, and a legal placement is not possible, reset the cell to an empty cell as we have tried all values without success, and return false. The recursive function will then backtrack to an earlier placed space to try a different state.

|  |  |  |  |
| --- | --- | --- | --- |
| **Comparing performance of search algorithms for test cases listed in the appendix** | | | |
| Algorithms: | Brute Force | Back-Tracking | Forward Checking with MRV |
| puzzle1.txt (Test case 1) | | | |
| Total clock time (ms) | N/A Too Long | 5.69796562195 | 11.7399692535 |
| Total search time (ms) | N/A Too Long | 5.65981864929 | 11.6810798645 |
| Nodes generated | ? | 687 | 41 |
| puzzle2.txt (Test case 2) | | | |
| Total clock time (ms) | N/A Too Long | 64.5699501038 | 20.1671123505 |
| Total search time (ms) | N/A Too Long | 64.5248889923 | 20.1210975647 |
| Nodes generated | ? | 8008 | 58 |
| puzzle3.txt (Test case 3) | | | |
| Total clock time (ms) | N/A Too Long | 117.506980896 | 62.9210472107 |
| Total search time (ms) | N/A Too Long | 117.410182953 | 62.8731250763 |
| Nodes generated | ? | 14340 | 167 |
| puzzle4.txt (Test case 4) | | | |
| Total clock time (ms) | N/A Too Long | 37.0609760284 | 33.0669879913 |
| Total search time (ms) | N/A Too Long | 37.0230674744 | 33.0278873444 |
| Nodes generated | ? | 4621 | 86 |
| puzzle5.txt (Test case 5) | | | |
| Total clock time (ms) | N/A Too Long | 20.4617977142 | 28.9080142975 |
| Total search time (ms) | N/A Too Long | 20.41888237 | 28.8689136505 |
| Nodes generated | ? | 2359 | 66 |

**Results Analysis:**

For all five puzzles, running brute force ran too long, unable to yield the clock/search time and number of nodes generated for any of them. This is expected, as trying every permuation possible has a worst case complexity of 9n , where n is the number of blank cells. Taking puzzle 1 as an example, which has 41 empty cells, there is 941 permuations of puzzle state, and surfing through these is an exaustive method.

When comparing the number of nodes generated between the back tracking anf FC-MRV methods, we get expected results for all puzzles where the number of nodes generated with FC-MRV are significantly smaller than BT (eg. For puzzle 3, FC-MRV only expanded 1.2% of the nodes expanded by BT. While theoretically, the worst case complexity for both BT and FC-MRV remains 9n (n = # of empty cells), best and average case significantly increase, with BT able to find solutions faster due to the fact it checks constraints after placing a possible value and back tracking when stuck, instead of starting from scratch, and FC-MRV faster due to the fact it checks contrainsts prior to placement, with the order of said placement determined dynamically based on the MRV heuristic, instead of a predefined static order.

While FC-MRV generated fewer nodes, unexpected results was observed where in some cases, the BT method performed faster time-wise compared to FC-MRV, even when generating substantially lesser nodes (e.g. puzzle 1 took double time with FC-MRV, puzzle 4 ran roughly the same time as BT, and puzzle 5 was a little longer than BT). This can attributed to the fact that in some scenarios, a significantly larger amount of computation is required to determine the MRV heuristic, compared to simply backtracking. Another interesting unexpected result was that most puzzles gave different solutions when using BT and FC-MRV, however both were correct valid solutions. With BT searching linearly and back tracking, it makes sense it was able to find an early solution out of several in it’s search, compared to FC-MRV searching optimally based on the heuristic, which could attribute to why in some cases, BT performed faster.