

Lecture 05

Abstract Data Type - Unsorted List and Sorted List (Array-based Implementation)

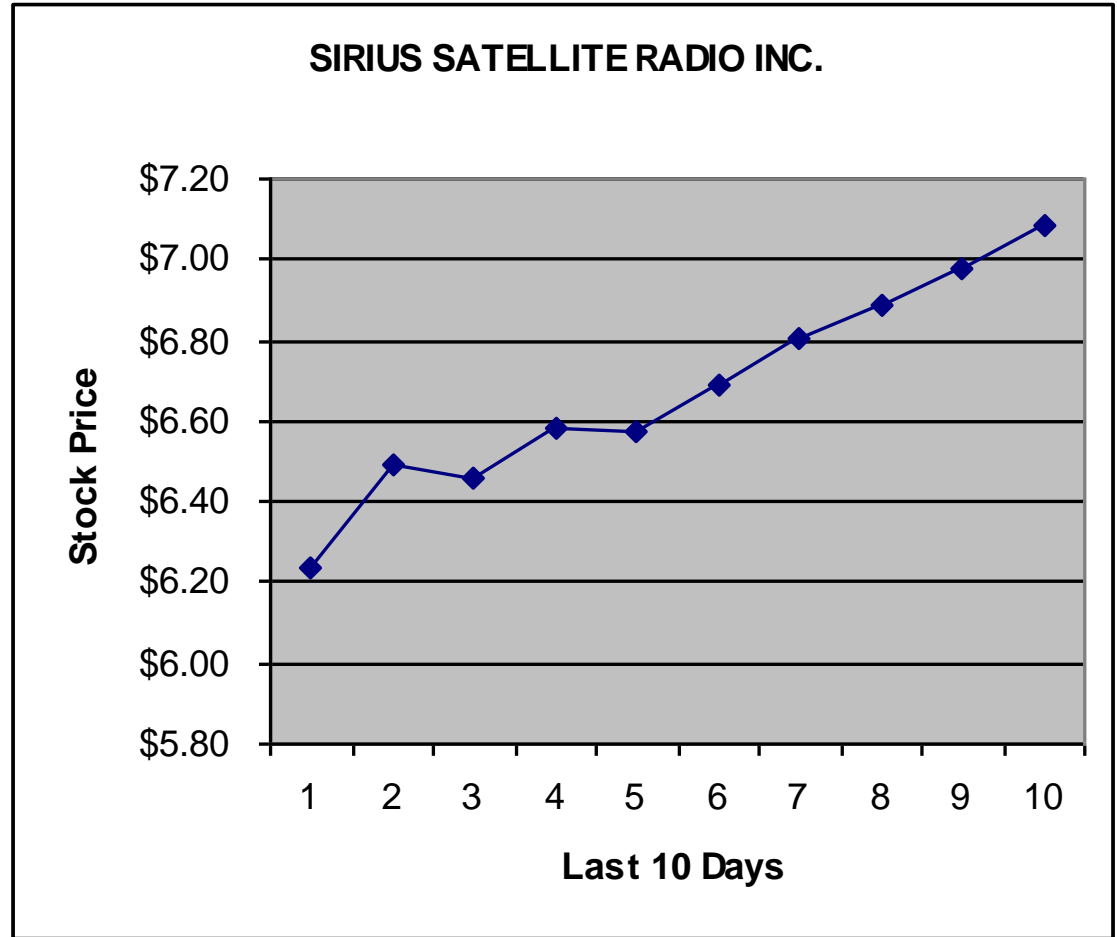
CSE225: Data Structures and Algorithms

Data vs. Information

Data

- 6.34
- 6.45
- 6.39
- 6.62
- 6.57
- 6.64
- 6.71
- 6.82
- 7.12
- 7.06

Information



Lists

- **Unsorted list:**

- A list in which data items are placed in no particular order.

- **Sorted List:**

- A list in which data items are placed in a particular order.
- Key: a member of the class whose value is used to determine the order of the items in the list.

Unsorted List

| |
|----|
| 22 |
| 12 |
| 46 |
| 35 |
| 14 |
| . |
| . |
| . |
| . |
| |

Sorted List

| |
|----|
| 12 |
| 14 |
| 22 |
| 35 |
| 46 |
| . |
| . |
| . |
| . |
| |

Sorted List

| ID | Name | Address |
|----|----------------|-------------------------|
| 22 | Jack Black | 120 S. Virginia Street |
| 45 | Simon Graham | 6762 St Petersburg |
| 59 | Susan O'Neal | 1807 Glenwood, Palm Bay |
| 66 | David peterson | 1207 E. Georgetown |

Key

Specification of UnsortedType

| | |
|---|---|
| Structure: | The list has a special property called the <i>current position</i> - the position of the last element accessed by GetNextItem during an iteration through the list. Only ResetList and GetNextItem affect the current position. |
| Operations (provided by Unsorted List ADT): | |
| MakeEmpty | |
| Function | Initializes list to empty state. |
| Precondition | |
| Postcondition | List is empty. |
| Boolean IsFull | |
| Function | Determines whether list is full. |
| Precondition | List has been initialized. |
| Postcondition | Returns true if list is full and false otherwise. |

Specification of UnsortedType

| | |
|--|---|
| int Lengths | |
| Function | Determines the number of elements in list. |
| Precondition | List has been initialized. |
| Postcondition | Returns the number of elements in list. |
| RetrieveItem (ItemType& item, Boolean& found) | |
| Function | Retrieves list element whose key matches item's key (if present). |
| Precondition | List has been initialized. Key member of item is initialized. |
| Postcondition | If there is an element someItem whose key matches item's key, then found = true and item is a copy of someItem; otherwise found = false and item is unchanged. List is unchanged. |
| InsertItem (ItemType item) | |
| Function | Adds item to list. |
| Precondition | List has been initialized. List is not full. item is not in list. |
| Postcondition | item is in list. |

Specification of UnsortedType

| | |
|---|---|
| DeleteItem (ItemType item) | |
| Function | Deletes the element whose key matches item's key. |
| Precondition | List has been initialized. Key member of item is initialized. One and only one element in list has a key matching item's key. |
| Postcondition | No element in list has a key matching item's key. |
| ResetList | |
| Function | Initializes current position for an iteration through the list. |
| Precondition | List has been initialized. |
| Postcondition | Current position is prior to first element in list. |
| GetNextItem (ItemType& item) | |
| Function | Gets the next element in list. |
| Precondition | List has been initialized. Current position is defined. Element at current position is not last in list. |
| Postcondition | Current position is updated to next position. item is a copy of element at current position. |

Specification of SortedType

| | |
|--|---|
| Structure: | The list has a special property called the <i>current position</i> - the position of the last element accessed by GetNextItem during an iteration through the list. Only ResetList and GetNextItem affect the current position. |
| Operations (provided by Unsorted List ADT): | |
| MakeEmpty | |
| Function | Initializes list to empty state. |
| Precondition | |
| Postcondition | List is empty. |
| Boolean IsFull | |
| Function | Determines whether list is full. |
| Precondition | List has been initialized. |
| Postcondition | Returns true if list is full and false otherwise. |

Specification of SortedType

| | |
|--|---|
| int Lengths | |
| Function | Determines the number of elements in list. |
| Precondition | List has been initialized. |
| Postcondition | Returns the number of elements in list. |
| RetrieveItem (ItemType& item, Boolean& found) | |
| Function | Retrieves list element whose key matches item's key (if present). |
| Precondition | List has been initialized. Key member of item is initialized. |
| Postcondition | If there is an element someItem whose key matches item's key, then found = true and item is a copy of someItem; otherwise found = false and item is unchanged. List is unchanged. |
| InsertItem (ItemType item) | |
| Function | Adds item to list. |
| Precondition | List has been initialized. List is not full. item is not in list. |
| Postcondition | item is in list. List is still sorted. |

Specification of SortedType

| | |
|---|---|
| DeleteItem (ItemType item) | |
| Function | Deletes the element whose key matches item's key. |
| Precondition | List has been initialized. Key member of item is initialized. One and only one element in list has a key matching item's key. |
| Postcondition | No element in list has a key matching item's key. List is still sorted. |
| ResetList | |
| Function | Initializes current position for an iteration through the list. |
| Precondition | List has been initialized. |
| Postcondition | Current position is prior to first element in list. |
| GetNextItem (ItemType& item) | |
| Function | Gets the next element in list. |
| Precondition | List has been initialized. Current position is defined. Element at current position is not last in list. |
| Postcondition | Current position is updated to next position. item is a copy of element at current position. |

unsortedtype.h

```
#ifndef UNSORTEDTYPE_H_INCLUDED
#define UNSORTEDTYPE_H_INCLUDED

const int MAX_ITEMS = 5;

template <class ItemType>
class UnsortedType
{
    public :
        UnsortedType();
        void MakeEmpty();
        bool IsFull();
        int LengthIs();
        void InsertItem(ItemType);
        void DeleteItem(ItemType);
        void RetrieveItem(ItemType&, bool&);
        void ResetList();
        void GetNextItem(ItemType&);
    private:
        int length;
        ItemType info[MAX_ITEMS];
        int currentPos;
};

#endif // UNSORTEDTYPE_H_INCLUDED
```

sortedtype.h

```
#ifndef SORTEDTYPE_H_INCLUDED
#define SORTEDTYPE_H_INCLUDED

const int MAX_ITEMS = 5;

template <class ItemType>
class SortedType
{
    public :
        SortedType();
        void MakeEmpty();
        bool IsFull();
        int LengthIs();
        void InsertItem(ItemType);
        void DeleteItem(ItemType);
        void RetrieveItem(ItemType&, bool&);
        void ResetList();
        void GetNextItem(ItemType&);
    private:
        int length;
        ItemType info[MAX_ITEMS];
        int currentPos;
};

#endif // SORTEDTYPE_H_INCLUDED
```

unsortedtype.cpp

```
#include "unsortedType.h"

template <class ItemType>

UnsortedType<ItemType>::UnsortedType()
{
    length = 0;
    currentPos = -1;
}

template <class ItemType>

void UnsortedType<ItemType>::MakeEmpty()
{
    length = 0;
}

template <class ItemType>

bool UnsortedType<ItemType>::IsFull()
{
    return (length == MAX_ITEMS);
}
```

```
template <class ItemType>

int UnsortedType<ItemType>::LengthIs()
{
    return length;
}

template <class ItemType>

void UnsortedType<ItemType>::ResetList()
{
    currentPos = -1;
}

template <class ItemType>

void UnsortedType<ItemType>::GetNextItem(ItemType&
item)
{
    currentPos++;

    item = info [currentPos] ;
}
```

unsortedtype.cpp

```
#include "unsortedType.h"

template <class ItemType>
UnsortedType<ItemType>::UnsortedType()
{
    length = 0;
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O(1)

O(1)

O(1)

```
template <class ItemType>
int UnsortedType<ItemType>::LengthIs()
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    currentPos++;
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O(1)

O(1)

sortedtype.cpp

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#include "sortedtype.h"

template <class ItemType>
SortedType<ItemType>::SortedType()
{
    length = 0;
    currentPos = -1;
}

template <class ItemType>
void SortedType<ItemType>::MakeEmpty()
{
    length = 0;
}

template <class ItemType>
bool SortedType<ItemType>::IsFull()
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    return (length == MAX_ITEMS);
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```
template <class ItemType>
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template <class ItemType>
void SortedType<ItemType>::ResetList()
{
    currentPos = -1;
}

template <class ItemType>
void SortedType<ItemType>::GetNextItem(ItemType&
item)
{
    currentPos++;
    item = info [currentPos];
}
```


sortedtype.cpp

```
#include "sortedtype.h"

template <class ItemType>
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    currentPos = -1;
}

template <class ItemType>
void SortedType<ItemType>::MakeEmpty()
{
    length = 0;
}

template <class ItemType>
bool SortedType<ItemType>::IsFull()
{
    return (length == MAX_ITEMS);
}
```

O(1)

O(1)

O(1)

```
template <class ItemType>
int SortedType<ItemType>::LengthIs()
{
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template <class ItemType>
void SortedType<ItemType>::ResetList()
{
    currentPos = -1;
}

template <class ItemType>
void SortedType<ItemType>::GetNextItem(ItemType&
item)
{
    currentPos++;
    item = info [currentPos];
}
```

O(1)

O(1)

O(1)

Inserting an Item into Unsorted List

| | |
|-----------------|---|
| [0] | 6 |
| [1] | 3 |
| [2] | 4 |
| [3] | 1 |
| [4] | 2 |
| . | |
| . | |
| . | |
| . | |
| [MAX_ITEMS - 1] | |

length = 5

Logical
garbage

| | |
|-----------------|---|
| [0] | 6 |
| [1] | 3 |
| [2] | 4 |
| [3] | 1 |
| [4] | 2 |
| [5] | 5 |
| . | |
| . | |
| . | |
| [MAX_ITEMS - 1] | |

length = 6

Logical
garbage

Insert 5

unsortedtype.cpp

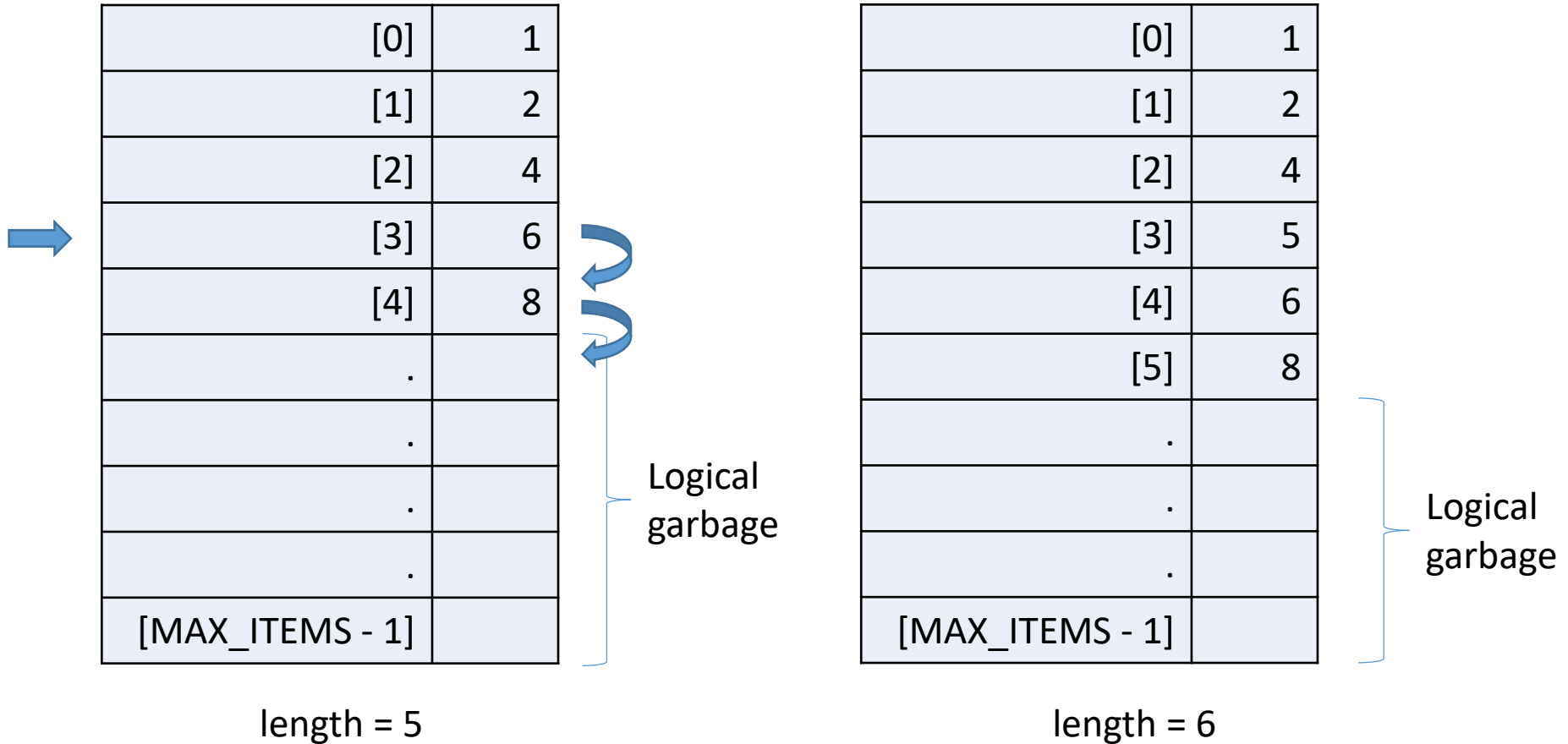
```
template <class ItemType>
void UnsortedType<ItemType>::InsertItem(ItemType item)
{
    info[length] = item;
    length++;
}
```

unsortedtype.cpp

```
template <class ItemType>
void UnsortedType<ItemType>::InsertItem(ItemType item)
{
    info[length] = item;
    length++;
}
```

O(1)

Inserting an Item into Sorted List



Insert 5

sortedtype.cpp

```
template <class ItemType>
void SortedType<ItemType>::InsertItem(ItemType item)
{
    int location = 0;
    bool moreToSearch = (location < length);

    while (moreToSearch)
    {
        if(item > info[location])
        {
            location++;
            moreToSearch = (location < length);
        }
        else if(item < info[location])
            moreToSearch = false;
    }
    for (int index = length; index > location; index--)
        info[index] = info[index - 1];
    info[location] = item;
    length++;
}
```

sortedtype.cpp

```
template <class ItemType>
void SortedType<ItemType>::InsertItem(ItemType item)
{
    int location = 0;
    bool moreToSearch = (location < length);

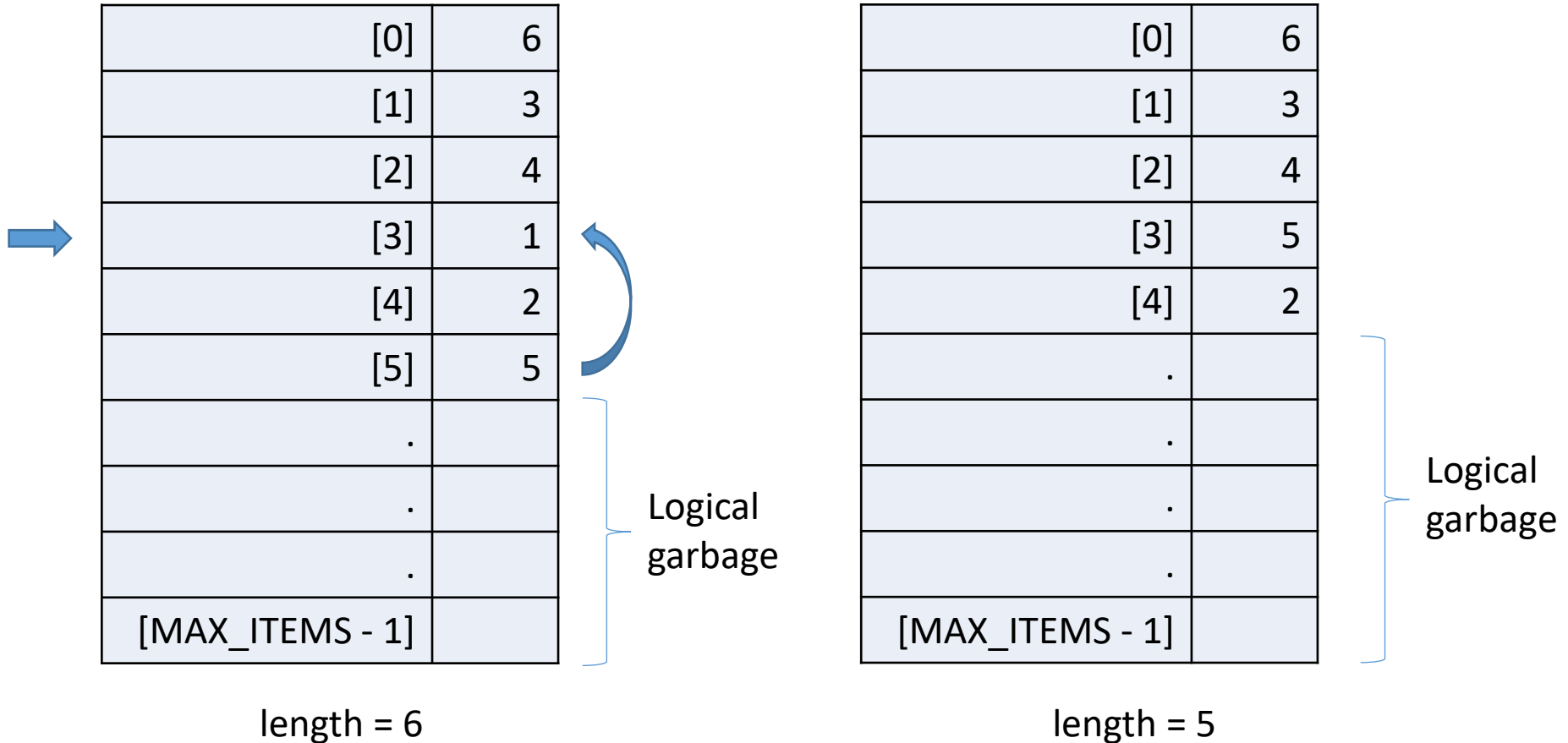
    while (moreToSearch)
    {
        if(item > info[location])
        {
            location++;
            moreToSearch = (location < length);
        }
        else if(item < info[location])
            moreToSearch = false;
    }
    for (int index = length; index > location; index--)
        info[index] = info[index - 1];
    info[location] = item;
    length++;
}
```

$O(N)$

$O(N)$

$O(N)$

Deleting an Item from Unsorted List



Delete 1

unsortedtype.cpp

```
template <class ItemType>
void UnsortedType<ItemType>::DeleteItem(ItemType item)
{
    int location = 0;
    while (item != info[location])
        location++;
    info[location] = info[length - 1];
    length--;
}
```

unsortedtype.cpp

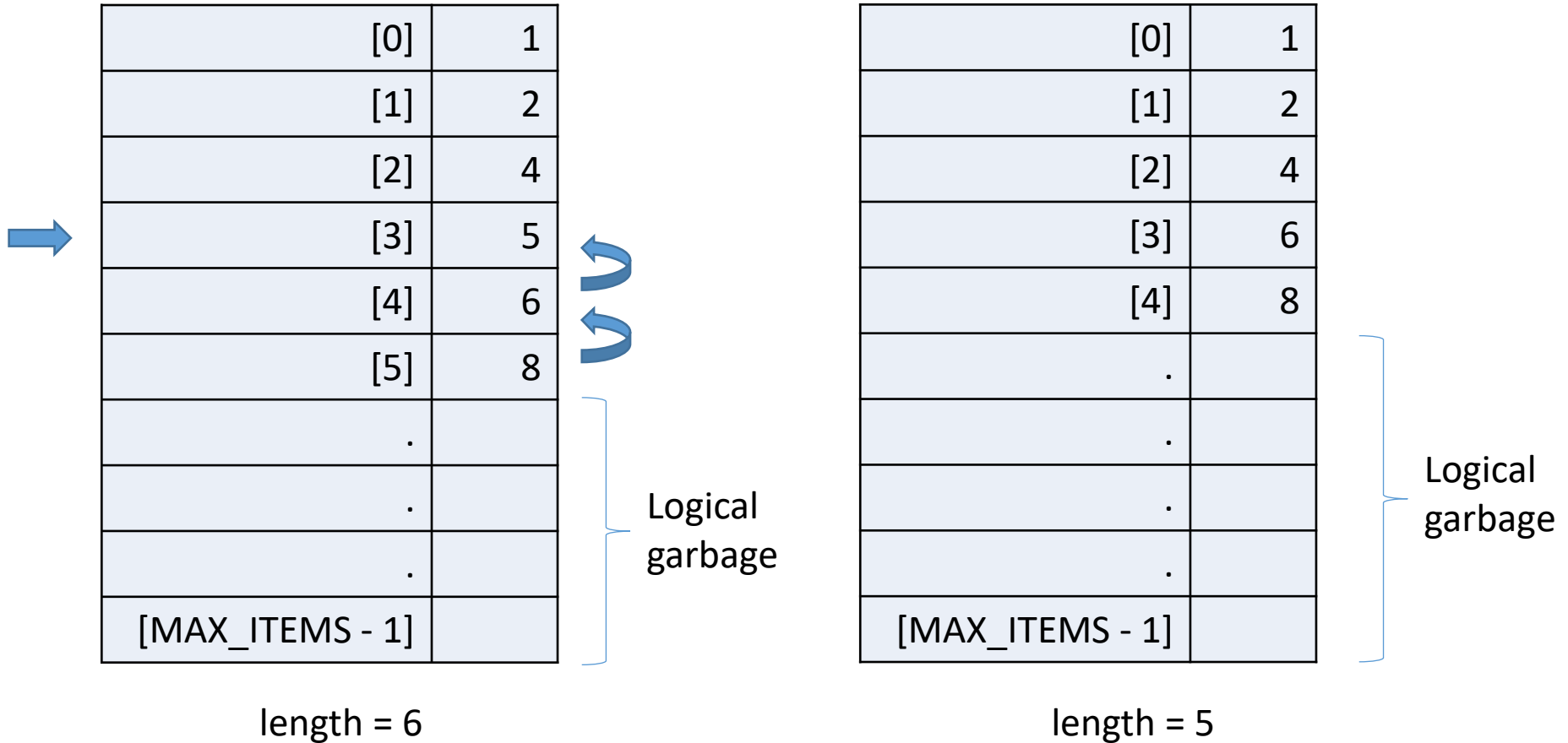
```
template <class ItemType>
void UnsortedType<ItemType>::DeleteItem(ItemType item)
{
    int location = 0;
    while (item != info[location])
        location++;
    info[location] = info[length - 1];
    length--;
}
```

$O(N)$

$O(1)$

$O(N)$

Deleting an Item from Sorted List



Delete 5

sortedtype.cpp

```
template <class ItemType>
void SortedType<ItemType>::DeleteItem(ItemType item)
{
    int location = 0;

    while (item != info[location])
        location++;
    for (int index = location + 1; index < length; index++)
        info[index - 1] = info[index];
    length--;
}
```

sortedtype.cpp

```
template <class ItemType>
void SortedType<ItemType>::DeleteItem(ItemType item)
{
    int location = 0;

    while (item != info[location])
        location++;
    for (int index = location + 1; index < length; index++)
        info[index - 1] = info[index];
    length--;
}
```

$O(N)$
 $O(N)$ } **$O(N)$**

Retrieving an Item from Unsorted List

- Visit each element in the list, one by one, until the item is found.

unsortedtype.cpp

```
template <class ItemType>
void UnsortedType<ItemType>::RetrieveItem(ItemType& item, bool &found)
{
    int location = 0;
    bool moreToSearch = (location < length);
    found = false;
    while (moreToSearch && !found)
    {
        if(item == info[location])
        {
            found = true;
            item = info[location];
        }
        else
        {
            location++;
            moreToSearch = (location < length);
        }
    }
}
```

unsortedtype.cpp

```
template <class ItemType>
void UnsortedType<ItemType>::RetrieveItem(ItemType& item, bool &found)
{
    int location = 0;
    bool moreToSearch = (location < length);
    found = false;
    while (moreToSearch && !found)
    {
        if(item == info[location])
        {
            found = true;
            item = info[location];
        }
        else
        {
            location++;
            moreToSearch = (location < length);
        }
    }
}
```

$O(N)$

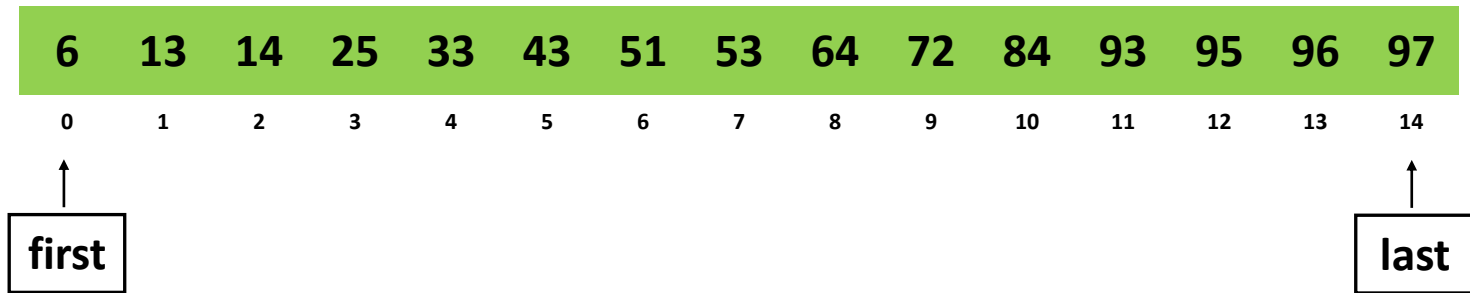
Retrieving an Item from Sorted List

- Find **84**

| | | | | | | | | | | | | | | |
|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 6 | 13 | 14 | 25 | 33 | 43 | 51 | 53 | 64 | 72 | 84 | 93 | 95 | 96 | 97 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |

Retrieving an Item from Sorted List

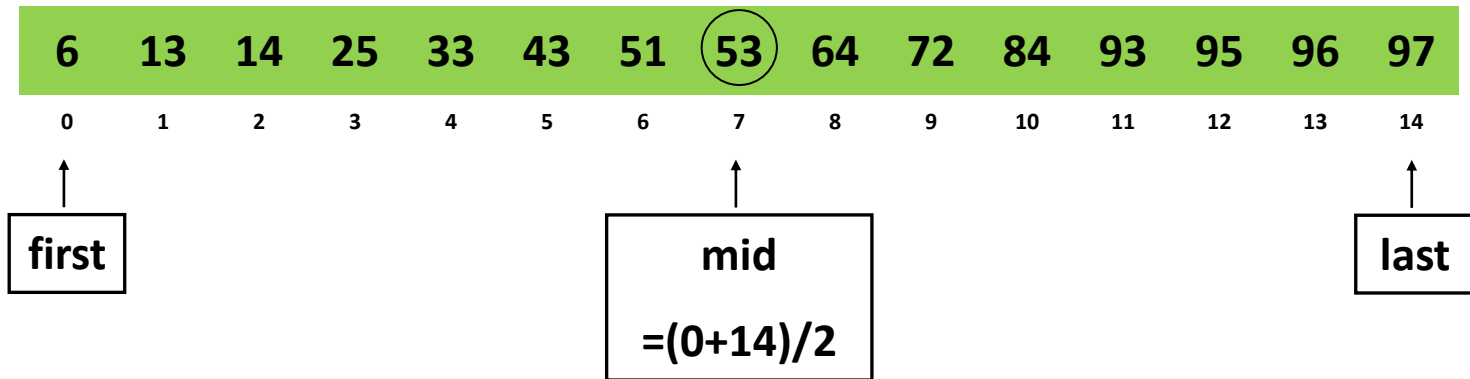
- Find **84**



- Step 1

Retrieving an Item from Sorted List

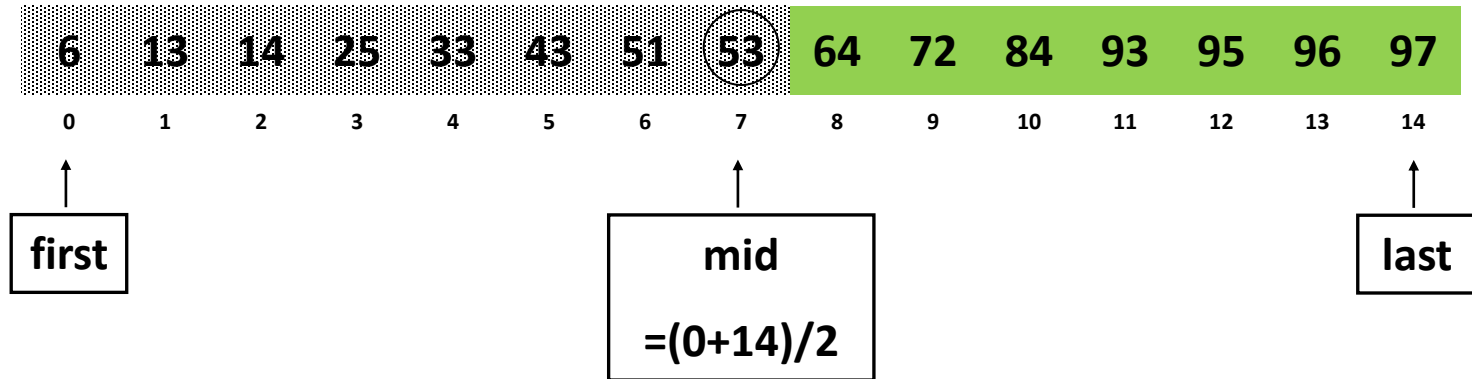
- Find **84**



- Step 1

Retrieving an Item from Sorted List

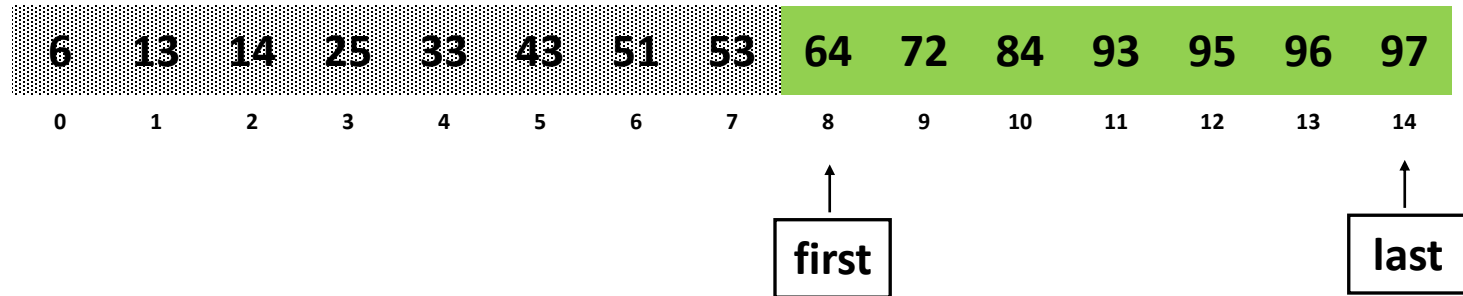
- Find **84**



- Step 1

Retrieving an Item from Sorted List

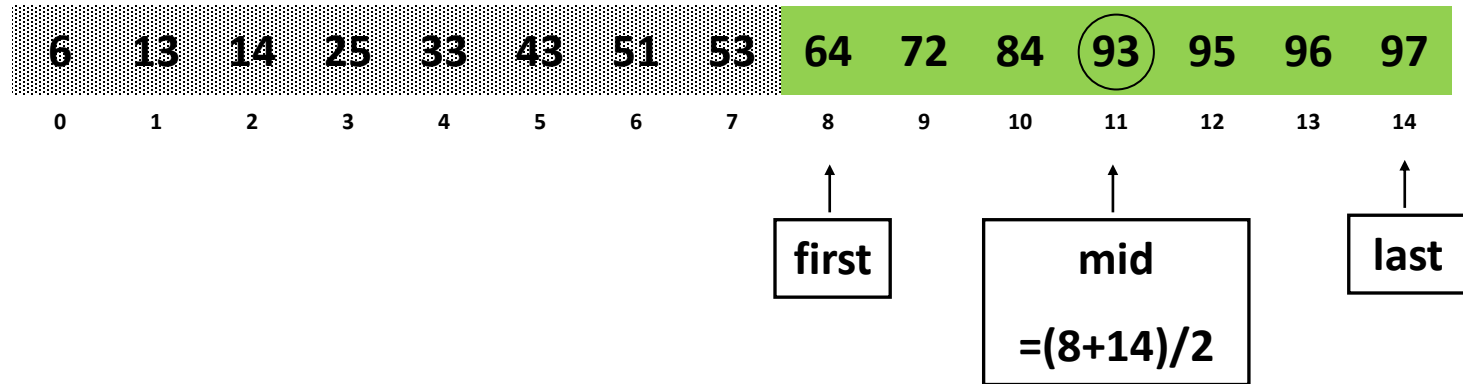
- Find **84**



- Step 2

Retrieving an Item from Sorted List

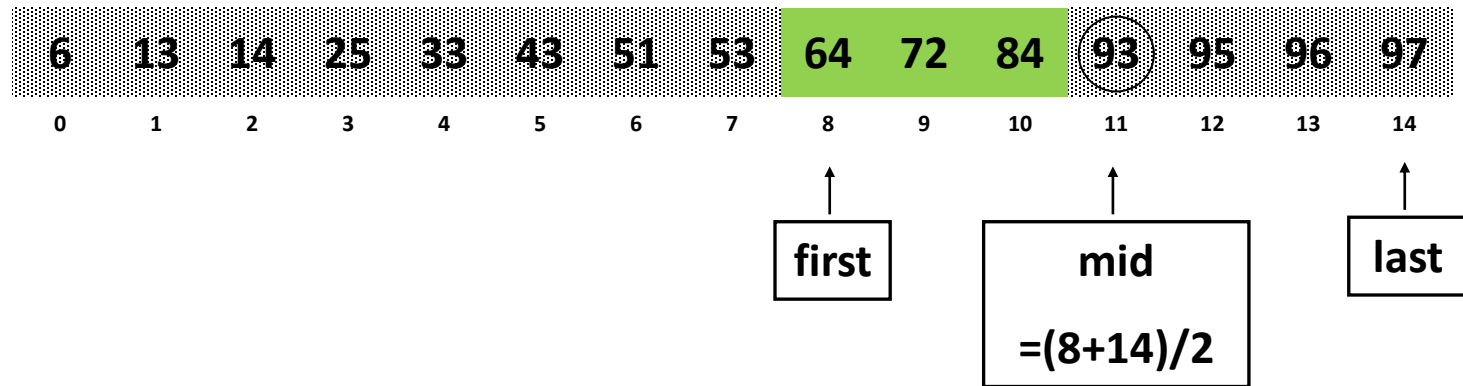
- Find **84**



- Step 2

Retrieving an Item from Sorted List

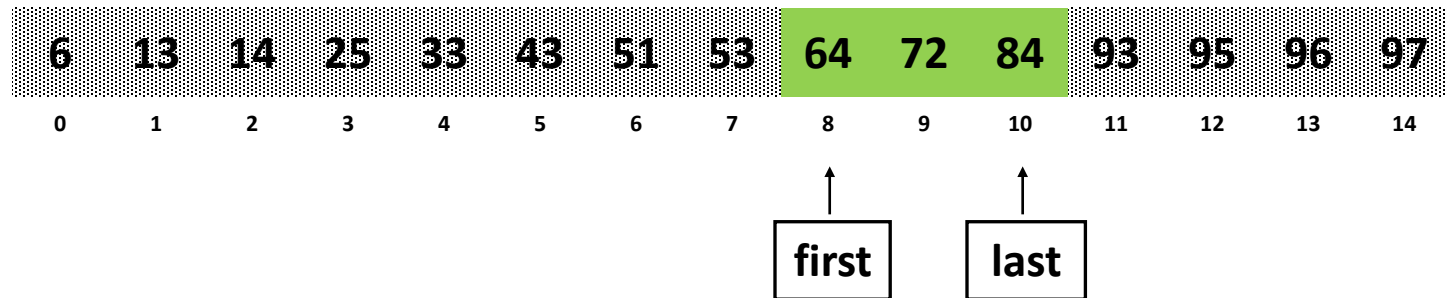
- Find **84**



- Step 2

Retrieving an Item from Sorted List

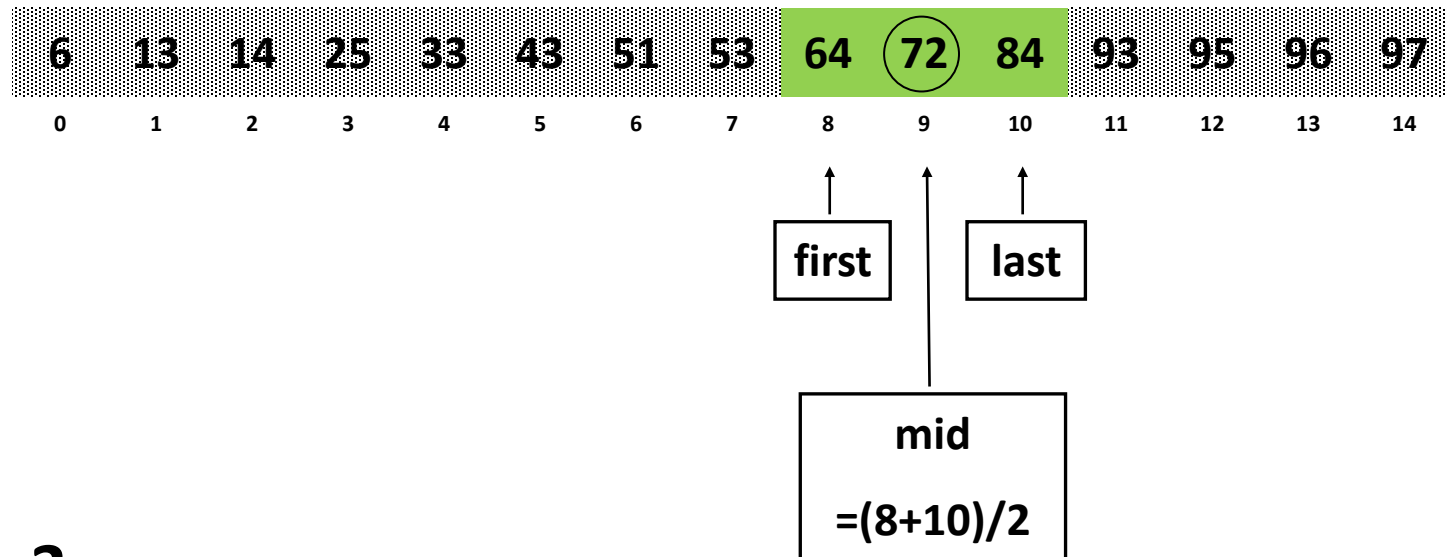
- Find **84**



- Step 3

Retrieving an Item from Sorted List

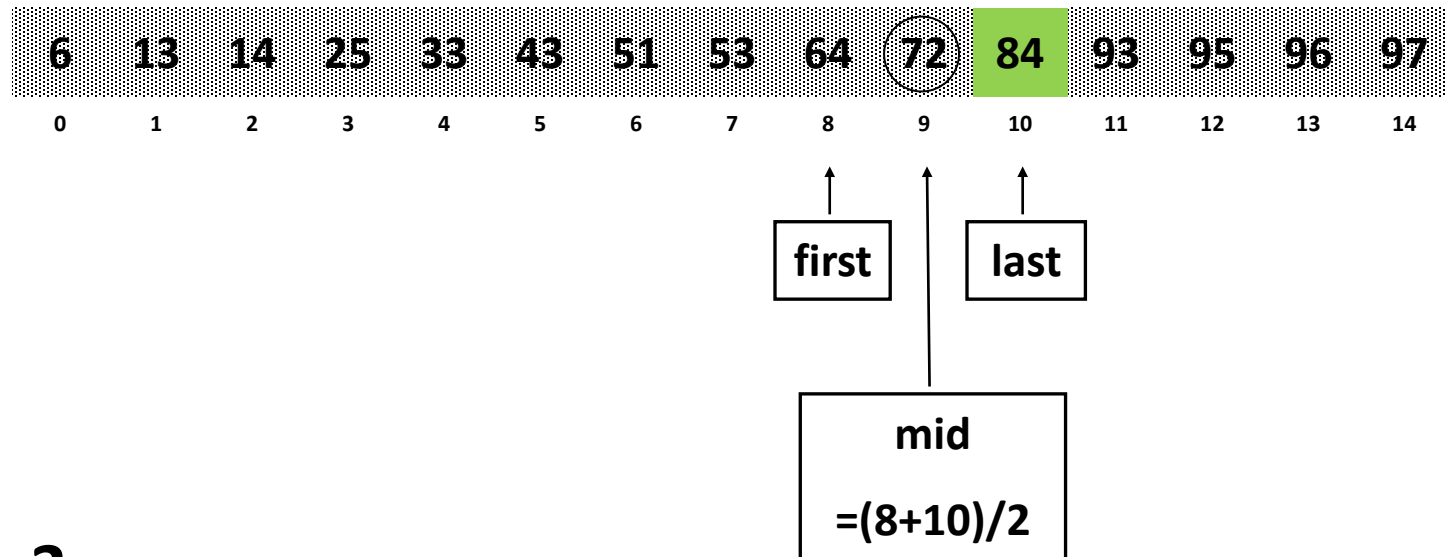
- Find **84**



- Step 3

Retrieving an Item from Sorted List

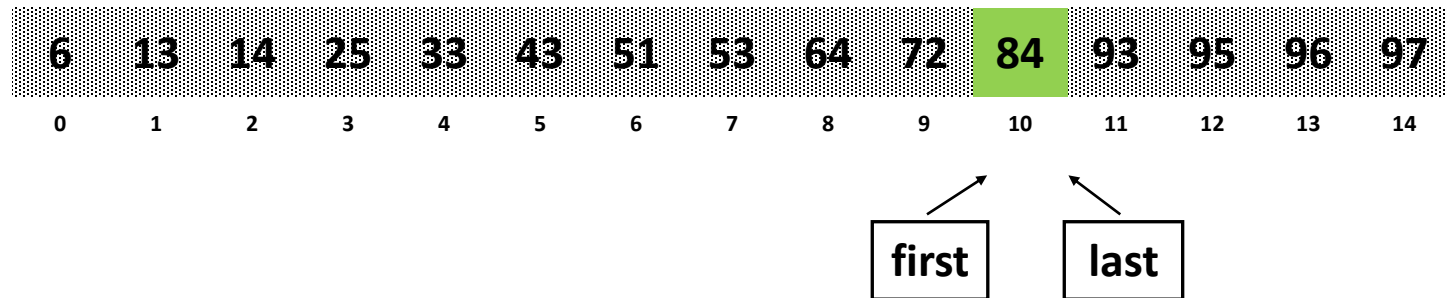
- Find **84**



- Step 3

Retrieving an Item from Sorted List

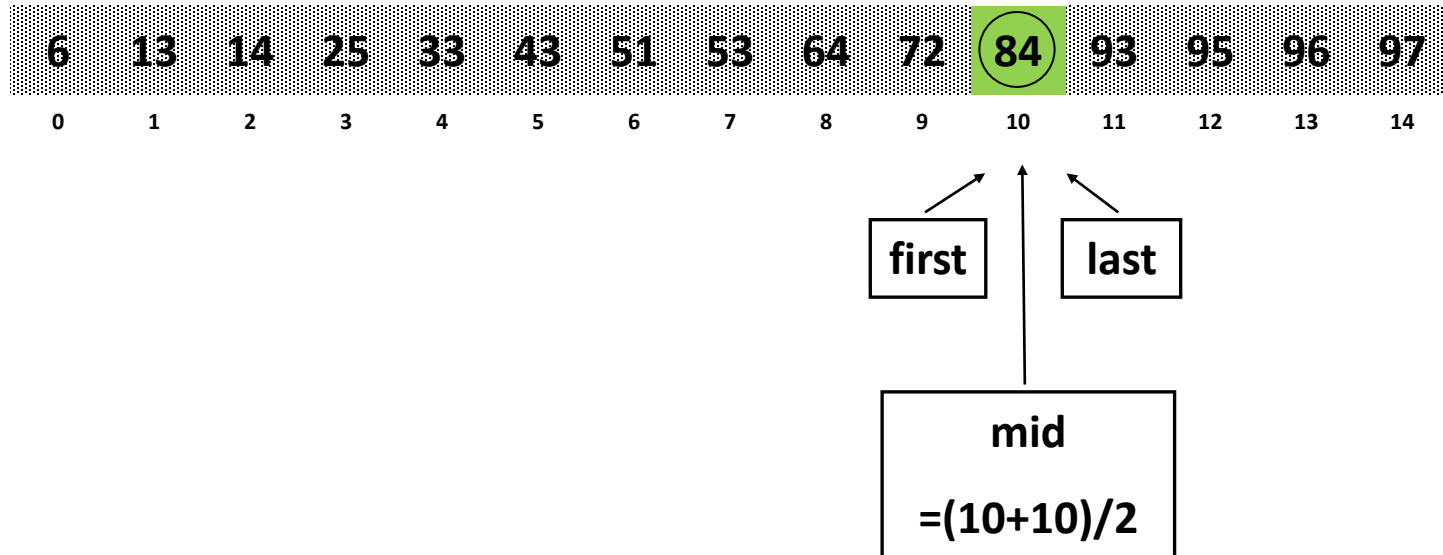
- Find **84**



- Step 4

Retrieving an Item from Sorted List

- Find **84**



- Step 4
- **84 found at the midpoint**

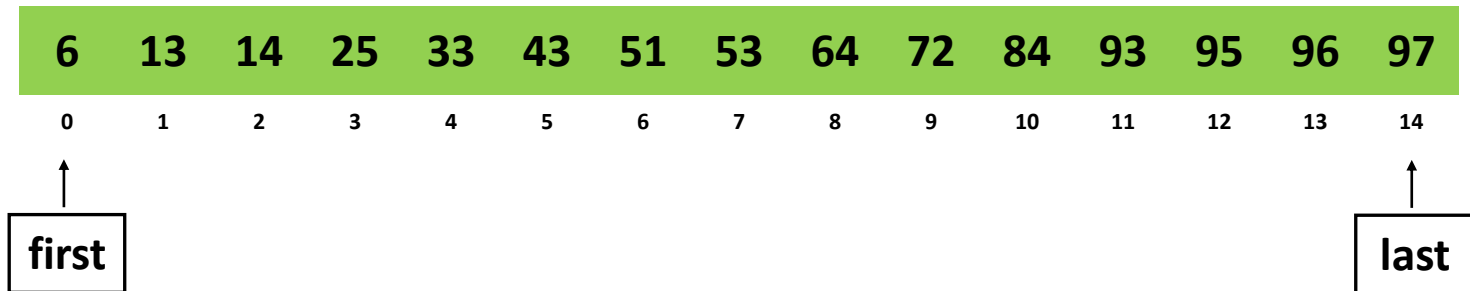
Retrieving an Item from Sorted List

- Find **73**

| | | | | | | | | | | | | | | |
|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 6 | 13 | 14 | 25 | 33 | 43 | 51 | 53 | 64 | 72 | 84 | 93 | 95 | 96 | 97 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |

Retrieving an Item from Sorted List

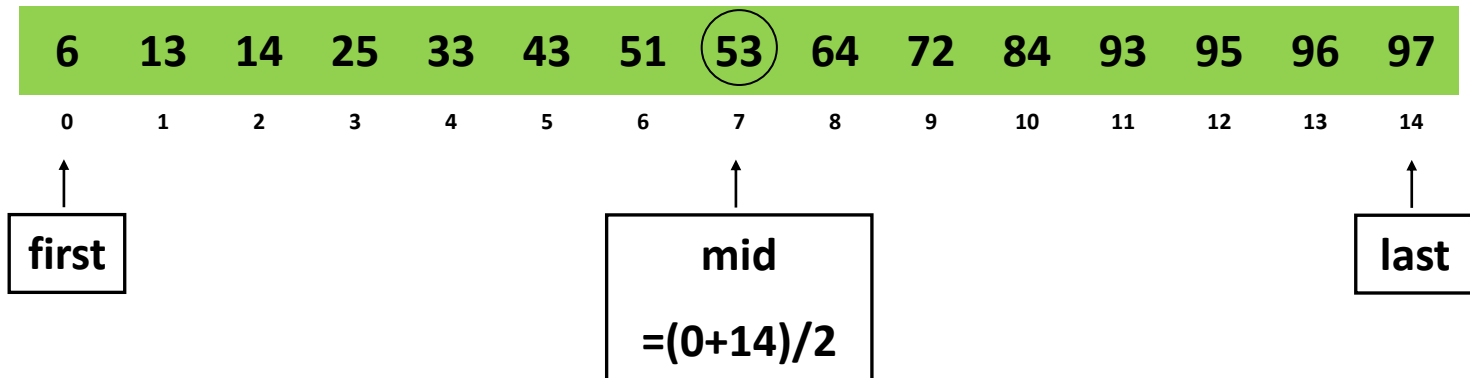
- Find **73**



- Step 1

Retrieving an Item from Sorted List

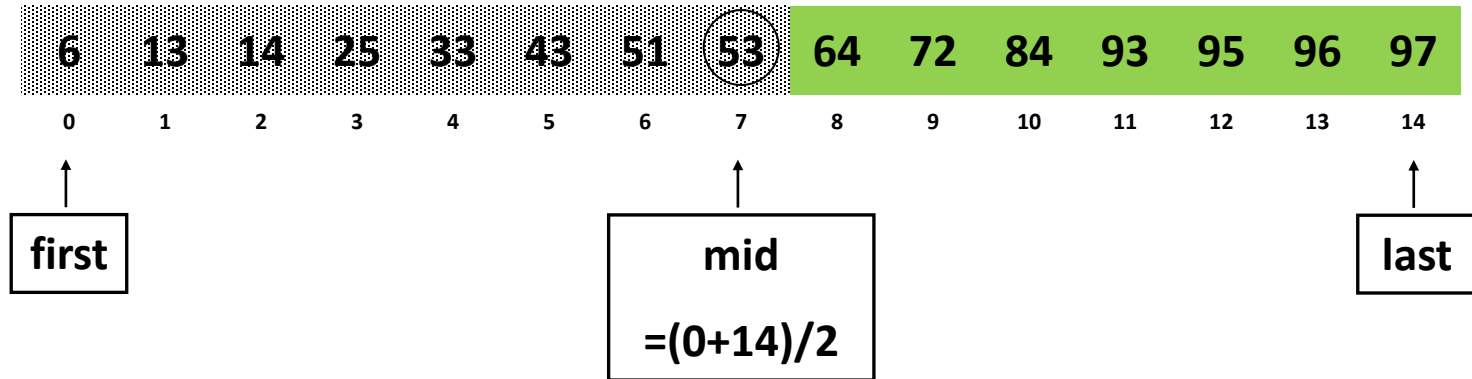
- Find **73**



- Step 1

Retrieving an Item from Sorted List

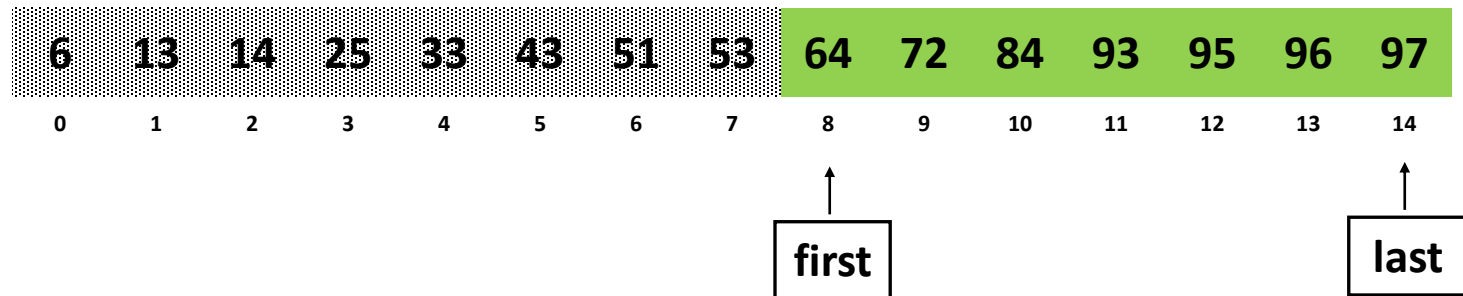
- Find **73**



- Step 1

Retrieving an Item from Sorted List

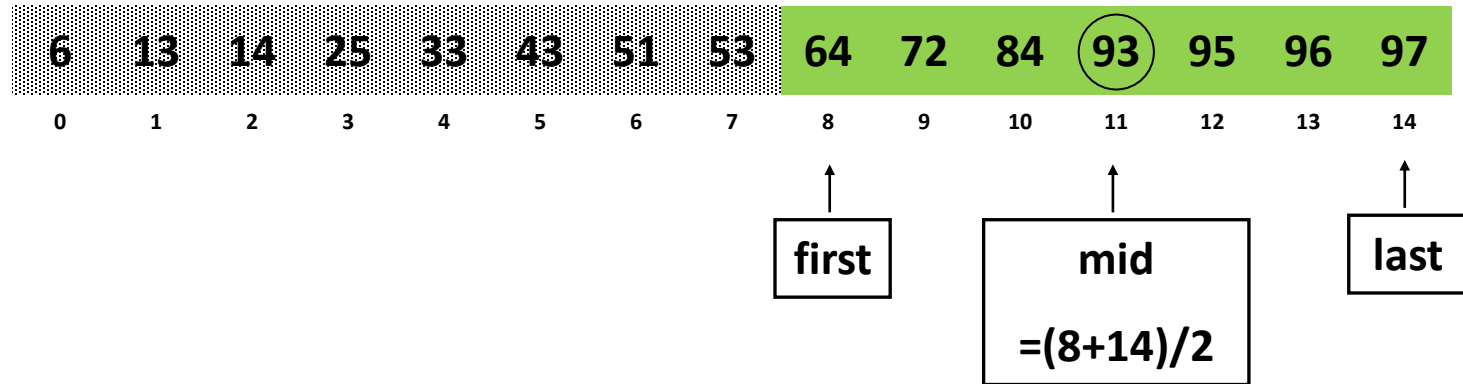
- Find **73**



- Step 2

Retrieving an Item from Sorted List

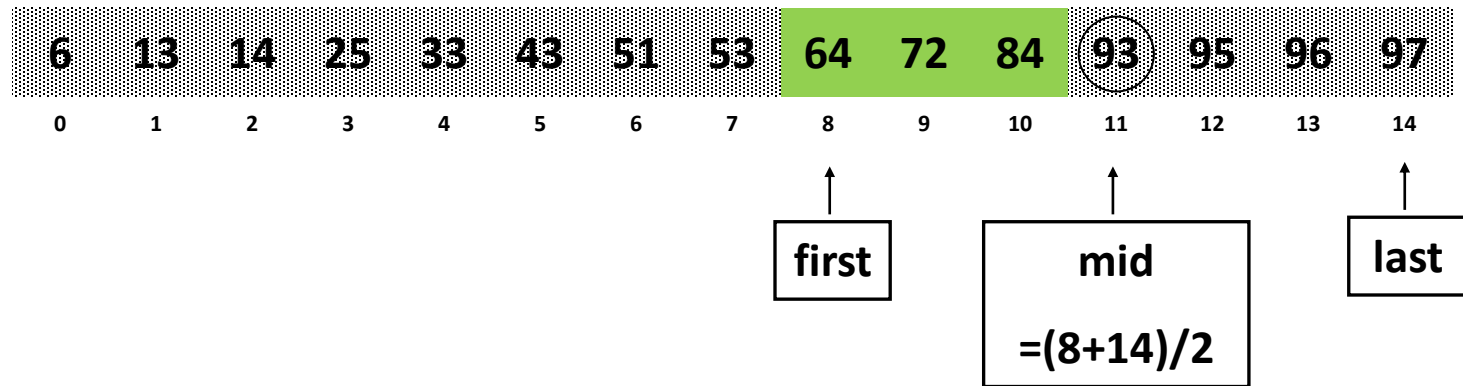
- Find **73**



- Step 2

Retrieving an Item from Sorted List

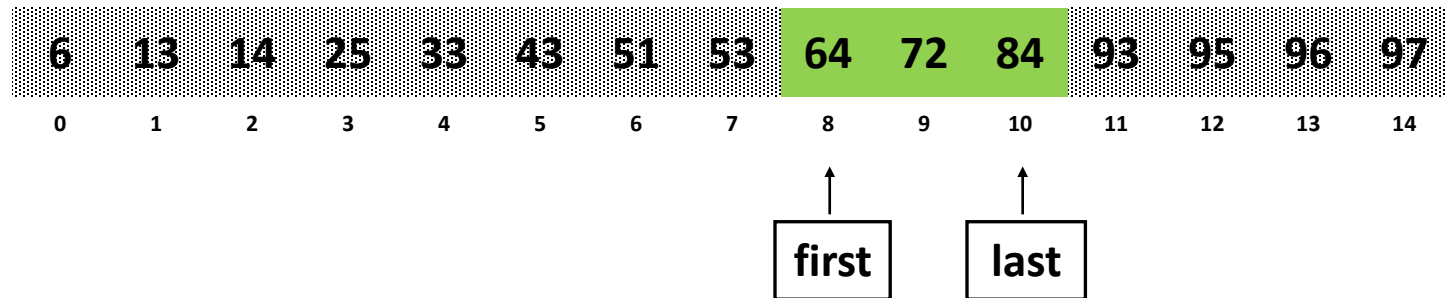
- Find **73**



- Step 2

Retrieving an Item from Sorted List

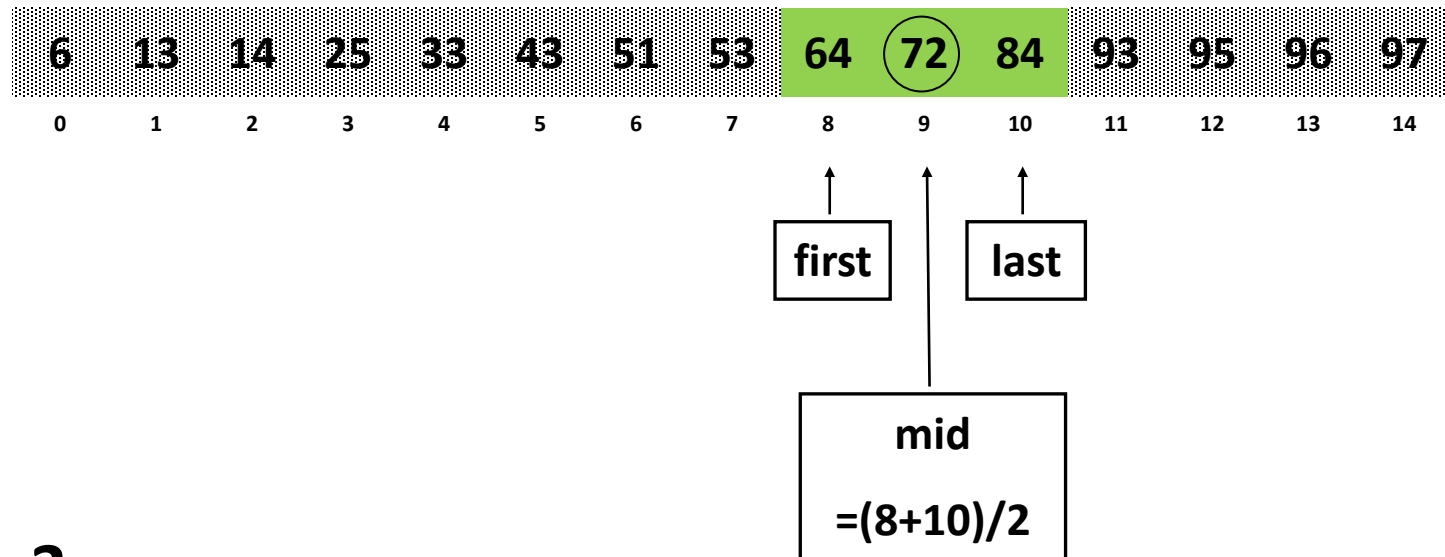
- Find **73**



- Step 3

Retrieving an Item from Sorted List

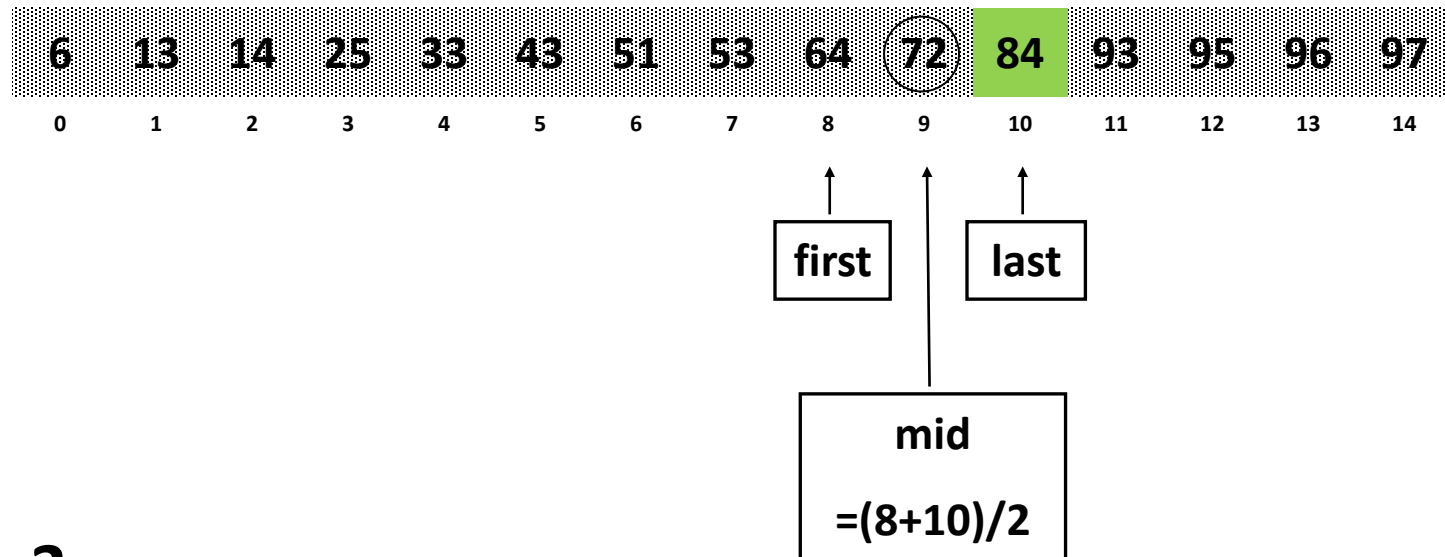
- Find **73**



- Step 3

Retrieving an Item from Sorted List

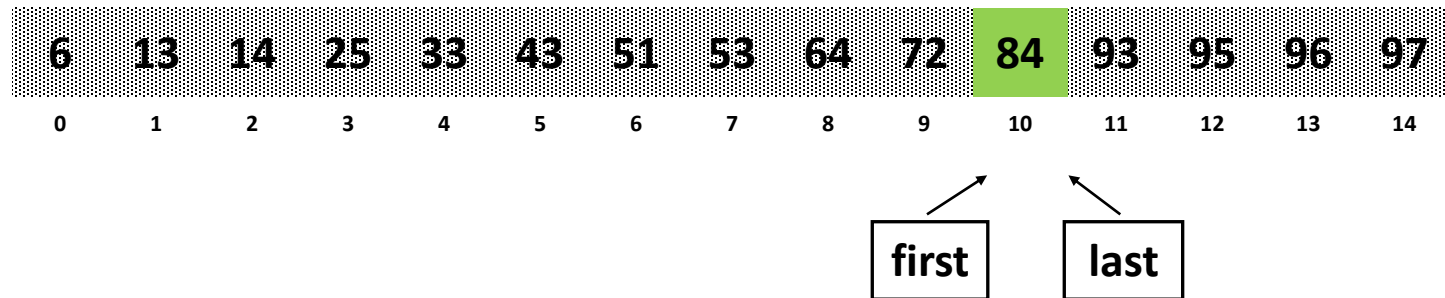
- Find **73**



- Step 3

Retrieving an Item from Sorted List

- Find **73**

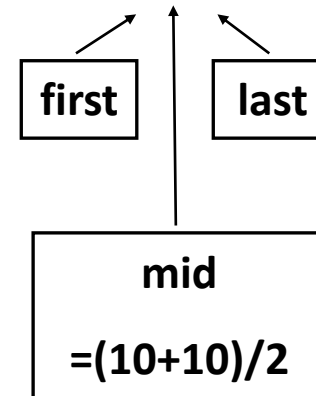


- Step 4

Retrieving an Item from Sorted List

- Find **73**

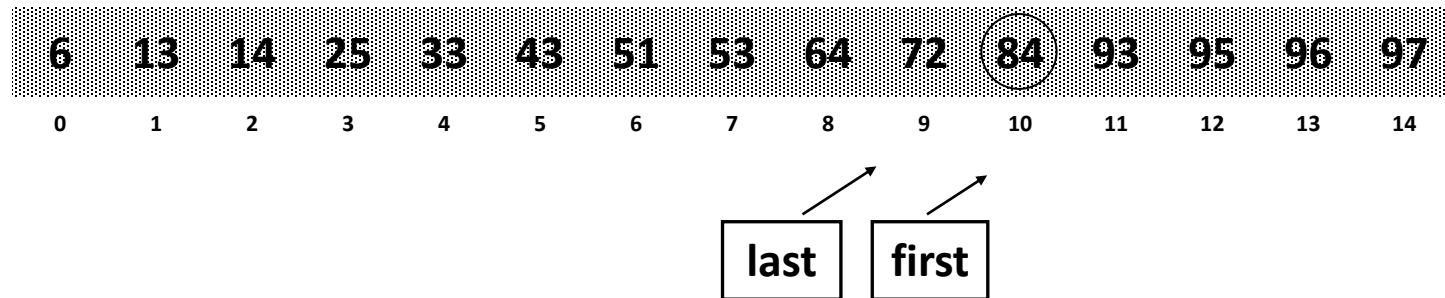
| | | | | | | | | | | | | | | |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 6 | 13 | 14 | 25 | 33 | 43 | 51 | 53 | 64 | 72 | 84 | 93 | 95 | 96 | 97 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |



- Step 4

Retrieving an Item from Sorted List

- Find **73**



- Step 5

- **last < first (indicates the absence of the item)**

Retrieving an Item from Sorted List

- What is the number of steps required?

| Array size | expressed as 2^a |
|------------|--------------------|
| N | $2^{(x)}$ |
| N/2 | $2^{(x-1)}$ |
| N/4 | $2^{(x-2)}$ |
| N/8 | $2^{(x-3)}$ |
| . | . |
| . | . |
| . | . |
| . | . |
| 4 | 2^2 |
| 2 | 2^1 |
| 1 | 2^0 |

Retrieving an Item from Sorted List

- What is the number of steps required?

| Array size | expressed as 2^a |
|------------|--------------------|
| N | $2^{(x)}$ |
| N/2 | $2^{(x-1)}$ |
| N/4 | $2^{(x-2)}$ |
| N/8 | $2^{(x-3)}$ |
| . | . |
| . | . |
| . | . |
| . | . |
| 4 | 2^2 |
| 2 | 2^1 |
| 1 | 2^0 |

$$2^x \sim N$$

Or,

$$x = \log_2 N$$

Or simply,

$$x = \log N$$

sortedtype.cpp

```
template <class ItemType>
void SortedType<ItemType>::RetrieveItem(ItemType& item, bool& found)
{
    int midPoint, first = 0, last = length - 1;
    bool moreToSearch = (first <= last);
    found = false;
    while (moreToSearch && !found)
    {
        midPoint = (first + last) / 2;
        if(item < info[midPoint])
        {
            last = midPoint - 1;
            moreToSearch = (first <= last);
        }
        else if(item > info[midPoint])
        {
            first = midPoint + 1;
            moreToSearch = (first <= last);
        }
        else
        {
            found = true;
            item = info[midPoint];
        }
    }
}
```

sortedtype.cpp

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        else if(item > info[midPoint])
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            first = midPoint + 1;
            moreToSearch = (first <= last);
        }
        else
        {
            found = true;
            item = info[midPoint];
        }
    }
}
```

$O(\log N)$