$$\hat{w}_t^*$$