

## Additional Errata and Addenda

- \* p. 74, Exercise 5.8(a). The stated formula for  $T(n, k)$  fails for  $n = 0$ . Also, it makes more sense to define  $T(0, 0) = 1$ .
- \* p. 81, Exercise 5.24(d). A solution was found by the Cambridge Combinatorics and Coffee Club (February 2000).
- \* p. 124, Exercise 5.28. A bijective proof based on Prüfer codes is due to the Cambridge Combinatorics and Coffee Club (December 1999).
- \* p. 124, Exercise 5.29(b). Update the Pitman reference to *J. Combinatorial Theory (A)* **85** (1999), 165–193. Further results on  $P_n$  and related posets are given by D. N. Kozlov, *J. Combinatorial Theory (A)* **88** (1999), 112–122.
- \* p. 136, last line of Exercise 5.41(j). A solution different from the one above was given by S. C. Locke, *Amer. Math. Monthly* **106** (1999), 168.
- \* p. 143, Exercise 5.50(c). The paper of Postnikov and Stanley has appeared in *J. Combinatorial Theory (A)* **91** (2000), 544–597.
- \* p. 144, Exercise 5.5.3. The identity

$$4^n = \sum_{j=0}^n 2^{n-j} \binom{n+j}{j} \quad (1)$$

follows immediately from “Banach’s match box problem,” an account of which appears for instance in W. Feller, *An Introduction to Probability Theory and Its Applications*, vol. 1, second ed., Wiley, New York, 1957 (§5.8). This yields a simple bijective proof of (1).

- \* p. 151, Exercise 5.62 (b). David Callan observed (private communication) that there is a very simple combinatorial proof. Any matrix of the type being enumerated can be written *uniquely* in the form  $P + 2Q$ , where  $P$  and  $Q$  are permutation matrices. Conversely  $P + 2Q$  is always of the type being enumerated, whence  $f_3(n) = n!^2$ .

- \* p. 212. For further details on the history of Catalan numbers, see P. J. Larcombe and P. D. C. Wilson, *Mathematics Today* **34** (1998), 114–117; P. J. Larcombe, *Mathematics Today* **35** (1999), 25, 89; and P. J. Larcombe, *Math. Spectrum* **32** (1999/2000), 5–7.
- \* p. 217, Exercise 6.2(a). It needs to be assumed that  $F(0) = 0$ ; otherwise e.g.  $F(x) = 1/2$  is a trivial counterexample.
- \* p. 231, Exercise 6.25 (i). This conjecture has been proved by M. Haiman, A geometric proof of the  $n!$  and Macdonald positivity conjectures, preprint available electronically at <http://math.ucsd.edu/~mhaiman>.
- \* p. 232, Exercise 6.27(c). Robin Chapman has found an elegant argument that there always exists an integral orthonormal basis.
- \* p. 250, Exercise 6.4. A complete description of a field of generalized power series that forms an algebraic closure of  $\mathbb{F}_p[[x]]$  is given by K. S. Kedlaya, The algebraic closure of the power series field in positive characteristic, *Proc. Amer. Math. Soc.*, to appear.
- \* pp. 261–262, Exercise 3.19(pp). A further reference on noncrossing partitions is the nice survey article R. Simion, *Discrete Math.* **217** (2000), 367–409.
- \* p. 264, Exercise 6.19(iii). It should be mentioned that the diagonals of the frieze patterns of Exercise 6.19(mmm) are precisely the sequences  $1a_1a_2 \cdots a_n1$  of the present exercise.
- \* p. 265, Exercise 6.19(III), lines 3– to 2–. The paper of Postnikov and Stanley has appeared in *J. Combinatorial Theory (A)* **91** (2000), 544–597.
- \* p. 265, Exercise 6.19(mmm). A couple of additional references to frieze patterns are H. S. M. Coxeter, *Acta Arith.* **18** (1971), 297–310, and H. S. M. Coxeter and J. F. Rigby, in *The Lighter Side of Mathematics* (R. K. Guy and R. E. Woodrow, eds.), Mathematical Association of America, Washington, DC, 1994, pp. 15–27.
- \* p. 269, line 1–, to p. 270, line 1. The paper of Postnikov and Stanley has appeared in *J. Combinatorial Theory (A)* **91** (2000), 544–597.
- \* p. 272, end of Exercise 6.33(c). Yet another proof was given by J. H. Przytycki and A. S. Sikora, Polygon dissections and Euler, Fuss, Kirkman and Cayley numbers, preprint available electronically at [math.CO/9811086](http://math.CO/9811086).
- \* p. 279, Exercise 6.56(c). In the paper N. Alon and E. Friedgut, *J. Combinatorial Theory (A)* **89** (2000), 133–140, it is shown that  $A_v(n) < c^n \gamma^*(n)$ , where  $\gamma^*(n)$  is an extremely slow growing function related to the Ackermann hierarchy. The paper is available electronically at <http://www.ma.huji.ac.il/~ehudf>.
- \* p. 291, line 9–. In general it is not true that  $\hat{\Lambda}_R = \hat{\Lambda} \otimes R$ ; one only has a natural surjection from the former onto the latter. Equality will hold if  $R$  is noetherian.

- \* p. 295, Figure 7-3. In the expansion of  $h_{41}$ , the coefficient of  $m_{41}$  should be 2.
- \* p. 399, line 7—. For additional information concerning Craige Schensted, see the webpage [ea.ea.home.mindspring.com](http://ea.ea.home.mindspring.com).
- \* p. 439, reference A1.13. An updated version of this paper of van Leeuwen, entitled “The Littlewood-Richardson rule, and related combinatorics,” is available electronically at [math.CO/9908099](http://math.CO/9908099).
- \* p. 467, Exercise 7.55(b). Let  $f(n)$  be the number of  $\lambda \vdash n$  satisfying (7.177). Then  $(f(1), f(2), \dots, f(30)) = (1, 1, 1, 2, 2, 7, 7, 10, 10, 34, 40, 53, 61, 103, 112, 143, 145, 369, 458, 579, 712, 938, 1127, 1383, 1638, 2308, 2754, 3334, 3925, 5092)$ .
- \* p. 484, Exercise 7.101(b). As in (a), the plane partitions being counted have largest part at most  $m$ .
- \* p. 485, line 7. The five displayed tableaux should be rotated  $180^\circ$ .
- \* p. 504, line 10—. Update the Babson, et al., reference to *Topology* **38** (1999), 271–299.
- \* p. 514, Exercise 7.47(m), lines 1–3. Update the reference to R. Stanley, *Discrete Math.* **193** (1998), 267–286.
- \* p. 515, Exercise 7.48(g). Further generalizations of shuffle posets are considered by P. Hersh, Two generalizations of posets of shuffles, preprint available electronically at <http://www.math.washington.edu/~hersh/papers.html>.
- \* p. 534, end of Exercise 7.74. For some connections between inner plethysm and graphical enumeration, see L. Travis, Ph.D. thesis, Brandeis University, 1999; available electronically at [math.CO/9811127](http://math.CO/9811127).
- \* p. 539, Exercise 7.85. A further reference to the evaluation of  $g_{\lambda\mu\nu}$  is M. H. Rosas, The Kronecker product of Schur functions indexed by two-row shapes or hook shapes, preprint available electronically at [math.CO/0001084](http://math.CO/0001084).
- \* p. 544, lines 4– to 2—. Update the reference to R. Stanley, *Discrete Math.* **193** (1998), 267–286.
- \* p. 542, line 10. Update the Babson, et al., reference to *Topology* **38** (1999), 271–299.
- \* p. 551, Exercise 7.102(b), lines 2– to 1—. The “nice” bijective proof asked for was given by M. Rubey, A nice bijection for a content formula for skew semistandard Young tableaux, preprint. The proof is based on jeu de taquin.
- \* p. 554, last two lines of Exercise 7.107(a). Update reference to *Annals of Combinatorics* **2** (1998), 103–110.