

# **Deep RL Foundations in 6 Lectures**

## **Lecture 5: DDPG and SAC**

Pieter Abbeel

# Lecture Series

---

- Lecture 1: MDPs Foundations and Exact Solution Methods
- Lecture 2: Deep Q-Learning
- Lecture 3: Policy Gradients, Advantage Estimation
- Lecture 4: TRPO, PPO
- **Lecture 5: DDPG, SAC**
- Lecture 6: Model-based RL

# Outline for This Lecture

---

- *Deep Deterministic Policy Gradient (DDPG)*
- Soft Actor Critic (SAC)

# Deep Deterministic Policy Gradient (DDPG)

- for iter = 1, 2, ...

## Roll-outs:

Execute roll-outs under current policy (+some noise for exploration)

## Q function update:

$$g \propto \nabla_{\phi} \sum_t (Q_{\phi}(s_t, u_t) - \hat{Q}(s_t, u_t))^2 \quad \text{with} \quad \hat{Q}(s_t, u_t) = r_t + \gamma Q_{\phi}(s_{t+1}, u_{t+1})$$

## Policy update:

Backprop through Q to compute gradient estimates for all t:

$$g \propto \sum_t \nabla_{\theta} Q_{\phi}(s_t, \pi_{\theta}(s_t, v_t))$$

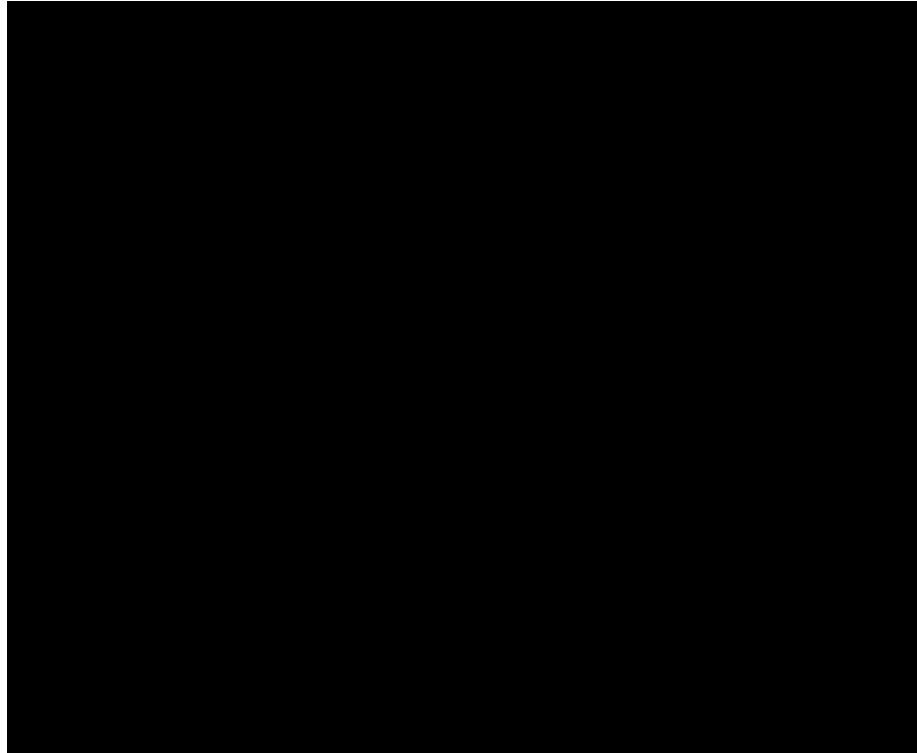
# Deep Deterministic Policy Gradient (DDPG)

- Add noise for exploration
- Incorporate replay buffer and target network ideas from DQN for increased stability
- Use lagged (Polyak-averaging) version of  $Q_\phi$  and  $\pi_\theta$  for target values  $\hat{Q}_t$

$$\hat{Q}_t = r_t + \gamma Q_{\phi'}(s_{t+1}, \pi_{\theta'}(s_{t+1}))$$

# DDPG

---



# DDPG

---

- + very sample efficient thanks to off-policy updates

- often unstable

→ Soft Actor Critic (SAC), which adds entropy of policy to the objective, ensuring better exploration and less overfitting of the policy to any quirks in the Q-function

# Outline for This Lecture

---

- Deep Deterministic Policy Gradient (DDPG)
- ***Soft Actor Critic (SAC)***



# Soft Policy Iteration

## 1. Soft policy evaluation:

Fix policy, apply soft Bellman backup until converges:

$$Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + \mathbb{E}_{\mathbf{s}' \sim p_{\mathbf{s}}, \mathbf{a}' \sim \pi} [Q(\mathbf{s}', \mathbf{a}') - \log \pi(\mathbf{a}' | \mathbf{s}')] ]$$

This converges to  $Q^\pi$ .

## 2. Soft policy improvement:

Update the policy through information projection:

$$\pi_{\text{new}} = \arg \min_{\pi'} D_{\text{KL}} \left( \pi'(\cdot | \mathbf{s}) \parallel \frac{1}{Z} \exp Q^{\pi_{\text{old}}}(\mathbf{s}, \cdot) \right)$$

For the new policy, we have  $Q^{\pi_{\text{new}}} \geq Q^{\pi_{\text{old}}}$ .

## 3. Repeat until convergence

# Soft Actor-Critic

Haarnoja, T., Zhou, A., Abbeel, P., and Levine, S. *Soft Actor-Critic: Off-Policy Maximum Entropy Deep Reinforcement Learning with a Stochastic Actor*. ICML, 2018.

1. Take one stochastic gradient step to minimize soft Bellman residual
2. Take one stochastic gradient step to minimize the KL divergence
3. Execute one action in the environment and repeat

# Soft Actor Critic

- Objective: 
$$J(\pi) = \sum_{t=0}^T \mathbb{E}_{(\mathbf{s}_t, \mathbf{a}_t) \sim \rho_\pi} [r(\mathbf{s}_t, \mathbf{a}_t) + \alpha \mathcal{H}(\pi(\cdot | \mathbf{s}_t))]$$
- Iterate:
  - Perform roll-out from  $\pi$ , add data in replay buffer
  - Learn 
$$J_V(\psi) = \mathbb{E}_{\mathbf{s}_t \sim \mathcal{D}} \left[ \frac{1}{2} \left( V_\psi(\mathbf{s}_t) - \mathbb{E}_{\mathbf{a}_t \sim \pi_\phi} [Q_\theta(\mathbf{s}_t, \mathbf{a}_t) - \log \pi_\phi(\mathbf{a}_t | \mathbf{s}_t)] \right)^2 \right]$$

$$\hat{Q}(\mathbf{s}_t, \mathbf{a}_t) = r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \mathbb{E}_{\mathbf{s}_{t+1} \sim p} [V_{\tilde{\psi}}(\mathbf{s}_{t+1})]$$

$$J_\pi(\phi) = \mathbb{E}_{\mathbf{s}_t \sim \mathcal{D}} \left[ \text{D}_{\text{KL}} \left( \pi_\phi(\cdot | \mathbf{s}_t) \parallel \frac{\exp(Q_\theta(\mathbf{s}_t, \cdot))}{Z_\theta(\mathbf{s}_t)} \right) \right]$$

**Algorithm 1** Soft Actor-Critic

---

```

1: Input: initial policy parameters  $\theta$ , Q-function parameters  $\phi_1, \phi_2$ , empty replay buffer  $\mathcal{D}$ 
2: Set target parameters equal to main parameters  $\phi_{\text{targ},1} \leftarrow \phi_1, \phi_{\text{targ},2} \leftarrow \phi_2$ 
3: repeat
4:   Observe state  $s$  and select action  $a \sim \pi_\theta(\cdot|s)$ 
5:   Execute  $a$  in the environment
6:   Observe next state  $s'$ , reward  $r$ , and done signal  $d$  to indicate whether  $s'$  is terminal
7:   Store  $(s, a, r, s', d)$  in replay buffer  $\mathcal{D}$ 
8:   If  $s'$  is terminal, reset environment state.
9:   if it's time to update then
10:    for  $j$  in range(however many updates) do
11:      Randomly sample a batch of transitions,  $B = \{(s, a, r, s', d)\}$  from  $\mathcal{D}$ 
12:      Compute targets for the Q functions:

```

$$y(r, s', d) = r + \gamma(1 - d) \left( \min_{i=1,2} Q_{\phi_{\text{targ},i}}(s', \tilde{a}') - \alpha \log \pi_\theta(\tilde{a}'|s') \right), \quad \tilde{a}' \sim \pi_\theta(\cdot|s')$$

```

13:    Update Q-functions by one step of gradient descent using

```

$$\nabla_{\phi_i} \frac{1}{|B|} \sum_{(s,a,r,s',d) \in B} (Q_{\phi_i}(s, a) - y(r, s', d))^2 \quad \text{for } i = 1, 2$$

```

14:    Update policy by one step of gradient ascent using

```

$$\nabla_\theta \frac{1}{|B|} \sum_{s \in B} \left( \min_{i=1,2} Q_{\phi_i}(s, \tilde{a}_\theta(s)) - \alpha \log \pi_\theta(\tilde{a}_\theta(s)|s) \right),$$

where  $\tilde{a}_\theta(s)$  is a sample from  $\pi_\theta(\cdot|s)$  which is differentiable wrt  $\theta$  via the reparametrization trick.

```

15:    Update target networks with

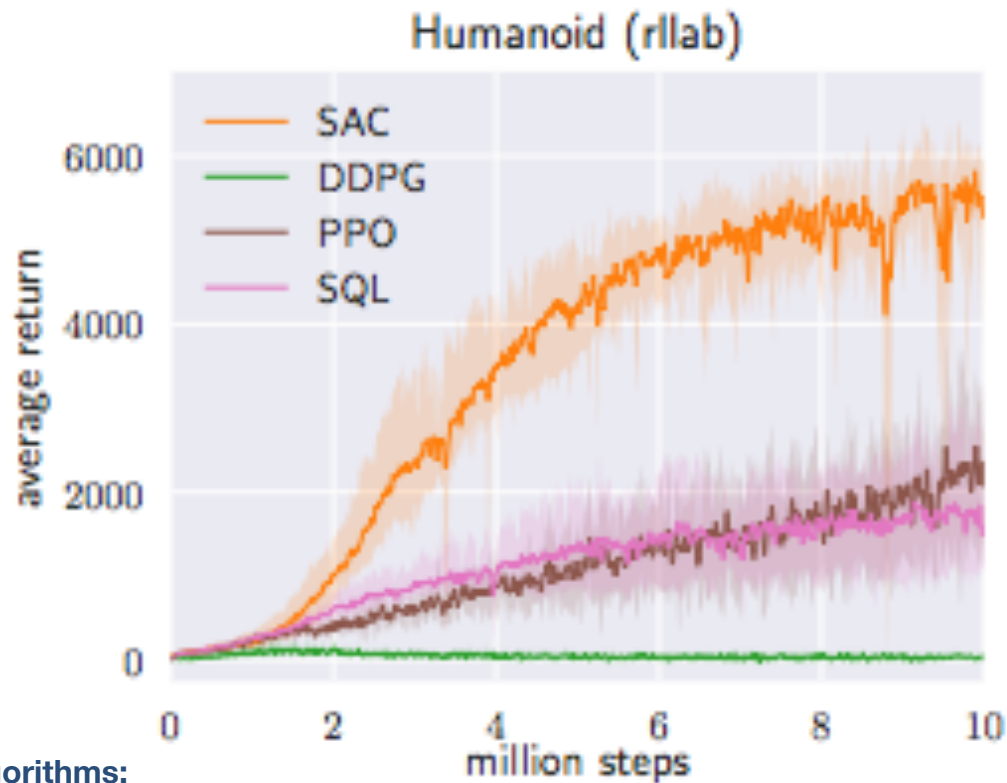
```

$$\phi_{\text{targ},i} \leftarrow \rho \phi_{\text{targ},i} + (1 - \rho) \phi_i \quad \text{for } i = 1, 2$$

```

16:    end for
17:  end if
18: until convergence

```



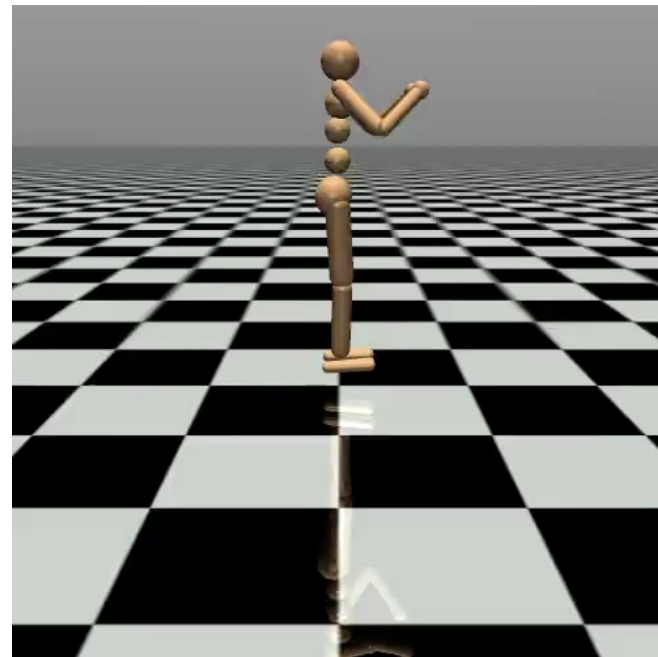
#### Algorithms:

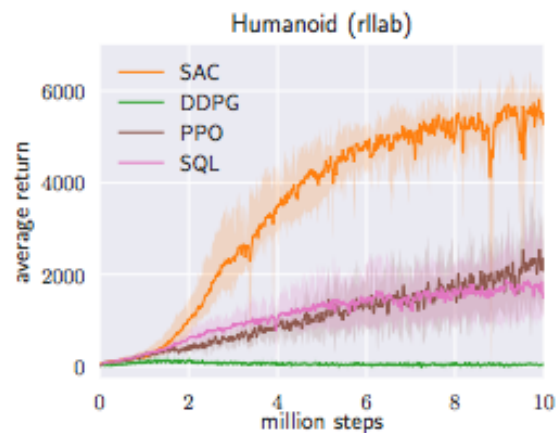
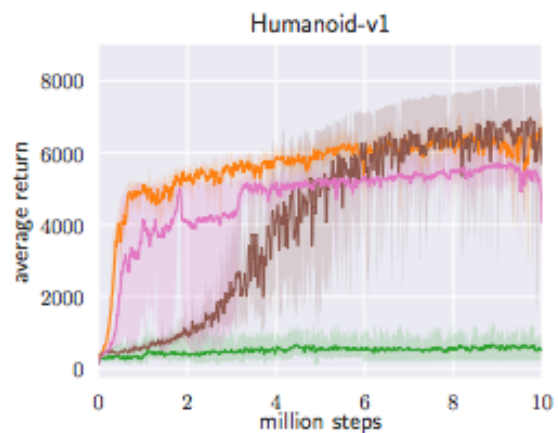
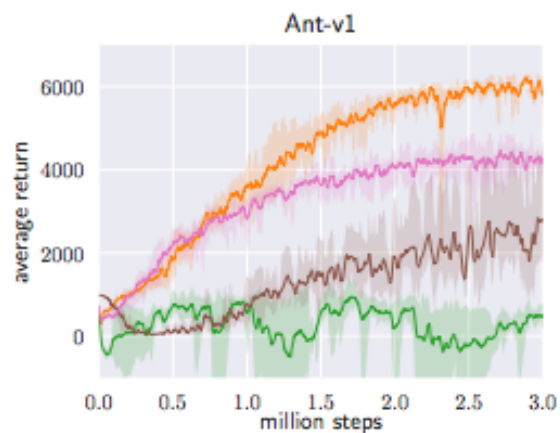
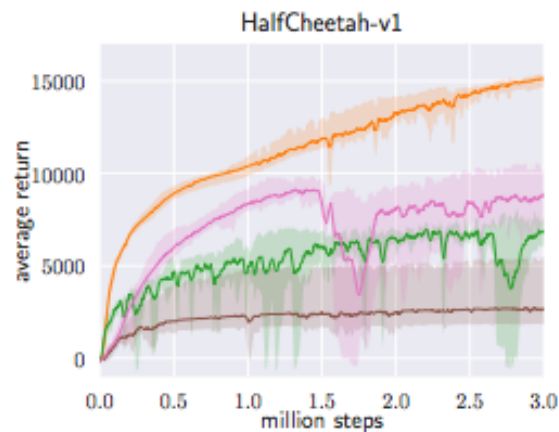
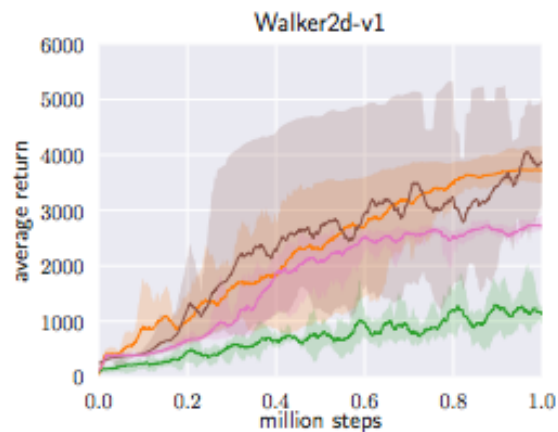
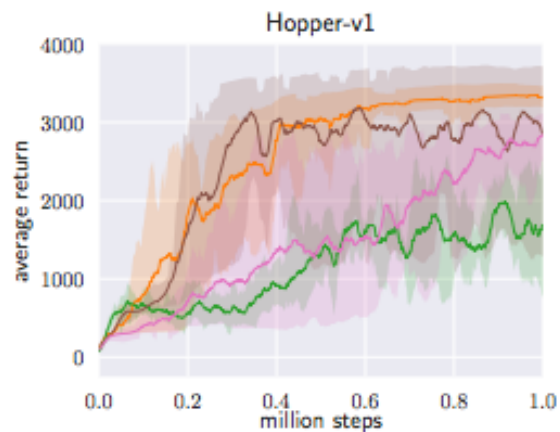
Soft Actor-Critic (SAC)

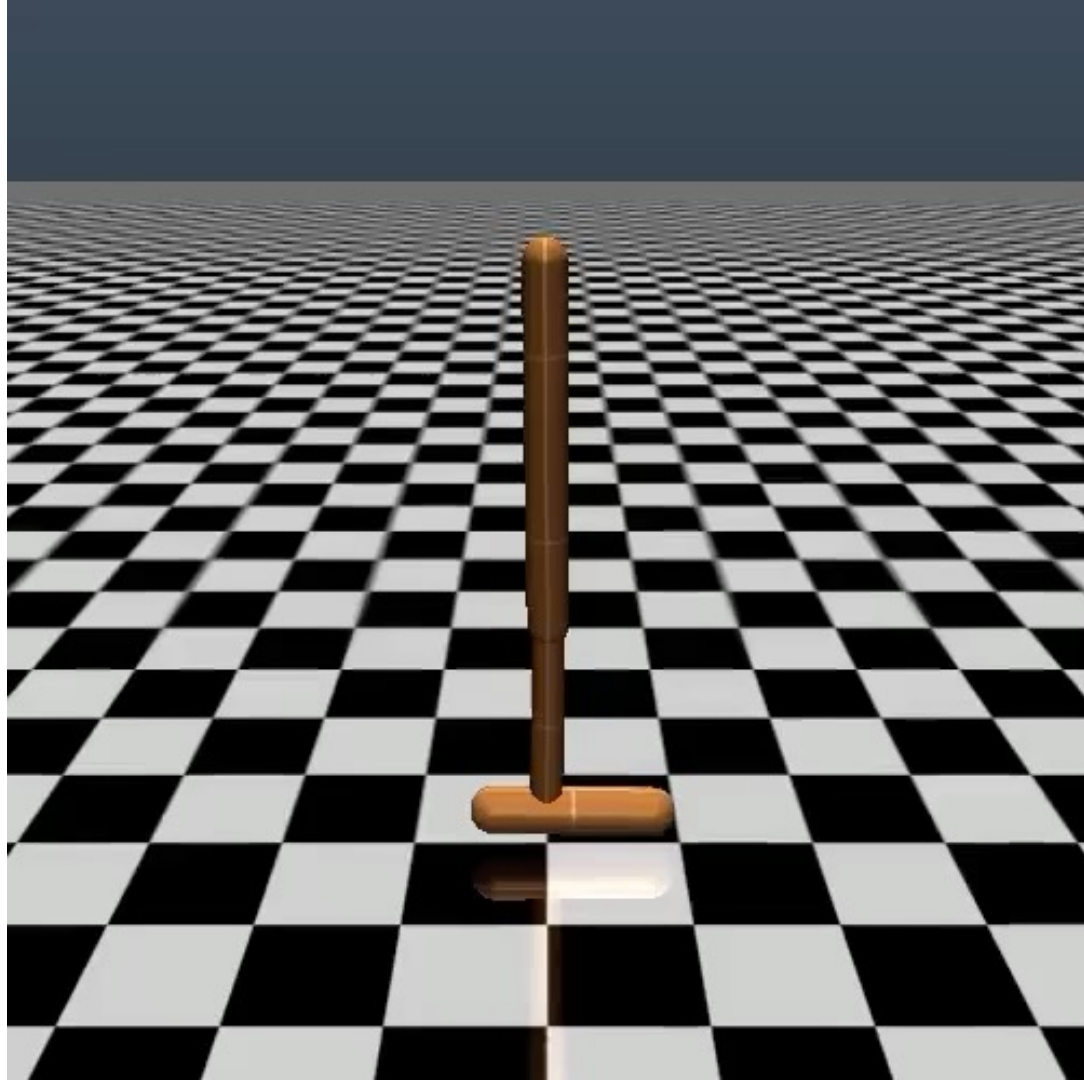
Deep Deterministic Policy Gradient (DDPG)

Proximal Policy Optimization (PPO)

Soft Q-Learning (SQL)







# Real Robot Results

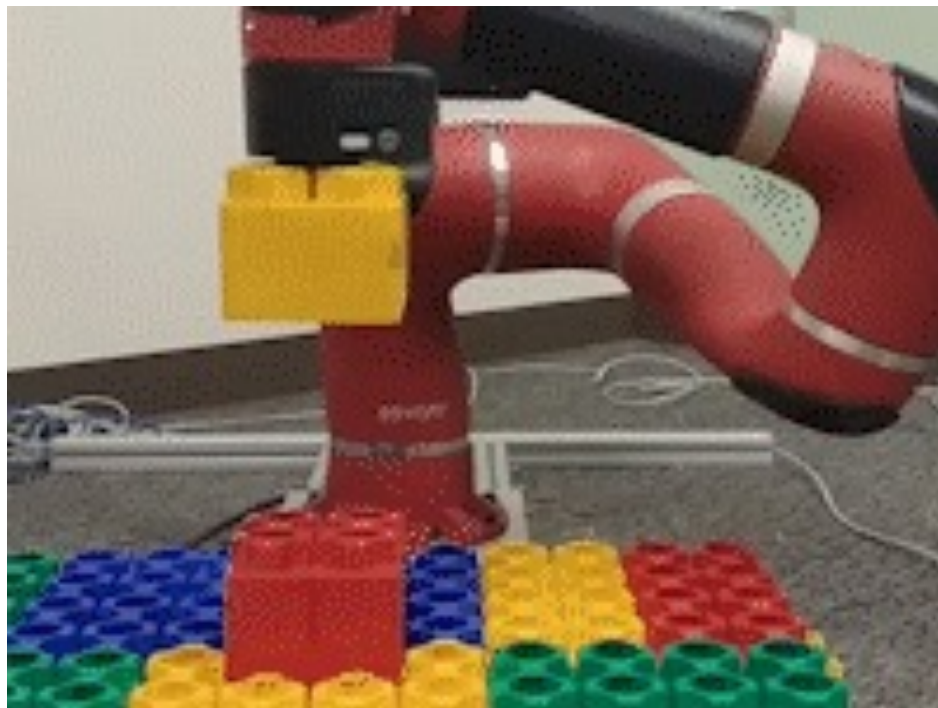


# Real Robot Results





# Real Robot Results



# Summary of This Lecture

---

- Deep Deterministic Policy Gradient (DDPG)
- Soft Actor Critic (SAC)