



# Compilers

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## Bottom-Up Parsing

- Bottom-up parsing is more general than (deterministic) top-down parsing
  - And just as efficient
  - Builds on ideas in top-down parsing
- Bottom-up is the preferred method

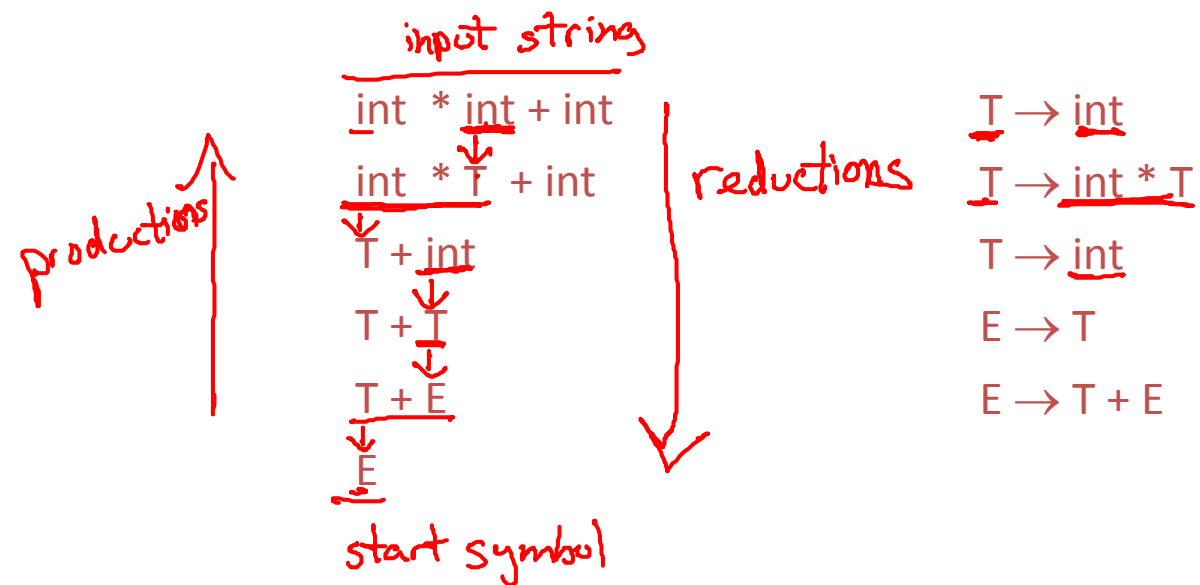
- Bottom-up parsers don't need left-factored grammars
- Revert to the “natural” grammar for our example:

$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

- Consider the string: int \* int + int

Bottom-up parsing reduces a string to the start symbol  
by inverting productions



Note the productions, read backwards, trace a rightmost derivation

int \* int + int

int \* T + int

T + int

T + T

T + E

E

*parsing*



$T \rightarrow \text{int}$

$T \rightarrow \text{int} * T$

$T \rightarrow \text{int}$

$E \rightarrow T$

$E \rightarrow T + E$

Important Fact #1 about bottom-up parsing:

*A bottom-up parser traces a rightmost derivation in reverse*

# Bottom-Up Parsing

int \* int + int

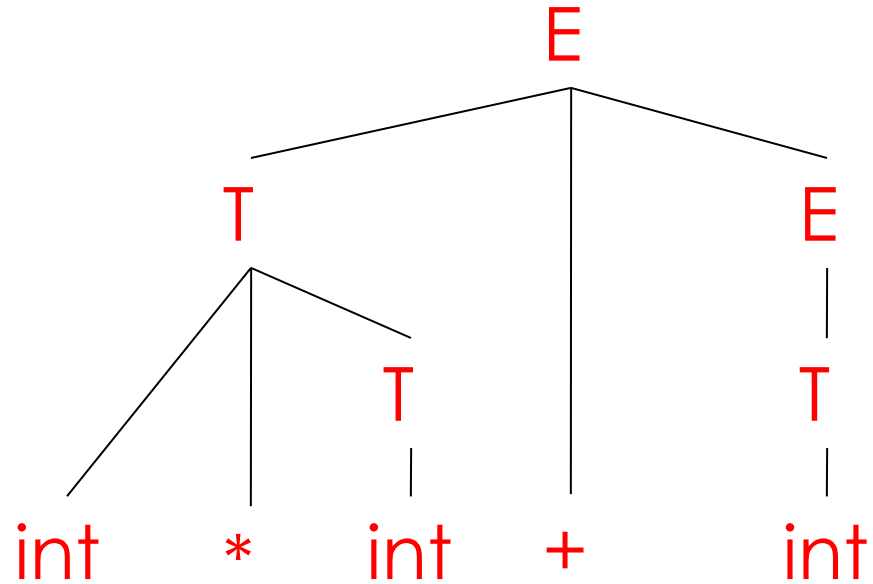
int \* T + int

T + int

T + T

T + E

E



# Bottom-Up Parsing

→ int \* int + int

→ int \* int + int



# Bottom-Up Parsing

int \* int + int

int \* I + int

int   \*   int   +   int

I

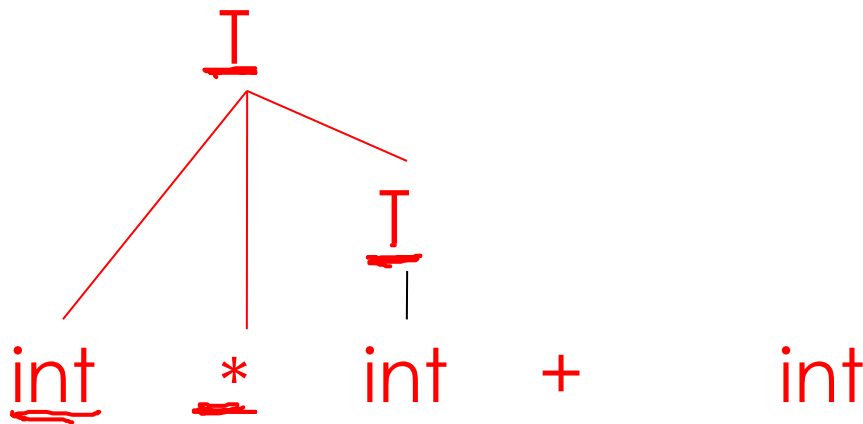
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# Bottom-Up Parsing

int \* int + int

int \* T + int

T + int



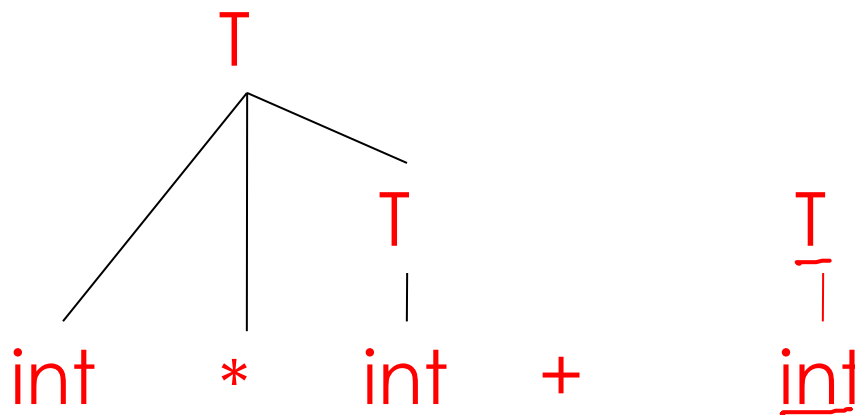
# Bottom-Up Parsing

int \* int + int

int \* T + int

T + int

T + T



# Bottom-Up Parsing

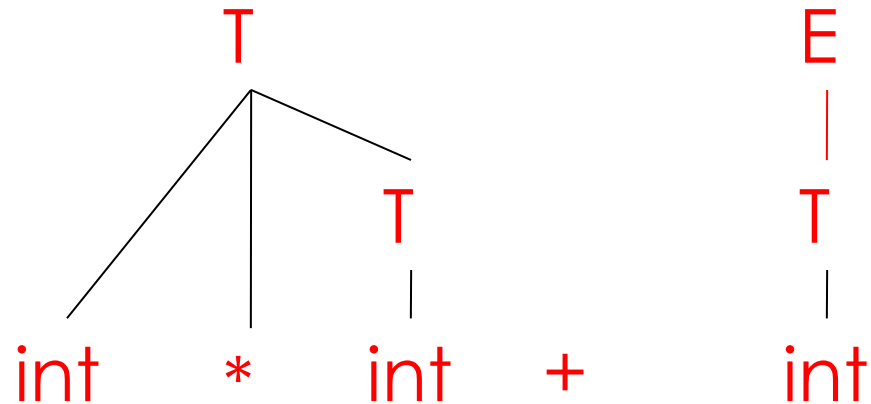
int \* int + int

int \* T + int

T + int

T + T

T + E



# Bottom-Up Parsing

int \* int + int

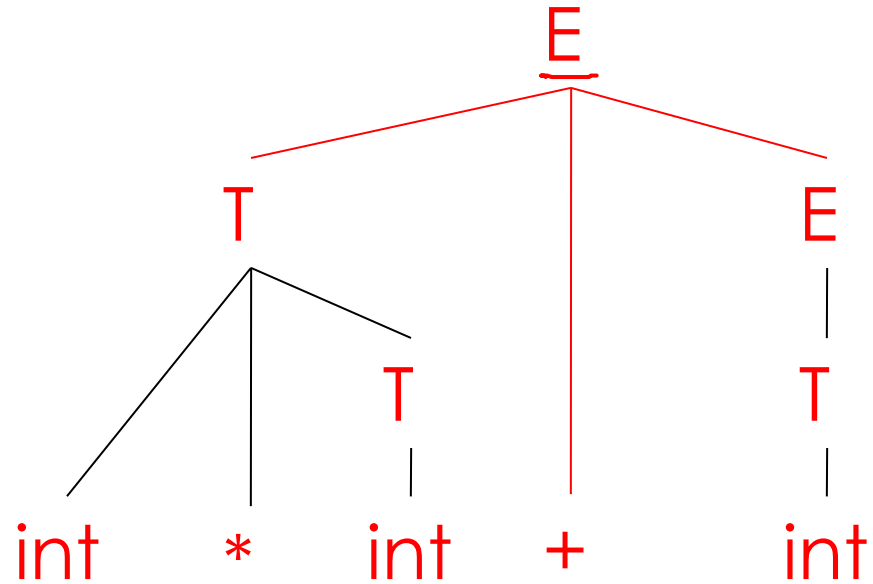
int \* T + int

T + int

T + T

T + E

E



For the given grammar, what is the correct series of reductions for the string:  $-(id + id) + id$

## Bottom-Up Parsing

$$E \rightarrow E' \mid E' + E$$

$$E' \rightarrow -E' \mid id \mid (E)$$

