



$$At \ t=0, [A]_0 = [A]_0$$

$$[A] = [A]_0 e^{-k_1 t}$$

$$[X] = [A]_0 \frac{k_1}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t})$$

The equation for the variation of  $[Z]$  can be obtained by noting that  $[A] + [X] + [Z] = [A]_0$

$$\text{So that } [Z] = [A]_0 - [A] - [X]$$

Insertion of the expressions for  $[A]$  and  $[X]$  in the eq. of  $[Z]$

leads to

$$\begin{aligned} [Z] &= [A]_0 - [A]_0 e^{-k_1 t} - [A]_0 \frac{k_1}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t}) \\ &= [A]_0 \left\{ 1 - e^{-k_1 t} - \frac{k_1}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t}) \right\} \\ &= [A]_0 \left\{ \frac{k_2 - k_1 - (k_2 - k_1)e^{-k_1 t} - k_1 e^{-k_1 t} + k_1 e^{-k_2 t}}{k_2 - k_1} \right\} \\ &= [A]_0 \left\{ \frac{k_2 - k_1 - k_2 e^{-k_1 t} + k_1 e^{-k_1 t} - k_1 e^{-k_1 t} + k_1 e^{-k_2 t}}{k_2 - k_1} \right\} \\ &= \frac{[A]_0}{k_2 - k_1} \left\{ k_2 (1 - e^{-k_1 t}) - k_1 (1 - e^{-k_2 t}) \right\} \end{aligned}$$