## TIP8419 - Tensor Algebra Homework 1

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## Hadamard, Kronecker and Khatri-Rao Products

**Problem 1** For randomly generated matrices **A** and  $\mathbf{B} \in \mathbb{C}^{N \times N}$ , create an algorithm to compute the Hadamard Product  $\mathbf{A} \odot \mathbf{B}$ . Then, compare the run time of your algorithm with the operator .\* of the *software* Octave/Matlab  $^{\textcircled{R}}$ . Plot the run time curve as a function of the number of rows/columns  $N \in \{2, 4, 8, 16, 32, 64, 128\}$ .

**Problem 2** For randomly generated matrices  $\mathbf{A}$  and  $\mathbf{B} \in \mathbb{C}^{N \times N}$ , create an algorithm to compute the Kronecker Product  $\mathbf{A} \otimes \mathbf{B}$ . Then, compare the run time of your algorithm with the operator  $kron(\mathbf{A}, \mathbf{B})$  of the software Octave/Matlab<sup>®</sup>. Plot the run time curve as a function of the number of rows/columns  $N \in \{2, 4, 8, 16, 32, 64, 128\}$ .

**Problem 3** For randomly generated matrices  $\mathbf{A}$  and  $\mathbf{B} \in \mathbb{C}^{N \times N}$ , create an algorithm to compute the Khatri-Rao product  $\mathbf{A} \diamond \mathbf{B}$  according with the following prototype function:

$$\mathbf{R} = kr(\mathbf{A}, \mathbf{B}).$$

<sup>⊙</sup> Denotes the Hadamard Product.

 $<sup>\</sup>otimes$  Denotes the Kronecker Product.

<sup>♦</sup> Denotes the Khatri-Rao Product.