Notation

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1 Font notation

$a, b, c, \ldots, A, B, C, \ldots$	Scalars
a, b, c, \dots	Vectors
$\overline{\mathbf{A},\mathbf{B},\mathbf{C},\dots}$	Matrices
$\mathcal{A}, \mathcal{B}, \mathcal{C}, \dots$	Tensors
$A, B, C, \ldots, A, B, C, \ldots, A, B, C, \ldots$	Sets

2 Signals and functions

2.1 Time indexing

x(t)	Continuous-time t
$x[n],x[k],x[m],x[i],\ldots$	Discrete-time n, k, m, i, \ldots (parenthe-
$x_n, x_k, x_m, x_i, \dots$	sis should be adopted only if there
$x(n), x(k), x(m), x(i), \dots$	are no continuous-time signals in the
	context to avoid ambiguity)
$x[((n-m))_N][32], x((n-m))_N[26]$	Circular shift in m samples within a
	N-samples window

2.2 Common signals

$\delta(t)$	Delta function
$\delta[n], \delta_{i,j}$	Kronecker function $(n = i - j)$
h(t), h[n]	Impulse response (continuous and
	discrete time)
$\tilde{x}[n], \tilde{x}(t)$	Periodic discrete- or continuous-time
	signal
$\hat{x}[n], \hat{x}(t)$	Estimate of $x[n]$ or $x(t)$
$\dot{x}[m]$	Interpolation of $x[n]$

2.3 Common functions

$\mathcal{O}(\cdot), O(\cdot)$	Big-O notation
$\Gamma(\cdot)$	Gamma function
$Q(\cdot)$	Quantization function
$\operatorname{sgn}(\cdot)$	Signum function
$\tanh(\cdot)$	Hyperbolic tangent function
$I_{\alpha}(\cdot)$	Modified Bessel function of the first
	kind and order α

	n	Binomial coefficient
- (k	Dinomai coemcient

2.4 Operations and symbols

$f:A\to B$	A function f whose domain is A and codomain is B
$\mathbf{f}:A\to\mathbb{R}^n$	A vector-valued function \mathbf{f} , i.e., $n \geq 2$
$f^n, x^n(t), x^n[k]$	<i>n</i> th power of the function f , $x[n]$ or
	x(t)
$f^{(n)}, \chi^{(n)}(t)$	nth derivative of the function f or
	x(t)
$f', f^{(1)}, x'(t)$	1th derivative of the function f or
	x(t)
$f'', f^{(2)}, x''(t)$	2th derivative of the function f or
	x(t)
$ \operatorname{argmax}_{x \in A} f(x) $	Value of x that minimizes x
$ \frac{x \in \mathcal{A}}{\arg\min f(x)} $ $ x \in \mathcal{A} $	Value of x that minimizes x
$f(\mathbf{x}) = \inf_{\mathbf{y} \in A} g(\mathbf{x}, \mathbf{y})$	Infimum, i.e., $f(\mathbf{x}) =$
$\mathbf{y}{\in}\mathcal{A}$	$\min \{ g(\mathbf{x}, \mathbf{y}) \mid \mathbf{y} \in \mathcal{A} \land (\mathbf{x}, \mathbf{y}) \in \text{dom}(g) \},\$
	which is the greatest lower bound of
	this set $[10]$
$f(\mathbf{x}) = \sup g(\mathbf{x}, \mathbf{y})$	Supremum, i.e., $f(\mathbf{x}) =$
$\mathbf{y} \in \mathcal{A}$	$\max \{g(\mathbf{x}, \mathbf{y}) \mid \mathbf{y} \in \mathcal{A} \land (\mathbf{x}, \mathbf{y}) \in \text{dom}(g)\}\$
	which is the least upper bound of
	this set $[10]$
$f \circ g$	Composition of the functions f and
	g
*	Convolution (discrete or continuous)
	Circular convolution

2.5 Digital signal processing

W_N	Twiddle factor, $e^{-j\frac{2\pi}{N}}$ [26]
N	Number of samples in the DFT/FFT
Ω [26]	Continuous angular frequency (in rad/s)

also used to denote continuous angular frequency outside the DSP context, it is always convenient to state that it denotes the discrete frequency when it does $f_{C} \qquad \qquad$		Digenete encular fraguence. As a sign
$\begin{array}{c} \text{lar frequency outside the DSP context, it is always convenient to state that it denotes the discrete frequency when it does} \\ f_{C} & \text{Continuous linear frequency (in Hz)} \\ f & \text{Discrete linear frequency. As } f \text{ is also used to denote continuous linear frequency outside the DSP context, it is always convenient to state that it denotes the discrete frequency when it does} \\ \overline{\mathcal{R}_{N}[n]} & \text{Rectangular window used to cut off the discrete sequences } [26] \\ \overline{\mathcal{R}_{S}[n]} & \text{Sampling period} \\ f_{S} & \text{Sampling frequency (in Hz), i.e., } 1/T \\ \Omega_{S} & \text{Sampling frequency (in Hz), i.e., } 1/T \\ \Omega_{S} & \text{Sampling frequency (in rad/s), i.e., } \\ 2\pi f_{S} & \text{Sampling frequency (in rad/s), i.e., } \\ 2\pi f_{S} & \text{Stop frequency } [26] \\ \omega_{P} & \text{Pass frequency } [26] \\ \omega_{Q} & \text{Cutoff frequency } [26] \\ \omega_{C} & \text{Cutoff frequency } [26] \\ \omega_{C} & \text{Cutoff frequency } [26] \\ \omega_{C} & \text{Cutoff frequency } [26] \\ s(t) & \text{Impulse train} \\ \text{gdr } [H(e^{j\omega})] [32] & \text{Group delay of } H(e^{j\omega}) \\ 2H(e^{j\omega}) [32] & \text{Phase response of } H(e^{j\omega}) \\ IH(e^{j\omega}) [32] & \text{Magnitude (or gain) of } H(e^{j\omega}) \\ x_{C}(t) [32], x(t) & \text{Continuous-time signal} \\ x_{S}(t) & \text{Sampled version of } x(t), \text{i.e., } x(t)s(t) \\ x_{T}(t) & \text{Reconstruction of } x(t) \text{ from interpolation} \\ \bar{x}[n] & \text{Periodic extension of the the aperi-} \\ \end{array}$	ω	Discrete angular frequency. As ω is
$\begin{array}{c} \text{text, it is always convenient to state} \\ \text{that it denotes the discrete frequency} \\ \text{when it does} \\ f_c & \text{Continuous linear frequency (in Hz)} \\ f & \text{Discrete linear frequency. As } f \text{ is also} \\ \text{used to denote continuous linear frequency outside the DSP context, it} \\ \text{is always convenient to state that it} \\ \text{denotes the discrete frequency when} \\ \text{it does} \\ \hline \mathcal{R}_N[n] & \text{Rectangular window used to cut off} \\ \text{the discrete sequences } [26] \\ \hline T[32], T_s & \text{Sampling period} \\ f_s & \text{Sampling frequency (in Hz), i.e., } 1/T \\ \hline \Omega_s & \text{Sampling frequency (in rad/s), i.e.,} \\ 2\pi f_s & \\ \hline \Omega_N [32], B & \text{One-sided effective bandwidth of the continuous-time signal spectrum} \\ \hline \omega_s & \text{Stop frequency } [26] \\ \hline \omega_p & \text{Pass frequency } [26] \\ \hline \omega_p & \text{Pass frequency } [26] \\ \hline \omega_c & \text{Cutoff frequency } [26] \\ \hline \omega_c & \text{Cutoff frequency } [26] \\ \hline \omega_t & \text{Goup delay of } H(e^{j\omega}) \\ \hline \mathcal{A}H(e^{j\omega}) [32] & \text{Phase response of } H(e^{j\omega}) \\ \hline \mathcal{A}L(e^{j\omega}) [32] & \text{Phase response of } H(e^{j\omega}) \\ \hline \mathcal{A}_s(t) & \text{Sampled version of } x(t), \text{ i.e., } x(t)s(t) \\ \hline \mathcal{X}_r(t) & \text{Sampled version of } x(t), \text{ i.e., } x(t)s(t) \\ \hline \mathcal{X}_r(t) & \text{Reconstruction of } s(t), \text{ from interpolation} \\ \hline \tilde{X}[n] & \text{Periodic extension of the the aperi-} \\ \hline \end{array}$		~
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ω_c Cutoff frequency [26] $s(t)$ Impulse train $gdr [H(e^{j\omega})]$ [32]Group delay of $H(e^{j\omega})$ $\angle H(e^{j\omega})$ [32]Phase response of $H(e^{j\omega})$ $[H(e^{j\omega})]$ [32]Magnitude (or gain) of $H(e^{j\omega})$ $x_c(t)$ [32], $x(t)$ Continuous-time signal $x_s(t)$ Sampled version of $x(t)$, i.e., $x(t)s(t)$ $x_r(t)$ Reconstruction of $x(t)$ from interpolation $\tilde{x}[n]$ Periodic extension of the the aperi-		$\omega_s - \omega_p$ [26]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	ω_c	
$ \begin{array}{c cccc} \angle H(e^{j\omega}) & \text{Saper response of } H(e^{j\omega}) \\ \hline H(e^{j\omega}) & \text{Saper response of } H(e^{j\omega}) \\ \hline x_c(t) & \text{Saper response of } H(e^{j\omega}) \\ \hline x_s(t) & \text{Continuous-time signal} \\ \hline x_s(t) & \text{Sampled version of } x(t), \text{ i.e., } x(t)s(t) \\ \hline x_r(t) & \text{Reconstruction of } x(t) \text{ from interpolation} \\ \hline \tilde{x}[n] & \text{Periodic extension of the the aperi-} \end{array} $	s(t)	Impulse train
$ \begin{array}{c cccc} \angle H(e^{j\omega}) & \text{Saper response of } H(e^{j\omega}) \\ \hline H(e^{j\omega}) & \text{Saper response of } H(e^{j\omega}) \\ \hline x_c(t) & \text{Saper response of } H(e^{j\omega}) \\ \hline x_s(t) & \text{Continuous-time signal} \\ \hline x_s(t) & \text{Sampled version of } x(t), \text{ i.e., } x(t)s(t) \\ \hline x_r(t) & \text{Reconstruction of } x(t) \text{ from interpolation} \\ \hline \tilde{x}[n] & \text{Periodic extension of the the aperi-} \end{array} $	$\operatorname{gdr}\left[H(e^{j\omega})\right]$ [32]	Group delay of $H(e^{j\omega})$
$ \begin{array}{c c} H(e^{j\omega}) & [32] & \text{Magnitude (or gain) of } H(e^{j\omega}) \\ x_c(t) & [32], x(t) & \text{Continuous-time signal} \\ x_s(t) & \text{Sampled version of } x(t), \text{ i.e., } x(t)s(t) \\ x_r(t) & \text{Reconstruction of } x(t) \text{ from interpolation} \\ \tilde{x}[n] & \text{Periodic extension of the the aperi-} \end{array} $		Phase response of $H(e^{j\omega})$
$x_c(t)$ [32], $x(t)$ Continuous-time signal $x_s(t)$ Sampled version of $x(t)$, i.e., $x(t)s(t)$ $x_r(t)$ Reconstruction of $x(t)$ from interpolation $\tilde{x}[n]$ Periodic extension of the the aperi-	$H(e^{j\omega})$ [32]	Magnitude (or gain) of $H(e^{j\omega})$
$x_r(t)$ Reconstruction of $x(t)$ from interpolation $\tilde{x}[n]$ Periodic extension of the the aperi-	$x_c(t)$ [32], $x(t)$	Continuous-time signal
$x_r(t)$ Reconstruction of $x(t)$ from interpolation $\tilde{x}[n]$ Periodic extension of the the aperi-	$x_s(t)$	Sampled version of $x(t)$, i.e., $x(t)s(t)$
$\begin{array}{c} \text{lation} \\ \tilde{x}[n] & \text{Periodic extension of the the aperi-} \end{array}$		Reconstruction of $x(t)$ from interpo-
		• • • • • • • • • • • • • • • • • • • •
	$\tilde{x}[n]$	Periodic extension of the the aperi-
		-

2.6 Transformations

$\mathcal{F}\left\{ \cdot ight\}$	Fourier transform (FT)
$\overline{\mathrm{DTFT}\left\{\cdot\right\},\mathrm{DFS}\left\{\cdot\right\},\mathrm{FFT}\left\{\cdot\right\}}$	Discrete-time Fourier Transform
	(DTFT), Discrete Fourier Trans-
	form (DFT), Discrete Fourier Series
	(DFS), respectively

$\mathcal{L}\left\{ \cdot \right\}$	Laplace transform
$\mathcal{Z}\left\{ \cdot \right\}$	z-transform
$\hat{x}(t), \hat{x}[n]$	Hilbert transform of $x(t)$ or $x[n]$
X(s)	Laplace transform of $x(t)$
X(f)	Fourier transform (FT) (in linear fre-
	quency, Hz) of $x(t)$
$X(j\omega)$	Fourier transform (FT) (in angular
	frequency, rad/sec) of $x(t)$
$X(e^{j\omega})$	Discrete-time Fourier transform
	(DTFT) of $x[n]$
$X[k], X(k), X_k$	Discrete Fourier transform (DFT) or
	fast Fourier transform (FFT) of $x[n]$,
	or even the Fourier series (FS) of the
	periodic signal $x(t)$
$\tilde{X}[k], \tilde{X}(k), \tilde{X}_k$	Discrete Fourier series (DFS) of $\tilde{x}[n]$
X(z)	z-transform of $x[n]$

3 Probability, statistics, and stochastic processes

3.1 Operators and symbols

$\mathbb{E}\left[\cdot\right],\mathbf{E}\left[\cdot\right]\left[31\right],E\left[\cdot\right],\mathbb{E}\left[\cdot\right]\left[16\right]$	Statistical expectation operator
$E_u[\cdot], E_u[\cdot][31], E_u[\cdot], \mathbb{E}_u[\cdot]$	Statistical expectation operator with
	respect to u
$\langle \cdot \rangle$	Ensemble average
$var [\cdot] [31], VAR[\cdot] [9, 25, 30, 34]$	Variance operator
$\operatorname{var}_{u}\left[\cdot\right]\left[\cdot\right], \operatorname{VAR}_{u}\left[\cdot\right]$	Variance operator with respect to u
$cov[\cdot], COV[\cdot]$	Covariance operator [9]
$\operatorname{cov}_{u}[\cdot], \operatorname{COV}_{u}[\cdot]$	Covariance operator with respect to
	и
$\mu_{\scriptscriptstyle X}$	Mean of the random variable x
$\mu_{\mathrm{x}}, \mathrm{m}_{\mathrm{x}}$	Mean vector of the random variable
	x [11]
μ_n	nth-order moment of a random vari-
	able
$\frac{\sigma_x^2, \kappa_2}{\mathcal{K}_x, \mu_4}$	Variance of the random variable x
\mathcal{K}_x, μ_4	Kurtosis (4th-order moment) of the
	random variable x
κ_n	nth-order cumulant of a random vari-
	able
$\rho_{x,y}$	Pearson correlation coefficient be-
	tween x and y

$a \sim P$	Random variable a with distribution P
\mathcal{R}	Rayleigh's quotient

3.2 Stochastic processes

PS: Estimated terms come with a hat above of it

$r_x(\tau)$ [31], $R_x(\tau)$	Autocorrelation function of the signal
	x(t) or $x[n]$
$S_X(f), S_X(j\omega)$	Power spectral density (PSD) of $x(t)$
	in linear (f) or angular (ω) frequency
$S_{x,y}(f), S_{x,y}(j\omega)$	Cross PSD of $x(t)$ and $y(t)$ in linear
	or angular (ω) frequency
R_{x}	(Auto)correlation matrix of $\mathbf{x}(n)$
$r_{x,d}(\tau), R_{x,d}(\tau)$	Cross-correlation between $x[n]$ and
	d[n] or $x(t)$ and $d(t)$ [31]
$\overline{\mathbf{R}_{\mathbf{x}\mathbf{y}}}$	Cross-correlation matrix of $\mathbf{x}(n)$ and
·	$\mathbf{y}(n)$
$\mathbf{r}_{\mathbf{x}d} [24], \mathbf{p}_{\mathbf{x}d} [16]$	y(n) Cross-correlation vector between
	Cross-correlation vector between
\mathbf{r}_{xd} [24], \mathbf{p}_{xd} [16]	Cross-correlation vector between $\mathbf{x}(n)$ and $d(n)$
\mathbf{r}_{xd} [24], \mathbf{p}_{xd} [16]	Cross-correlation vector between $\mathbf{x}(n)$ and $d(n)$ Autocovariance function of the signal
\mathbf{r}_{xd} [24], \mathbf{p}_{xd} [16] $c_x(\tau), C_x(\tau)$	Cross-correlation vector between $\mathbf{x}(n)$ and $d(n)$ Autocovariance function of the signal $x(t)$ or $x[n]$ [31]
\mathbf{r}_{xd} [24], \mathbf{p}_{xd} [16] $c_x(\tau), C_x(\tau)$	Cross-correlation vector between $\mathbf{x}(n)$ and $d(n)$ Autocovariance function of the signal $x(t)$ or $x[n]$ [31] (Auto)covariance matrix of \mathbf{x} [9, 25,
$ c_{xd} [24], \mathbf{p}_{xd} [16] $ $ c_{x}(\tau), C_{x}(\tau) $ $ C_{x}, \mathbf{K}_{x}, \mathbf{\Sigma}_{x}, \text{cov} [\mathbf{x}] $	Cross-correlation vector between $\mathbf{x}(n)$ and $d(n)$ Autocovariance function of the signal $x(t)$ or $x[n]$ [31] (Auto)covariance matrix of \mathbf{x} [9, 25, 30, 34, 41]

3.3 Functions

$Q(\cdot)$	Q-function, i.e., $P[\mathcal{N}(0,1) > x]$ [34]
$erf(\cdot)$	Error function [34]
$erfc(\cdot)$	Complementary error function i.e.,
	$\operatorname{erfc}(x) = 2Q(\sqrt{2}x) - \operatorname{erf}(x)$ [34]
P[A]	Probability of the event or set A [30]
$p(\cdot), f(\cdot)$	Probability density function (PDF)
	or probability mass function (PMF)
	[30]
$p(x \mid A)$	Conditional PDF or PMF [30]
$F(\cdot)$	Cumulative distribution function
	(CDF)

$\Phi_{X}(\omega), M_{X}(j\omega), E\left[e^{j\omega X}\right]$	First characteristic function (CF) of x [34, 40]
$M_X(t), \Phi_X(-jt), E\left[e^{tX}\right]$	Moment-generating function (MGF)
	of $x [34, 40]$
$\Psi_{x}(\omega), \ln \Phi_{x}(\omega), \ln E\left[e^{j\omega x}\right]$	Second characteristic function
$K_x(t), \ln E\left[e^{tx}\right], \ln M_x(t)$	Cumulant-generating function
	(CGF) of x [25]

3.4 Distributions

$\mathcal{N}(\mu, \sigma^2)$	Gaussian distribution of a random variable with mean μ and variance σ^2
$\mathcal{CN}(\mu, \sigma^2)$	Complex Gaussian distribution of a random variable with mean μ and variance σ^2
$\mathcal{N}(\mu, \Sigma)$	Gaussian distribution of a vector random variable with mean μ and covariance matrix Σ
$\mathcal{CN}(\mu, \Sigma)$	Complex Gaussian distribution of a vector random variable with mean μ and covariance matrix Σ
$\frac{\mathcal{U}(a,b)}{\chi^2(n),\chi_n^2}$	Uniform distribution from a to b
$\chi^2(n), \chi_n^2$	Chi-square distribution with n degree of freedom (assuming that the Gaussians are $\mathcal{N}(0,1)$)
$\operatorname{Exp}(\lambda)$	Exponential distribution with rate parameter λ
$\Gamma(\alpha, \beta)$	Gamma distribution with shape parameter α and rate parameter β
$\Gamma(\alpha, \theta)$	Gamma distribution with shape parameter α and scale parameter $\theta = 1/\beta$
$- \operatorname{Nakagami}(m,\Omega)$	Nakagami-m distribution with shape parameter or fading figure m and spread, scale, or shape parameter Ω
Rayleigh(σ)	Rayleigh distribution with scale parameter σ
$\operatorname{Rayleigh}(\Omega)$	Rayleigh distribution with the second moment $\Omega = E[x^2] = 2\sigma^2$
$\mathrm{Rice}(s,\sigma)$	Rice distribution with noncentrality parameter s and σ . s^2 represent the specular component power

$\operatorname{Rice}(\Omega, K), \operatorname{Rice}(A, K)$	Rice distribution with Rice factor
	$K = s^2/2\sigma^2$ and scale parameter $\Omega =$
	$A = s^2 + 2\sigma^2 = 2\sigma^2(K+1)$ (Ω is pref-
	ered over A)

4 Machine learning, optimization theory, and statistical signal processing

4.1 Matrix Calculus (in denominator layout)

PS: Estimated terms come with a hat above of it

$\mathbf{g}, \nabla f, \frac{\partial f}{\partial \mathbf{w}}$	Gradient descent vector, used in the steepest descent method, also called gradient descent method or deterministic gradient method.
g if the gradient vector is ∇f (or $\hat{\mathbf{g}}$ if	Stochastic gradient descent (SGD)
the gradient vector is g)	vector, i.e., instantaneous approximation of gradient descent vector
$\mathbf{g}_{\mathbf{x}}, abla_{\mathbf{w}} f, rac{\partial f}{\partial \mathbf{w}}$	Gradient descent vector with respect \mathbf{w} [9]
$\mathbf{J}, \frac{\partial \mathbf{y}^{T}}{\partial \mathbf{x}}, \nabla \mathbf{y}^{T} $ [24]	Jacobian matrix.
$ \frac{\mathbf{J}, \frac{\partial \mathbf{y}^{T}}{\partial \mathbf{x}}, \nabla \mathbf{y}^{T} [24]}{\mathbf{H}, \frac{\partial^{2} f}{\partial \mathbf{w}^{2}}, \nabla^{2} f [24], \nabla \nabla f [9]} $	Hessian matrix. The notation ∇^2 is sometimes used in Matrix Calculus to denote the second-order vector derivative. However, it must be avoided since, in Vector Calculus, ∇^2 also denotes the Laplacian operator which in turn may be scalar or vector Laplacian operator depending on whether f is scalar- or vector-valued, respectively. Some discussion about can be found in [5–7]

4.2 Estimated terms

4.3 Signals, (hyper)parameters, system performance, and criteria

N	Number of instances (or samples),
	i.e., $n \in \{1, 2,, N\}$
$N_{ m trn}$	Number of instances in the training
	set, i.e., $n \in \{1, 2,, N_{\text{trn}}\}$
$N_{ m tst}$	Number of instances in the test set.
	i.e., $n \in \{1, 2, \dots, N_{\text{tst}}\}$
$N_{ m val}$	Number of instances in the validation
	set, i.e., $n \in \{1, 2,, N_{\text{val}}\}\$
N_e	Number of epochs
	Number os attributes
$\frac{N_a}{K [24]}$	Number of classes (which is the num-
	ber of outputs in multiclass prob-
	lems). Use k to iterate over it
L	Number of layers, i.e., the depth of
	the network. Use l to iterate over it
M_l, m_l [24], J [24]	Number of neurons at the <i>l</i> th layer.
$[m_l, m_l \ [24], \ J \ [24]]$	You might prefer J in the case of the
	single-layer perceptron (use j to it-
	erate over it). If you want to iter-
	ate through it, a sensible variation
	of Haykin notation is M_l , where m_l
	can be used as an iterator. m_0 is the
	length of the input vector without the
	bias.
$\mathbf{x}(n), \mathbf{x}_n$	Input signal (in \mathbb{R}^{N_a+1})
$x_0(n)$	Dummy input of the bais, which is
	usually ± 1 . ± 1 is preferred [9, 24].
$\varphi(\cdot)[24], h(\cdot)[9]$ $\varphi'(v_{m_l}^{(l)}(n))[24], \frac{\partial y_{m_l}^{(l)}(n)}{\partial v_{m_l}^{(l)}(n)} [24]$	Activation function
$(y_{m_l}^{(l)}(n))[24] = \partial y_{m_l}^{(l)}(n)$	Partial derivative of the activation
$\varphi'(v_{m_l}^{(l)}(n))[24], \frac{\partial y_{m_l}(n)}{\partial v_{m_l}^{(l)}(n)}[24]$	(1)
2 · m ₁ (- ·)	function with respect to $v_{m_l}^{(l)}(n)$ (m_l)
	neuron at l th layer)
$y_{m_l}^{(l)}(n), \varphi\left(v_{m_l}^{(l)}(n)\right)$	Output signal of the m_l th neuron at
,	the l th layer
$\mathbf{y}^{(l)}(n)$	Output signal of the l th layer
$\mathbf{y}(n),\mathbf{y}^{(L)}(n)$	Output of the neural network
$\mathbf{d}(n), \mathbf{d}_n$	Desired label (in case of supervised
$\mathbf{u}(n), \mathbf{u}_n$	learning). For multiclass classifi-
	cation, one-hot encoding is usually
	used. For binary (scalar) classifi-
	cation, however antipodal encoding
	i.e., $\{-1,1\}$ is more recommended
	[24].
	L 3
a (m)	
$e_{m_l}(n)$	Error signal of the neuron m_l at the l th layer

$\mathbf{e}(n), \mathbf{d}(n) - \mathbf{y}(n)$	Error signal
$\mathbf{w}_{m_l}^{(l)}(n), \mathbf{\theta}_{m_l}^{(l)}(n)$	Parameters, coefficients, or synaptic
$ [w_{m_{l},0}^{(l)}(n) w_{m_{l},1}^{(l)}(n) \dots w_{m_{l},m_{l-1}}^{(l)}(n) $	weights vector in the <i>l</i> th layer. In the case of Single Layer Perceptrons or adaptive filters, the superscript is omitted
$w_{m_l,0}^{(l)}(n), b_{m_l}^{(l)}(n)$	Bias (the first term of the weight vec-
m_l ,0 · · · · · · · · · · · · · · · · · · ·	tor) of the l th layer
$\frac{\mathbf{W}(n), \begin{bmatrix} \mathbf{w}(1) & \mathbf{w}(2) & \cdots & \mathbf{w}(N) \end{bmatrix}^{T}}{\tilde{\mathbf{W}}(n)}$	Matrix of the synaptic weights
	Matrix of the synaptic weights, but without the bias
$v_{m_l}^{(l)}(n), \mathbf{w}_{m_l}^{(l)\top}(n)\mathbf{y}_{m_{l-1}}^{(l-1)}(n)$	Induced local field or activation potential. At the first layer $\mathbf{y}_{m_0}^{(0)}(n) = \mathbf{x}(n)$ [9]
$\mathbf{v}^{(l)}(n), \mathbf{W}^{(l)}(n)\mathbf{y}_{m_{l-1}}^{(l-1)}(n)$	Vector of the local fields at the l th layer
$\mathbf{w}^{\star}, \mathbf{w}_{o}, \mathbf{\theta}^{\star}, \mathbf{\theta}_{o}$	Optimum value of the parameters, coefficients, or synaptic weights vector (w * is also used [9] but it is not recommended as it may be confused with the conjugation operator)
$\overline{\delta_{m_l}^{(l)}(n),rac{\partial\mathscr{C}(n)}{\partial u_{m_l}^{(l)}(n)}}$	Local gradient of the m_l th neuron of the l th layer.
$oldsymbol{\delta}^{(l)}(n)$	Vector of the local gradients of all neurons at the l th layer
$\mathbf{X}, \begin{bmatrix} \mathbf{x}(1) & \mathbf{x}(2) & \cdots & \mathbf{x}(N) \end{bmatrix}$	Data matrix
	Learning rate hyperparameter [24]
$\frac{\eta(n)}{\mathscr{R}}$	Bayes risk or average risk [24]
c_{ij}, C_{ij}	Misclassification cost in deciding in favor of class \mathcal{C}_i (represented in the subspace \mathcal{H}_i) when the \mathcal{C}_j is the true class (used in Bayes classifiers/detectors) [12, 24]
\mathscr{C}_k	kth class [24]
$\frac{\mathscr{C}_k}{\mathscr{T}[24], \mathbb{X}[22]}$	Training set, i.e., the set $\{\mathbf{x}(n), d(n)\}$ that is used in the training phase.
\mathscr{H}_k	Subspace of the training vector belonging to the class \mathcal{C}_k
\mathcal{H}	Complete space of the input vector, i.e., $\mathcal{H}_1 \cup \mathcal{H}_2 \cup \cdots \mathcal{H}_K$
\mathcal{X} [24]	Set of all vectors in the training, batch, validation, or test dataset that was misclassified

$\mathscr{E}(\mathbf{w}), \mathscr{E}(\mathbf{w}(n)), \mathscr{E}(n)$	Cost function or objective function
	(the way it is written depends on the
	purpose of the text)
$J(\mathbf{w}), J(\mathbf{w}(n)), J(n)$	Alternative to the cost function
$\Delta \mathcal{E}(\mathbf{w}(n)), \Delta \mathcal{E}(n), \mathcal{E}(\mathbf{w}(n+1))$ -	Cost function or objective function
$\mathscr{E}(\mathbf{w}(n))$	(the way it is written depends on the
	purpose of the text)
$\mathscr{E}_{\mathrm{av}}(\cdot)$	Error energy averaged over the train-
	ing sample or the empirical risk [9]
$\Lambda(\cdot)$	Likelihood function
$\Lambda_l(\cdot)$	Log-likelihood function
$\hat{ ho}_{x,y}$	Estimated Pearson correlation coeffi-
	cient between x and y
ρ	Distance of the margin of separation
	between two classes (Support Vector
	Machine, SVM)
$g(\cdot)$	Discriminant function, i.e., $g(\mathbf{w}^*) = 0$

5 Linear Algebra

5.1 Common matrices and vectors

\mathbf{W}, \mathbf{D}	Diagonal matrix
P	Projection matrix; Permutation ma-
	trix
J	Jordan matrix
L	Lower matrix
U	Upper matrix
C	Cofactor matrix
$\mathbf{C}_{\mathbf{A}}, \operatorname{cof}\left(\mathbf{A}\right)$	Cofactor matrix of A
S	Symmetric matrix
Q	Orthogonal matrix
\mathbf{I}_N	$N \times N$ -dimensional identity matrix
$0_{M imes N}$	$M \times N$ -dimensional null matrix
0_N	N-dimensional null vector
$1_{M imes N}$	$M \times N$ -dimensional ones matrix
1_N	N-dimensional ones vector
0	Null matrix, vector, or tensor (di-
	mensionality understood by context)
1	Ones matrix, vector, or tensor (di-
	mensionality understood by context)

5.2 Indexing

$x_{i_1,i_2,,i_N}, [\mathcal{X}]_{i_1,i_2,,i_N}$	Element in the position
2,2, ,1,	(i_1, i_2, \ldots, i_N) of the tensor \mathcal{X}
$\mathcal{X}^{(n)}$	nth tensor of a nontemporal sequence
$\mathbf{x}_n, \mathbf{x}_{:n}$	nth column of the matrix X
X_{n} :	nth row of the matrix X
$\mathbf{x}_{i_1,\ldots,i_{n-1},:,i_{n+1},\ldots,i_N}$	Mode- n fiber of the tensor \mathcal{X}
$\mathbf{x}_{:,i_2,i_3}$	Column fiber (mode-1 fiber) of the
	thrid-order tensor \mathcal{X}
$\mathbf{x}_{i_1,:,i_3}$	Row fiber (mode-2 fiber) of the thrid-
	order tensor \mathcal{X}
$X_{i_1,i_2,:}$	Tube fiber (mode-3 fiber) of the
	thrid-order tensor \mathcal{X}
$X_{i_1,:,:}$	Horizontal slice of the thrid-order
	tensor \mathcal{X}
$X_{:,i_2,:}$	Lateral slices slice of the thrid-order
	tensor \mathcal{X}
$X_{i_3}, X_{:,:,i_3}$	Frontal slices slice of the thrid-order
	tensor \mathcal{X}

5.3 General operations

$\langle \mathbf{a}, \mathbf{b} angle$, $\mathbf{a}^{T} \mathbf{b}$, $\mathbf{a} \cdot \mathbf{b}$	Inner or dot product
$\mathbf{a} \circ \mathbf{b}, \mathbf{a} \mathbf{b}^{ op}$	Outer product
⊗	Kronecker product
· ·	Hadamard (or Schur) (elementwise)
	product
.⊙n	nth-order Hadamard power
$0.00 \frac{1}{n}$	nth-order Hadamard root
Ø	Hadamard (or Schur) (elementwise)
	division
♦	Khatri-Rao product
8	Kronecker Product
\times_n	<i>n</i> -mode product

5.4 Operations with matrices and tensors

\mathbf{A}^{-1}	Inverse matrix
$\mathbf{A}^{+}, \mathbf{A}^{\dagger}$	Moore-Penrose left pseudoinverse
$\mathbf{A}^{T}, \mathbf{A}^{T}, \mathbf{A}^{t}, \mathbf{A}^{t}$ [37]	Transpose

$\mathbf{A}^{-\top}$	Transpose of the inverse, i.e.,
	$(\mathbf{A}^{-1})^{T} = (\mathbf{A}^{T})^{-1} [21, 33]$
\mathbf{A}^*	Complex conjugate
\mathbf{A}^{H}	Hermitian
$\ \mathbf{A}\ _{\mathrm{F}}$	Frobenius norm
A	Matrix norm
$ \mathbf{A} , \det(\mathbf{A})$	Determinant
diag (A)	The elements in the diagonal of A
E [A]	Vectorization: stacks the columns of
	the matrix \mathbf{A} into a long column vec-
	tor
$E_d[A]$	Extracts the diagonal elements of a
	square matrix and returns them in a
	column vector
$\mathbf{E}_l\left[\mathbf{A}\right]$	Extracts the elements strictly below
	the main diagonal of a square matrix
	in a column-wise manner and returns
	them into a column vector
$\mathbf{E}_{u}\left[\mathbf{A}\right]$	Extracts the elements strictly above
	the main diagonal of a square matrix
	in a column-wise manner and returns
	them into a column vector
$\mathbf{E}_b\left[\mathbf{A}\right]$	Block vectorization operator: stacks
	square block matrices of the input
	into a long block column matrix
$\operatorname{unvec}\left(\mathbf{A}\right)$	Reshapes a column vector into a ma-
	trix
$\operatorname{tr}\{\mathbf{A}\}$	trace
$\overline{\mathbf{X}_{(n)}}$	<i>n</i> -mode matricization of the tensor \mathcal{X}

5.5 Operations with vectors

$\ \mathbf{a}\ $	l_1 norm, 1-norm, or Manhattan norm
$\ \mathbf{a}\ , \ \mathbf{a}\ _2$	l_2 norm, 2-norm, or Euclidean norm
$\ \mathbf{a}\ _p$	l_p norm, p -norm, or Minkowski norm
$\ \mathbf{a}\ _{\infty}$	l_{∞} norm, ∞ -norm, or Chebyshev
	norm
diag (a)	Diagonalization: a square, diagonal
	matrix with entries given by the vec-
	tor a

5.6 Decompositions

Λ	Eigenvalue matrix [39]
Q	Eigenvectors matrix; Orthogonal ma-
	trix of the QR decomposition[39]
R	Upper triangular matrix of the QR
	decomposition[39]
U	Left singular vectors[39]
$\frac{\mathrm{U}_r}{\Sigma}$	Left singular nondegenerated vectors
Σ	Singular value matrix
Σ_r	Singular value matrix with nonzero
	singular values in the main diagonal
Σ^+	Singular value matrix of the pseu-
	doinverse [39]
Σ_r^+	Singular value matrix of the pseu-
	doinverse with nonzero singular val-
	ues in the main diagonal
V	Right singular vectors [39]
$\overline{\mathbf{V}_r}$	Right singular nondegenerated vec-
	tors
$eig(\mathbf{A})$	Set of the eigenvalues of A [13, 30,
	33]
$\llbracket \mathbf{A}, \mathbf{B}, \mathbf{C}, \ldots bracket$	CANDECOMP/PARAFAC (CP) de-
	composition of the tensor \mathcal{X} from the
	outer product of column vectors of \mathbf{A} ,
	B, C,
$[\![\boldsymbol{\lambda}; \mathbf{A}, \mathbf{B}, \mathbf{C}, \ldots]\!]$	Normalized CANDE-
	COMP/PARAFAC (CP) decom-
	position of the tensor \mathcal{X} from the
	outer product of column vectors of
	A, B, C, \dots

5.7 Spaces and sets

5.7.1 Common spaces and sets

\mathbb{R}	Set of real numbers
a,b	Closed interval of a real set from a to
	b
(a,b)	Opened interval of a real set from a
	to b
$\overline{[a,b),(a,b]}$	Half-opened intervals of a real set
	from a to b
C	Set of complex numbers
\mathbb{Z}	Set of integer number

$\overline{\{1,2,\ldots,n\}}$	Discrete set containing the integer el-
	ements $1, 2, \ldots, n$
$\mathbb{B} = \{0, 1\}$	Boolean set
Ø	Empty set
N	Set of natural numbers
$\mathbb{K} \in \{\mathbb{R}, \mathbb{C}\}$	Real or complex space (field)
$\mathbb{K}^{I_1 \times I_2 \times \cdots \times I_N}$	$I_1 \times I_2 \times \cdots \times I_N$ -dimensional real (or
	complex) space
K ₊	Nonnegative real (or complex) space
	[10]
K++	Positive real (or complex) space, i.e.,
	$\mathbb{K}_{++} = \mathbb{K}_+ \setminus \{0\} \ [10]$
U	Universe
2^A	Power set of A

5.7.2 Convex sets (or spaces)

\mathbb{S}^n [15], \mathcal{S}^n [10]	Conic set of the symmetric matrices
	in $\mathbb{R}^{n \times n}$
$\mathbb{S}^n_+,\mathcal{S}^n_+$	Conic set of the symmetric positive
	semidefinite matrices in $\mathbb{R}^{n \times n}$ [10]
$\mathbb{S}^n_{++}, \mathcal{S}^n_{++}$	Conic set of the symmetric positive
	definite matrices in $\mathbb{R}^{n\times n}$, i.e., \mathbb{S}^n_{++} =
	$\mathbb{S}^n_+ \setminus \{0\} [10]$
\mathbb{H}^n	Set of all hermitian matrices in $\mathbb{C}^{n\times n}$
conv C	Convex hull
aff C	Affune hull
$\overline{\mathcal{R}}$	Ray
\mathcal{H}	Hyperplane
$\mathcal{H}_+, \mathcal{H}$	Positive/negative halfspace
$B(\mathbf{x}_c, r)$	Euclidean ball with radium r and
	centered at \mathbf{x}_c
\mathcal{E}	Ellipsoid
C	Norm cone
K	Proper cone
	Dual cone
$\frac{\mathcal{P}}{S}$	Polyhedra
	Simplex
C_{α}	α -sublevel set
epi f	Epigraph of the function f
hypo f	Hypograph of the function f

5.7.3 Spaces from matrices or vectors

$\mathrm{span}\left\{\mathbf{a}_1,\mathbf{a}_2,\ldots,\mathbf{a}_n\right\}$	Vector space spanned by the argu-
	ment vectors [21]
$C(\mathbf{A})$, columnspace(\mathbf{A}), range(\mathbf{A}),	Columnspace, range or image, i.e.,
$\operatorname{span} \{\mathbf{A}\}, \operatorname{image}(\mathbf{A})$	the space span $\{\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_n\}$, where
	\mathbf{a}_i is the ith column vector of the ma-
	trix A [31, 39]
$C(\mathbf{A}^{H})$	Row space (also called left
	columnspace) [31, 39]
$N(\mathbf{A})$, nullspace(\mathbf{A}), null(\mathbf{A}), kernel(\mathbf{A}	Nullspace (or kernel space) [31, 39,
	40]
$N(\mathbf{A}^{H})$	Left nullspace
rank A	Rank, that is, $\dim (\operatorname{span} \{A\}) =$
	$\dim \left(\mathrm{C} \left(\mathbf{A} \right) \right) \left[31 \right]$
nullity (A)	Nullity of \mathbf{A} , i.e., dim $(N(\mathbf{A}))$

5.8 Set operations

A + B	Set addition (Minkowski sum), i.e.,
	$\{\mathbf{v} \in \mathbb{R}^n \mid \mathbf{v} = \mathbf{x} + \mathbf{y}, \ \forall \ \mathbf{x} \in \mathcal{X} \land \mathbf{y} \in \mathcal{Y}\}$
	[28]
A - B	Minkowski difference, i.e.,
	$\{\mathbf{v} \in \mathbb{R}^n \mid \mathbf{v} = \mathbf{x} - \mathbf{y}, \ \forall \ \mathbf{x} \in \mathcal{X} \land \mathbf{y} \in \mathcal{Y}\}$
$A\ominus B$	Pontryagin difference, i.e.,
	$\{\mathbf{v} \in \mathbb{R}^n \mid \mathbf{v} + \mathbf{y} \in \mathcal{X}, \ \forall \ \mathbf{y} \in \mathcal{Y}\} $ [28]
$A \setminus B, A - B$	Set difference or set subtraction, i.e.,
	$A \setminus B = \{x x \in A \land x \notin B\}$ the set con-
	taining the elements of A that are not
	in $B[\overline{36}]$
$A \cup B$	Set of union
$A \cap B$	Set of intersection
$A \times B$	Cartesian product
A^n	$A \times A \times \cdots \times A$
	n times
A^{\perp}	Orthogonal complement of A , e.g.,
	$N(\mathbf{A}) = C(\mathbf{A}^{T})^{\perp} [10]$
$a \perp b$	a is orthogonal to b
a ∠ b	a is not orthogonal to b
$A \oplus B$	Direct sum, i.e., each $\mathbf{v} \in$
	$\{\sum \mathbf{a}_i \mid \mathbf{a}_i \in S_i, i = 1, \dots, k\}$ has a
	unique representation of $\sum \mathbf{a}_i$ with
	$\mathbf{a}_i \in S_i$. That is, they expand to a
	space. Note that $\{S_i\}$ might not be
	orthogonal each other [21]

$A\overset{\perp}{\oplus} B$	Direct sum of two spaces that are orthogonal and span a n -dimensional
	space, e.g., $C(\mathbf{A}^{T}) \stackrel{\perp}{\oplus} C(\mathbf{A}^{T})^{\perp} =$
	\mathbb{R}^n (this decomposition of \mathbb{R}^n is
	called the orthogonal decomposition
	induced by \mathbf{A}) [10]
\overline{A}, A^c	Complement set (given U)
#A, A	Cardinality of A
$a \in A$	a is element of A
$a \notin A$	a is not element of A

5.9 Inequalities

$\mathcal{X} \le 0$	Nonnegative tensor
$\mathbf{a} \leq_K \mathbf{b}$	Generalized inequality meaning that
	$\mathbf{b} - \mathbf{a}$ belongs to the conic subset K in
	the space $\mathbb{R}^n[10]$
$a <_K b$	Strict generalized inequality meaning
	that $\mathbf{b} - \mathbf{a}$ belongs to the interior of
	the conic subset K in the space $\mathbb{R}^n[10]$
$a \le b$	Generalized inequality meaning that
	$\mathbf{b} - \mathbf{a}$ belongs to the nonnegative or-
	thant conic subset, \mathbb{R}^n_+ , in the space
	$\mathbb{R}^n.[10]$
a < b	Strict generalized inequality meaning
	that $\mathbf{b} - \mathbf{a}$ belongs to the positive or-
	thant conic subset, \mathbb{R}^n_{++} , in the space
	$\mathbb{R}^n[10]$
$A \leq_K B$	Generalized inequality meaning that
	${\bf B}-{\bf A}$ belongs to the conic subset K
	in the space $\mathbb{S}^n[10]$
$A \prec_K B$	Strict generalized inequality meaning
	that $\mathbf{B} - \mathbf{A}$ belongs to the interior of
	the conic subset K in the space $\mathbb{S}^n[10]$
$A \leq B$	Generalized inequality meaning that
	$\mathbf{B} - \mathbf{A}$ belongs to the positive semidef-
	inite conic subset, \mathbb{S}_{+}^{n} , in the space
	$\mathbb{S}^n[10]$
A < B	Strict generalized inequality meaning
	that $\mathbf{B} - \mathbf{A}$ belongs to the positive or-
	thant conic subset, \mathbb{S}_{++}^n , in the space
	$\mathbb{S}^n[10]$

6 Communication systems

6.1 Common symbols

B	One-sided bandwidth of the trans-
	mitted signal, in Hz
W	One-sided bandwidth of the trans-
	mitted signal, in rad/s
x_i	Real or in-phase part of x
x_q	Imaginary or quadrature part of x
f_c, f_{RF}	Carrier frequency (in Hertz)
f_L	Carrier frequency in L-band (in
	Hertz)
$\frac{f_{IF}}{f_s}$	Intermediate frequency (in Hertz)
f_s	Sampling frequency or sampling rate
	(in Hertz)
T_s	Sampling time interval/duration/pe-
	riod
R	Bit rate
T	Bit interval/duration/period
T_c	Chip interval/duration/period
T_{sy}, T_{sym}	Symbol/signaling[34] interval/dura-
	tion/period
SRF	Transmitted signal in RF
s_{FI}	Transmitted signal in FI
s, s_l	Lowpass (or baseband) equivalent
	signal or envelope complex of trans-
	mitted signal
r_{RF}	Received signal in RF
r_{FI}	Received signal in FI
r, r_l	Lowpass (or baseband) equivalent
	signal or envelope complex of re-
	ceived signal
ϕ	Signal phase
ϕ_0	Initial phase
η_{RF}, w_{RF}	Noise in RF
η_{FI}, w_{FI}	Noise in FI
η , w	Noise in baseband
τ	Timing delay
$\Delta \tau$	Timing error (delay - estimated)
$\overline{\varphi}$	Phase offset
$\Delta \varphi$	Phase error (offset - estimated)
f_d	Linear Doppler frequency

Δf_d	Frequency error (Doppler frequency -
	estimated)
ν	Angular Doppler frequency
$\Delta \nu$	Frequency error (Doppler frequency -
	estimated)
γ, A	Transmitted signal amplitude
γ_0, A_0	Combined effect of the path loss and
	antenna gain

${\bf 6.2} \quad {\bf Fading\ multipath\ channels}$

$t \stackrel{\mathcal{F}}{\leftrightarrow} \lambda \ [34]$	Support temporal of the signal. λ is obtained after taking the Fourier transform on t .
$\tau \stackrel{\mathcal{F}}{\leftrightarrow} f \ [34]$	Second support temporal of the signal $(c(t))$ varies with with the input at the time τ). f is obtained after taking the Fourier transform on τ .
$c(t,\tau) [34]$	Complex envelope of the channel response at the time t due to an impulse
C(f, t) [94]	applied at the $t - \tau$
$\frac{C(f,t) [34]}{\alpha(t,\tau) [34]}$	Transfer function of $c(t,\tau)$ in τ
$\alpha(t,\tau)$ [54]	Attenuation of $c(t,\tau)$, i.e., $c(t,\tau) = \alpha(t,\tau)e^{e\pi f_c\tau}$
$R_c(\tau_1, \tau_2, \Delta t)$ [34]	Autocorrelation function of
, , , , , , , , , , , , , , , , , , ,	$c(t,\tau)$, i.e., $R_c(\tau_1,\tau_2,\Delta t) =$
	$\mathrm{E}\left[c^*(t,\tau_1),c^*(t+\Delta t,\tau_2)\right]$
$R_c(\tau, \Delta t)$ [34]	Autocorrelation function of $c(t, \tau)$ as-
	suming uncorrelated scattering
$R_c(\tau), R_c(\tau, \Delta t)\Big _{\Delta t=0}$ [34]	Multipath intensity profile or delay
-24-0	power spectrum
$R_C(\Delta f, \Delta t), R_C(f_1, f_2; \Delta t),$	Spaced-frequency, spaced-time corre-
$\mathrm{E}\left[C(f_1,t),C(f_2,t+\Delta t)\right],$	lation function $(\Delta f = f_2 - f_1)$
$\mathcal{F}_{\tau}\left\{R_{c}(\tau,\Delta t)\right\} [20]$	
$R_C(\Delta f), R_C(\Delta f, \Delta t) _{\Delta t=0} [34],$	Spaced-frequency correlation func-
$\mathcal{F}\left\{R_c(\tau)\right\} [20]$	tion
$(\Delta f)_c$	Coherence bandwidth of $c(t)$, that
	is, the frequency interval in which
	$R_C(\Delta f)$ is nonzero [34]
T_m	Multipath spread of the channel, that
	is, the time interval in which $R_c(\tau)$ is
	nonzero $(T_m \approx 1/(\Delta f)_c)$ [34]

$R_C(\Delta t), R_C(\Delta f, \Delta t)\Big _{\Delta f=0}$	Spaced-time correlation function [34]
$S_C(\lambda)$ [34], $\mathcal{F}\{R_C(\Delta t)\}$ [20]	Doppler power spectrum
$(\Delta t)_c$	Coherence time of $c(t)$, that is, the
	time interval in which $R_C(\Delta t)$ is
	nonzero [34]
B_m	Multipath spread of the channel, that
	is, the frequency interval in which
	$S_c(\lambda)$ is nonzero $(B_d \approx 1/(\Delta t)_c)$ [34]
$S_C(\tau,\lambda)$ [34], $\mathcal{F}_{\Delta f,\Delta t} \left\{ R_C(\Delta f,\Delta t) \right\}$	Scattering function
[20]	

7 Discrete mathematics

7.1 Quantifiers, inferences

\forall	For all (universal quantifier) [23]
3	There exists (existential quantifier)
	[23]
∄	There does not exist [23]
∃!	There exists an unique [23]
\exists_n	There exists exactly n [36]
€	Belongs to [23]
∉	Does not belong to [23]
:	Because [23]
<u> ,:</u>	Such that, sometimes that parenthe-
	ses is used [23]
$\overline{}$,,(·)	Used to separate the quantifier with
	restricted domain from its scope, e.g.,
	$\forall x < 0 (x^2 > 0) \text{ or } \forall x < 0, x^2 > 0$
	[23]
··	Therefore [23]

7.2 Propositional Logic

$\neg a$	Logical negation of a [36]
$a \wedge b$	Conjunction (logical AND) operator
	between a and $b[36]$
$a \lor b$	Disjunction (logical OR) operator be-
	tween a and $b[36]$
$a \oplus b$	Exclusive OR (logical XOR) operator
	between a and $b[36]$

$a \rightarrow b$	Implication (or conditional) state-
	ment[36]
$a \leftrightarrow b$	Bi-implication (or biconditional)
	statement, i.e., $(a \rightarrow b) \land (b \rightarrow a)$
	[36]
$a \equiv b, a \iff b, a \Leftrightarrow b$	Logical equivalence, i.e., $a \leftrightarrow b$ is a
	tautology[36]

7.3 Operations

a	Absolute value of a
log	Base-10 logarithm or decimal loga-
	rithm
ln	Natual logarithm
$Re\{x\}$	Real part of x
$\overline{\text{Im}\left\{x\right\}}$	Imaginary part of x
۷٠	Phase (complex argument)
$x \mod y$	Remainder, i.e., $x - y \lfloor x/y \rfloor$, for $y \neq 0$
x div y	Quotient [36]
$x \equiv y \pmod{m}$	Congruent, i.e., $m \setminus (x - y)$ [36]
$\operatorname{frac}(x)$	Fractional part, i.e., $x \mod 1$ [23]
$a \setminus b, a \mid b$	b is a positive integer multiple of a ,
	i.e., $\exists n \in \mathbb{Z}_{++} \mid b = na \ [23, 36]$
$a \not \setminus b, a \not \mid b$	b is not a positive integer multiple of
	$a, \text{ i.e., } \not\exists n \in \mathbb{Z}_{++} \mid b = na \ [23, 36]$
[·]	Ceiling operation [23]
[.]	Floor operation [23]

8 Vector Calculus

$\nabla f[38]$, grad $f[35]$	Vector differential operator (Nabla symbol), i.e., ∇f is the gradient of the scalar-valued function f , i.e., f : $\mathbb{R}^n \to \mathbb{R}$
t,(u,v)	Parametric variables commonly used,
	t for one variable, (u, v) for two vari-
	ables[38]
$l(x, y, z)$ [35], $\mathbf{r}(x, y, z)$ [38], $x\hat{\mathbf{i}} + y\hat{\mathbf{j}} + z\hat{\mathbf{k}}$	Vector position, i.e., (x, y, z) .
$\overline{1(t)}$	Vector position parametrized by t ,
	i.e., $(x(t), y(t), z(t))$ [35, 38]

1/(4) 31 /34	First desirative of 1(4) is the
$\mathbf{l}'(t), \mathrm{d}\mathbf{l}/\mathrm{d}t$	First derivative of $\mathbf{l}(t)$, i.e., the tangent vector of the curve
	tangent vector of the curve $(x(t), y(t), z(t))$ [38]
$\mathbf{u}(t)[29] \ \mathbf{T}(t)[38], \ \mathrm{dl}(t)[35]$	Tangent unit vector of $\mathbf{l}(t)$, i.e.,
$\mathbf{u}(t)[29] 1(t)[30], \mathbf{u}(t)[30]$	
$-\frac{1}{\left(\frac{y'(t)}{y'(t)} - \frac{y'(t)}{y'(t)} \right)}$	$\mathbf{u}(t) = \mathbf{l}'(t)/ \mathbf{l}'(t) $
$\mathbf{n}(t), \left(\frac{y'(t)}{ l'(t) }, -\frac{x'(t)}{ l'(t) }\right)$	Normal vector of $\mathbf{l}(t)$, i.e.,
-	$\mathbf{n}(t) \perp \mathbf{T}(t)[38]$
C	Contour that traveled by $\mathbf{l}(t)$, for $a \le t \le b$ [38]
L, L(C)	Total length of the contour C
	(which can be defined the vector
	\hat{l} , parametrized by t), i.e., $L_C =$
	$\int_a^b \mathbf{l}'(t) \mathrm{d}t [38]$
s(t)	Length of the arc, which can be de-
~(*)	fined by the vector \mathbf{l} and t , that is,
ds	$s(t) = \int_{a}^{t} \mathbf{l}'(u) \mathrm{d}u \ (s(b) = L)[38]$ Differential operator of the length of
us	the contour C , i.e., $ds = \mathbf{l}'(t) dt$ [38]
$\int_C f(1) \mathrm{d}s, \int_a^b f(1(t)) 1'(t) \mathrm{d}t$	Line integral of the function $f: \mathbb{R}^n \to$
$\int_C \int (\mathbf{I}) \mathrm{d}\mathbf{s}, \ \int_a \int (\mathbf{I}(t)) \mathbf{I}(t) \mathrm{d}t$	\mathbb{R} along the contour C . In the context
	of integrals in the complex plane, it
	is also called "contour integral"
θ [35]	Angle between the contour C and the
. [60]	vector field ${f F}$
$\int_C \mathbf{F} \cdot d\mathbf{l}, \ \int_a^b \mathbf{F}(\mathbf{l}(t)) \cdot \mathbf{l}'(t) dt \ [8, 38],$	Line integral of vector field F along
$ \int_{C} \mathbf{F} \cdot \mathbf{u} ds, \int_{C} \mathbf{F} \cos \theta ds [35] $ $ \int_{C} \mathbf{F} \cdot d\mathbf{u} [35] $	the contour C
$\int_{C} \mathbf{F} \cdot d\mathbf{u} \ [35]$	In the field of electromagnetics, it is
	common to apply the line integral be-
	tween the vector field ${f F}$ and the unit
	vector $\mathbf{u}(t)$. Therefore, this line inte-
	gral may appear as well
$\int_{\mathbf{a}}^{\mathbf{b}} \mathbf{F}, \int_{\mathbf{a}}^{\mathbf{b}} \mathbf{F} \cdot d\mathbf{l}$	Alternative notation to the line inte-
va va	gral, where the parametric variable t
	goes from a to b , making r goes from
	$\mathbf{l}(a) = \mathbf{a} \text{ to } \mathbf{l}(b) = \mathbf{b} [8]$
\oint_C, \oint_C	Line integral along the closed contour
	C. The arrow indicates the contour
	integral orientation, which is counter-
	clockwise, by default. In the context
	of integrals in the complex plane, it is
	also called "closed contour integral".

$ \not\vdash_S $	Surface integral over the closed sur-
	face S
l(u, v)	Vector position
	(x(u, v), y(u, v), z(u, v)) parametrized
	by (u, v)
\mathbf{l}_u	$(\partial x/\partial u, \partial y/\partial u, \partial z/\partial u)$
l_{ν}	$(\partial x/\partial v, \partial y/\partial v, \partial z/\partial v)$
$\mathrm{d}A$	Differential operator of a 2D area
	(denoted by D or R) in the \mathbb{R}^2 do-
	main. This differential operator can
	be solved in different ways (rectangu-
	lar, polar, cylindric, etc) [38]
D,R	Integration domain in which dA is
	integrated, i.e., $\iint_D f dA$. R is pre-
	ferred when the integration domain
	is a rectangle, while $\stackrel{\circ}{D}$ is used when
	it has nonrectangular shape [38]
S	Smooth surface $S \subset \mathbb{R}^3$, i.e., a 2D
	area in a 3D space
$\mathrm{d}S$, $ \mathbf{l}_u \times \mathbf{l}_v $ $\mathrm{d}A$	Differential operator of a 2D area in
/ W V	a 3D domain (an surface). Note that
	$dS = \mathbf{l}_u \times \mathbf{l}_v dA$ should be accompa-
	nied with the change of the integra-
	tion interval(from S to D)
$A(S), \iint_S dS, \iint_D \mathbf{l}_u \times \mathbf{l}_v dA$	Area of the surface S parametrized by
$J_{J} = J_{J} = J_{J$	(u, v), in which dA is the area defined
	in the D domain (which is form by
	the u -by- v graph)
$\mathrm{d}V$	Differential operator of a shape vol-
	ume (denoted by E) in \mathbb{R}^3 domain,
	i.e., $\iiint_E dV = V$
E	Integration domain in which dV is in-
	tegrated, i.e., $\iiint_E f dV$ [38]
$V, \iint_D f \mathrm{d}A, \iiint_E f \mathrm{d}V$	Volume of the function f over the re-
W.E	gions D (in the case of double inte-
	grals) or E (in the case of triple inte-
	grals)
$\iint_{S} f \mathrm{d}S, \iint_{D} f \mathbf{l}_{u} \times \mathbf{l}_{v} \mathrm{d}A$	Surface integral over S
$\iint_{S} f dS, \iint_{D} f \mathbf{l}_{u} \times \mathbf{l}_{v} dA$ $\mathbf{n}(u, v), \frac{\mathbf{l}_{u}(u, v) \times \mathbf{l}_{v}(u, v)}{ \mathbf{l}_{u}(u, v) \times \mathbf{l}_{v}(u, v) }$	Normal vector of of the smooth surface S
$\iint_{\mathbf{S}} \mathbf{F} \cdot \mathbf{n} \mathrm{d}S$, $\iint_{\mathbf{S}} \mathbf{F} \cdot \mathrm{d}\mathbf{S}$,	Flux integral of vector field ${f F}$ through
$\iint_D \mathbf{F} \cdot (\mathbf{l}_u \times \mathbf{l}_v) \mathrm{d}A$	the smooth surface S ($\mathbf{n} dS \triangleq d\mathbf{S}$)

$ \oint_{S} \mathbf{F} \cdot \mathbf{n} dS, \oint_{S} \mathbf{F} \cdot d\mathbf{S}, $	Flux integral of vector field ${f F}$ through
$\iint_{D} \mathbf{F} \cdot (\mathbf{l}_{u} \times \mathbf{l}_{v}) \mathrm{d}A$	the smooth and closed surface S
JJD	$(\mathbf{n} \mathrm{d} S \triangleq \mathrm{d} \mathbf{S})$
$\nabla \times \mathbf{F}$, curl \mathbf{F}	Curl (rotacional) of the vector field ${f F}$
$\nabla \cdot \mathbf{F}, \operatorname{div} \mathbf{F}$	Divercence of the vector field ${f F}$
$\nabla^2 f, \nabla \cdot (\nabla f), \Delta f,$	Scalar Laplacian operator (per-
$\partial^2 f/\partial x^2 + \partial^2 f/\partial y^2 + \partial^2 f/\partial z^2$	formed on a scalar-valued function
	$f: \mathbb{R}^n \to \mathbb{R}$
$\overline{\nabla^2 \mathbf{F}, \nabla \times \nabla \times \mathbf{F} - \nabla(\nabla \cdot \mathbf{F}), \Delta \mathbf{F},}$	Vector Laplacian operator (per-
$(\partial^2 \mathbf{F}/\partial x^2, \partial^2 \mathbf{F}/\partial y^2, \partial^2 \mathbf{F}/\partial z^2)$	formed on a vector field, i.e., a
	vector-valued function, $\mathbf{F} : \mathbb{R}^n \to$
	\mathbb{R}^n). ∇^2 denotes the scalar (vector)
	Laplacian if the function is scalar-
	valued (vector-valued). The notation
	Δ must be avoided as it is overused
	in many contexts

9 Electromagnetic waves

Φ	Electric flux (scalar) (in V m)
Н	Magnetic field vector (in A/m)
В	Magnetic flux density vector (in
	$Wb/m^2 = T$
$\Phi[14]$	Magnetic flux
$q_{ m f},q_{ m free},Q_{ m free}[18]$	Free electric charge (in C)
$q_{ m b},q_{ m bound},Q_{ m bound}[18]$	Bound electric charge (in C)
$q, q_{\rm f} + q_{\rm b}$	Electric charge (in C)
$\rho_{\rm f}[1], \rho_{\rm free}$ [18]	Free electric charge density
$\rho_{\rm b}[1], \rho_{\rm bound}$ [18]	Electric charge density
$\rho, \rho_{\rm f} + \rho_{\rm b}$	Electric charge density (it can be
	in C/m^3 , C/m^2 or C/m depending
	whether it is a volume, surface, or
	line shapes)
f [35], F [2]	Electrostatic force (Coulomb force),
	$(\text{in kg m/s}^2).$
ε	Electric permittivity(in F/m). If the
	medium is isotropic, it is a scalar. If
	it is anisotropic, it is a tensor. [35]
$\overline{\varepsilon_r}$	Relative electric permittivity or di-
	electric constant (in F/m) [35]
ϵ_0	Electric permittivity in vacuum,
	$8.854 \times 10^{-12} \mathrm{F/m}$ [35]

E	Electric field vector (in V/m)
σ	Electric conductivity (in S/m)
J	Electric current density vector (in
	$\mathrm{A/m^2})$
$J_m[14]$	Magnetization current density vector
	(in A/m^2)
D	Electric flux density, electric dis-
	placement, or electric induction vec-
	tor (in C/m^2)
\overline{U}	Electric potential energy
$V[3, 14], \Phi[35]$	Electric potential (in voltage, V).
	However, keep in mind that there is
	a subtle difference between both def-
	initions [4]
$\Phi_E[19], \oiint_S \mathbf{E} \mathrm{d}\mathbf{S}$	Electric flux (in V m)
$\Phi_D[18], \varPsi[35], \oiint_S \mathbf{D} d\mathbf{S}$	Electric flux (D -field flux)
P	Electric polarization of the material
	$(in C/m^2)$
χ_e	Electric susceptibility (for linear and
	isotropic materials)
μ	Magnetic permeability
μ_0	Magnetic permeability in vacuum

10 Generic mathematical symbols

■.	Q.E.D.
	Equal by definition
:=,←	Assignment [36]
≠	Not equal
∞	Infinity
i	${\sqrt{-1}}$

11 Abbreviations

PS: Only names of methods and algorithms, technical abbreviations, and mathematical functions are considered.

With respect to
Subject to
If and only if
Eigenvalue decomposition, or eigendecomposition [31]

DNN	Deep Neural Network
DL	Deep Learning
ANN	Artificial Neural Networks [22]
NN	Nearest Neighbor
AI	Artificial Intelligence
SVD	Singular value decomposition
CP	CANDECOMP/PARAFAC
SGD	Stochastic gradient descent
SVM	Support vector machine
BPNN	Backpropagation neural network [27]
RBF	Radial basis function
OLS	Ordinary Least Squares
LMS	Least Mean Squares

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