

Notation

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1 Font notation

$a, b, c, \dots, A, B, C, \dots$	Scalars
$\mathbf{a}, \mathbf{b}, \mathbf{c}, \dots$	Vectors
$\mathbf{A}, \mathbf{B}, \mathbf{C}, \dots$	Matrices
$\mathcal{A}, \mathcal{B}, \mathcal{C}, \dots$	Tensors
$A, B, C, \dots, \mathcal{A}, \mathcal{B}, \mathcal{C}, \dots, \mathbb{A}, \mathbb{B}, \mathbb{C}, \dots$	Sets

2 Signals and functions

2.1 Time indexing

$x(t)$	Continuous-time t
$x[n], x[k], x[m], x[i], \dots$	Discrete-time n, k, m, i, \dots (parenthesis should be adopted only if there are no continuous-time signals in the context to avoid ambiguity)
$x_n, x_k, x_m, x_i, \dots$	
$x(n), x(k), x(m), x(i), \dots$	
$x[((n-m))_N], x((n-m))_N$	Circular shift in m samples within a N -samples window

2.2 Common functions

$\delta(t)$	Delta function
$\delta[n], \delta_{i,j}$	Kronecker function ($n = i - j$)
$h(t), h[n]$	Impulse response (continuous and discrete time)

$\tilde{x}[n], \tilde{x}(t)$	Periodic discrete- or continuous-time signal
$\hat{x}[n], \hat{x}(t)$	Estimate of $x[n]$ or $x(t)$
$\dot{x}[m]$	Interpolation of $x[n]$

2.3 Operations and symbols

$f : A \rightarrow B$	A function f whose domain is A and codomain is B
$f^n, x^n(t), x^n[k]$	n th power of the function f , $x[n]$ or $x(t)$
$f^{(n)}, x^{(n)}(t)$	n th derivative of the function f or $x(t)$
$f', f^{(1)}, x'(t)$	1th derivative of the function f or $x(t)$
$f'', f^{(2)}, x''(t)$	2th derivative of the function f or $x(t)$
$f \circ g$	Composition of the functions f and g
$*$	Convolution (discrete or continuous)
$\otimes, \textcircled{\mathbb{N}}$	Circular convolution

2.4 Transformations

$\mathcal{F}\{\cdot\}$	Fourier transform
$\mathcal{L}\{\cdot\}$	Laplace transform
$\mathcal{Z}\{\cdot\}$	z -transform
$\hat{x}(t), \hat{x}[n]$	Hilbert transform of $x(t)$ or $x[n]$
$X(s)$	Laplace transform of $x(t)$
$X(f)$	Fourier transform (FT) (in linear frequency, Hz) of $x(t)$
$X(j\omega)$	Fourier transform (FT) (in angular frequency, rad/sec) of $x(t)$
$X(e^{j\omega})$	Discrete-time Fourier transform (DTFT) of $x[n]$
$X[k], X(k), X_k$	Discrete Fourier transform (DFT) or fast Fourier transform (FFT) of $x[n]$, or even the Fourier series (FS) of the periodic signal $x(t)$
$\tilde{X}[k], \tilde{X}(k), \tilde{X}_k$	Discrete Fourier series (DFS) of $\tilde{x}[n]$
$X(z)$	z -transform of $x[n]$

3 Probability, statistics, and stochastic processes

3.1 Operators and symbols

$E[\cdot]$	Statistical expectation
$E_u[\cdot]$	Statistical expectation with respect to u
μ_x	Mean of the random variable x
$\mathbf{\mu}_x, \mathbf{m}_x$	Mean vector of the random variable \mathbf{x}
μ_n	n th-order moment of a random variable
\mathcal{K}_x, μ_4	Kurtosis (4th-order moment) of the random variable x
$\text{VAR}[\cdot]$	Variance operator
$\text{VAR}_u[\cdot]$	Variance operator with respect to u
κ_n	n th-order cumulant of a random variable
σ_x, κ_2	Variance of the random variable x
$\rho_{x,y}$	Pearson correlation coefficient between x and y
$a \sim P$	Random variable a with distribution P
\mathcal{R}	Rayleigh's quotient

3.2 Stochastic processes

$r_x(\tau), R_x(\tau)$	Autocorrelation function of the signal $x(t)$ or $x[n]$
$S_x(f), S_x(j\omega)$	Power spectral density (PSD) of $x(t)$ in linear (f) or angular (ω) frequency
$S_{x,y}(f), S_{x,y}(j\omega)$	Cross PSD of $x(t)$ and $y(t)$ in linear or angular (ω) frequency
\mathbf{R}_x	(Auto)correlation matrix of $\mathbf{x}(n)$
$r_{x,d}(\tau), R_{x,d}(\tau)$	Cross-correlation between $x[n]$ and $d[n]$ or $x(t)$ and $d(t)$
\mathbf{R}_{xy}	Cross-correlation matrix of $\mathbf{x}(n)$ and $\mathbf{y}(n)$
\mathbf{p}_{xd}	Cross-correlation vector between $\mathbf{x}(n)$ and $d(n)$
$c_x(\tau), C_x(\tau)$	Autocovariance function of the signal $x(t)$ or $x[n]$
$\mathbf{C}_x, \mathbf{K}_x, \mathbf{\Sigma}_x$	(Auto)covariance matrix of \mathbf{x}

$c_{xy}(\tau), C_{xy}(\tau)$

Cross-covariance function of the signal $x(t)$ or $x[n]$

$\mathbf{C}_{xy}, \mathbf{K}_{xy}, \mathbf{\Sigma}_{xy}$

Cross-covariance matrix of \mathbf{x} and \mathbf{y}

3.3 Functions

$Q(\cdot)$

Q -function, i.e., $P[\mathcal{N}(0, 1) > x]$

$\text{erf}(\cdot)$

Error function

$\text{erfc}(\cdot)$

Complementary error function i.e., $\text{erfc}(x) = 2Q(\sqrt{2}x) - \text{erf}(x)$

$P[A]$

Probability of the event or set A

$p(\cdot), f(\cdot)$

Probability density function (PDF) or probability mass function (PMF)

$p(x | A)$

Conditional PDF or PMF

$F(\cdot)$

Cumulative distribution function (CDF)

$\Phi_x(\omega), M_x(j\omega), E[e^{j\omega x}]$

First characteristic function (CF) of x

$M_x(t), \Phi_x(-jt), E[e^{tx}]$

Moment-generating function (MGF) of x

$\Psi_x(\omega), \ln \Phi_x(\omega), \ln E[e^{j\omega x}]$

Second characteristic function

$K_x(t), \ln E[e^{tx}], \ln M_x(t)$

Cumulant-generating function (CGF) of x

3.4 Distributions

$\mathcal{N}(\mu, \sigma^2)$

Gaussian distribution of a random variable with mean μ and variance σ^2 . The same notation can be used to denote a real-valued white Gaussian process with mean equal to μ and power spectral density equal to $N_0/2$, e.g., $s(t) \sim \mathcal{N}(\mu, N_0/2)$

$\mathcal{CN}(\mu, \sigma^2)$

Complex Gaussian distribution of a random variable with mean μ and variance σ^2 . The same notation can be used to denote a complex-valued white Gaussian process with mean equal to μ and power spectral density equal to N_0 , e.g., $s(t) \sim \mathcal{CN}(\mu, N_0)$

$\mathcal{N}(\mathbf{\mu}, \mathbf{\Sigma})$

Gaussian distribution of a vector random variable with mean $\mathbf{\mu}$ and covariance matrix $\mathbf{\Sigma}$

$\mathcal{CN}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$	Complex Gaussian distribution of a vector random variable with mean $\boldsymbol{\mu}$ and covariance matrix $\boldsymbol{\Sigma}$
$\mathcal{U}(a, b)$	Uniform distribution from a to b
$\chi^2(n), \chi_n^2$	Chi-square distribution with n degree of freedom (assuming that the Gaussians are $\mathcal{N}(0, 1)$)
$\text{Exp}(\lambda)$	Exponential distribution with rate parameter λ
$\Gamma(\alpha, \beta)$	Gamma distribution with shape parameter α and rate parameter β
$\Gamma(\alpha, \theta)$	Gamma distribution with shape parameter α and scale parameter $\theta = 1/\beta$
$\text{Nakagami}(m, \Omega)$	Nakagami-m distribution with shape parameter m and spread parameter Ω
$\text{Rayleigh}(\sigma)$	Rayleigh distribution with scale parameter σ
$\text{Rayleigh}(\Omega)$	Rayleigh distribution with the second moment $\Omega = E[x^2] = 2\sigma^2$
$\text{Rice}(s, \sigma)$	Rice distribution with noncentrality parameter (specular component) s and σ
$\text{Rice}(A, K)$	Rice distribution with Rice factor $K = s^2/2\sigma^2$ and scale parameter $A = s^2 + 2\sigma^2$

4 Statistical signal processing

$\nabla f, \mathbf{g}$	Gradient descent vector
$\nabla_x f, \mathbf{g}_x$	Gradient descent vector with respect x
\mathbf{g} (or $\hat{\mathbf{g}}$ if the gradient vector is \mathbf{g})	Stochastic gradient descent (SGD)
$J(\cdot), \mathcal{E}(\cdot)$	Cost-function or objective function
$\Lambda(\cdot)$	Likelihood function
$\Lambda_l(\cdot)$	Log-likelihood function
$\hat{x}(t)$ or $\hat{x}[n]$	Estimate of $x(t)$ or $x[n]$
$\hat{\boldsymbol{\mu}}_x, \hat{\mathbf{m}}_x$	Sample mean of $x[n]$ or $x(t)$
$\hat{\boldsymbol{\mu}}_{\mathbf{x}}, \hat{\mathbf{m}}_{\mathbf{x}}$	Sample mean vector of $\mathbf{x}[n]$ or $\mathbf{x}(t)$
$\hat{r}_x(\tau), \hat{R}_x(\tau)$	Estimated autocorrelation function of the signal $x(t)$ or $x[n]$
$\hat{S}_x(f), \hat{S}_x(j\omega)$	Estimated power spectral density (PSD) of $x(t)$ in linear (f) or angular (ω) frequency

$\hat{\mathbf{R}}_x$	Sample (auto)correlation matrix
$\hat{r}_{x,d}(\tau), \hat{R}_{x,d}(\tau)$	Estimated cross-correlation between $x[n]$ and $d[n]$ or $x(t)$ and $d(t)$
$\hat{S}_{x,y}(f), \hat{S}_{x,y}(j\omega)$	Estimated cross PSD of $x(t)$ and $y(t)$ in linear or angular (ω) frequency
$\hat{\mathbf{R}}_{xy}$	Sample cross-correlation matrix of \mathbf{R}_{xy}
$\hat{\rho}_{x,y}$	Estimated Pearson correlation coefficient between x and y
$\hat{c}_x(\tau), \hat{C}_x(\tau)$	Estimated autocovariance function of the signal $x(t)$ or $x[n]$
$\hat{\mathbf{C}}_x, \hat{\mathbf{K}}_x, \hat{\Sigma}_x$	Sample (auto)covariance matrix
$\hat{c}_{xy}(\tau), \hat{C}_{xy}(\tau)$	Estimated cross-covariance function of the signal $x(t)$ or $x[n]$
$\hat{\mathbf{C}}_{xy}, \hat{\mathbf{K}}_{xy}, \hat{\Sigma}_{xy}$	Sample cross-covariance matrix
$\mathbf{w}, \boldsymbol{\theta}$	Parameters, coefficients, or weights vector
$\mathbf{w}_o, \mathbf{w}^*, \boldsymbol{\theta}_o, \boldsymbol{\theta}^*$	Optimum value of the parameters, coefficients, or weights vector
\mathbf{W}	Matrix of the weights
\mathbf{J}	Jacobian matrix
\mathbf{H}	Hessian matrix
$\hat{\mathbf{H}}$	Estimate of the Hessian matrix

5 Linear Algebra

5.1 Common matrices and vectors

\mathbf{W}, \mathbf{D}	Diagonal matrix
\mathbf{P}	Projection matrix; Permutation matrix
\mathbf{J}	Jordan matrix
\mathbf{L}	Lower matrix
\mathbf{U}	Upper matrix
\mathbf{C}	Cofactor matrix
$\mathbf{C}_A, \text{cof}(\mathbf{A})$	Cofactor matrix of \mathbf{A}
\mathbf{S}	Symmetric matrix
\mathbf{Q}	Orthogonal matrix
\mathbf{I}_N	$N \times N$ -dimensional identity matrix
$\mathbf{0}_{M \times N}$	$M \times N$ -dimensional null matrix
$\mathbf{0}_N$	N -dimensional null vector
$\mathbf{1}_{M \times N}$	$M \times N$ -dimensional ones matrix
$\mathbf{1}_N$	N -dimensional ones vector

$\mathbf{0}$	Null matrix, vector, or tensor (dimensionality understood by context)
$\mathbf{1}$	Ones matrix, vector, or tensor (dimensionality understood by context)

5.2 Indexing

$x_{i_1, i_2, \dots, i_N}, [\mathcal{X}]_{i_1, i_2, \dots, i_N}$	Element in the position (i_1, i_2, \dots, i_N) of the tensor \mathcal{X}
$\mathcal{X}^{(n)}$	n th tensor of a nontemporal sequence
$\mathbf{x}_n, \mathbf{X}_{:,n}$	n th column of the matrix X
\mathbf{x}_n	n th row of the matrix X
$\mathbf{X}_{i_1, \dots, i_{n-1}, :, i_{n+1}, \dots, i_N}$	Mode- n fiber of the tensor \mathcal{X}
$\mathbf{X}_{:, i_2, i_3}$	Column fiber (mode-1 fiber) of the thrid-order tensor \mathcal{X}
$\mathbf{X}_{i_1, :, i_3}$	Row fiber (mode-2 fiber) of the thrid-order tensor \mathcal{X}
$\mathbf{X}_{i_1, i_2, :}$	Tube fiber (mode-3 fiber) of the thrid-order tensor \mathcal{X}
$\mathbf{X}_{i_1, :, :}$	Horizontal slice of the thrid-order tensor \mathcal{X}
$\mathbf{X}_{:, i_2, :}$	Lateral slices slice of the thrid-order tensor \mathcal{X}
$\mathbf{X}_{i_3}, \mathbf{X}_{:, :, i_3}$	Frontal slices slice of the thrid-order tensor \mathcal{X}

5.3 General operations

$\langle \cdot, \cdot \rangle$	Inner product, e.g., $\langle \mathbf{a}, \mathbf{b} \rangle = \mathbf{a}^\top \mathbf{b}$
\circ	Outer product, e.g., $\mathbf{a} \circ \mathbf{b} = \mathbf{a} \mathbf{b}^\top$
\otimes	Kronecker product
\odot	Hadamard (or Schur) (elementwise) product
$\cdot^{\odot n}$	n th-order Hadamard power
$\cdot^{\odot \frac{1}{n}}$	n th-order Hadamard root
\oslash	Hadamard (or Schur) (elementwise) division
\diamond	Khatri-Rao product
\otimes	Kronecker Product
\times_n	n -mode product

5.4 Operations with matrices and tensors

\mathbf{A}^{-1}	Inverse matrix
$\mathbf{A}^+, \mathbf{A}^\dagger$	Moore-Penrose left pseudoinverse
\mathbf{A}^\top	Transpose
$\mathbf{A}^{-\top}$	Transpose of the inverse
\mathbf{A}^*	Complex conjugate
\mathbf{A}^H	Hermitian
$\ \mathbf{A}\ _F$	Frobenius norm
$\ \mathbf{A}\ $	Matrix norm
$ \mathbf{A} , \det(\mathbf{A})$	Determinant
$\text{diag}(\mathbf{A})$	The elements in the diagonal of \mathbf{A}
$\text{vec}(\mathbf{A})$	Vectorization: stacks the columns of the matrix \mathbf{A} into a long column vector
$\text{vec}_d(\mathbf{A})$	Extracts the diagonal elements of a square matrix and returns them in a column vector
$\text{vec}_l(\mathbf{A})$	Extracts the elements strictly below the main diagonal of a square matrix in a column-wise manner and returns them into a column vector
$\text{vec}_u(\mathbf{A})$	Extracts the elements strictly above the main diagonal of a square matrix in a column-wise manner and returns them into a column vector
$\text{vec}_b(\mathbf{A})$	Block vectorization operator: stacks square block matrices of the input into a long block column matrix
$\text{unvec}(\mathbf{A})$	Reshapes a column vector into a matrix
$\text{tr}(\mathbf{A})$	trace
$\mathbf{X}_{(n)}$	n -mode matricization of the tensor \mathcal{X}

5.5 Operations with vectors

$\ \mathbf{a}\ $	l_1 norm, 1-norm, or Manhattan norm
$\ \mathbf{a}\ , \ \mathbf{a}\ _2$	l_2 norm, 2-norm, or Euclidean norm
$\ \mathbf{a}\ _p$	l_p norm, p -norm, or Minkowski norm
$\ \mathbf{a}\ _\infty$	l_∞ norm, ∞ -norm, or Chebyshev norm
$\text{diag}(\mathbf{a})$	Diagonalization: a square, diagonal matrix with entries given by the vector \mathbf{a}

5.6 Decompositions

\mathbf{A}	Eigenvalue matrix
\mathbf{Q}	Eigenvectors matrix; Orthogonal matrix of the QR decomposition
\mathbf{R}	Upper triangular matrix of the QR decomposition
\mathbf{U}	Left singular vectors
\mathbf{U}_r	Left singular nondegenerated vectors
$\mathbf{\Sigma}$	Singular value matrix
$\mathbf{\Sigma}_r$	Singular value matrix with nonzero singular values in the main diagonal
$\mathbf{\Sigma}^+$	Singular value matrix of the pseudoinverse
$\mathbf{\Sigma}_r^+$	Singular value matrix of the pseudoinverse with nonzero singular values in the main diagonal
\mathbf{V}	Right singular vectors
\mathbf{V}_r	Right singular nondegenerated vectors
$\text{eig}(\mathbf{A})$	Set of the eigenvalues of \mathbf{A}
$\llbracket \mathbf{A}, \mathbf{B}, \mathbf{C}, \dots \rrbracket$	CANDECOMP/PARAFAC (CP) decomposition of the tensor \mathcal{X} from the outer product of column vectors of $\mathbf{A}, \mathbf{B}, \mathbf{C}, \dots$
$\llbracket \boldsymbol{\lambda}; \mathbf{A}, \mathbf{B}, \mathbf{C}, \dots \rrbracket$	Normalized CANDECOMP/PARAFAC (CP) decomposition of the tensor \mathcal{X} from the outer product of column vectors of $\mathbf{A}, \mathbf{B}, \mathbf{C}, \dots$

5.7 Spaces

$\text{span}(\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_n)$	Vector space spanned by the argument vectors
$\mathbf{C}(\mathbf{A}), \text{columnspace}(\mathbf{A}), \text{range}(\mathbf{A}), \text{span}(\mathbf{A}), \text{image}(\mathbf{A})$	Columnspace, range or image, i.e., the space $\text{span}(\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_n)$, where \mathbf{a}_i is the i th column vector of the matrix \mathbf{A}
$\mathbf{C}(\mathbf{A}^H)$	Row space
$\mathbf{N}(\mathbf{A}), \text{nullspace}(\mathbf{A}), \text{kernel}(\mathbf{A})$	Nullspace (or kernel space)
$\mathbf{N}(\mathbf{A}^H)$	Left nullspace
$\text{rank}(\mathbf{A})$	Rank, that is, $\dim(\text{span}(\mathbf{A})) = \dim(\mathbf{C}(\mathbf{A}))$
$\text{nullity}(\mathbf{A})$	Nullity of \mathbf{A} , i.e., $\dim(\mathbf{N}(\mathbf{A}))$
$\mathbf{a} \perp \mathbf{b}$	\mathbf{a} is orthogonal to \mathbf{b}
$\mathbf{a} \not\perp \mathbf{b}$	\mathbf{a} is not orthogonal to \mathbf{b}

5.8 Inequalities

$$\mathcal{X} \leq 0$$

$$\mathbf{a} \preceq_K \mathbf{b}$$

$$\mathbf{a} \prec_K \mathbf{b}$$

$$\mathbf{a} \leq \mathbf{b}$$

$$\mathbf{a} < \mathbf{b}$$

$$\mathbf{A} \preceq_K \mathbf{B}$$

$$\mathbf{A} \prec_K \mathbf{B}$$

$$\mathbf{A} \leq \mathbf{B}$$

$$\mathbf{A} < \mathbf{B}$$

Nonnegative tensor

Generalized inequality meaning that $\mathbf{b} - \mathbf{a}$ belongs to the conic subset K in the space \mathbb{R}^n

Strict generalized inequality meaning that $\mathbf{b} - \mathbf{a}$ belongs to the interior of the conic subset K in the space \mathbb{R}^n

Generalized inequality meaning that $\mathbf{b} - \mathbf{a}$ belongs to the nonnegative orthant conic subset, \mathbb{R}_+^n , in the space \mathbb{R}^n .

Strict generalized inequality meaning that $\mathbf{b} - \mathbf{a}$ belongs to the positive orthant conic subset, \mathbb{R}_{++}^n , in the space \mathbb{R}^n

Generalized inequality meaning that $\mathbf{B} - \mathbf{A}$ belongs to the conic subset K in the space \mathbb{S}^n

Strict generalized inequality meaning that $\mathbf{B} - \mathbf{A}$ belongs to the interior of the conic subset K in the space \mathbb{S}^n

Generalized inequality meaning that $\mathbf{B} - \mathbf{A}$ belongs to the positive semidefinite conic subset, \mathbb{S}_+^n , in the space \mathbb{S}^n

Strict generalized inequality meaning that $\mathbf{B} - \mathbf{A}$ belongs to the positive orthant conic subset, \mathbb{S}_{++}^n , in the space \mathbb{S}^n

6 Sets

$$A + B$$

$$A - B$$

$$A \setminus B, A - B$$

$$A \cup B$$

$$A \cap B$$

$$A \times B$$

$$A^n$$

Set addition (Minkowski sum)

Minkowski difference

Set difference or set subtraction, i.e., the set containing the elements of A that are not in B

Set of union

Set of intersection

Cartesian product

$$\underbrace{A \times A \times \cdots \times A}_{n \text{ times}}$$

n times

A^\perp	Orthogonal complement of A , e.g., $N(\mathbf{A}) = C(\mathbf{A}^\top)^\perp$
$A \oplus B$	Direct sum, e.g., $C(\mathbf{A}^\top) \oplus C(\mathbf{A}^\top)^\perp = \mathbb{R}^n$
A^c, \bar{A}	Complement set (given U)
$\#A, A $	Cardinality
$a \in A$	a is element of A
$a \notin A$	a is not element of A
$\{1, 2, \dots, n\}$	Discrete set containing the integer elements $1, 2, \dots, n$
U	Universe
2^A	Power set of A
\mathbb{R}	Set of real numbers
\mathbb{C}	Set of complex numbers
\mathbb{Z}	Set of integer number
$\mathbb{B} = \{0, 1\}$	Boolean set
\emptyset	Empty set
\mathbb{N}	Set of natural numbers
$\mathbb{K} \in \{\mathbb{R}, \mathbb{C}\}$	Real or complex space (field)
$\mathbb{K}^{I_1 \times I_2 \times \dots \times I_N}$	$I_1 \times I_2 \times \dots \times I_N$ -dimensional real (or complex) space
\mathbb{K}_+	Nonnegative real (or complex) space
\mathbb{K}_{++}	Positive real (or complex) space, i.e., $\mathbb{K}_{++} = \mathbb{K}_+ \setminus \{\mathbf{0}\}$
$\mathbb{S}^n, \mathcal{S}^n$	Conic set of the symmetric matrices in $\mathbb{R}^{n \times n}$
$\mathbb{S}_+^n, \mathcal{S}_+^n$	Conic set of the symmetric positive semidefinite matrices in $\mathbb{R}^{n \times n}$
$\mathbb{S}_{++}^n, \mathcal{S}_{++}^n$	Conic set of the symmetric positive definite matrices in $\mathbb{R}^{n \times n}$, i.e., $\mathbb{S}_{++}^n = \mathbb{S}_+^n \setminus \{\mathbf{0}\}$
\mathbb{H}^n	Set of all hermitian matrices in $\mathbb{C}^{n \times n}$
$[a, b]$	Closed interval of a real set from a to b
(a, b)	Opened interval of a real set from a to b
$[a, b), (a, b]$	Half-opened intervals of a real set from a to b

7 Communication systems

B	One-sided bandwidth of the transmitted signal, in Hz
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W	One-sided bandwidth of the transmitted signal, in rad/s
x_i	Real or in-phase part of x
x_q	Imaginary or quadrature part of x
s_{RF}	Transmitted signal in RF
s_{FI}	Transmitted signal in FI
s, s_l	Low-pass equivalent signal or envelope complex of transmitted signal
r_{RF}	Received signal in RF
r_{FI}	Received signal in FI
r, r_l	Low-pass equivalent signal or envelope complex of received signal
ϕ	Signal phase
η_{RF}, w_{RF}	Noise in RF
η_{FI}, w_{FI}	Noise in FI
η, w	Noise in baseband
τ	Timing delay
$\Delta\tau$	Timing error (delay - estimated)
φ	Phase offset
$\Delta\varphi$	Phase error (offset - estimated)
f_d	Linear Doppler frequency
Δf_d	Frequency error (Doppler frequency - estimated)
ν	Angular Doppler frequency
$\Delta\nu$	Frequency error (Doppler frequency - estimated)
γ	Transmitted signal amplitude
γ_0	Combined effect of the path loss and antenna gain

8 Other notations

8.1 Mathematical symbols

\exists	There exists
\nexists	There does not exist
$\exists!$	There exist an unique
\in	Belongs to
\notin	Does not belong to
■	Q.E.D.
\therefore	Therefore
\because	Because
\forall	For all
$, :$	Such that

\Longleftrightarrow	Logical equivalence
$\triangleq, :=$	Equal by definition
\neq	Not equal
∞	Infinity
j	$\sqrt{-1}$
W_N	Twiddle factor, $e^{-j\frac{2\pi}{N}}$

8.2 Operations

$\arg \max_{x \in \mathcal{A}} f(x)$	Value of x that minimizes x
$\arg \min_{x \in \mathcal{A}} f(x)$	Value of x that minimizes x
$\inf_{y \in \mathcal{A}} g(\mathbf{x}, \mathbf{y})$	Infimum
$\sup_{y \in \mathcal{A}} g(\mathbf{x}, \mathbf{y})$	Supremum
$ a $	Absolute value of a
\log	Base-10 logarithm or decimal logarithm
\ln	Natural logarithm
$\operatorname{Re}\{x\}$	Real part of x
$\operatorname{Im}\{x\}$	Imaginary part of x
$\angle \cdot$	phase (complex argument)
$x \bmod y$	Remainder, i.e., $x - y\lfloor x/y \rfloor$
$\operatorname{frac}(x)$	Fractional part, i.e., $x \bmod 1$
$a \wedge b$	Logical AND of a and b
$a \vee b$	Logical OR of a and b
$\neg a$	Logical negation of a
$\lceil \cdot \rceil$	Ceiling operation
$\lfloor \cdot \rfloor$	Floor operation

8.3 Functions

$\mathcal{O}(\cdot), O(\cdot)$	Big-O notation
$\Gamma(\cdot)$	Gamma function

9 Abbreviations

wrt.	With respect to
st.	Subject to
iff.	If and only if
EVD	Eigenvalue decomposition, or eigen-decomposition

SVD
CP

Singular value decomposition
CANDECOMP/PARAFAC