

# **Ionospheric Scintillation Effect on GNSS**

**Prepared by Antonio Macilio Pereira de Lucena**

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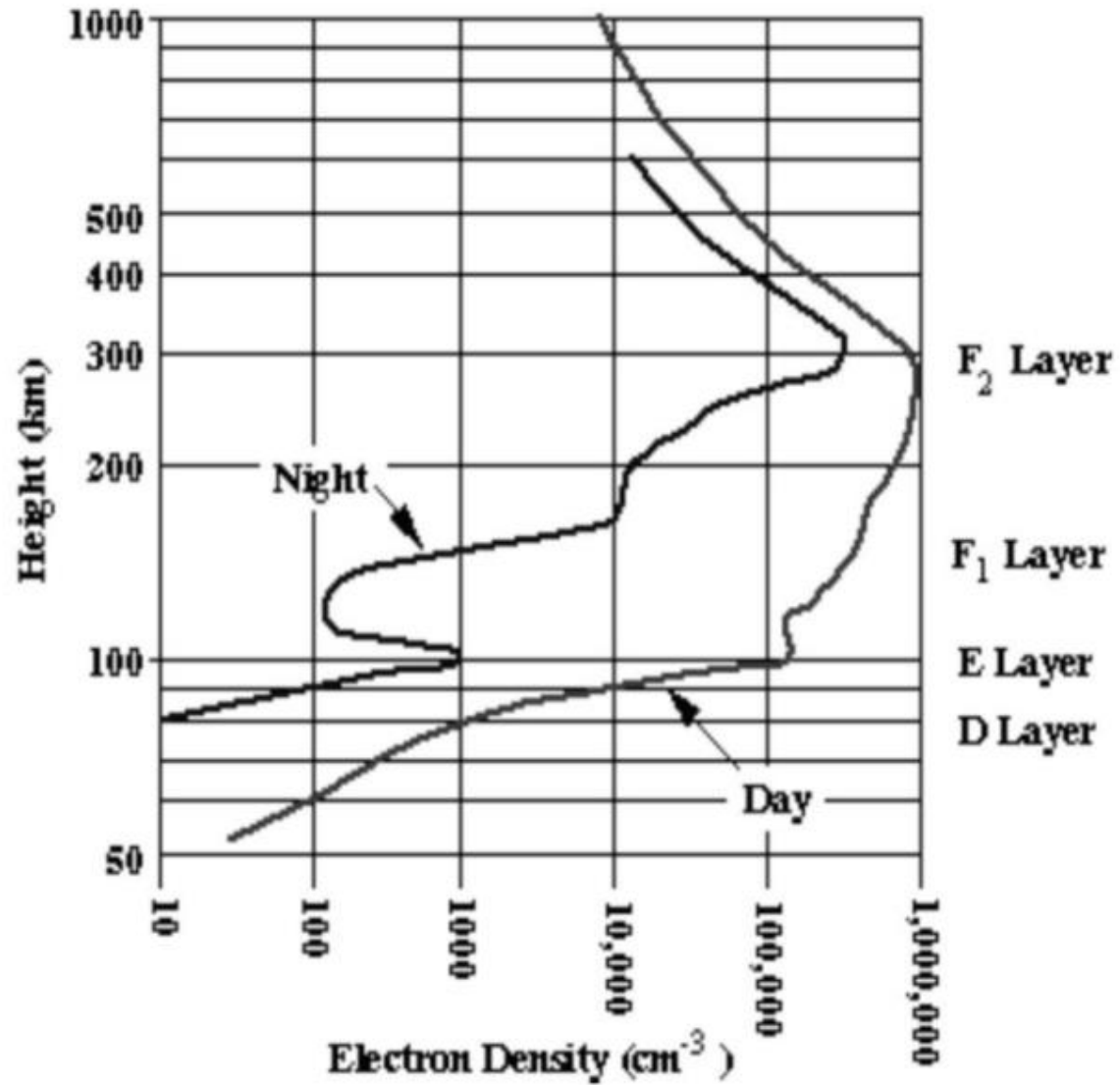
# Contents

- Introduction to ionospheric scintillation;
- Generation mechanisms of equatorial scintillation;
- Scintillation effects on the GNSS signal;
- Statistical model of scintillation;
- Costas loop and cycle slip;
- Conclusions.

# Ionospheric scintillation

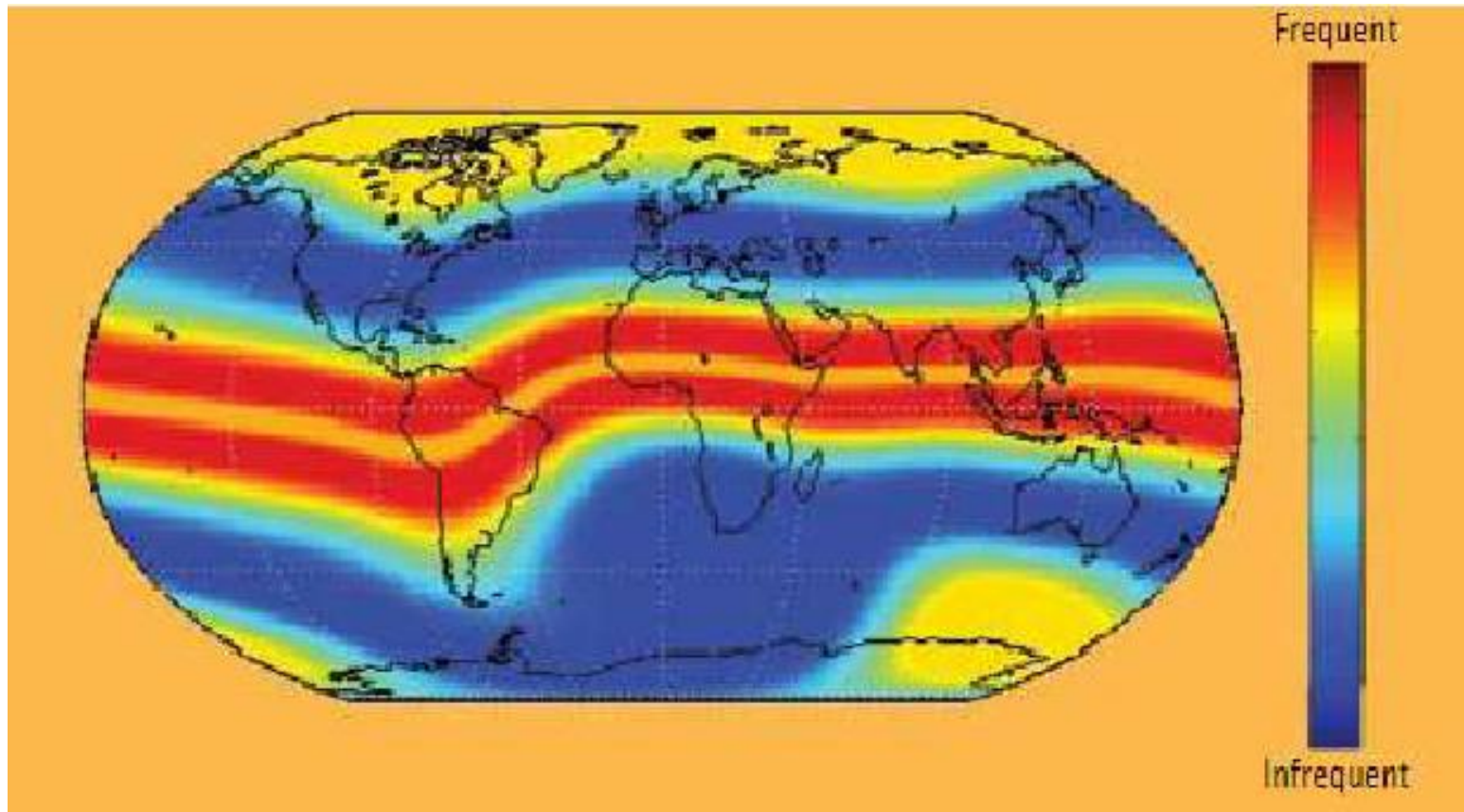
- Ionospheric scintillation are rapid fluctuations in the amplitude and phase of transionospheric signals;
- These distortions are caused by irregularities in the density of electrons (TEC) in the ionosphere through which the signal propagates;
- The phenomenon is more intense and frequent in regions around the magnetic equator (equatorial scintillation) and in the aural and polar regions;
- It significantly affects communications in the VHF and UHF bands;
- The occurrence of ionospheric scintillation depends on the season and the 11-year solar cycle.

# Ionospheric layers



(Moraes, A. O. et al., 2009)

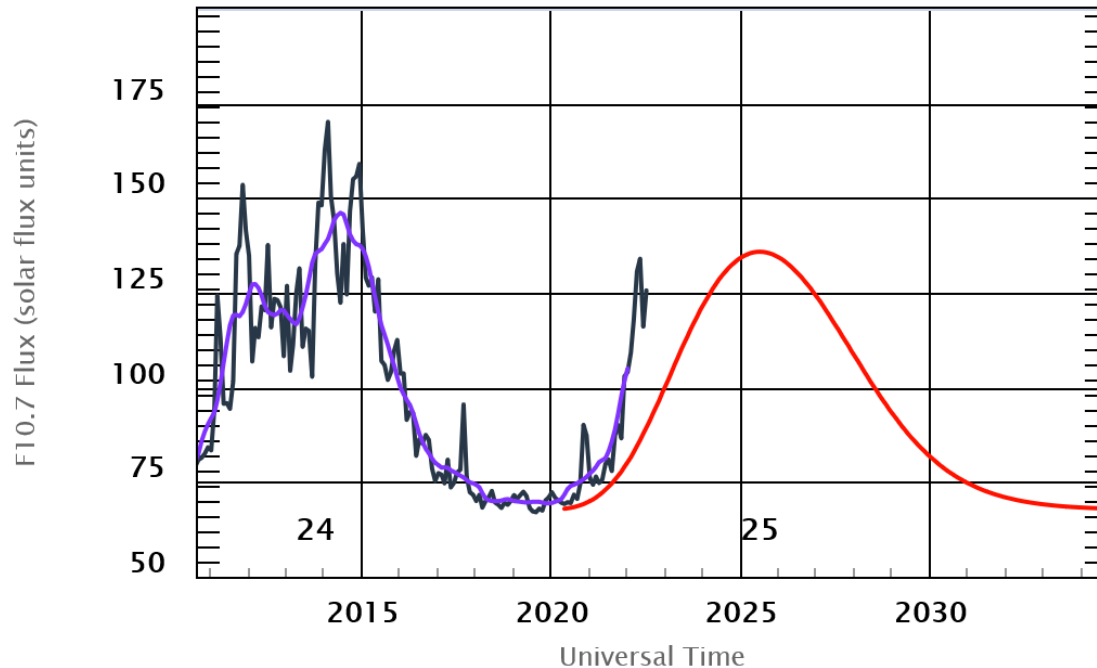
# Frequency of scintillation by geographic regions



(Kintner et al., 2009)

# Eleven-year solar cycle

ISES Solar Cycle F10.7cm Radio Flux Progression



◆ Monthly Values    — Smoothed Monthly Values    — Predicted Values

Space Weather Prediction Center

(<https://www.swpc.noaa.gov/products/solar-cycle-progression>)

# Equatorial ionospheric scintillation

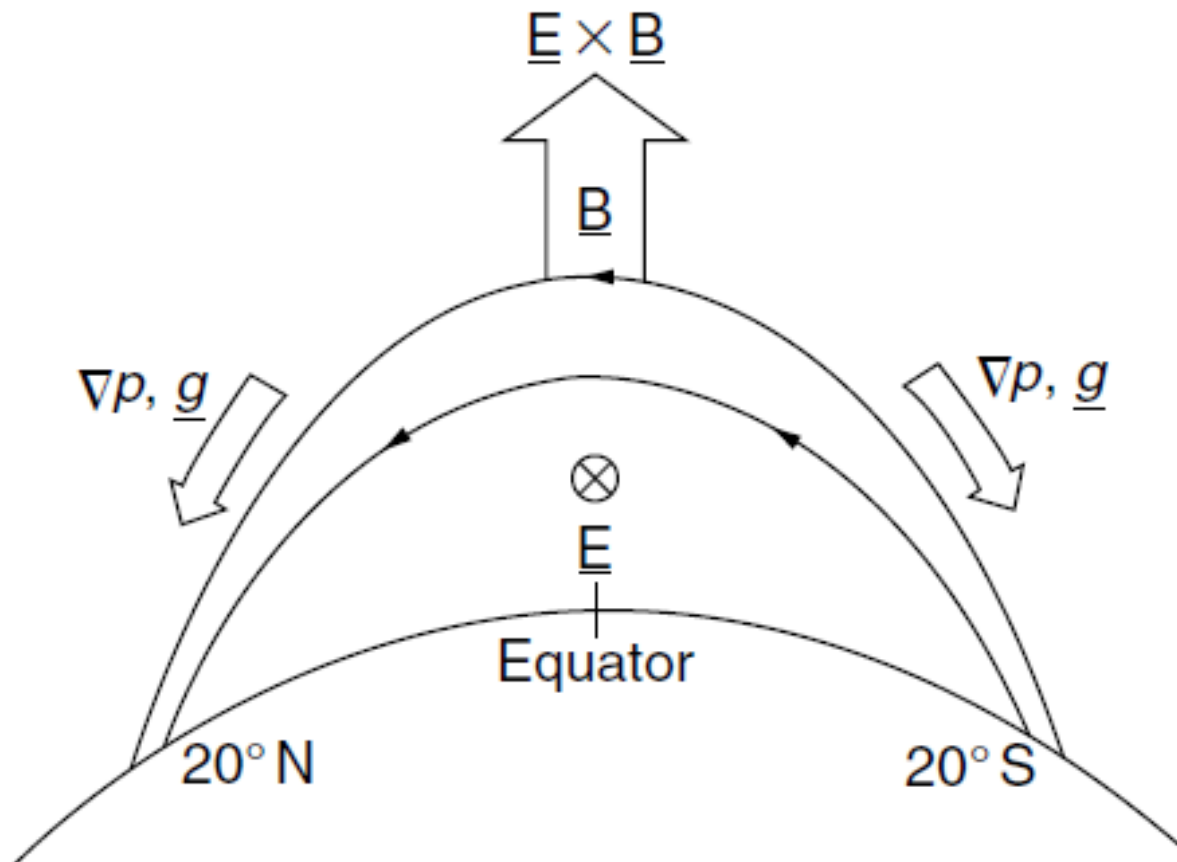
- It usually occurs after sunset;
- It results from the irregularities of the electronic density in the ionosphere caused by plasma bubbles in the equatorial anomaly (EA);
- Its intensity increases with magnetic latitude, being maximum at the anomaly crest;
- It depends on the seasons and occurs more frequently at the equinoxes (September and March);
- Its intensity and frequency depend on solar activity.

## About equatorial anomaly

- **Characteristic:** It is characterized by the ionization of the ionosphere with maximum intensity at approximately  $\pm 20^\circ$  of magnetic latitude and minimum ionization at the equator;
- **Dynamics in the anomaly:** During the daytime, the plasma generated by the solar ionization in the F layer is raised by the action of the electric and magnetic fields;
- Then, by the action of gravity and the pressure gradient, the ions move along the lines of the geomagnetic field, intensifying the TEC at  $\pm 20^\circ$  latitude;
- At sunset, recombination in the E layer creates a low-density plasma layer;
- Due to Rayleigh-Taylor instability, low density plasma bubbles are formed at the base of the F layer.

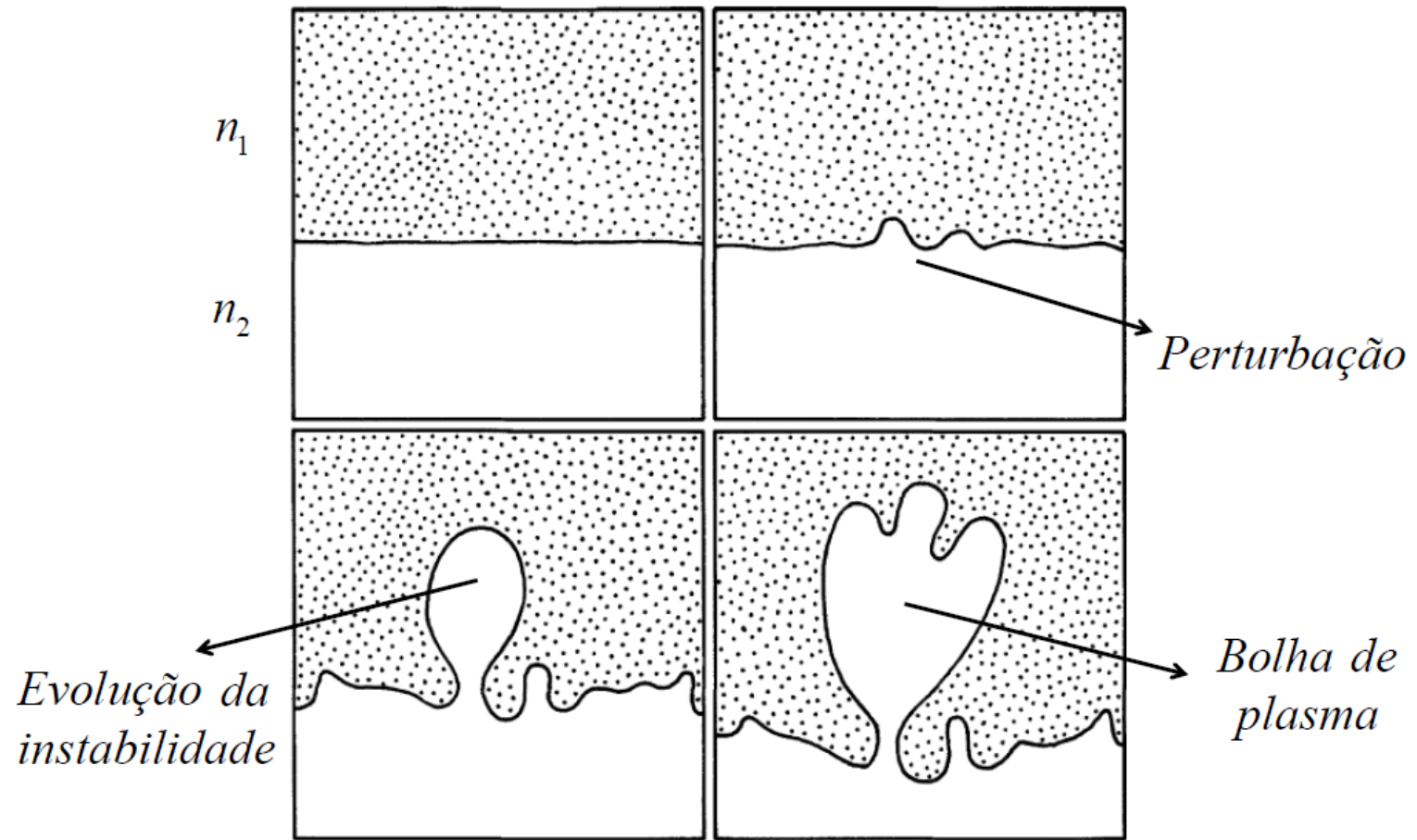


## Generation of equatorial anomaly (Fountain effect)



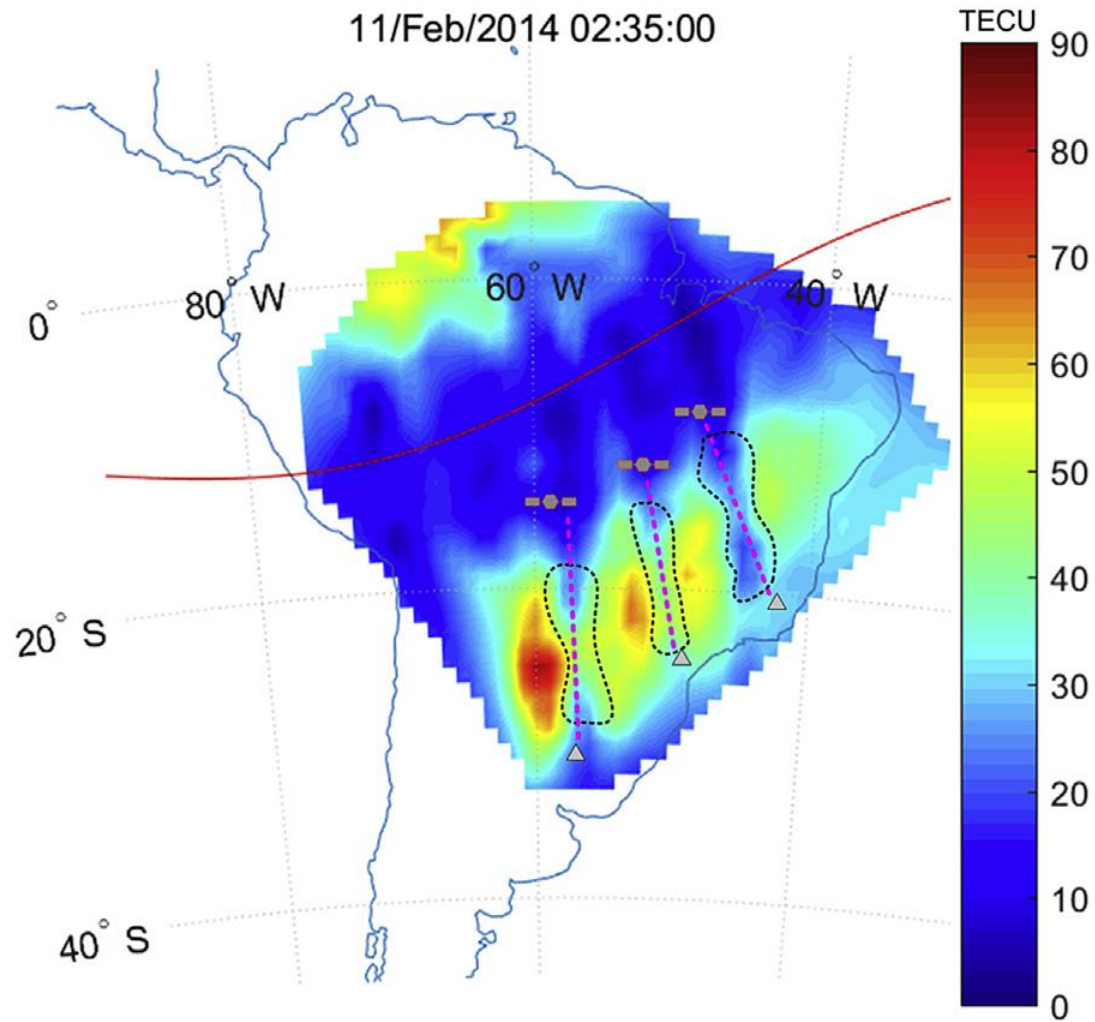
(Silva, D. B., 2017)

# Formation of equatorial plasma bubbles due to Rayleigh-Taylor instability (RTI)



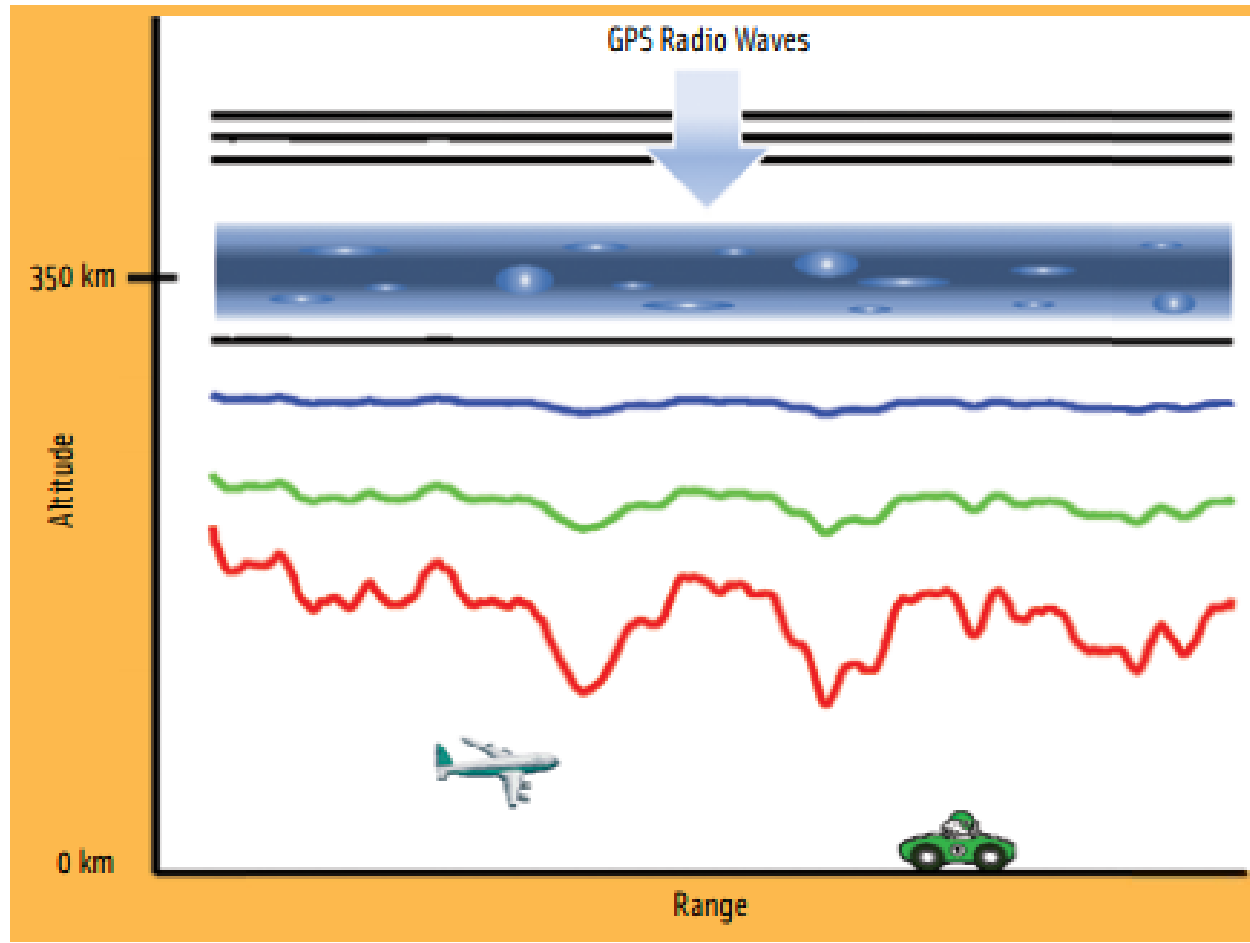
(Silva, D. B., 2017)

# TEC map on the Brazilian territory



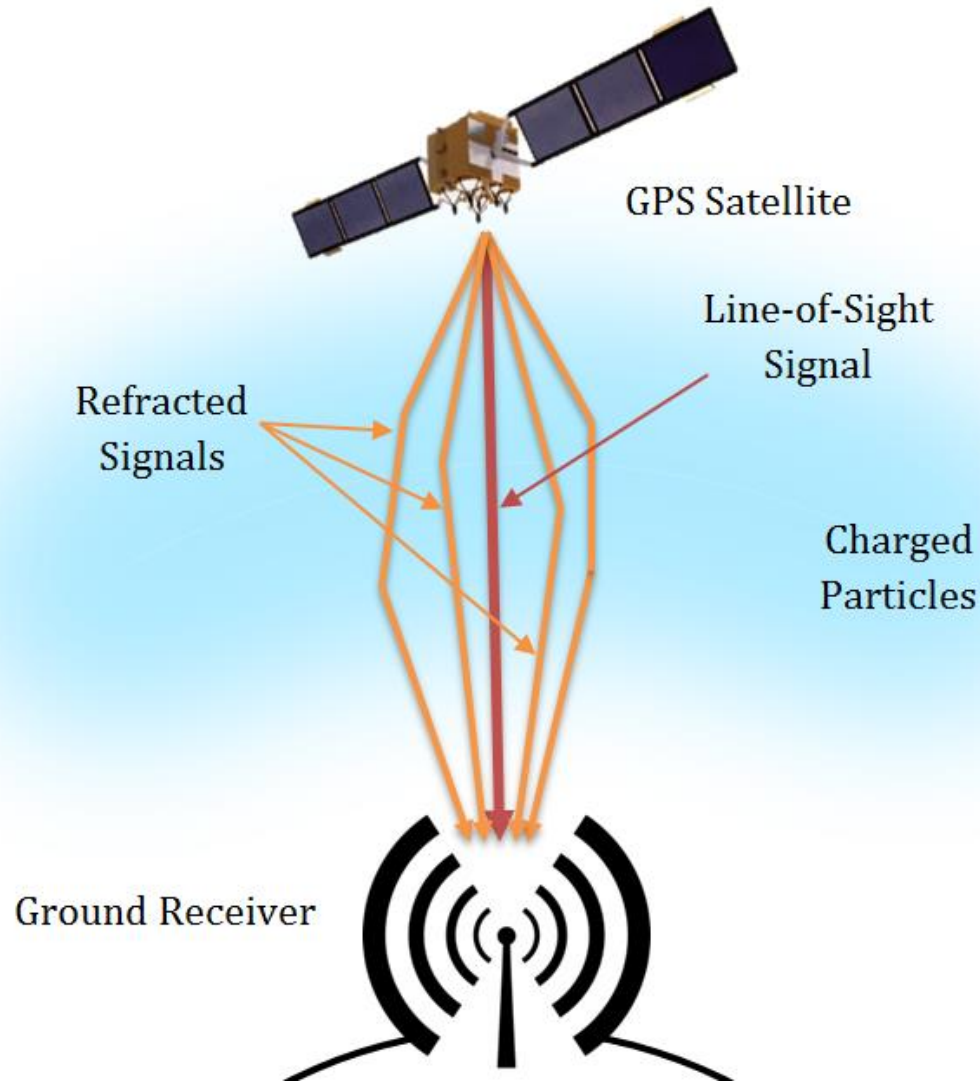
(Vani, B. C. et al, 2021)

# Effect of TEC irregularities over GNSS radio waves



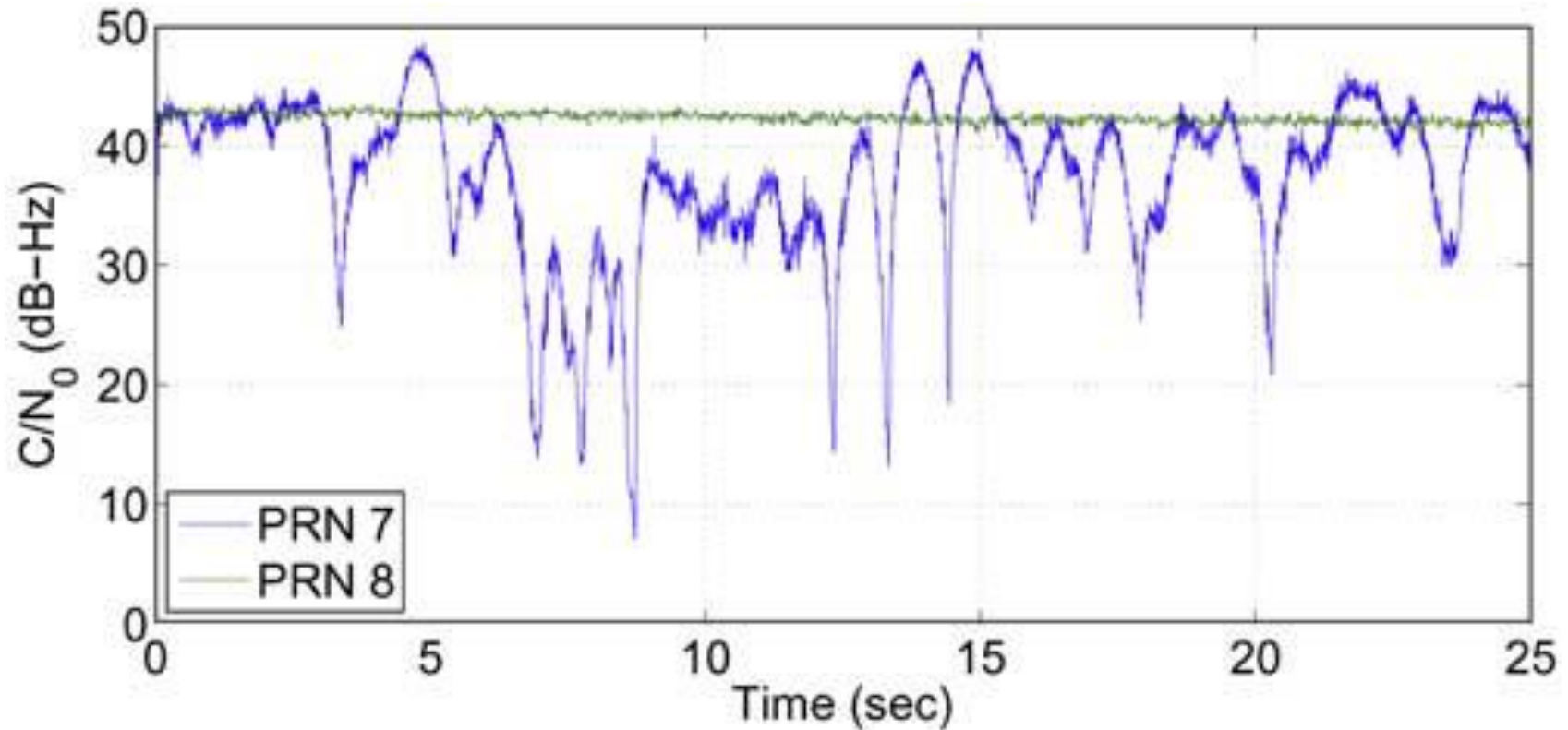
(Kintner et al., 2009)

# Multipath due to ionospheric scintillation



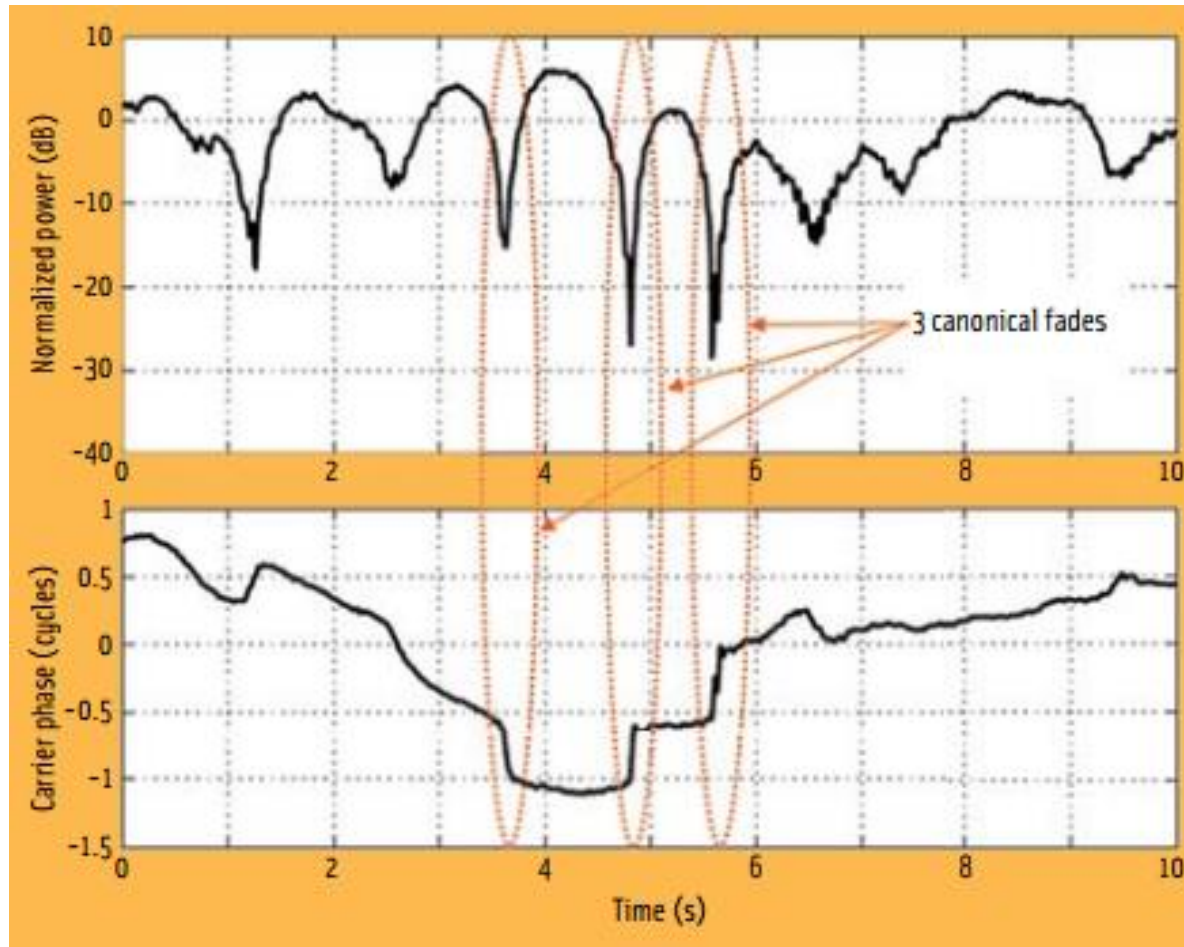
(Olivarez, N., 2013)

# Magnitude of received GNSS signal with scintillation and scintillation free



(Kintner et al., 2007)

# Effect of scintillation on magnitude and phase of the received GNSS signal



(Kintner et al., 2009)

# Consequencies of scintillation in the GNSS system

- Possibility of loss of lock in the receiver's carrier recovery loop;
- Degradation in the accuracy of phase and delay measurements;
- Reduction in positioning accuracy due to the decrease in available satellites;
- In Brazil, it can cause disruption to services such as precision agriculture, offshore operations and navigation;
- The operation of the GBAS (Ground-Based Augmentation Service) system to support civil aviation operations is not available in Brazil.



# Intensity characterization of the scintillation

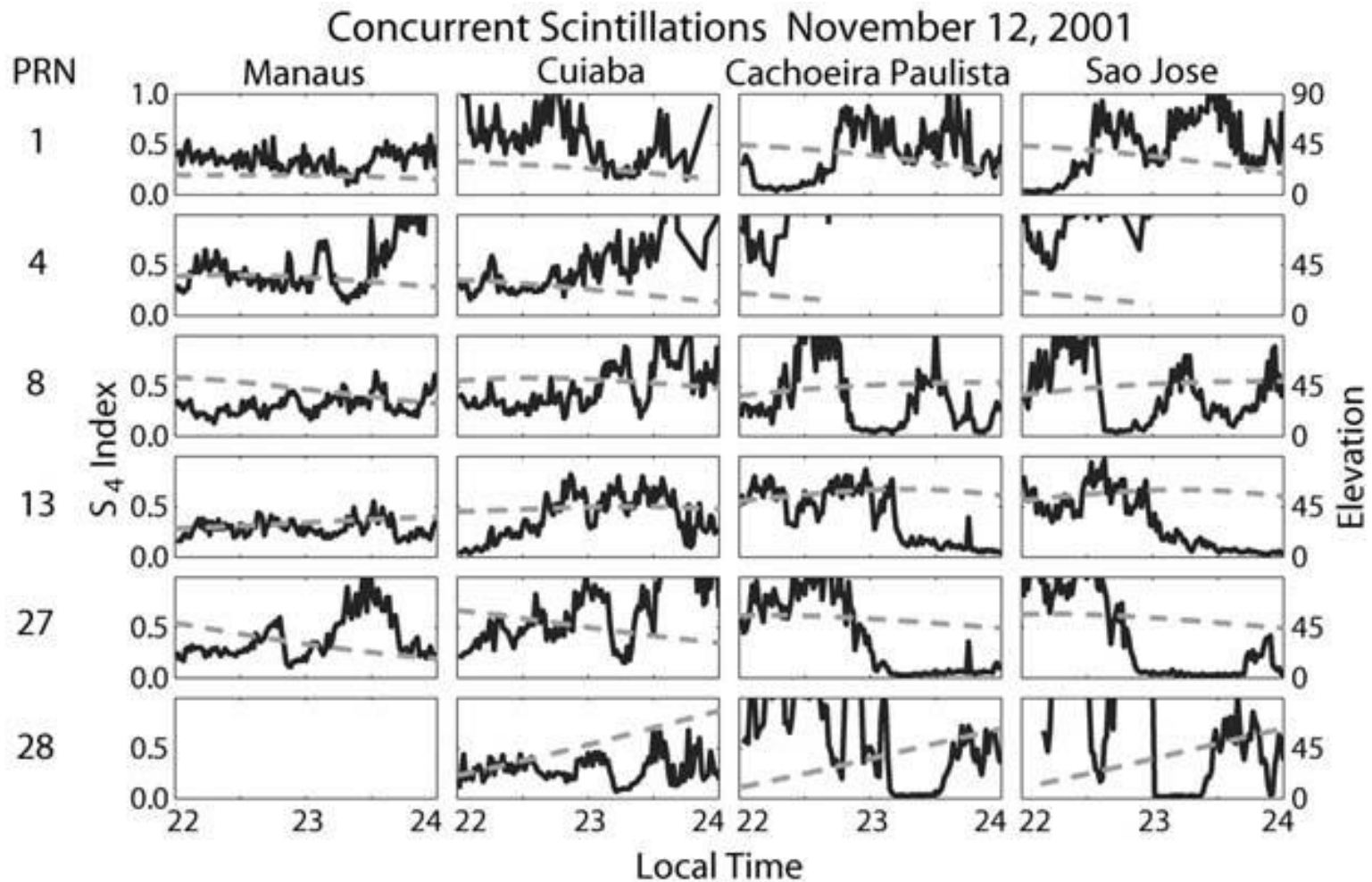
- The  $S_4$  index describes the scintillation intensity in terms of amplitude. It is defined by:

$$S_4 = \sqrt{\frac{\langle I^2 \rangle - \langle I \rangle^2}{\langle I \rangle^2}},$$

where  $I$  is the square of the magnitude of the received signal and the operator  $\langle . \rangle$  represents the time average;

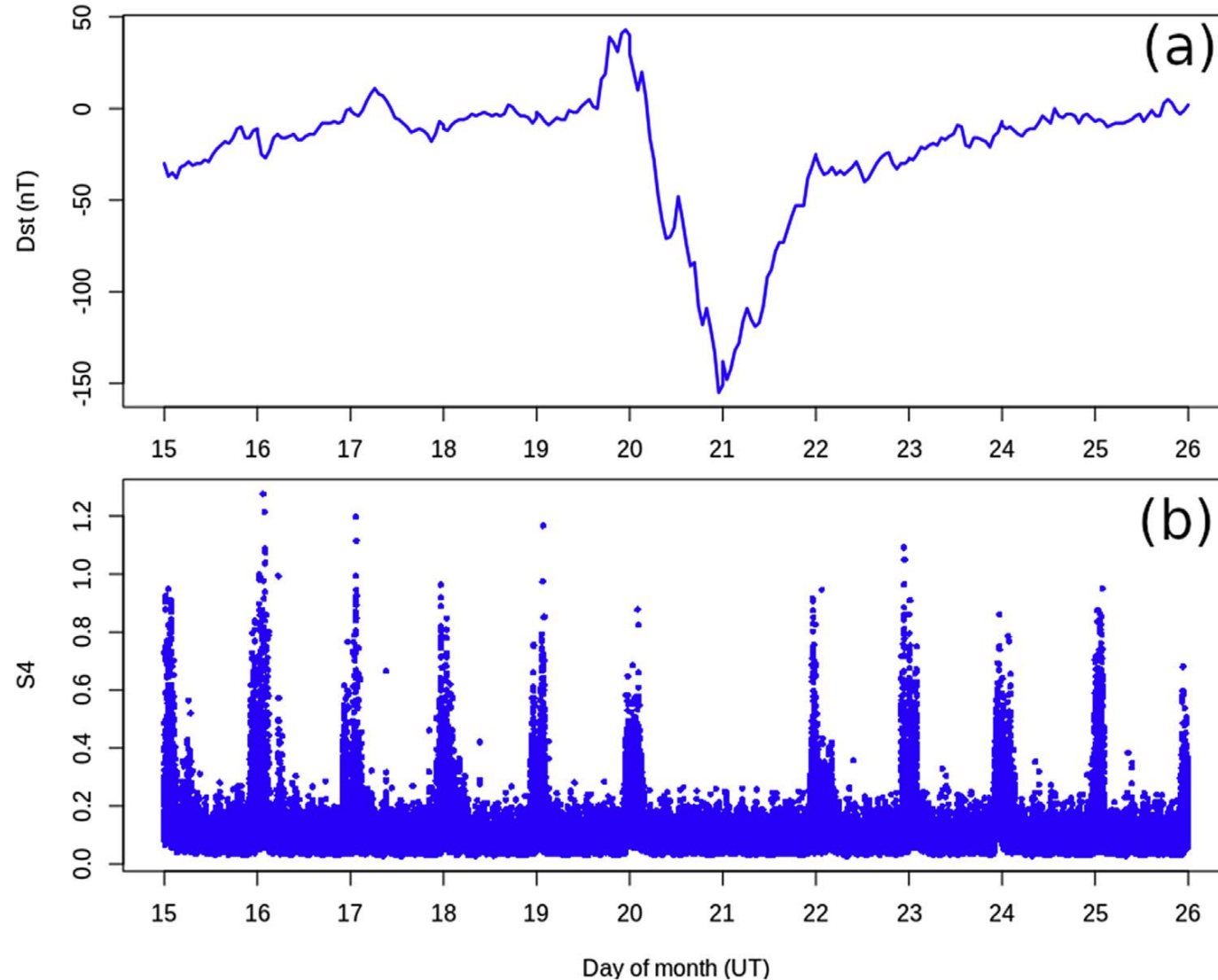
- $S_4 < 0.3$  corresponds to low level of scintillation,  $0.3 \leq S_4 < 0.5$  is moderate level and  $0.5 \leq S_4 < 1$  represents high level;
- The intensity of the phase scintillation is measured by the index  $\sigma_\phi$  which represents the standard deviation of the phase fluctuation caused by the scintillation.

# $S_4$ measurements at stations in Brazilian territory



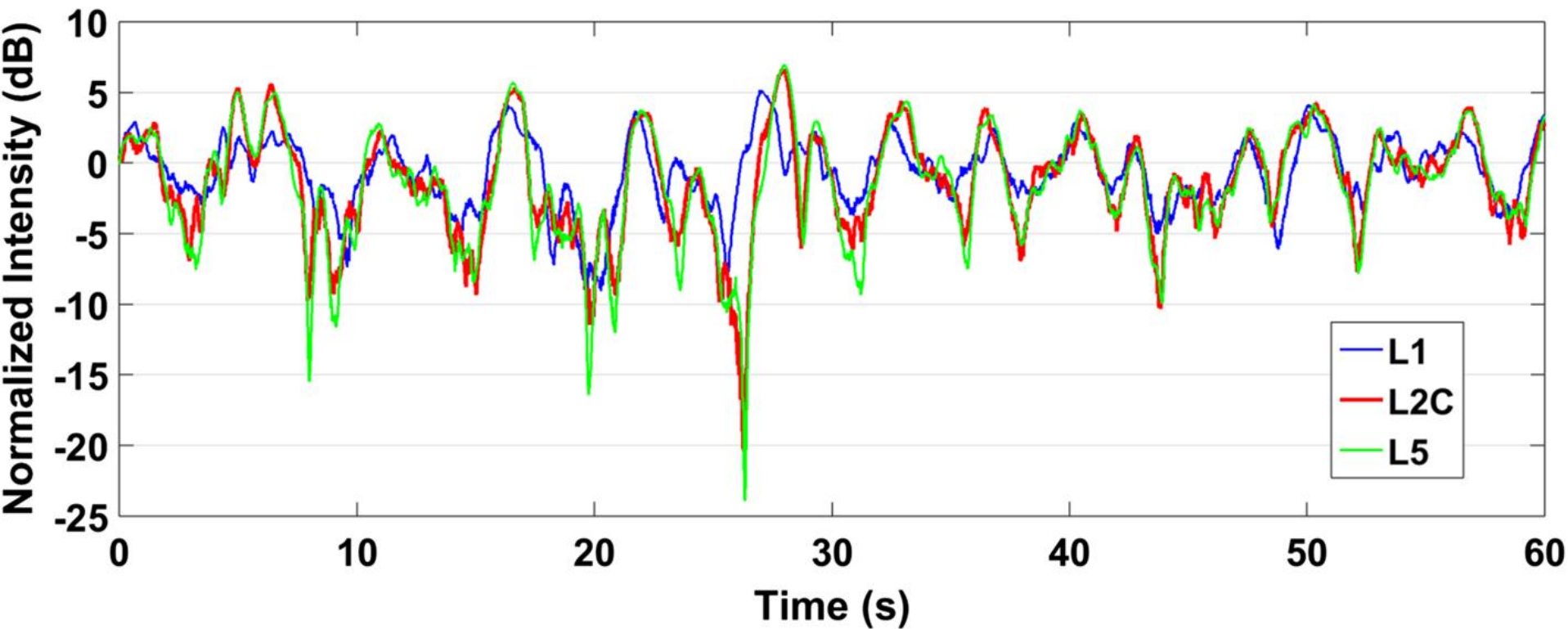
(Kintner et al., 2007)

# $S_4$ measurements in Fortaleza (December 2015)



(Vani, B. C. et al, 2021)

# Measurements of $S_4$ in São José dos Campos (day 13/11/2015)



(Salles, L. A. et al, 2021)

# Statistical model of channel with scintillation (Cornell model)

- Received signal:

$$r_l(t) = a(t)e^{j\theta(t)}c(t)s_l(t - \tau) + n_l(t)$$

- Scintillation effect:** Flat fade represented by  $c(t)$ :

$$c(t) = Ae^{\phi} + d(t),$$

$A$  is a constant proportional to the amplitude of the part of the signal that reaches the receiver directly through the line-of-sight (specular component) and  $d(t)$  is a complex Gaussian process with zero mean and variance  $2\sigma^2$ , associated with the part of the signal that undergoes dispersion (multipath component).

# Probability Density Function (PDF) of the magnitude of $c(t)$ (Distribuição de Rice)

- The magnitude of  $c(t)$  is  $\alpha = |c(t)|$  whose PDF é

$$p_{\alpha}(\alpha) = 2\alpha(1 + K)e^{-K-\alpha^2(1+K)}I_0[2\alpha\sqrt{K(1 + K)}],$$

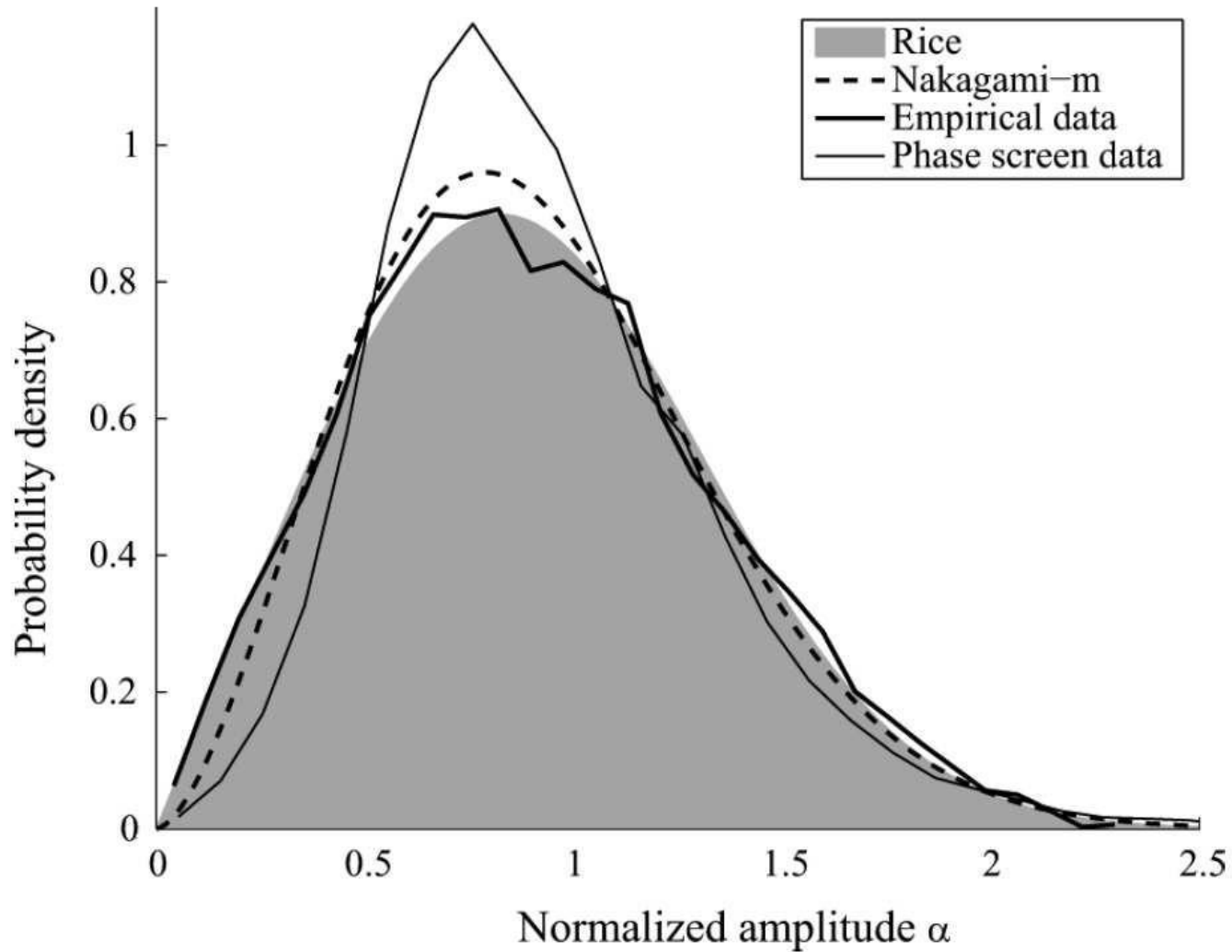
where

$$K = A^2/2\sigma^2$$

and

$$K = \frac{\sqrt{1 - S_4^2}}{1 - \sqrt{1 - S_4^2}}.$$

# Comparisons of Rice probability distribution



(Humphreys et al, 2008)

# Autocorrelation function of the process $d(t)$

- Expressions for the autocorrelation function of  $d(t)$ :

$$R_d(\tau) = E\{d(t)d^*(t + \tau)\},$$

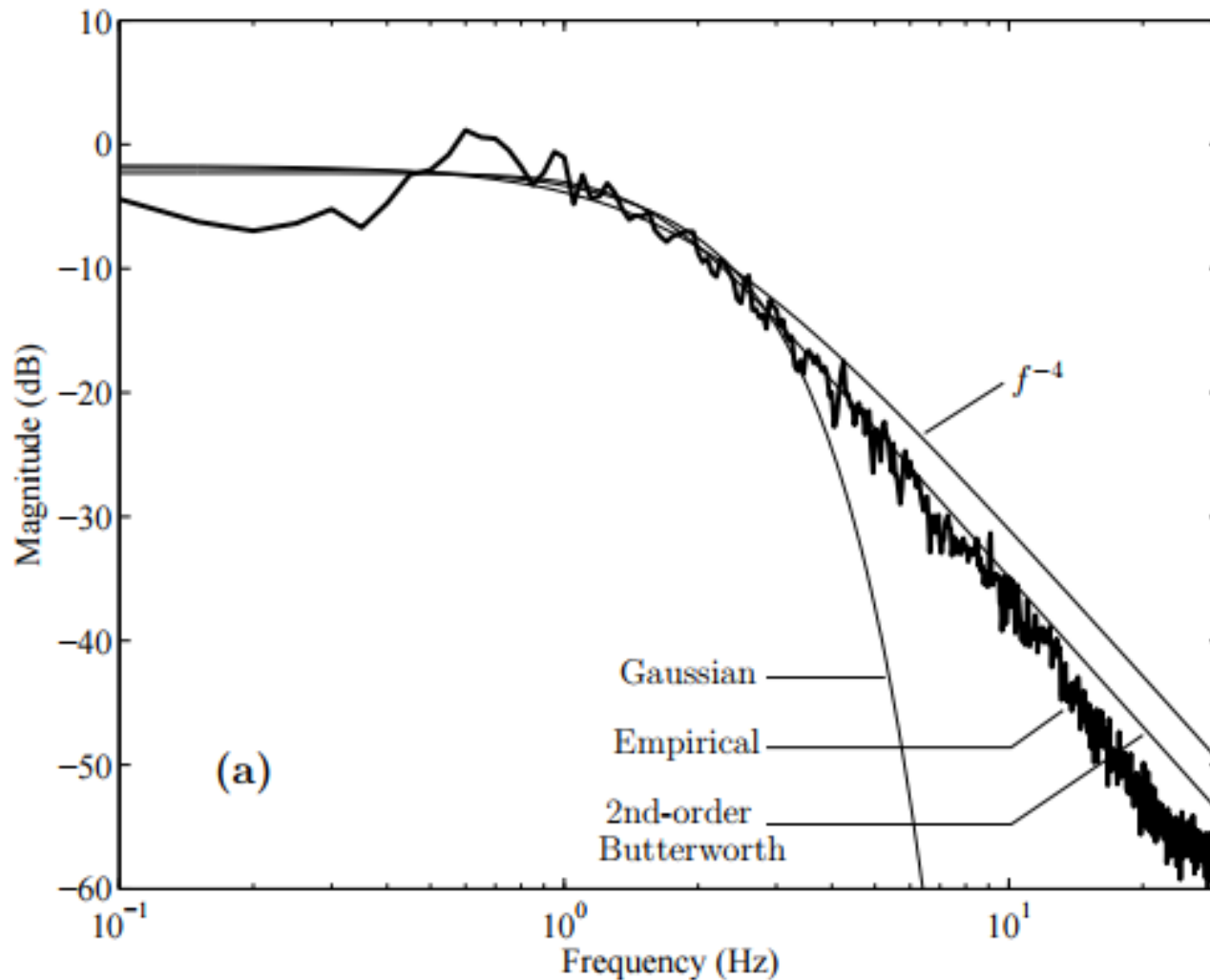
$$R_d(\tau) = 2\sigma^2 \exp\left(-\frac{\beta\tau}{\tau_0}\right) [\cos(\beta\tau/\tau_0) + \text{sen}(|\beta\tau|/\tau_0)],$$

$\beta=1.239646$  and  $\tau_0$  is the channel decorrelation time;

- A process with this autocorrelation function may be obtained by the passage of a Gaussian and white process through a second-order low-pass Butterworth filter.

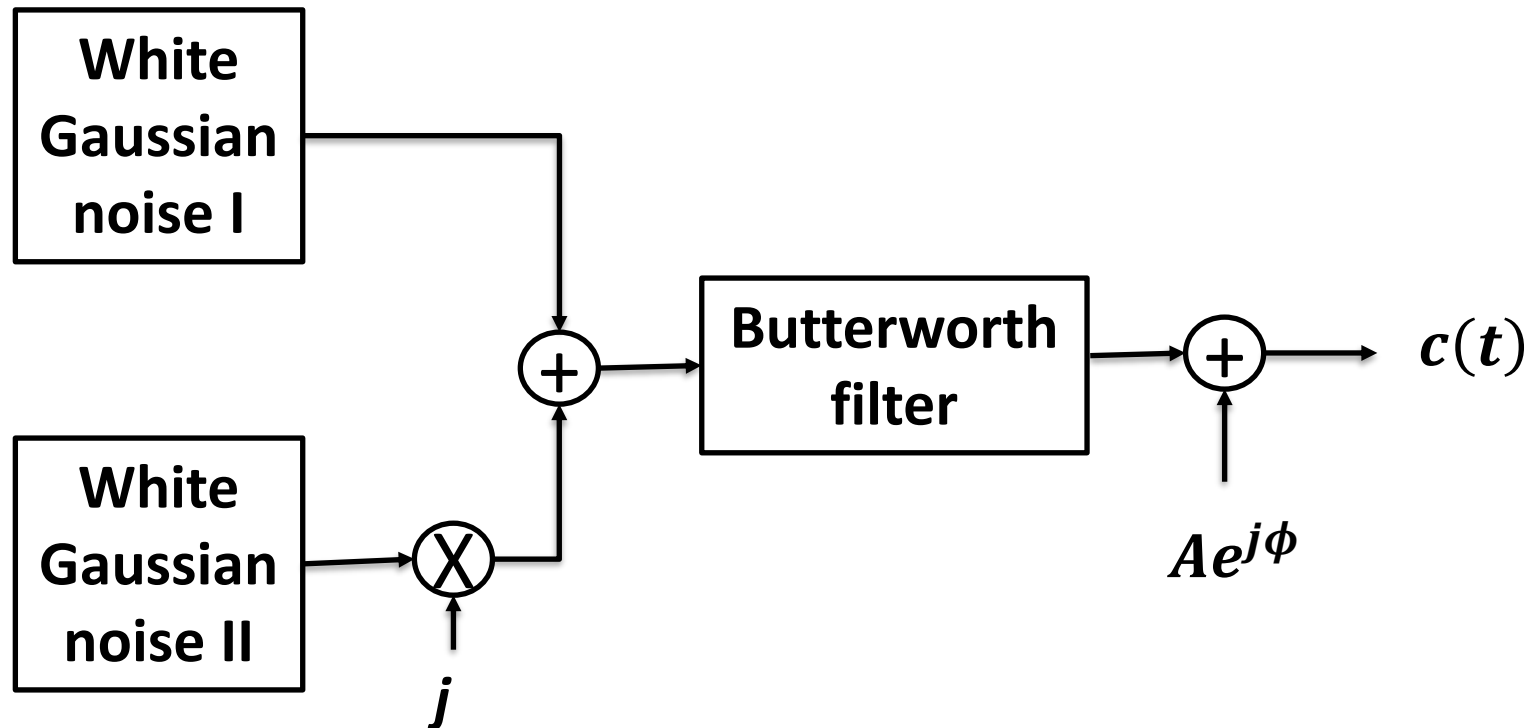


# Power spectral density of the process $d(t)$

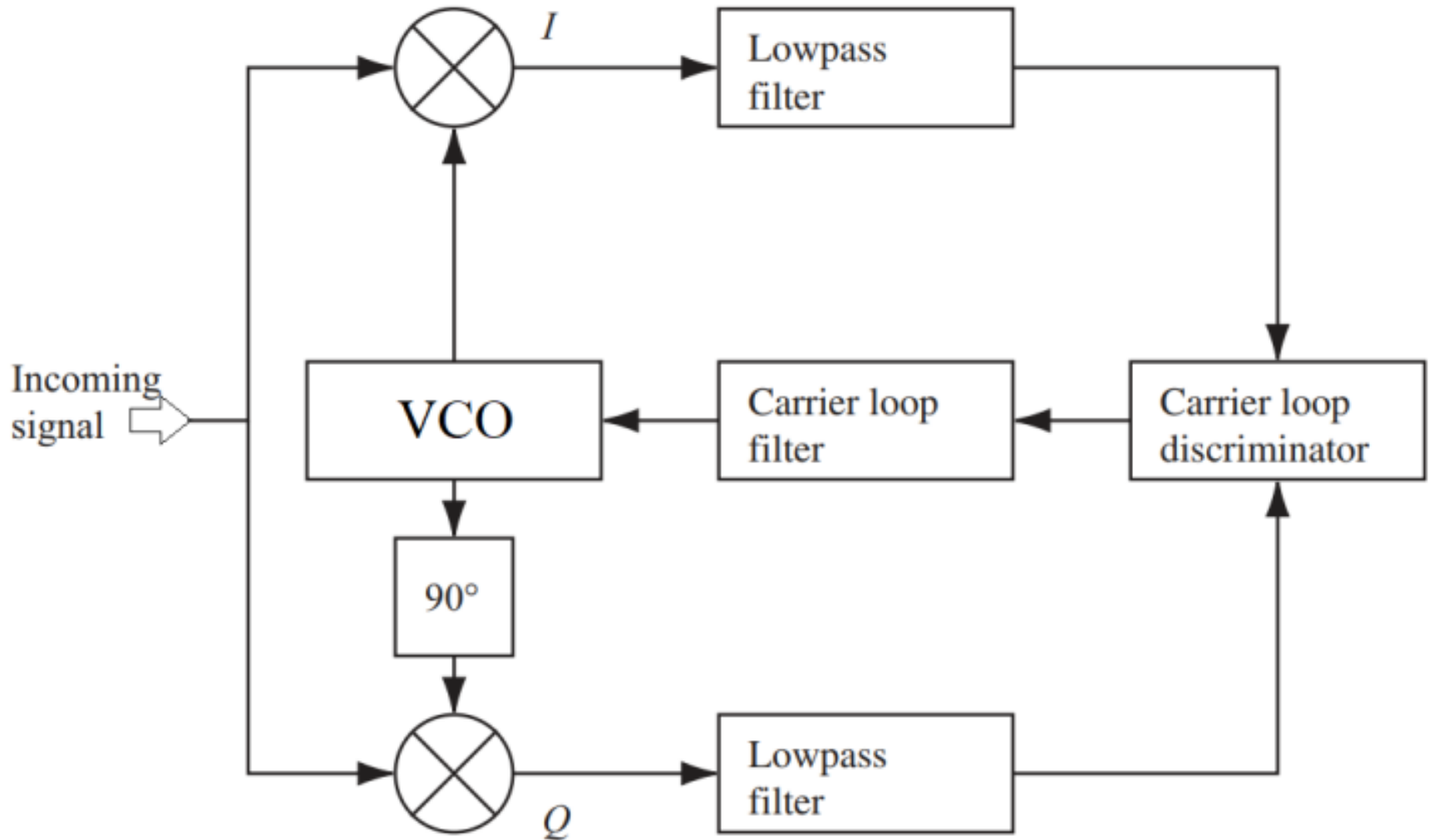


(Humphreys et al, 2008)

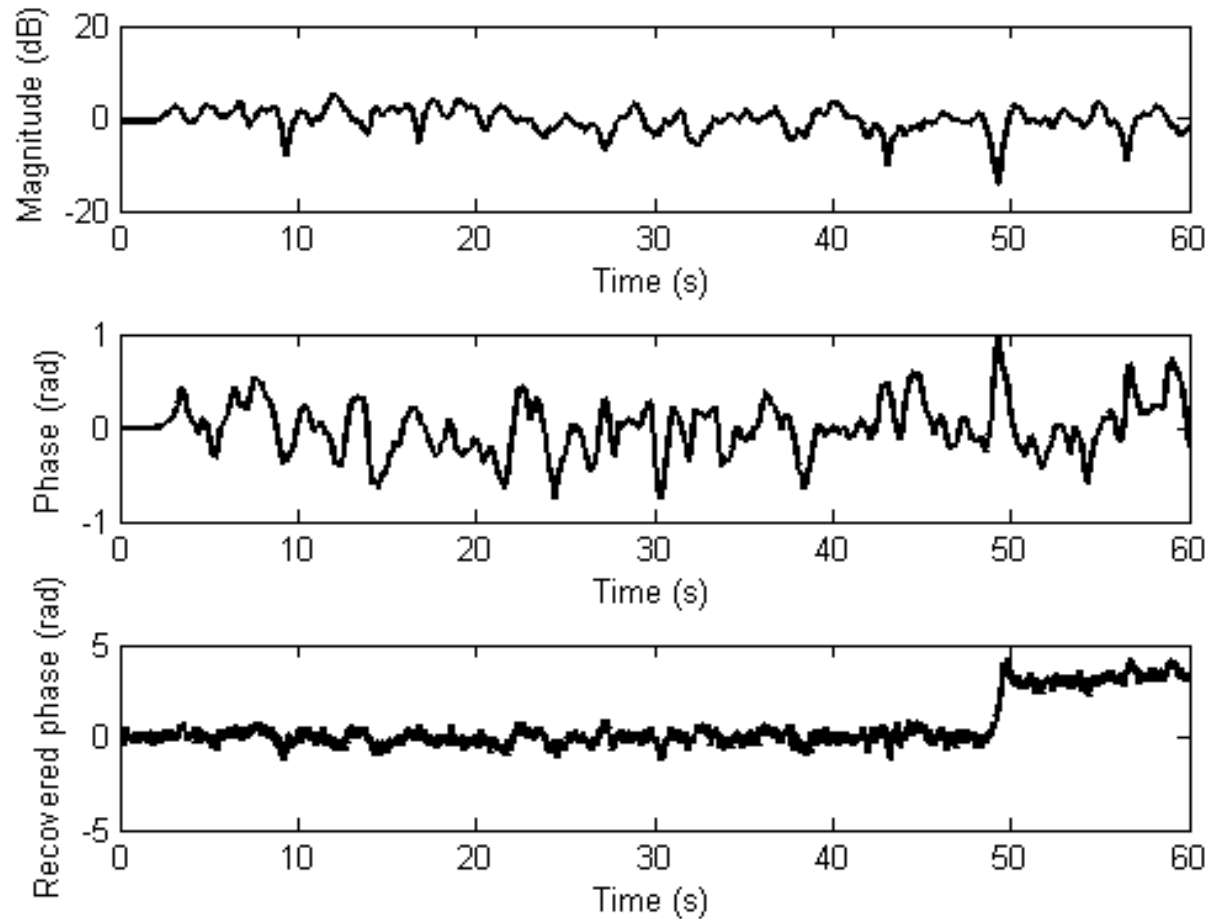
# Mechanization of the scintillation model



# Carrier phase recovery loop (Costas loop)



# Phase recovered by a Costas loop with $B_L=10$ Hz, $C/N_0=30$ dB-Hz and $S_4=0.5$



# Main conclusions

- Ionospheric scintillation occurs in equatorial and high latitude regions;
- In addition to geographic position, it also depends on signal frequency, solar activity, season and time of day;
- It distorts the amplitude and phase of transionospheric signals;
- The communication channel under scintillation can be modeled as a Rice channel;
- It mainly affects the carrier phase recovery of the receivers;
- It reduces the positioning accuracy of GNSS systems;
- Depending on its intensity, it can lead to complete interruption of some services.

# References

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