

Demo ticket

Session

ID: demoN8T32H-67U
Time limit: 120 min.

Status: closed

Created on: 2014-03-20 16:16 UTC
Started on: 2014-03-20 16:16 UTC
Finished on: 2014-03-20 16:56 UTC

Tasks in test

1 | CountSemiprimes

Task score

100%

Test score

100%
100 out of 100 points

MEDIUM

1. CountSemiprimes

Count the semiprime numbers in the given range [a..b]

score: 100 of 100



Task description

The *prime* is a positive integer X that has exactly two distinct divisors: 1 and X . The first few prime integers are 2, 3, 5, 7, 11 and 13. The *semiprime* is a natural number that is the product of two (not necessarily distinct) prime numbers. The first few semiprimes are 4, 6, 9, 10, 14, 15, 21, 22, 25, 26.

You are given two non-empty zero-indexed arrays P and Q , each consisting of M integers. These arrays represent queries about the number of semiprimes within specified ranges.

Query K requires you to find the number of semiprimes within the range $(P[K], Q[K])$, where $1 \leq P[K] \leq Q[K] \leq N$.

For example, consider an integer $N = 26$ and arrays P, Q such that:

```
P[0] = 1   Q[0] = 26
P[1] = 4   Q[1] = 10
P[2] = 16  Q[2] = 20
```

The number of semiprimes within each of these ranges is as follows:

- (1, 26) is 10,
- (4, 10) is 4,
- (16, 20) is 0.

Write a function:

```
def solution(N, P, Q)
```

that, given an integer N and two non-empty zero-indexed arrays P and Q consisting of M integers, returns an array consisting of M elements specifying the consecutive answers to all the queries.

For example, given an integer $N = 26$ and arrays P, Q such that:

```
P[0] = 1   Q[0] = 26
P[1] = 4   Q[1] = 10
P[2] = 16  Q[2] = 20
```

the function should return the values [10, 4, 0], as explained above. Assume that:

- N is an integer within the range [1..50,000];
- M is an integer within the range [1..30,000];
- each element of array P is an integer within the range [1..50,000];
- each element of array Q is an integer within the range [1..50,000];

Solution

Programming language used: Python

Total time used: 40 minutes

Effective time used: 40 minutes

Notes: correct functionality and scalability

Task timeline



16:16:59

16:56:29

Code: 16:56:29 UTC, py, final, score: 100.00

```
01. def solution(N, P, Q):
02.     F = [0] * (N + 1)
03.     R = range(N+1)
04.     i = 2
05.     while i <= N:
06.         if F[i] == 0:
07.             j = i
08.             while j <= N:
09.                 F[j] += 1
10.                 R[j] /= i
11.                 j += i
12.             i += 1
13.
14.     count = [0] * (N + 1)
15.     for i in xrange(4, N+1):
16.         count[i] = count[i-1]
17.         if (F[i] == 1 and i == R[i] * R[i]) \
18.             or (F[i] == 2 and R[i] == 1):
19.             count[i] += 1
20.
21.     M = len(P)
22.     ret = [0] * M
```

- each element of array P is an integer within the range [1..N];
- each element of array Q is an integer within the range [1..N];
- $P[i] \leq Q[i]$.

Complexity:

- expected worst-case time complexity is $O(N \cdot \log(\log(N)) + M)$;
- expected worst-case space complexity is $O(N + M)$, beyond input storage (not counting the storage required for input arguments).

Elements of input arrays can be modified.

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Test results - Codility

```
23. for i in xrange(M):
24.     ret[i] = count[Q[i]] - count[P[i]-1]
25. return ret
26.
```

Analysis

Detected time complexity:

$O(N \cdot \log(\log(N)) + M)$

test	time	result
example		
example test	0.050 s.	OK
extreme_one		
small N = 1	0.050 s.	OK
extreme_four		
small N = 4	0.050 s.	OK
small_functional		
small functional	0.050 s.	OK
small_random		
small random, length = ~40	0.050 s.	OK
medium_random		
small random, length = ~300	0.050 s.	OK
large_small_slices		
large with very small slices, length = ~30,000	0.260 s.	OK
large_random1		
large random, length = ~30,000	0.320 s.	OK
large_random2		
large random, length = ~30,000	0.310 s.	OK
extreme_large		
all max ranges	0.300 s.	OK

Training center