

Neuro-computing : an introduction

Ashish Ghosh

Professor, Machine Intelligence Unit

In-Charge, Center for Soft Computing Research

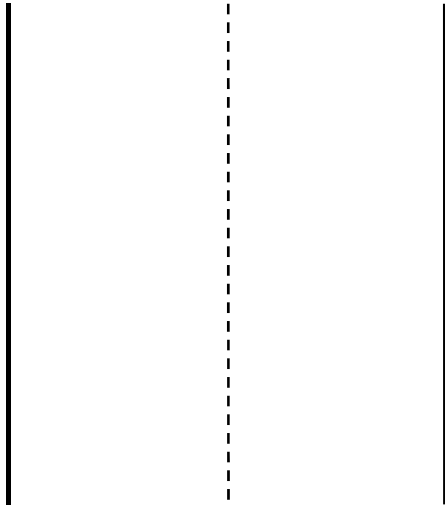
Indian Statistical Institute

203 B. T. Road, Kolkata 700108.

ash@isical.ac.in

<http://www.isical.ac.in/~ash>

Parking a vehicle: learning



- Hits the left boundary
- Move right
- Hits the right boundary
- Move left (little less)
- Not perfect, move right (less amount)
- Perfect
- *Learning (Neural Network)*

- ❖ Primary task of all biological neural systems is to control various functions (mainly behavioral).
- ❖ Human being can do it almost instantaneously and without much effort. e.g., recognizing a scene or music immediately.
- ❖ **Artificial Neural Network** (ANN) or **Neural Network** (NN) models try to **simulate** the **biological neural network** with electronic circuitry.
- ❖ Also known as **Connectionists Model/ Parallel Distributed Processing** (PDP).

Purpose : To achieve human like performance (particularly in pattern recognition & image processing).

Definition

Definition : Massively parallel interconnected network of simple processing elements which are intended to interact with the objects of the real world in the same way as biological systems do.

- ❖ NN models are extreme simplifications of human neural systems.
- ❖ Computational elements (neurons/nodes/ processors) are **analogous** to that of the fundamental constituents (**neurons**) of the biological nervous system.

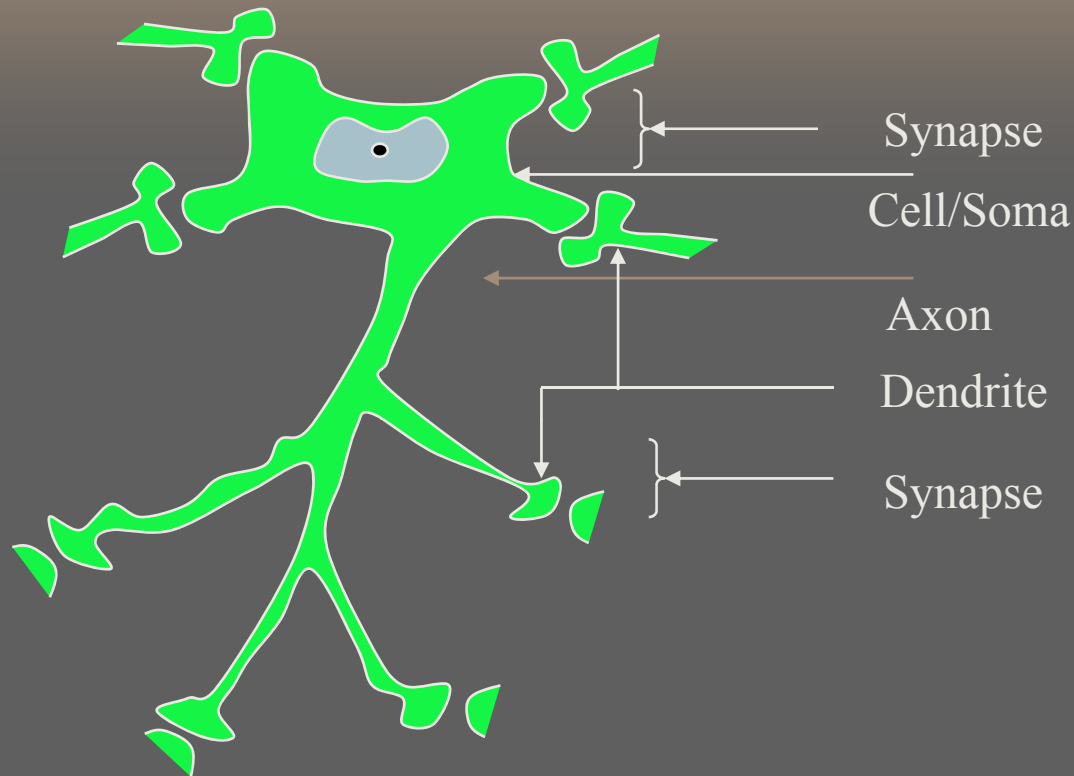
What are ANNs?

An extremely simplified model of the brain

Essentially a function approximator

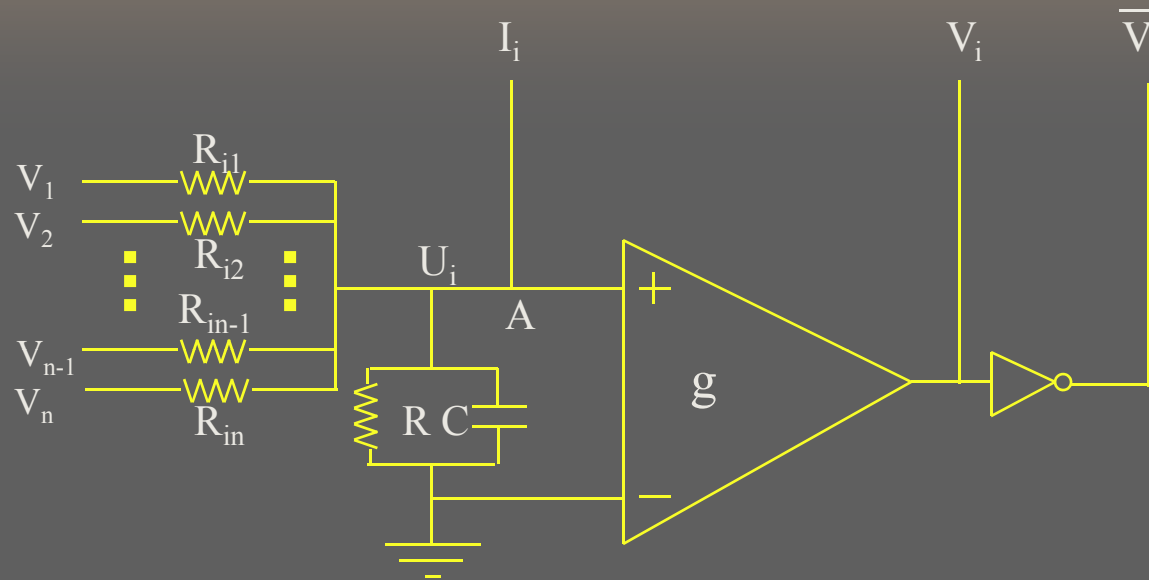
► Transforms inputs into outputs to the best of its ability

Similarity between BNN and ANN



- ❖ Gets input via synaptic connection
- ❖ Accumulated input is transformed to a single output
- ❖ Output is transmitted through axon
- ❖ If input > 0 , the neuron fires
- ❖ Total output \Leftarrow firing rate

An artificial neuron



Artificial /electronic neuron

- ❖ Gets input through resistors
- ❖ Total input is converted to a single output by OP-AMP
- ❖ Output is transmitted via resistors

Summary

- ❖ An electronic neuron emulates a biological neuron
- ❖ Artificial neurons are then connected to form a network to mimic (!) the topology of human nervous system
- ❖ Functions performed by a NN is determined by the network *topology, connection strength, processing* performed at computing elements or nodes, and *status updating rule*

General framework of neural networks

❖ Processing units

- Receives input from connected neurons, compute an output value and sends it to other connected neurons.
- Three types of units - *input, output, hidden*.

❖ Output value - $o_i(t) = f(I_i(t))$

- Total input for i^{th} neuron is I_i .
- f is a *threshold* or *squashing* function.

❖ Unidirectional connections (w_{ij})

- $w_{ij} < 0 \rightarrow$ unit u_j inhibits unit u_i .
- $w_{ij} = 0 \rightarrow$ unit u_j has no direct effect on unit u_i .
- $w_{ij} > 0 \rightarrow$ unit u_j excites unit u_i .

Characteristics of neural networks

Exhibit a number of human brain's characteristics (partially).

- ❖ **Learn from example** - shown a set of inputs, they self-adjust to produce consistent response.
- ❖ **Generalize from previous examples to new ones** - once trained, a network's response is mostly insensitive to variations in input.
- ❖ **Abstract essential characteristics from inputs** - find the ideals (prototype) from imperfect inputs.

Major advantages

- ❖ **adaptivity** - adjusting the connection strengths to new data/information,
- ❖ **speed** - due to massively parallel architecture,
- ❖ **robustness** - to missing, confusing, ill-defined/noisy data,
- ❖ **ruggedness** - to failure of components,
- ❖ **optimality** - as regards error rates in performance.

Learning (parameter updating)

❖ Associative (supervised) learning

Learning pattern pair association.

Input = $\mathbf{X} = \{x_1, x_2, \dots, x_n\}$

Output = $\mathbf{T} = \{t_1, t_2, \dots, t_n\}$

Learn (\mathbf{X}, \mathbf{T})

- auto-associator ($\mathbf{T} \cong \mathbf{X}$).
- hetero-associator (any arbitrary combination of \mathbf{X}, \mathbf{T}) (classification).

❖ Regularity detection (unsupervised)

System discovers statistically salient features of input population (clustering).

Popularly used NN models

Some common feature are there; but **differ in finer details**.

- ❖ Multi-layer perceptron (hetero associator/supervised classifier)
- ❖ Hopfield's model of associative memory (auto associator/CAM)
- ❖ Kohonen's model of self-organizing neural network (regularity detector/ unsupervised classifier)
- ❖ Radial basis function network (supervised)
- ❖ Adaptive resonance theory (regularity detector)
- ❖ Cellular neural network
- ❖ Neo-cognitron

Applicability

- ❖ Where human intelligence functions effortlessly & conventional computers are inadequate and cumbersome.
- ❖ Where collective & co-operative decisions are needed.

Application to pattern recognition/image processing

Pattern recognition (PR) tasks mainly involve

- Searching a complex decision space
- Detecting non-linear decision boundaries
- Discovering underlying regularities

ANN based systems

- Use adaptive learning for searching complex space
- Attempt to find out relation between input & output
- Can model complex non-linear boundaries
- Learn from examples
- Can extract underlying regularities

Thus **PR tasks are good candidates for NN implementation**

Image processing tasks involve

- ❖ Simple arithmetic operations at each pixel cite in parallel
- ❖ Neighborhood information (co-operative processing)
- ❖ Collective decision to represent overall status

NN based systems

- ❖ Are based on parallel distributed processing principle
- ❖ Perform simple arithmetic operation at each node independently
- ❖ Overall status provides a measure of collective decision

A NN in which a node corresponds to a pixel and is connected to its neighbors can do this task.

Example : Pixel classification

❖ Input features

- Gray value
- Positional information
- Contextual information

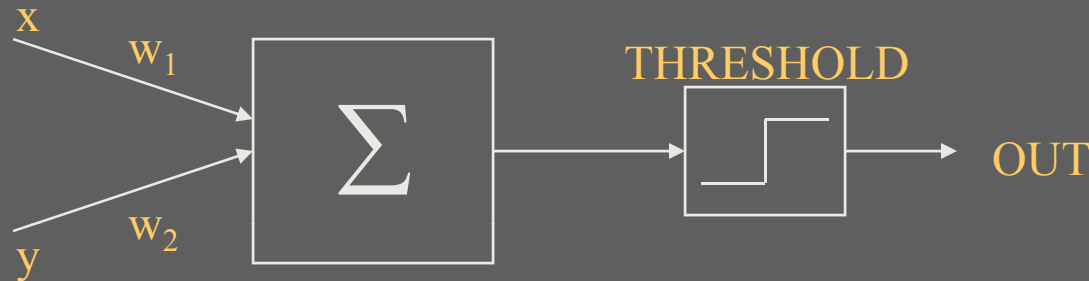
❖ Different pixels are classified independently

❖ Mathematical operations needed are simple

A NN in which a single neuron is assigned to each pixel and each neuron is connected to its neighbors can be applied for this task.

Two input perceptron

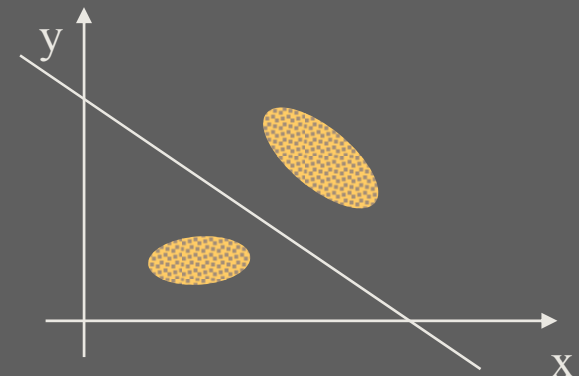
Perceptron: A single neuron connected by weights to a set of inputs



❖ Let x & y be two inputs and w_1, w_2 be the weights.

❖ If $w_1x + w_2y > \theta$ then the output is **1** else **0**, where $\theta = \text{threshold}$

❖ $w_1x + w_2y = \theta \rightarrow \text{separating line}$



Learning rule

Learning: Present a set of input patterns, adjust the weights until the desired output occurs for each of them.

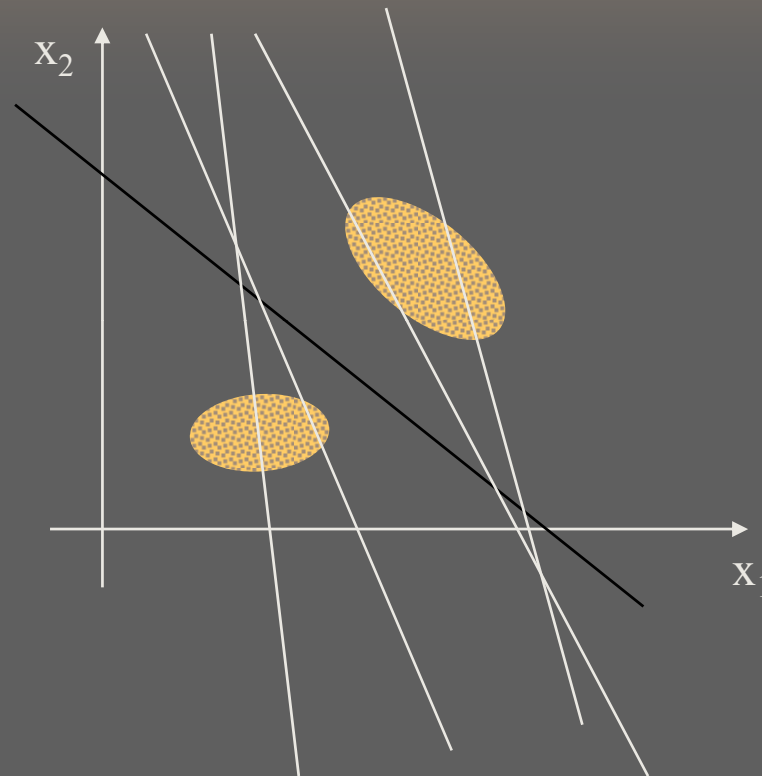
$$w_i(t+1) = w_i(t) + \Delta_i;$$

$$\Delta_i = \eta \delta x_i;$$

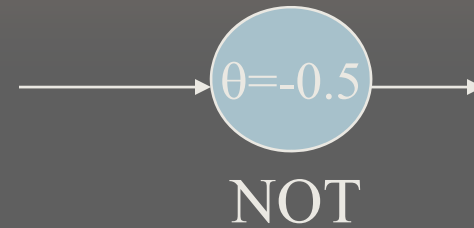
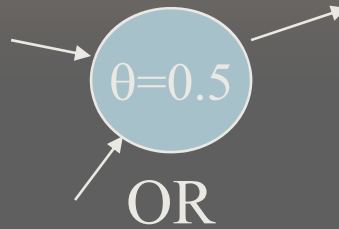
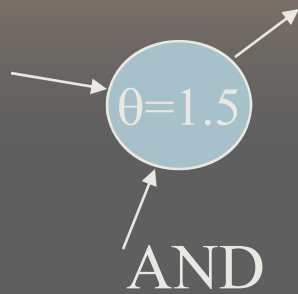
$$\delta = T - A \text{ (i.e., target - actual).}$$

❖ If the sets of patterns are linearly separable, the single layer perceptron algorithm is guaranteed to find a separating hyperplane in a finite number of steps.

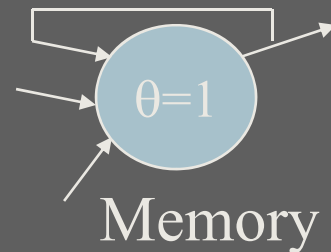
Change of weights



Boolean functions

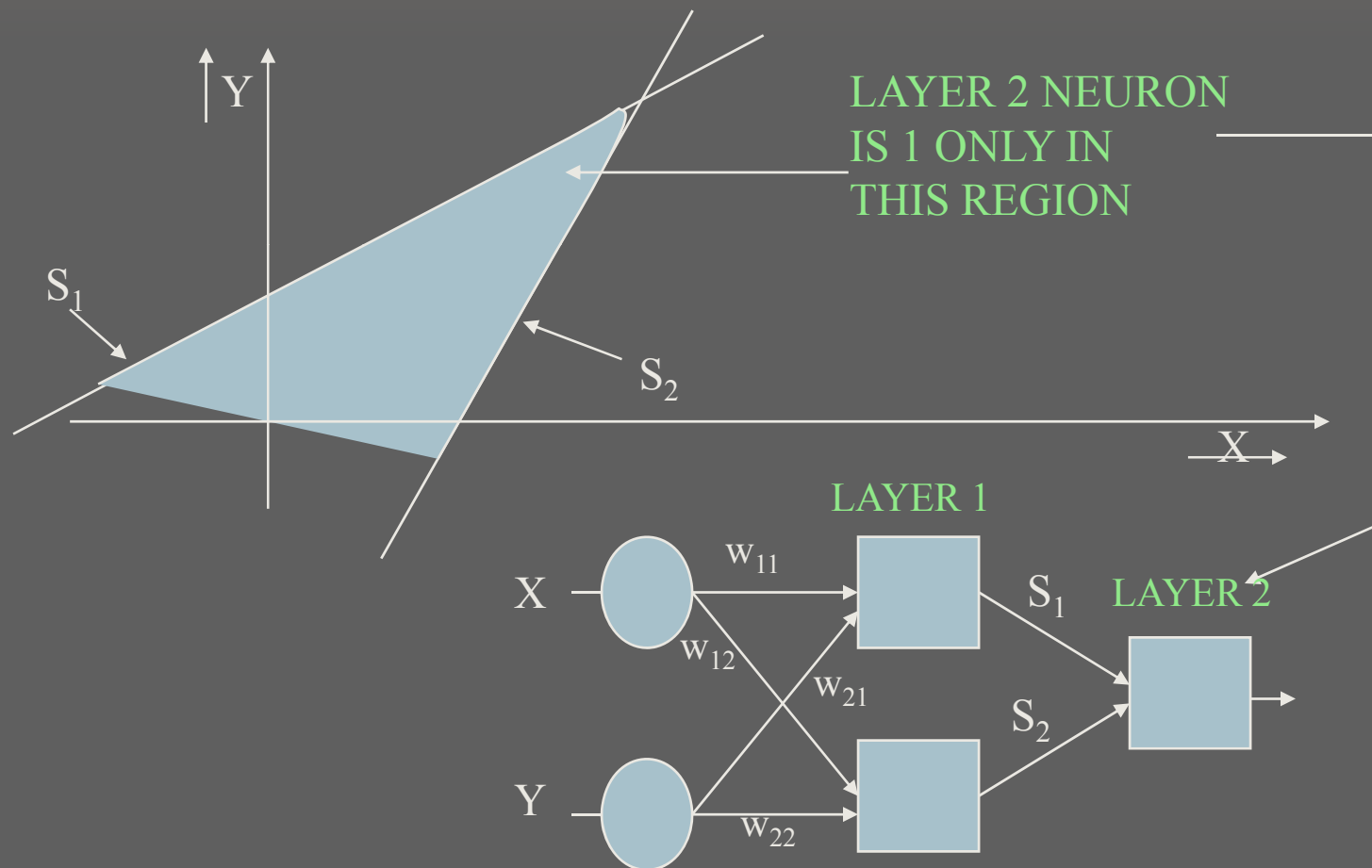


How to design other gates (NOR, NAND) ?

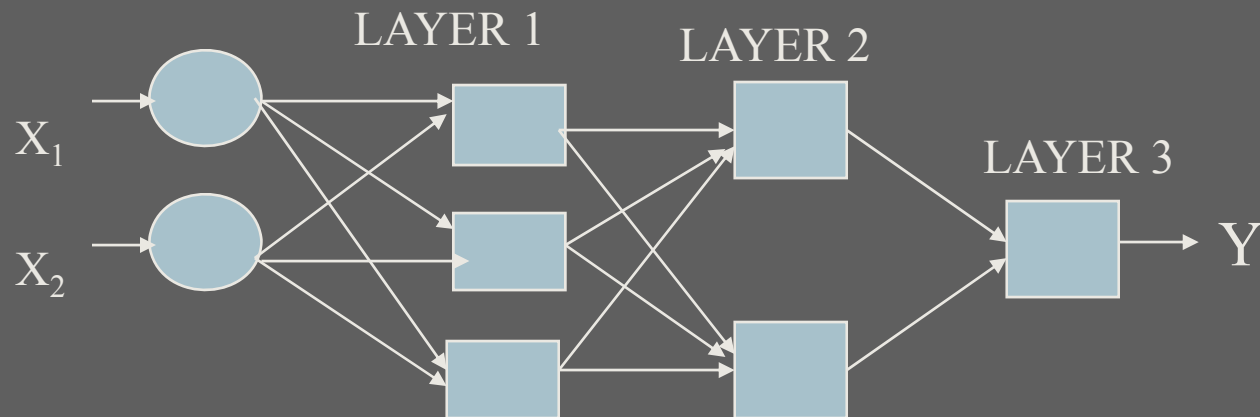
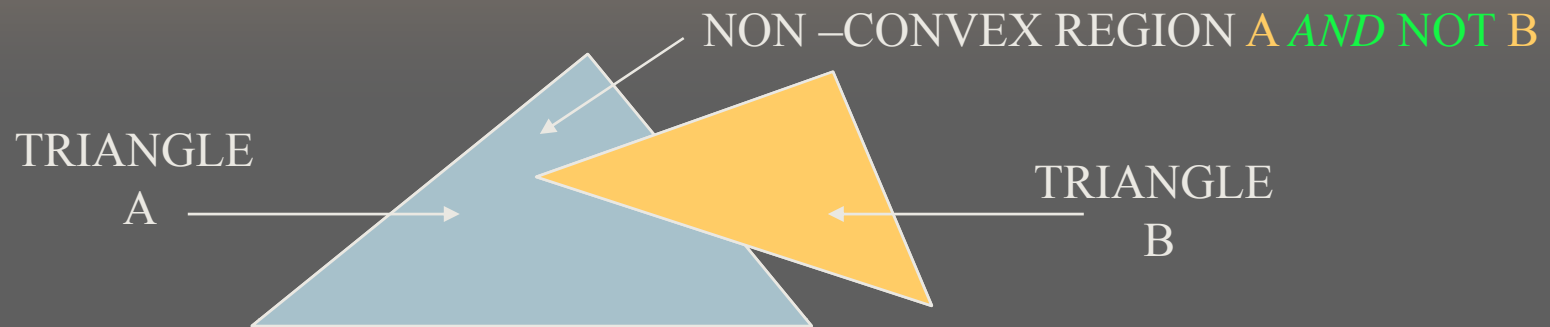


Cascading layers

Two layers : Generates convex decision regions



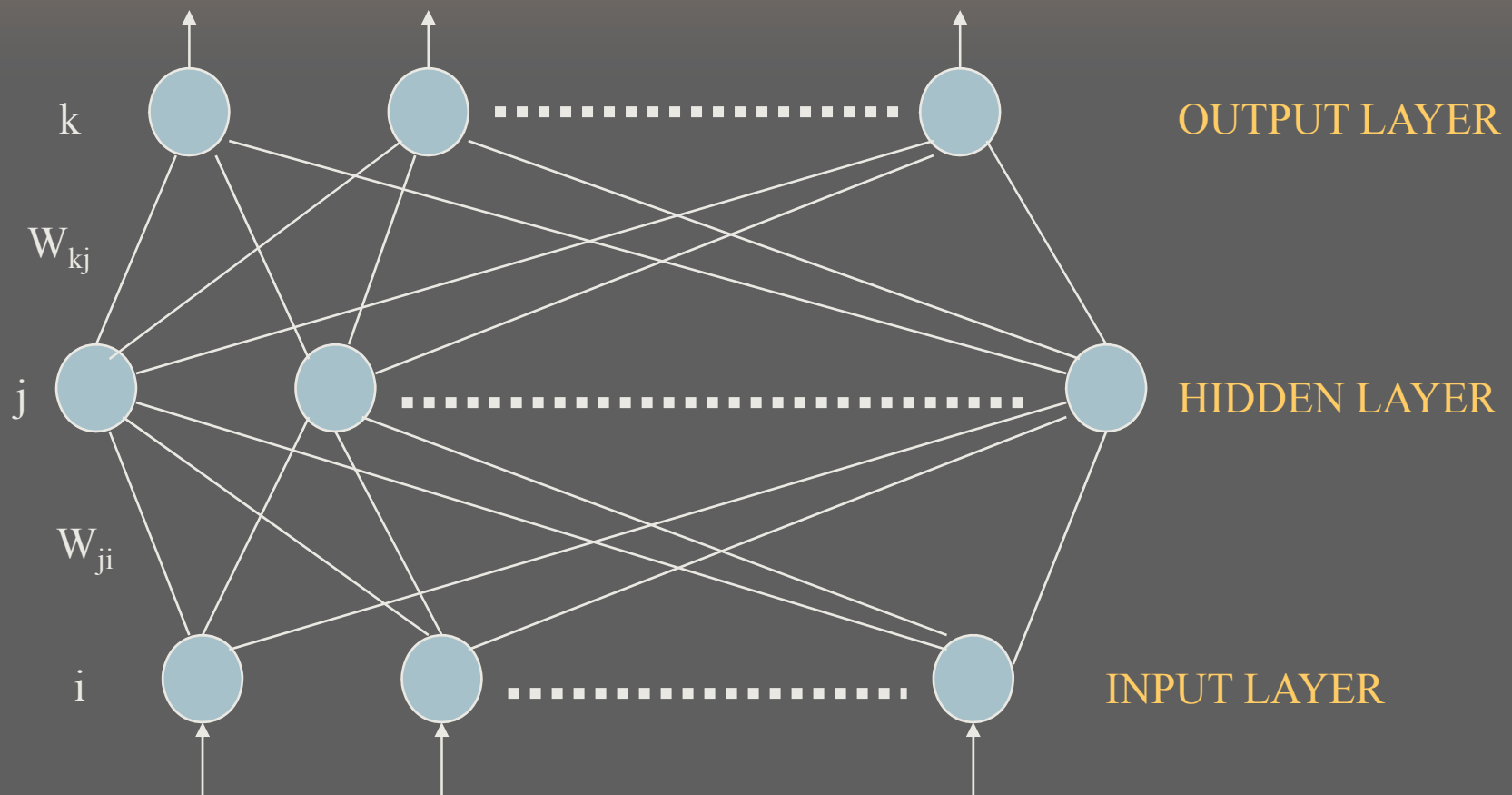
Three layers: Decision regions of any shape



Multi-layer network

Multi-layer perceptron

OUTPUT PATTERN



INPUT PATTERN

- ❖ Nodes of two different consecutive layers are connected by *links* or *weights*.
- ❖ There is no connection among the elements of the same layer.
- ❖ The layer where the inputs are presented is known as the *input layer*.
- ❖ On the other hand the output producing layer is called the *output layer*.
- ❖ The layers in between the input and the output layers are known as *hidden layers*.
- ❖ The total input (I_i) to the i^{th} unit

$$I_i = \sum_j w_{ij} o_j$$

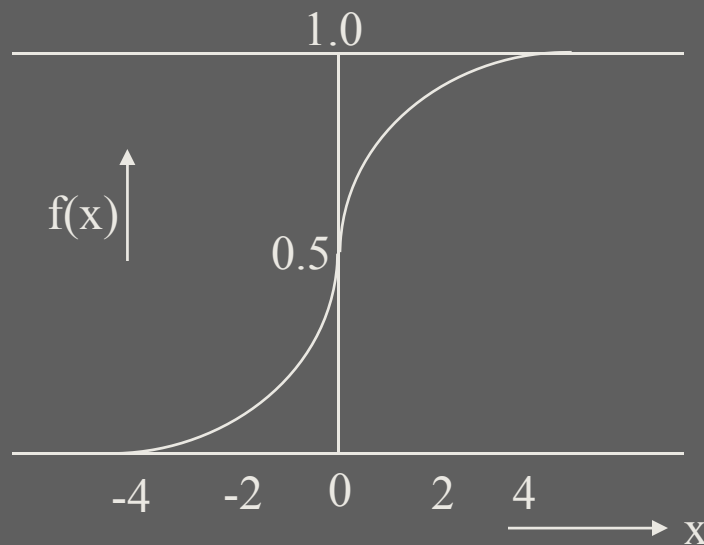
o_j is the output of the j^{th} neuron.

❖ The output of a node i is obtained as

$$o_i = f(I_i), \quad f \text{ is the activation function.}$$

❖ Mostly the activation function is sigmoidal/squashing, with the form (smooth, non-linear, differentiable & saturating),

$$f(x) = 1/(1 + e^{-(x-\theta)/\theta_0}).$$



❖ Initially very small random values are assigned to the links/weights.

Parameter updating

- ❖ For learning (*training*) we present the input pattern $X=\{x_i\}$, and ask the net to adjust its set of weights/biases in the connecting links such that the desired output $T=\{t_i\}$ is obtained at the output layer.
- ❖ Then another pair of X and T is presented for learning.
- ❖ Learning tries to find a simple set of weights and biases that will be able to discriminate among all the input/output pairs presented to it.
- ❖ The output $\{o_i\}$ will not be the same as the target $\{t_i\}$.

Error is,

$$E = \frac{1}{2} \sum_i (t_i - o_i)^2$$

- ❖ For learning the correct set of weights error is E is reduced as rapidly as possible.
- ❖ Use gradient descent technique.

The incremental change in the direction of negative gradient is

$$\Delta w_{ji} \propto -\frac{\partial E}{\partial w_{ji}} = -\eta \frac{\partial E}{\partial w_{ji}} = -\eta \frac{\partial E}{\partial I_j} \frac{\partial I_j}{\partial w_{ji}} = \eta \delta_j o_i$$

where $\delta_j = -\frac{\partial E}{\partial I_j} = -\frac{\partial E}{\partial o_j} \frac{\partial o_j}{\partial I_j} = -\frac{\partial E}{\partial o_j} f'(I_j).$

For the links connected to the output layer the change in weight is given by

$$\Delta w_{ji} = \eta \left(-\frac{\partial E}{\partial o_j} \right) f'(I_j) o_i.$$

For nodes in the hidden layers

$$\frac{\partial E}{\partial o_j} = \sum_k \frac{\partial E}{\partial I_k} \frac{\partial I_k}{\partial o_j} = \sum_k \frac{\partial E}{\partial I_k} \frac{\partial}{\partial o_j} \sum_i w_{ki} o_i = \sum_k \frac{\partial E}{\partial I_k} w_{kj} = \sum_k (-\delta_k) w_{kj}.$$

Hence for the hidden layer we have

$$\Delta w_{ji} = \eta \left(\sum_k \delta_k w_{kj} \right) f'(I_j) o_i$$

If $o_j = \frac{1}{1 + e^{-\left(\sum_i w_{ji} o_i - \theta_j\right)}}$ then $f'(I_j) = \frac{\partial o_j}{\partial I_j} = o_j(1 - o_j)$

and thus we get

$$\Delta w_{ji} = \begin{cases} \eta \left(-\frac{\partial E}{\partial o_j} \right) o_j (1 - o_j) o_i & \rightarrow \text{output layer} \\ \eta \left(\sum_k \delta_k w_{kj} \right) o_j (1 - o_j) o_i & \rightarrow \text{hidden layer} \end{cases}$$

❖ A large value of η corresponds to rapid learning but might result in oscillations.

❖ A momentum term of $\alpha \Delta w_{ji}(t)$ can be added to increase the learning rate without oscillation.

$$\Delta w_{ji}(t+1) = \eta \delta_j o_i + \alpha \Delta w_{ji}(t)$$

❖ The second term is used to specify that the change in w_{ji} at $(t+1)^{th}$ instant should be somewhat similar to the change undertaken at instant t .

Designing Optimum Architecture

- ❖ Design of an optimum neural network for a given problem is still not formally specified.
- ❖ Pruning/growing algorithm are used for optimizing the architectures of neural networks.
- ❖ In growing, people start with a small architecture and gradually add neurons/weights/layer to get an optimum architecture.
- ❖ In pruning, people start with a big architecture and gradually delete neurons/weights/layer to get an optimum architecture.
- ❖ Genetic algorithms are also used to design optimum architectures.



Thank you