

DESIGN OF A FIXED-ORDER RST CONTROLLER FOR INTERVAL SYSTEMS: APPLICATION TO THE CONTROL OF PIEZOELECTRIC ACTUATORS

Sofiane Khadraoui, Micky Rakotondrabe, and Philippe Lutz

ABSTRACT

This paper presents a technique for designing a robust polynomial *RST* controller for parametric uncertain systems. The uncertain parameters are assumed to be bounded by intervals. The computation of the controller is addressed by introducing the interval arithmetic. The controller synthesis is formulated as a set inversion problem that can be solved using the SIVIA algorithm. The proposed method is afterwards applied to design a robust controller for a piezoelectric microactuator. The experimental results show the efficiency of the proposed method. Finally, a fine stability analysis is performed to analytically prove the robustness of the designed controller.

Key Words: Parametric uncertainty, interval model, robust performance, *RST* controller design, piezoelectric microactuators.

I. INTRODUCTION

During the last decade, the problem of designing robust control laws for parametric uncertain systems has attracted much attention [1–9]. Practical considerations have motivated the study of control systems with unknown but bounded parameter uncertainties. Indeed, these uncertainties are often due to various factors such as the sensitivity to environmental conditions (vibrations, evolution of ambient temperature, *etc.*), nonlinearities (hysteresis, time varying parameters, creep, *etc.*), sensor limitations and un-modelled dynamics of systems [1,5,6]. If not considered, these uncertainties cause the degradation of the closed-loop performances or the loss of stability. It is therefore necessary to take them into account and to incorporate enough robustness to the controller in order to maintain the nominal performances.

The compensation of these parametric uncertainties is often accomplished by means of adaptative control [9,10] or by means of robust control laws such as H_2 , H_∞ and μ -synthesis [11,12]. The adaptative control methods require a precise model which is difficult to obtain. Concerning the robust H_2 , H_∞ and μ -synthesis approaches, their efficiency is proved in several applications (Single input single output (SISO) and multiple input multiple output (MIMO) systems) while their major disadvantage is the derivation of high-order

controllers which are time consuming and which limit their embedding possibilities, particularly for embedded microsystems. One way to represent parametric uncertainties is to let each parameter take its value within a range called interval [3,4,13]. In addition to the natural way and simplicity of using intervals to bound uncertain parameters, interval arithmetic presents a symbolic or a numeric certificate of the results. Thus, using interval arithmetic for modeling and control design leads to certified robust stability and performances if a solution exists. For instance, the stability analysis of a characteristic polynomial subjected to uncertain parameters has been discussed in many works [3,14,15]. It was often based on the Routh's criteria and/or on the Kharitonov's theorem. The work in [16] presents the stability of uncertain systems with interval time-varying delay. Reference [17] discusses an approach to design robust stabilizing controllers for interval systems in the state-space representation. A systematic computational technique to design robust stabilizing controllers for interval systems using the constrained optimization problem was proposed in [18]. While the above works consider robust stability, robustness on performances for interval systems has also been discussed in several works [19,4,20–23]. The work in [19] presents an interesting result on the inclusion of interval system performances. Reference [20] proposed a prediction-based control algorithm and its application to a welding process modelled by intervals. In [21], a state feedback controller was first considered to ensure the robust stability, then a pre-filter that guarantees the required performances was constructed by applying a curve fitting technique. In [22], an approach to design a robust proportional–integral–derivative (PID) controller for interval transfer function was derived. However the method was

Manuscript received April 11, 2011; revised August 23, 2011; accepted January 11, 2012.

The authors are with FEMTO-ST Institute, UMR CNRS 6174-UFC/ENSMM/UTBM, Automatic Control and Micro-Mechatronic Systems Depart., AS2M, 24 rue Alain Savary, Besançon 25000, France.

Micky Rakotondrabe is the corresponding author (e-mail: mrakoton@femto-st.fr). This work is supported by Conseil General du Doubs.

limited to 2^{nd} order uncertain systems. In our previous work [23], we proposed to extend the method for n^{th} order uncertain systems but still with zero-order numerator. However, the order of the derived controller was not *a priori* fixed and thus might not adapt to the hardware for implementation in embedded microsystems.

In this paper, we propose the interval modeling of a generalized n^{th} order uncertain parameter (without restriction on the numerator's order), and the design of a robust fixed-order controller to ensure specified performances. The robust controller considered in this contribution is a polynomial RST controller. The polynomials R and S allow creation of a feedback control in order to be robust to the uncertainties, while the polynomial T is introduced in the feedforward to improve the tracking. The computation of these polynomials is based on the inclusion performances theorem [19]. The main advantages of the proposed method relative to existing works are: i) no restriction is imposed on the system order; ii) and the order of the controller is *a priori* fixed, thus low-order (robust) controllers can be yielded. Furthermore, the suggested approach in this paper is simple and involves less computational complexity. The controller synthesis problem is formulated as a set-inversion problem defined as the inclusion parameter by parameter.

The paper is organized as follows. In Section II, preliminaries related to interval arithmetic and systems are recalled. Section III is dedicated to the computation of the controller using the proposed approach. In Section IV, we apply the proposed method to model and control piezoelectric actuators. The experimental results and discussion are presented in Section V. Finally, to evaluate the robustness of the implemented controller, a closed-loop stability analysis is presented in Section VI.

II. INTERVAL ANALYSIS PRELIMINARIES

2.1 Definition of interval

An interval $[x]$ can be defined by the set of all real numbers given as follows:

$$[x] = [x^-, x^+] = \{x \in \mathbb{R} / x^- \leq x \leq x^+\} \quad (1)$$

x^- and x^+ are the left and right endpoints respectively. $[x]$ is degenerate if $x^- = x^+$.

The width of an interval $[x]$ is given by:

$$width([x]) = x^+ - x^- \quad (2)$$

The midpoint of $[x]$ is given by:

$$mid([x]) = \frac{x^+ + x^-}{2} \quad (3)$$

The radius of $[x]$ is defined by:

$$rad([x]) = \frac{x^+ - x^-}{2} \quad (4)$$

2.2 Operations on intervals

The result of an operation between two intervals is an interval that contains all possible solutions as follows. Given two intervals $[x] = [x^-, x^+]$, $[y] = [y^-, y^+]$ and $\circ \in \{+, -, \cdot, /\}$, we can write:

$$[x] \circ [y] = \{x \circ y | x \in [x], y \in [y]\}. \quad (5)$$

Therefore, the sum of two intervals $[x] + [y]$ is given by:

$$[x] + [y] = [x^- + y^-, x^+ + y^+] \quad (6)$$

the difference of two intervals $[x] - [y]$ is:

$$[x] - [y] = [x^- - y^+, x^+ - y^-] \quad (7)$$

the product of two intervals $[x] \cdot [y]$ is:

$$[x] \cdot [y] = [\min(x^-y^-, x^-y^+, x^+y^-, x^+y^+), \max(x^-y^-, x^-y^+, x^+y^-, x^+y^+)] \quad (8)$$

and finally, the quotient $[x]/[y]$ is given by

$$[x]/[y] = [x] \cdot [1/y^+, 1/y^-], 0 \notin [y]. \quad (9)$$

The intersection of two intervals $[x] \cap [y]$ is defined by:

1. if $y^+ < x^-$ or $x^+ < y^-$ the intersection is an empty set:

$$[x] \cap [y] = \emptyset \quad (10)$$

2. Otherwise:

$$[x] \cap [y] = [\max\{x^-, y^-\}, \min\{x^+, y^+\}]. \quad (11)$$

In the latter case, the union of $[x]$ and $[y]$ is also an interval:

$$[x] \cup [y] = [\min\{x^-, y^-\}, \max\{x^+, y^+\}]. \quad (12)$$

When $[x] \cap [y] = \emptyset$, the union of the two intervals is not an interval. For that, the interval hull is defined:

$$[x] \sqcup [y] = [\min\{x^-, y^-\}, \max\{x^+, y^+\}]. \quad (13)$$

It is verified that $[x] \cup [y] \subseteq [x] \cup [y]$ for any two intervals $[x]$ and $[y]$.

2.3 Interval systems

Definition II.1. Parametric uncertain systems can be modelled by interval systems. A SISO interval system that defines a family of systems is denoted $[G](s, [p], [q])$ and is given by:

$$[G](s, [p], [q]) = \frac{\sum_{j=0}^m [q_j] s^j}{\sum_{i=0}^n [p_i] s^i} = \left\{ \frac{\sum_{j=0}^m p_j s^j}{\sum_{i=0}^n p_i s^i} \mid p_i \in [p_i^-, p_i^+], p_j \in [p_j^-, p_j^+] \right\} \quad (14)$$

Such as: $[q] = [[q_0], \dots, [q_m]]$ and $[p] = [[p_0], \dots, [p_n]]$ are boxes (*i.e.* vectors of interval).

The following lemma and theorem concern the performances of two interval systems and are due to [19]. Consider two interval systems having the same structure (degrees of polynomials):

$$[G_1](s) = \frac{\sum_{j=0}^m [b_{1j}] s^j}{\sum_{i=0}^n [a_{1i}] s^i} \quad (15)$$

and

$$[G_2](s) = \frac{\sum_{l=0}^m [b_{2l}] s^l}{\sum_{k=0}^n [a_{2k}] s^k} \quad (16)$$

Lemma II.1. (Inclusion of two interval systems)

$$\left\{ \begin{array}{l} [a_{1k}] \subseteq [a_{2k}], \forall k = 1 \dots n \\ \text{and} \\ [b_{1l}] \subseteq [b_{2l}], \forall l = 1 \dots m \end{array} \right\} \Rightarrow [G_1](s) \subseteq [G_2](s);$$

Theorem II.1. (Performances inclusion theorem)

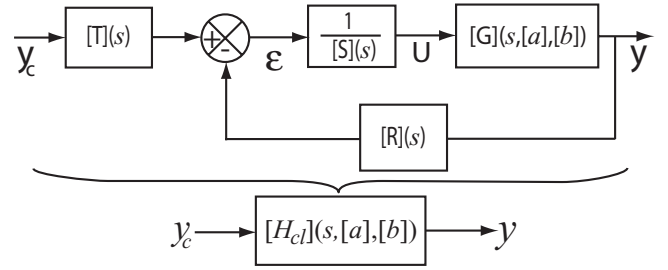


Fig. 1. Closed-loop system transfer $[H_{cl}](s, [a], [b])$.

$$\begin{aligned} \text{if } [G_1](s) &\subseteq [G_2](s); \\ \Rightarrow \left\{ \begin{array}{l} [g_1](t) \subseteq [g_2](t) \quad \forall t \\ [\rho]([G_1](j\omega)) \subseteq [\rho]([G_2](j\omega)) \quad \forall \omega \\ [\phi]([G_1](j\omega)) \subseteq [\phi]([G_2](j\omega)) \end{array} \right. \end{aligned}$$

where $[g_i](t)$ is the (temporal) impulse response of system $[G_i](s)$, $[\rho]([G_i](j\omega))$ is its modulus and $[\phi]([G_i](j\omega))$ is its phase.

Proof II.1. See [19].

Theorem II.1 states that if $[G_1](s)$ is included in $[G_2](s)$, its temporal response (impulse response, step response, *etc.*) will be included in that of $[G_2](s)$. The same holds for the frequential response (Bode, Nyquist, Black-Nichols). Such inclusion of responses directly induces the performances inclusion and can be used to design a robust controller, as we propose in this paper.

III. PROBLEM STATEMENT

Consider an interval system $[G](s, [a], [b])$ to be controlled by an *RST* controller (Fig. 1). The choice of the *RST* structure of controller is that it is a more general structure. The PID controller is a particular case of the *RST* controller when $R(s) = T(s)$. Now, the problem consists of finding the different polynomials R , S and T of the controller that ensures some given performances for the closed-loop system $[H_{cl}](s, [a], [b])$ (see Fig. 1) whatever the parameters a and b ranging in $[a]$ and $[b]$ respectively.

In the following, the system $[G](s, [a], [b])$ will be denoted by:

$$[G](s, [a], [b]) = \frac{[N](s, [b])}{[D](s, [a])} \quad (17)$$

where $[N](s, [b])$ and $[D](s, [a])$ are interval polynomials defined by:

$$[N](s, [b]) = 1 + \sum_{j=1}^m [b_j] s^j$$

$$[D](s, [a]) = \sum_{i=0}^n [a_i] s^i$$

such that $[a] = [[a_0], \dots, [a_n]]$, $[b] = [1, [b_1], \dots, [b_m]]$ and $m \leq n$.

This form of representation (unit on the numerator) facilitates the application of the proposed control method. In fact, it is always possible to describe the system using this representation form.

Consider the following performances that we expect for the closed-loop system:

- no overshoot,
- settling time $tr_{5\%} \in [tr^-, tr^+]$, and
- static error $|\varepsilon| \leq \eta$.

These specifications can be easily described by means of an interval model, called an interval reference model, denoted $[H](s)$:

$$[H](s) = \frac{[K_e]}{1 + [\tau]s} \quad (18)$$

where $[\tau] = [\tau^-, \tau^+]$, $[K_e] = [K_e^-, K_e^+]$.

Settling time and static error of (18) are defined by $[tr_{5\%}] = 3 \cdot [\tau]$ and $|\varepsilon| = |[K_e] - 1|$ respectively.

Based on Theorem II.1, the following problem is there-for addressed.

Problem III.1. Given an interval system $[G](s)$ and an interval reference model $[H](s)$ that defines some given performances, find a controller $[C](s)$ such that $[H_{cl}](s) \subseteq [H](s)$. In other words, the problem consists of finding a set of controllers $[C](s)$, gathered in an interval $[C](s)$, such that the performances of the closed-loop system $[H_{cl}](s)$ are included in the specified performances.

3.1 Computation of the closed-loop model $[H_{cl}](s)$

In this part, we compute the closed-loop model using the interval system and the controller transfers. The generalized form of the RST controller can be defined as follows:

$$[R](s) = \sum_{i=1}^{r_n} [r_i] s^i$$

$$[S](s) = \sum_{i=1}^{s_n} [s_i] s^i \quad (19)$$

$$[T](s) = \sum_{i=1}^{t_n} [t_i] s^i$$

such that $s_n \geq r_n \geq t_n$ in order to have the causality of the controller.

Let us now define fixed-order RST structure with a fixed and low degree for each of the interval polynomials $[R]$, $[S]$ and $[T]$. Polynomials with first-degree are chosen for that:

$$\begin{aligned} [R](s) &= [r_1]s + [r_0] \\ [S](s) &= [s_1]s + [s_0] \\ [T](s) &= [t_1]s + 1 \end{aligned} \quad (20)$$

We have chosen t_0 equals to one in order to minimize the number of the controller parameters to be sought. On one hand, this facilitates the computation of the controller. On the other hand, even if we choose $t_0 \neq 1$, any setting on the parameters t_1 , r_1 and r_0 will lead to $t_0 = 1$.

Remark III.1. If we cannot find a controller $[C](s)$ that satisfies Problem III.1, the degree of one or more of the polynomials $[R]$, $[S]$, and $[T]$ can be increased and the controller synthesis is performed again.

Let us define the box of the controller parameters $[\theta] = [[t_1], [r_1], [r_0], [s_1], [s_0]]$.

From Fig. 1, and using the interval system (17) and the controller RST (20), the interval closed-loop transfer $[H_{cl}](s, [a], [b], [\theta])$ is derived:

$$[H_{cl}](s, [a], [b], [\theta]) = \frac{[T](s)}{\frac{[S](s)}{[G](s, [a], [b])} + [R](s)} \quad (21)$$

(21) can be rewritten as follows:

$$[H_{cl}](s, [a], [b], [\theta]) = \frac{[T](s) \cdot [N](s, [b])}{[S](s) \cdot [D](s, [a]) + [R](s) \cdot [N](s, [b])} \quad (22)$$

After replacing the different polynomials, we obtain the interval closed-loop transfer $[H_{cl}](s, [a], [b], [\theta])$ depending on the different interval parameters:

$$[H_{cl}](s, [a], [b], [\theta]) = \frac{([t_1]s + 1) \left(1 + \sum_{j=1}^m [b_j] s^j \right)}{([s_1]s + [s_0]) \sum_{i=0}^n [a_i] s^i + ([r_1]s + [r_0]) \left(1 + \sum_{j=1}^m [b_j] s^j \right)} \quad (23)$$

After developing (23), we obtain:

$$[H_{cl}](s, [p], [q]) = \frac{1 + \sum_{j=1}^e [q_j] s^j}{\sum_{i=0}^r [p_i] s^i} \quad (24)$$

Where $e = m + 1$ and $r = n + 1$. The boxes of interval parameters $[p]$ and $[q]$ are function of the boxes $[a]$, $[b]$ and $[\theta]$.

3.2 Controller derivation

The main objective consists of finding the set Θ of the controller parameters vector for which robust performances hold:

$$\Theta := \{\theta \in [\theta] \mid [H_{cl}](s, [p], [q]) \subseteq [H](s)\}. \quad (25)$$

This computation of Θ is feasible if and only if $[H_{cl}](s, [p], [q])$ has the same structure as $[H](s)$, *i.e.* their numerators have the same degree and the same holds for their denominators. As the structure of $[H_{cl}](s, [p], [q])$ is *a priori* fixed, we should adjust the structure of $[H](s)$ to satisfy such condition if it was not yet the case. For that, first let us look at the structure of $[H_{cl}](s, [p], [q])$ as in (24). The degree of the numerator is $(m + 1)$ while it is $(n + 1)$ for the denominator. Let us now adjust the structure of $[H](s)$ (see (18)) in order to have the same structure by adding some zeros and poles far away from the imaginary axes. This leads to the following reference model:

$$[H](s) = \frac{\left(1 + \frac{[\tau]}{\kappa}s\right)^{m+1}}{\frac{1}{[K_e]} \cdot (1 + [\tau]s) \left(1 + \frac{[\tau]}{\kappa}s\right)^n} \quad (26)$$

with $\kappa \gg 1$.

After developing (26), we have:

$$[H](s, [w], [x]) = \frac{1 + \sum_{j=1}^{m+1} [x_j]s^j}{\sum_{i=0}^{n+1} [w_i]s^i} \quad (27)$$

where $[x_j]$ and $[w_i]$ (for $j = 1, \dots, m + 1$ and $i = 0, \dots, n + 1$) are functions of the interval parameters $[K_e]$, $[\tau]$ and of the real number κ .

3.3 Inclusion condition

The research of parameter Θ in (25) of the controller is done by using the inclusion $[H_{cl}](s) \subseteq [H](s)$ (see Problem III.1). However, according to Lemma II.1, such inclusion can be satisfied by considering the inclusion of each parameter of $[H_{cl}](s)$ inside that of $[H](s)$. Thus, by using (24) and (27), the problem becomes the research of the controller parameters under the following constraints:

Table I. Algorithm SIVIA for solving a set-inversion problem [3,24].

SIVIA(in: $[p]$, $[q]$, $[w]$, $[x]$, $[\theta]$, \in ; inout: $\underline{\Theta}$, $\bar{\Theta}$)
1 if $[[p]([\theta]), [q]([\theta]), [w]([\theta])] \cap [[w], [x]] = \emptyset$ return;
2 if $[[p]([\theta]), [q]([\theta])] \subseteq [[w], [x]]$ then $\underline{\Theta} := \underline{\Theta} \cup [\theta]$; $\bar{\Theta} := \bar{\Theta} \cup [\theta]$ } return;
4 if $\text{width}([\theta]) < \epsilon$ then $\bar{\Theta} := \bar{\Theta} \cup [\theta]$; return
5 bisection of $[\theta]$ into $L([\theta])$ and $R([\theta])$;
6 SIVIA($[p]$, $[q]$, $[w]$, $[x]$, $L([\theta])$, \in ; $\underline{\Theta}$, $\bar{\Theta}$); SIVIA($[p]$, $[q]$, $[w]$, $[x]$, $R([\theta])$, \in ; $\underline{\Theta}$, $\bar{\Theta}$).

$$\begin{aligned} [q_j] &\subseteq [x_j], \forall j = 1, \dots, m + 1 \\ [p_i] &\subseteq [w_i], \forall i = 0, \dots, n + 1 \end{aligned} \quad (28)$$

and therefore, the computation problem in (25) of the set parameters Θ is reduced to the following problem:

$$\Theta := \left\{ \theta \in [\theta] \mid \begin{aligned} &[q_j]([\theta]) \subseteq [x_j], \forall j = 1, \dots, m + 1 \\ &[p_i]([\theta]) \subseteq [w_i], \forall i = 0, \dots, n + 1 \end{aligned} \right\} \quad (29)$$

This problem is known as a Set-Inversion Problem which can be solved using interval techniques [3,13]. The set inversion operation consists of computation the reciprocal image of a compact set called subpaving. The set-inversion algorithm SIVIA (more details are given in [3,24]) allows the approximation with subpavings, of the set solution Θ described in (29). This approximation is realized with inner and outer subpavings, respectively $\underline{\Theta}$ and $\bar{\Theta}$, such that $\underline{\Theta} \subseteq \Theta \subseteq \bar{\Theta}$. The subpaving $\underline{\Theta}$ corresponds to the controller parameter vector for which the problem (29) holds. If $\bar{\Theta} = \emptyset$, then it is guaranteed that no solution exists for (29).

Table I resumes the recursive SIVIA algorithm allowing the solving of a set of inversion problem in intervals. We give, in Fig. 2, a flow chart that describes this recursive SIVIA algorithm when applied to the computation of the RST controller parameters and which is given by the problem (29). The SIVIA algorithm requires a search box $[\theta_0]$ (possibly very large) called initial box to which $\bar{\Theta}$ is guaranteed to belong. The inner and outer subpavings ($\underline{\Theta}$ and $\bar{\Theta}$) are initially empty.

Remark III.2. In most cases, we are interested computing an inner subpaving $\underline{\Theta}$ for which we are sure that $\underline{\Theta}$ is included in the set solution Θ , *i.e.* $\underline{\Theta} \subseteq \Theta$, but when no inner subpaving exists ($\underline{\Theta} = \emptyset$), it is possible to choose parameters inside the outer subpaving, *i.e.* choose $\theta \in \bar{\Theta}$.

IV. APPLICATION TO PIEZOCANTILEVERS

In this section, we apply the proposed method to control the deflection of piezoelectric actuators used in micro-grippers. The latter are considered as microsystems. These

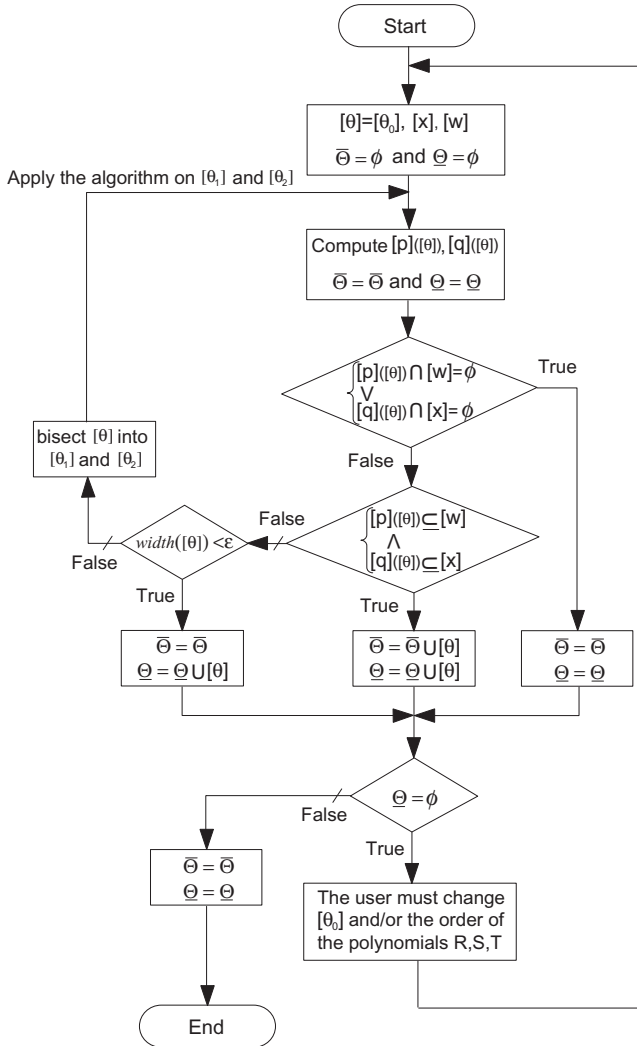


Fig. 2. Algorithm SIVIA used to solve the set-inversion problem (29)[3,24].

microgrippers are widely used in micromanipulation and microassembly tasks where the required performances are severe (submicrometric accuracy, tens of milliseconds of settling time, no overshoot, etc.) [25]. A microgripper is based on two piezoelectric cantilevers (microactuators) also called piezocantilevers [26,27]. While one piezocantilever is controlled on position (deflection), the second one is controlled on force. This allows the precise positioning of a manipulated small object by controlling, at the same time, the handling force. In this work, we focus our study on the position control. The piezocantilever used during the experiments is a unimorph piezocantilever with rectangular cross-section. Such a cantilever is made up of one piezoelectric layer (piezolayer) and one passive layer. When a voltage U is applied to the piezolayer, it contracts/expands accordingly to the direction

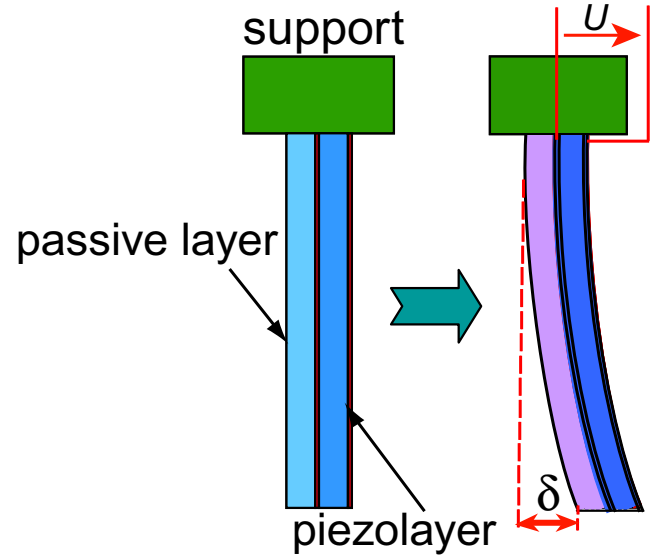


Fig. 3. Principle of a unimorph piezocantilever.

of the applied electric field. As the piezolayer and the passive layer are glued themselves, a global deflection y of the structure is yielded (Fig. 3).

Due to their small sizes, piezocantilevers are very sensitive to their environment (thermal variation, vibration, surrounding surface forces, etc.) and to the reaction of the manipulated objects. This high sensitivity leads to a change of their behavior during the tasks (manipulation, etc.). Unfortunately, the change of the environment is hardly known and hardly modelizable at the micro/nano-scale, making the use of a kind of real-time adaptive control law impossible. Furthermore, this difficulty is confirmed by the lack of convenient sensors that can be used to measure the environmental variation at this scale. This is why it is more attractive to employ more simplified models and to synthesize robust control laws for piezocantilevers. Classical H_∞ robust control laws have successfully been used in our previous works [28], however the orders of the derived controllers were high and may not be convenient for embedded microsystems, such as embedded microgrippers. Controllers that account for eventual nonlinearities were also used but they required the use of precise models of these nonlinearities [29,30] which finally make the controller implementation complex. The technique presented in this paper is thus used. Its advantages are: i) the ease of modeling the parametric uncertainties by just bounding them with intervals; and ii) the derivation of a low order controller since its structure is *a priori* fixed.

As it is impossible to characterize the model variation of a given piezocantilever during its functioning and then to derive an interval model $[G](s, [a], [b])$, we use the following procedure.

Two piezocantilevers are randomly taken from a set of stock piezocantilevers having the same dimensions and the same physical characteristics. Such stock is essential in the micromanipulation and microassembly context in order to ensure a quick replacement in case of breakage of actuators. In that case, it is desired that the same controller is used for the new actuator. However, even if these piezocantilevers are physically and geometrically similar, there are always non negligible differences in their model parameters. These differences on model parameters are due to small and non-perceptible differences in the sizes of the piezocantilevers (in the order of tens of micrometres) due to the fabrication accuracy. The two different models of the chosen piezocantilevers will be therefore used to derive an interval model $[G](s, [a], [b])$.

4.1 Presentation of the setup

Fig. 4 presents the experimental setup. It is composed of:

- two unimorph piezocantilevers. Each piezocantilever is based on a PZT (lead zirconate titanate) for the piezolayer and on copper for the passive layer. The dimensions of the cantilevers are approximately $L \times b \times h = 15 \text{ mm} \times 2 \text{ mm} \times 0.3 \text{ mm}$, where the thicknesses are 0.2 mm and 0.1 mm for the PZT and for the Copper respectively,
- an optical sensor (Keyence LC-242) used to measure the deflection of the piezocantilevers. The sensor has 10 nm of resolution,
- a computer-Dspace hardware combined with the Matlab-Simulink software for the implementation of the controller and for data acquisition,
- and a high voltage (HV: $\pm 200 \text{ V}$) amplifier used to amplify the input voltage from the computer-Dspace material.

4.2 Modeling of the two piezocantilevers

The linear relation between the deflection at the tip of the piezocantilever and the applied input voltage U is:

$$\delta = G(s)U. \quad (30)$$

To identify the two models $G_1(s)$ and $G_2(s)$ corresponding to the two piezocantilevers, a step response is used. A second order was chosen for the model of each piezocantilever because of its sufficiency to account the first resonance which is sufficient for the expected applications. The identification of the two models $G_1(s)$ and $G_2(s)$ was afterwards performed using the output error method and the MATLAB software. We obtain:

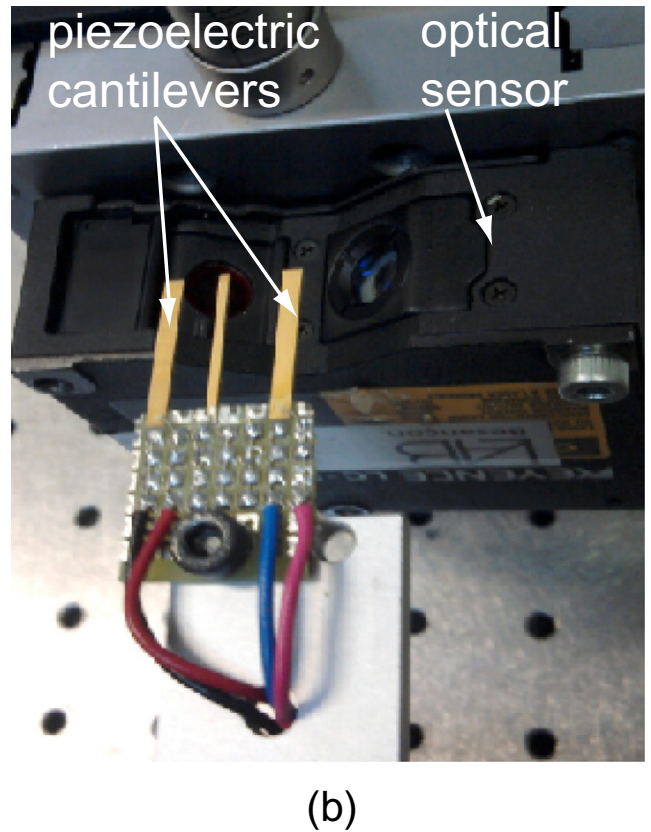
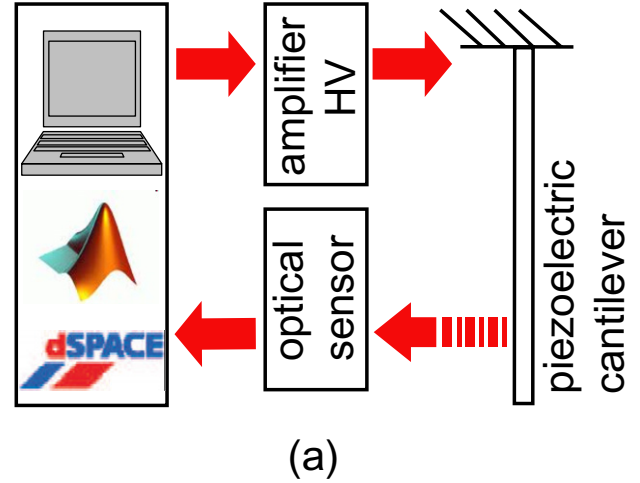


Fig. 4. The experimental setup: piezocantilevers controlled through computer DSpace material.

$$\begin{aligned} G_1(s) &= \frac{8.08 \times 10^{-8} s^2 + 1.809 \times 10^{-4} s + 1}{8.753 \times 10^{-8} s^2 + 5.234 \times 10^{-6} s + 1.283} \\ G_2(s) &= \frac{6.992 \times 10^{-8} s^2 + 1.807 \times 10^{-4} s + 1}{9.844 \times 10^{-8} s^2 + 5.37 \times 10^{-6} s + 1.448} \end{aligned} \quad (31)$$

4.3 Derivation of the interval model

Let us rewrite each model $G_i(s)$ ($i = 1, 2$) as follows:

$$G_i(s) = \frac{b_{2i}s^2 + b_{1i}s + 1}{a_{2i}s^2 + a_{1i}s + a_{0i}} \quad (32)$$

The interval model $[G](s, [a], [b])$ which represents a family of piezocantilever models is derived using the two point models $G_i(s)$. Considering each parameter of $G_1(s)$ and its counterpart in $G_2(s)$ as an endpoint of the interval parameter in $[G](s, [a], [b])$, we have:

$$[G](s, [a], [b]) = \frac{[b_2]s^2 + [b_1]s + 1}{[a_2]s^2 + [a_1]s + [a_0]} \quad (33)$$

such that:

$$[b_2] = [\min(b_{21}, b_{22}), \max(b_{21}, b_{22})]$$

$$[b_1] = [\min(b_{11}, b_{12}), \max(b_{11}, b_{12})]$$

$$[a_2] = [\min(a_{21}, a_{22}), \max(a_{21}, a_{22})]$$

$$[a_1] = [\min(a_{11}, a_{12}), \max(a_{11}, a_{12})]$$

$$[a_0] = [\min(a_{01}, a_{02}), \max(a_{01}, a_{02})]$$

After computation, we obtain:

$$[b_2] = [6.992, 8.08] \times 10^{-8}$$

$$[b_1] = [1.807, 1.809] \times 10^{-4}$$

$$[a_2] = [8.753, 9.844] \times 10^{-8}$$

$$[a_1] = [5.234, 5.37] \times 10^{-6}$$

$$[a_0] = [1.283, 1.448]$$

To increase the stability margin of the closed-loop system, we propose to extend the widths of the interval parameters of the model (33). This extension is a compromise. In fact, if the widths of these interval parameters are too large, it is difficult to find a controller that respects both the stability and performances of the closed-loop system. After some trials of controller design, we choose to expand the width of each interval parameter of (33) by 10%. It represents a good compromise between the extension of the width and the possibility to find a robust controller. Finally, the extended parameters of the interval model which will be used to compute the controller are:

$$\begin{aligned} [b_2] &= [6.937, 8.134] \times 10^{-8} \\ [b_1] &= [1.8067, 1.809] \times 10^{-4} \\ [a_2] &= [8.698, 9.898] \times 10^{-8} \\ [a_1] &= [5.227, 5.376] \times 10^{-6} \\ [a_0] &= [1.274, 1.456] \end{aligned} \quad (34)$$

4.4 Performances specifications

Microassembly and micromanipulation tasks generally require a submicrometric accuracy and high repeatability. Furthermore, the behavior of actuators used in these tasks is often desired to be without overshoot to ensure better quality tasks and to avoid destroying the manipulated micro-object or conversely to avoid the destruction of the actuators themselves. To incorporate all of the above, we consider the following specifications:

- behavior without or with small overshoot,
- settling time $tr_{5\%} < 30$ ms,
- static error allowed $|\varepsilon| \leq 1\%$.

4.5 Computation of the closed-loop transfer

From the model $[G](s, [a], [b])$ in (33) and from the RST controller in (20) to be designed, we derive the closed-loop $[H_{cl}](s, [a], [b], [\theta])$:

$$\begin{aligned} [H_{cl}](s, [a], [b], [\theta]) &= \frac{([t_1]s + 1)([b_2]s^2 + [b_1]s + 1)}{([s_1]s + [s_0])([a_2]s^2 + [a_1]s + 1) + ([r_1]s + [r_0])([b_2]s^2 + [b_1]s + 1)} \end{aligned} \quad (35)$$

After developing (35), the closed-loop can be written as follows:

$$[H_{cl}](s, [p], [q]) = \frac{[q_3]s^3 + [q_2]s^2 + [q_1]s + 1}{[p_3]s^3 + [p_2]s^2 + [p_1]s + [p_0]} \quad (36)$$

where the boxes $[q]$, $[p]$ depend on the boxes $[a]$ and $[b]$ of the interval model and on the interval parameters $[\theta] = [[t_1], [r_0], [r_1], [s_1], [s_0]]$ of the controller as described below:

$$\begin{aligned} [q_3] &= [t_1][b_2] \\ [q_2] &= [t_1][b_1] + [b_2] \\ [q_1] &= [t_1] + [b_1] \\ [p_3] &= [s_1][a_2] + [r_1][b_2] \\ [p_2] &= [s_1][a_1] + [s_0][a_2] + [r_1][b_1] + [r_0][b_2] \\ [q_1] &= [s_1][a_0] + [s_0][a_1] + [r_0][b_1] + [r_1] \\ [p_0] &= [s_0][a_0] + [r_0] \end{aligned} \quad (37)$$

4.6 Computation of the interval reference model

The specifications in Section 4.4 can be transcribed into an interval reference model. According to the remark in

Section 3.2, this reference model must have the same structure as the closed-loop (36). So, the reference model must be characterized by an order $n = m = 2$. We have:

$$[H](s) = \frac{\left(1 + \frac{[\tau]}{\kappa}s\right)^3}{\frac{1}{[K_e]} \cdot (1 + [\tau]s) \left(1 + \frac{[\tau]}{\kappa}s\right)^2} \quad (38)$$

that such as $[\tau] = [0, 10 \text{ ms}]$, $[K_e] = [0.99, 1.01]$ and $\kappa = 10$.

After developping (38), we obtain:

$$[H](s) = \frac{[x_3]s^3 + [x_2]s^2 + [x_1]s + 1}{[w_3]s^3 + [w_2]s^2 + [w_1]s + [w_0]} \quad (39)$$

where the boxes $[x]$ and $[w]$ are a function of the box $[[K_e], [\tau], [\kappa]]$ as follows:

$$\begin{aligned} [x_3] &= \frac{\tau^3}{\kappa^3} \\ [x_2] &= \frac{3\tau^2}{\kappa^2} \\ [x_1] &= \frac{3\tau}{\kappa} \\ [w_3] &= \frac{\tau^3}{\kappa^2 K_e} \\ [w_2] &= \frac{(1+2\kappa)\tau^2}{\kappa^2 K_e} \\ [w_1] &= \frac{(\kappa+2)\tau}{\kappa K_e} \\ [w_0] &= \frac{1}{K_e} \end{aligned} \quad (40)$$

4.7 Derivation of the controller

The derivation of the controller consists of finding the set (or subset) of the interval parameters $[\theta] = [[t_1], [r_0], [r_1], [s_1], [s_0]]$ for which specifications hold, *i.e.* find $[\Theta]$ such that:

$$\Theta := \left\{ \theta \in [\theta] \mid \begin{aligned} &[q_j](\theta) \subseteq [x_j], \forall j = 1, \dots, 3 \\ &[p_i](\theta) \subseteq [w_i], \forall i = 0, \dots, 3 \end{aligned} \right\} \quad (41)$$

where $[[p_i], [q_j]]$ and $[[w_i], [x_j]]$ (for $i = 0, \dots, 3$ and $j = 1, \dots, 3$) are defined in (37) and (40) respectively.

Remark IV.1. The number of unknown parameters (see (20)) is 5 while the number of inclusions (41) is 7. Therefore, there are more inclusions than unknown variables. In such a situation, the set solution Θ is given by the intersection of the set solution of each inclusion in (41), *i.e.*:

$$\Theta = \bigcap_{i=1}^7 (\text{set_sol})_i$$

such that: $(\text{set_sol})_i$ is the set solution of the i^{th} inclusion.

The SIVIA algorithm is applied to solve problem (41) and to characterize the set solution Θ . However, the computation time increases exponentially with the number of parameters making, it difficult to solve such a problem with multiple parameters. Since our objective is not to compute all possible *RST* controllers that ensure specifications but to find a set (or subset) of *RST* controllers satisfying desired behaviors of the closed-loop (see Section 4.4), we choose to solve the problem (41) not through SIVIA alone but also through some hand-tuning prior to this algorithm. The procedure consists of manually settling some parameters (as given scalars or as given intervals) and then to seek for the remaining parameters with the SIVIA algorithm.

The three first inclusions $[q_j] \subseteq [x_j]$ for $j = 1, \dots, 3$ depend only on the parameter $[t_1]$, so they can be solved independently. These inclusions are linear and have one parameter which can be solved using the SIVIA algorithm. After application of SIVIA, we obtain the following solution:

$$[t_1] = [0, 2.81 \times 10^{-3}]. \quad (42)$$

Now, the second part of the inclusions (41) remain to be solved, *i.e.* the inclusions $[p_i] \subseteq [w_i]$ for $i = 0, \dots, 3$. In order to cancel the static error, *i.e.* $[p_0] = p_0 = 1$, the parameters $[s_0]$ and $[r_0]$ are manually adjusted as follows:

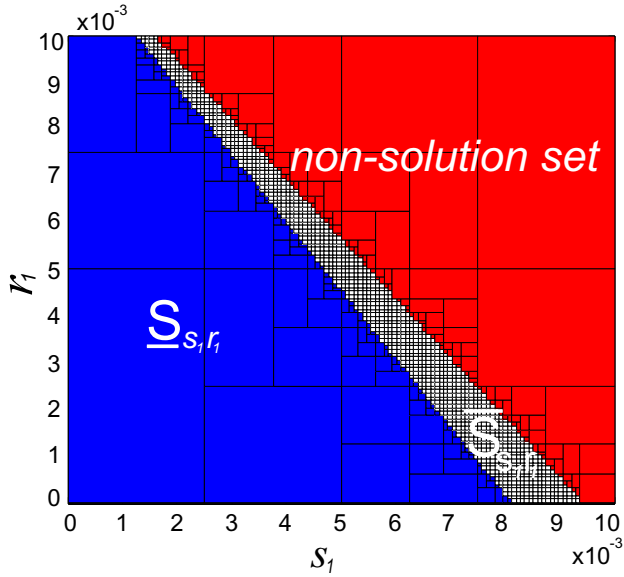
$$\begin{cases} [s_0] = s_0 = 0 \\ [r_0] = r_0 = 1 \end{cases} \quad (43)$$

which also confirms that the last inclusion $[p_0] \subseteq [w_0]$ is respected.

Finally, we have to solve the following problem with two parameters $[s_1]$ and $[r_1]$:

$$\begin{aligned} [s_1][a_2] + [r_1][b_2] &\subseteq \frac{\tau^3}{\kappa^2 K_e} \\ [s_1][a_1] + [r_1][b_1] + [b_2] &\subseteq \frac{1+2\kappa}{\kappa^2} \frac{\tau^2}{K_e} \\ [s_1][a_0] + [b_1] + [r_1] &\subseteq \frac{\kappa+2}{\kappa} \frac{\tau}{K_e} \end{aligned} \quad (44)$$

To characterize the set solution $S_{s_1 r_1}$ of the parameters $[s_1]$ and $[r_1]$, we apply the SIVIA algorithm for the second time to the inclusions (44). We choose an initial box $[s_{10}] \times [r_{10}] = [0.01 \times 10^{-3}, 10 \times 10^{-3}] \times [0.01 \times 10^{-3}, 10 \times 10^{-3}]$ and an accuracy of $\varepsilon = 0.1 \times 10^{-3}$. The obtained subpartition is given in Fig. 5.

Fig. 5. Resulting subpaving $[s_1] \times [r_1]$.

The area in blue corresponds to the inner subpaving $\underline{S}_{s_1 r_1}$ i.e. the set solution $[s_1] \times [r_1]$ of the inclusions (44). The area in white corresponds to the outer subpaving $\bar{S}_{s_1 r_1}$, it contains the boxes for which no decision on the test of inclusion in (44) can be taken. $\bar{S}_{s_1 r_1}$ can be minimized by increasing the computation accuracy. The boxes in red correspond to the parameters $[s_1]$ and $[r_1]$ for which the inclusions (44) do not hold. A controller with the parameters $t_1 \in [0, 2.8 \times 10^{-3}]$, $s_0 = 0$, $r_0 = 1$ and any choice of s_1 , r_1 in the blue colored area $\underline{S}_{s_1 r_1}$ applied to the interval model (uncertain model) $[G](s, [a], [b])$ with parameters given in (34) will satisfy the required performances specified in Section 4.4.

Note that the set $\underline{S}_{s_1 r_1}$ does not represent the set of all possible controllers that satisfy the required performances but a subset of these controllers. Therefore, any change on the values of the parameters $[s_0]$ and $[r_0]$ leads to a change on the subset $\underline{S}_{s_1 r_1}$.

The searched inner subpaving $\underline{\Theta}$ is defined as follows:

$$\underline{\Theta} := \left\{ \begin{array}{l} \theta \in [\theta] \mid t_1 \in [0, 2.8 \times 10^{-3}], \\ r_1 = 1, s_0 = 0, \{s_1, r_1\} \in \underline{S}_{s_1 r_1} \end{array} \right\} \quad (45)$$

For the implementation, we choose the following polynomials for the RST controller:

$$\begin{aligned} R(s) &= 0.5 \times 10^{-3} s + 1 \\ S(s) &= 5 \times 10^{-3} s \\ T(s) &= 1 \times 10^{-5} s + 1 \end{aligned} \quad (46)$$

In fact, there is no method for choosing the optimal controller that will ensure the best behaviours of the closed-

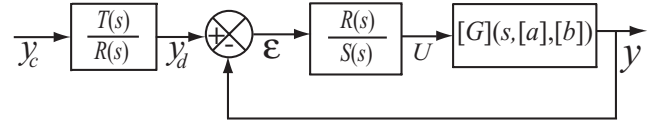


Fig. 6. Loop control with RST.

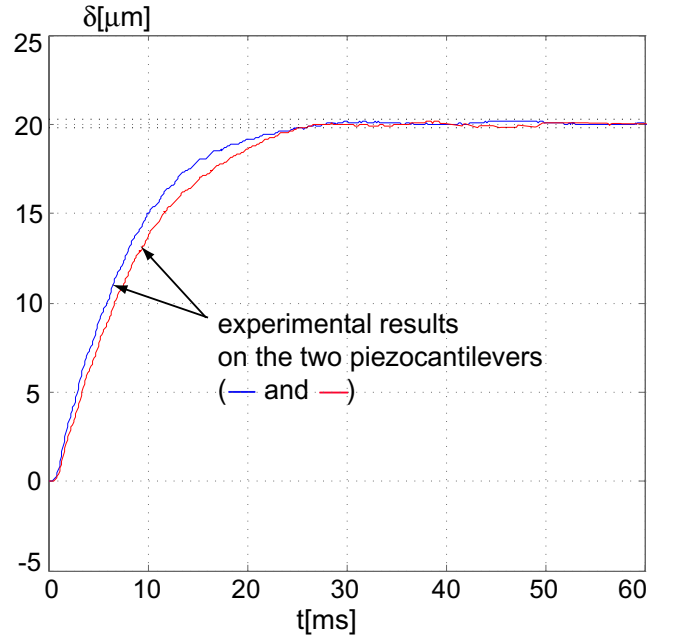


Fig. 7. Step responses envelope compared with the experimental results.

loop system among these solutions $\underline{S}_{s_1 r_1}$. However, it is guaranteed that any choice within them will ensure the specified performances.

V. CONTROLLER IMPLEMENTATION AND EXPERIMENTAL RESULTS

5.1 Controller implementation

This part consists of the application of the RST controller (46) for controlling the deflection of the piezocantilevers. For that, the closed-loop scheme in Fig. 1 is transformed into the scheme presented in Fig. 6 in order to have a causal controller:

5.2 Experimental result

Fig. 7 presents the experimental results when a step reference input $y_c = 20 \mu\text{m}$ is applied. As shown on Fig. 7, the computed controller has played its role. Indeed the experimental behavior of the closed-loop (tested on the two piezocantilevers) is without overshoot, with settling times

$tr_1 = 19.5 \text{ ms} \leq 30 \text{ ms}$, $tr_2 = 21.5 \text{ ms} \leq 30 \text{ ms}$ respectively for the piezocantilevers 1 and 2 and the static errors remain bounded by the specified interval.

VI. CLOSED-LOOP STABILITY ANALYSIS

In this section, we present a robust stability result of the closed-loop system with the designed RST controller (Fig. 6). The stability analysis is done analytically and graphically. As the transfer $\frac{T(s)}{R(s)}$ is stable, the robust stability analysis of the closed-loop $\frac{y(s)}{y_d(s)}$ can be reduced to the robust stability analysis of the transfer $\frac{y(s)}{y_d(s)}$ (Fig. 6).

The stability analysis of an interval system is based on the roots of the corresponding characteristic polynomial. This polynomial is the denominator of the interval closed-loop system. The interval closed-loop system is stable if and only if all the roots of the characteristic polynomial are in the left part \mathbb{C}^- of the complex plane.

The characteristic polynomial of the transfer from the input signal y_d to the output y is defined as follows:

$$[P](s) = [p_3]s^3 + [p_2]s^2 + [p_1]s + 1 \quad (47)$$

such that: $[p_3] = [a_2]s_1 + [b_2]r_1$, $[p_2] = [b_2] + [a_1]s_1 + r_1[b_1]$, $[p_1] = [b_1] + r_1 + [a_0]s_1$, where $r_1 = 0.5 \times 10^{-3}$ and $s_1 = 5 \times 10^{-3}$ are the parameters of the implemented polynomials $R(s)$ and $S(s)$ (46).

According to the Routh's criterion, all the roots of the interval polynomial $[P](s)$ are in the left part \mathbb{C}^- if and only if the following conditions are satisfied:

$$\begin{aligned} [p_3] &> 0 \\ [p_2] &> 0 \\ [p_1] &> 0 \\ [p_2][p_1] - [p_3] &> 0 \end{aligned} \quad (48)$$

After computation, we obtain:

$$\begin{aligned} [p_3] &= [4.696, 5.355] \times 10^{-10} > 0 \\ [p_2] &= [1.597, 1.7418] \times 10^{-7} > 0 \\ [p_1] &= [7.054, 7.962] \times 10^{-3} > 0 \\ [p_2][p_1] - [p_3] &= [5.951, 8.981] \times 10^{-10} > 0 \end{aligned} \quad (49)$$

As all the terms in (49) are strictly positive, the implemented controller ensures the robust stability for the interval system $[G](s, [a], [b])$.

Now let us analyze the δ -stability of the closed-loop. The δ -stability is an interesting way of evaluating the stability margin of a system, in that, instead of using the Laplace variable s , the variable $s - \delta$ (with $\delta > 0$) is used. So, the

interval polynomial $[P](s)$ is δ -stable if and only if all its roots are in the part Γ_δ of the complex plane and are located on the left of the vertical line $Re(s) = -\delta$. In this analysis, we compute the maximal δ for which the implemented RST controller still ensures the δ -stability for the interval system $[G](s, [a], [b])$. We can rewrite $[P](s - \delta)$ as follows:

$$[P](s - \delta) = \alpha_3 s^3 + \alpha_2 s^2 + \alpha_1 s + \alpha_0 \quad (50)$$

where:

$$\alpha_3 = [p_3], \quad \alpha_2 = [p_2] - 3\delta[p_3], \quad \alpha_1 = [p_1] - 2\delta[p_2] - 3\delta^2[p_3] \text{ and } \alpha_0 = 1 - \delta[p_1] + \delta^2[p_2] + 3\delta^3[p_3].$$

The polynomial $[P](s - \delta)$ is stable if and only if:

$$\begin{aligned} [\alpha_3] &> 0 \\ [\alpha_2] &> 0 \\ [\alpha_1] &> 0 \\ [\alpha_2][\alpha_1] - [\alpha_3][\alpha_0] &> 0 \end{aligned} \quad (51)$$

The resolution of this nonlinear inequalities problem leads to the admissible values of δ that satisfy the inequalities (51). After computation, we obtain the interval parameter δ :

$$\delta = [0, 30.493] \quad (52)$$

To resume, we can conclude that the implemented RST controller ensures the δ -stability for the interval system for δ less than 30.493.

Finally, we analyze the Black-Nichols diagram of the open-loop system $[L](s)$ in order to assess the stability margins (phase and gain). The open-loop $[L](s)$ is defined by:

$$[L](s) = \frac{R(s)}{S(s)} [G](s, [a], [b]) \quad (53)$$

Fig. 8 presents the Black-Nichols diagram of the open-loop system $[L](s)$ and that of the controlled system $[G](s, [a], [b])$. The Black-Nichols diagram of the interval system $[L](s)$ (resp. $[G](s, [a], [b])$) encloses the Black-Nichols diagram of all the transfer functions contained in $[L](s)$ (resp. in $[G](s, [a], [b])$). From the figure, we can see first that the performances of the closed-loop system are improved relative to those of the system it-self. Indeed, the gain of $[L]$ tends towards ∞ when $\omega \rightarrow 0$ while that of $[G]$ is finite. This means that the static gain of the closed-loop tends towards zero, which is not the case for the non-controlled system $[G]$. This figure indicates also that the phase and the gain margins were improved when implementing the RST controller. They can be computed from the Black-Nichols diagram. For the controlled system, these margins are $M\phi \approx 95$ (at a pulsation about 150 Hz) and $MG = \infty$, respectively.

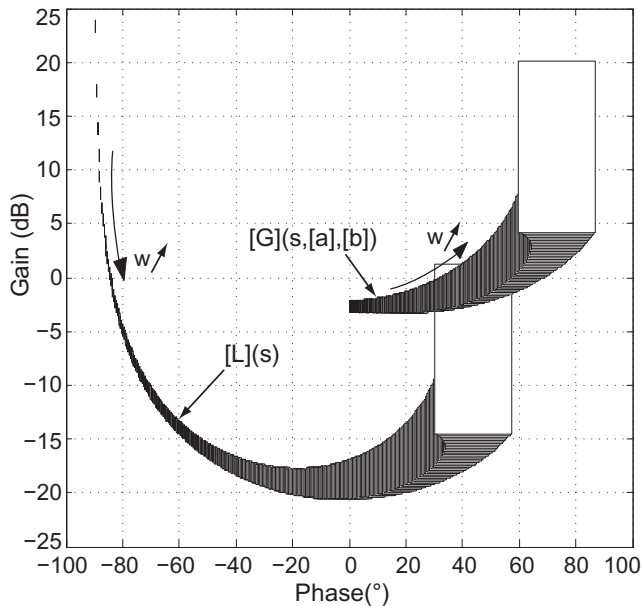


Fig. 8. Black-Nichols diagrams of the open-loop system $[L](s)$ and the interval system $[G](s, [a], [b])$.

VII. CONCLUSION

In this paper, a method to design robust controllers for systems with uncertain parameters has been proposed. While the uncertain parameters are described by intervals, the controller structure is given *a priori* (a fixed-order RST controller). The main advantages of the proposed approach are the natural way of modelling the uncertainties and the derivation of a low order controller. Starting from specified performances, the calculation of the controller parameters is formulated as a set-inversion problem that can be solved using an existing algorithm. Experimental tests of the proposed method were carried out on piezoelectric actuators. The experimental results showed its efficiency. Finally, a stability analysis of the closed-loop system was carried out and confirmed the robustness of the computed controller.

REFERENCES

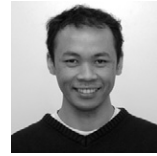
1. Barmish, B. R. *New Tools for Robustness of Linear Systems*. Macmillan, New York (1994).
2. Dasgupta, S., B. D. O. Anderson, G. Chockalingam, and M. Fu, Lyapunov functions for uncertain systems with applications to the stability of time varying systems. *IEEE Trans. Circuits Syst.*, Vol. 41, pp. 93–106 (1994).
3. Jaulin, L., M. Kieffer, O. Didrit, and E. Walter, *Applied Interval Analysis*. Springer-Verlag, London (2001).
4. Bondia, J., M. Kieffer, E. Walter, J. Monreal, and J. Picó, Guaranteed tuning of PID controllers for parametric uncertain systems. *IEEE CDC*, pp. 2948–2953 (2004).
5. Dullerud, G. E. and F. G. Paganini, *A course in robust control theory: a convex approach*. 1st edition, Springer-Verlag, New York, NY (2000).
6. Reza Moheimani, S. O. *Perspectives in Robust Control*. 1st edition, Springer-Verlag, London (2001).
7. Ur Rehman, O., B. Fidan, and I. Petersen, Uncertainty modeling and robust minimax LQR control of multivariable nonlinear systems with application to hypersonic flight. *Asian J. Control*, DOI: 10.1002/asjc.399 (2012).
8. Sadeghzadeh, A. Identification and robust control for systems with ellipsoidal parametric uncertainty by convex optimization. *Asian J. Control*, DOI: 10.1002/asjc.437 (2012).
9. Chen, W. and Z. Zhang, Nonlinear adaptive learning control for unknown time-varying parameters and unknown time-varying delays. *Asian J. Control*, Vol. 13, No. 6, 903–913 (2011).
10. Liu, Y. J., S. C. Tong, and T. S. Li, Adaptive fuzzy controller design with observer for a class of uncertain nonlinear MIMO systems. *Asian J. Control*, Vol. 13, No. 6, 868–877 (2011).
11. Banjerdpongchai, D. and J. P. How, “LMI synthesis of parametric robust H_∞ controllers,” in *Proceeding of the 1977 American Control Conference, Albuquerque, New Mexico*, pp. 493–498 (1997).
12. Balas, G. J., J. C. Doyle, K. Glover, A. Packard, and R. Smith, *μ -Analysis and Synthesis Toolbox*. The Mathworks, Natick, MA (1993).
13. Moore, R. E. *Interval analysis*. Prentice-Hall, Englewood Cliffs N-J (1966).
14. Kharitonov, V. L. Asymptotic stability of an equilibrium position of a family of systems of linear differential equations. *Differentsial'nye Uravneniya*, Vol. 14, 2086–2088 (1978).
15. Walter, E. and L. Jaulin, Guaranteed characterization of stability domains via set inversion. *IEEE Trans. Autom. Control*, Vol. 39, No. 4, 886–889 (1994).
16. Wang, C. New delay-dependent stability criteria for descriptor systems with interval time delay. *Asian J. Control*, Vol. 14, No. 1, 197–206 (2012).
17. Smagina, Y. and I. Brewerb, Using interval arithmetic for robust state feedback design. *Syst. Control Lett.*, 187–194 (2002).
18. Chen, C. T. and M. D. Wang, Robust controller design for interval process systems. *Computs & Chemical Engineering*, Vol. 21, 739–750 (1997).
19. Rakotondrabe, M. Performances inclusion for stable interval systems. *IEEE—ACC (American Control Conference)*, pp. 4367–4372, San Francisco CA USA, June–July 2011 (2011).

20. Li, K. and Y. Zhang, Interval Model Control of Consumable Double-Electrode Gas Metal Arc Welding Process. *IEEE Trans. Autom. Sci. Engineering (T-ASE)*, pp. 1–14 (2009).
21. Chen, C. T. and M. D. Wang, A two-degrees-of-freedom design methodology for interval process systems. *Computs and Chemical Engineering*, Vol. 23, pp. 1745–1751 (2000).
22. Bondia, J. and J. Picó, A geometric approach to robust performance of parametric uncertain systems. *Int. J. Robust Nonlinear Control*, Vol. 13, pp. 1271–1283 (2003).
23. Khadraoui, S., M. Rakotondrabe, and P. Lutz, Robust control for a class of interval model: application to the force control of piezoelectric cantilevers. *IEEE—CDC*, pp. 4257–4262, Atlanta Georgia USA (2010).
24. Jaulin, L. and E. Walter, Set inversion via interval analysis for nonlinear bounded-error estimation. *Automatica*, Vol. 29, No. 4, pp. 1053–1064 (1993).
25. Bargiel, S., K. Rabenoroso, C. Cleve, C. Gorecki, and P. Lutz, Towards Micro-Assembly of Hybrid MOEMS Components on Reconfigurable Silicon Free-Space Micro-Optical Bench. *J. Micromech. Microeng.*, Vol. 20, No. 4, (2010).
26. Haddab, Y., N. Chaillet, and A. Bourjault, A microgripper using smart piezoelectric actuators. *IEEE/RSJ Int. Conference on Intelligent Robot and Syst. (IROS)*, Takamatsu—Japan, 1, pp. 659–664 (2000).
27. Agnus, J., J. M. Breguet, N. Chaillet, O. Cois, P. De Lit, A. Ferreira, P. Melchior, C. Pellet, and J. Sabatier, A smart microrobot on chip: design, identification and modeling. *IEEE/ASME AIM*, Kobe Japan, pp. 685–690 (2003).
28. Rakotondrabe, M., Y. Haddab, and P. Lutz, Quadrilateral modelling and robust control of a nonlinear piezoelectric cantilever. *IEEE Trans. Control Syst. Technol.*, Vol. 17, No. 3, pp. 528–539, May (2009).
29. Huang, Yi-Chen and De-Yao Lin, Ultra-fine tracking control on piezoelectric actuated motion stage using piezoelectric hysteretic model. *Asian J. Control*, Vol. 6, No. 2, pp. 208–216 (2004).
30. Shen, J.-C., W.-Y. Jywe, C.-H. Liu, Y.-T. Jian, and J. Yang, Sliding-mode control of a three-degrees-of-freedom nanopositioner. *Asian J. Control*, Vol. 10, No. 3, pp. 267–276 (2008).



Sofiane Khadraoui obtained Engineering Diploma and Magister in Automatic Control from Abou Bekr Belkaid University at Tlemcen (Algeria) in 2004 and 2007, respectively, and Ph.D. in Control Systems from University of Franche-Comté at Besançon (France) in January 2012. His Ph.D. works concerned the guaranteed design and the robust control of piezo-

electric microsystems and microactuators by combining interval techniques with standard modeling and classical control design.



Micky Rakotondrabe graduated from Institut Catholique des Arts et Métiers (ICAM Engineering School, Lille, France) in 2002, obtained M.Sc. in Control Systems from Institut National des Sciences Appliquées (INSA, Lyon, France) in 2003, and Ph.D. in Control Systems from University of Franche-Comté at Besançon (UFC, Besançon, France) in 2006. His Ph.D. research was led at FEMTO-ST Institute, Besançon France, and concerns the design, development and control of a microassembly cell. He was Assistant Professor at UFC University and FEMTO-ST Institute in 2006–2007. Since September 2007, he has been Associate Professor at the same University and Institute. His research fields concern the design, modeling, signal estimation and control for piezoelectric actuators. He also works on interval techniques combined with systems design and combined with control theory, and on hysteresis modeling and control; all with applications to systems working at the microscale.

Micky Rakotondrabe was UFC-best Ph.D. thesis finalist, and obtained ICARCV-2006 best paper award finalist and the CASE-2011 best application paper award finalist. In July 2011, he obtained CNRS-delegation award for one year (2011–2012). Micky Rakotondrabe is co-inventor of three patents, and co-editor of the book “Signal measurement and estimation techniques issues in the micro/nano world” (Springer-Verlag, ISBN 978-1-4419-9945-0, August 2011). He has organized several workshops on the control and on signal estimation all for systems working at the microscale, at IEEE-ICRA-2009 (Kobé, Japan), IEEE-ICRA-2010 (Anchorage Alaska USA) and IEEE-CASE-2011 (Trieste Italy).



Philippe Lutz joined University of Franche-Comté in Besançon as Professor in 2002. He is currently the head of the research group ‘Automated Systems for Micromanipulation and Micro’assembly’ of the AS2M department of FEMTO-ST.

His research activities are focussed on the design and the control of MicroMechatronic Systems. He teaches the design of Mechatronic Systems and Production Systems at the master level.

An engineer of ENSMM in 1990 and Doctor of University of Franche-Comté in Automation and Computer Science in 1994, he was Associate Professor in INSA of Strasbourg since 1994 until 2002. During this period, he led the Mechatronics activities and developed research on inventive theory for solving problems.