

SOEN331: Introduction to Formal Methods for Software Engineering

Assignment 4 on algebraic specifications

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Spec: Location;

Sort: Location;

Imports:String, Point

Description: A location contains a point and a description.

- newlocation (String, Point): Creates a new location with the given description and point.
- setdescription (String): Modifies the description of a location, and returns the updated location.
- getdescription: Returns the description of the location.
- setpoint (Point): Modifies the point of the location, and returns the updated location.
- getpoint: Returns the point of the location.

Operations:

newlocation: $\text{String} \times \text{Point} \rightarrow \text{Location}$;

setdescription: $\text{String} \times \text{Location} \rightarrow \text{Location}$;

$\text{getdescription} : \text{Location} \rightarrow \text{String};$
 $\text{setpoint} : \text{Point} \times \text{Location} \rightarrow \text{Location};$
 $\text{getpoint} : \text{Location} \rightarrow \text{Point};$

Variables:

$\text{newDesc}, d: \text{String}; \text{newPoint}, p: \text{Point};$

Axioms:

[A1] $\text{getdescription}(\text{newlocation}(d, p)) = d;$
[A2] $\text{getpoint}(\text{newlocation}(d, p)) = p;$
[A3] $\text{setdescription}(\text{newDesc}, \text{newlocation}(d, p)) = \text{newlocation}(\text{newDesc}, p);$
[A4] $\text{setpoint}(\text{newPoint}, \text{newlocation}(d, p)) = \text{newlocation}(d, \text{newPoint});$

Spec: Map (Location);

Sort: Map;

Imports: Boolean, Location, \mathbb{N} , Point, String;

Description: A Map ADT contains a collection of locations.

- **newmap:** Creates a new empty map.
- **addlocation (Location):** Adds a new location on the map. A location whose description already exists in the map will override the corresponding location with a new point. Returns updated Map.
- **deletelocation (String):** Deletes the location from the map that corresponds to a given description. Returns updated map
- **containsdescription (String):** Determines whether the map contains the given description. Returns true if a description is found, and it returns false otherwise.
- **containspoint (Point):** Determines whether the map contains the given point. Returns true if a description is found, and it returns false otherwise.
- **findlocation (String):** Returns the point for the location on the map that corresponds to the given description.
- **isempty:** Determines whether the map is empty of annotations. Returns true if the map contains no annotations and it returns false otherwise.
- **clear:** Erases all locations from a map.
- **size:** Returns the number of annotations in the map.

Operations:

newmap: \rightarrow Map;

addlocation: $\text{Map} \times \text{Location} \rightarrow \text{Map}$;

deletelocation : $\text{Map} \times \text{String} \rightarrow \text{Map}$;

containsdescription : $\text{Map} \times \text{String} \rightarrow \text{Boolean}$;

containspoint : $\text{Map} \times \text{Point} \rightarrow \text{Boolean}$;

findlocation : Map \times String \rightarrow Point;

isempty : Map \rightarrow Boolean;

clear : Map \rightarrow Map;

size : Map \rightarrow \mathbb{N}

Variables:

d: String; p, q: Point; loc: Location; map: Map

Axioms:

[A1] isempty(newmap) = true;

[A2] isempty(clear(map)) = true;

[A3] containsdescription(addlocation(map, new), getdescription(loc)) = true;

[A4] containsdescription(map, d) \rightarrow findlocation(addlocation(map, newlocation(d, q)), d)
= q

[A5] size (addLocation(map, newlocation(d, q))) =

if (containsdescription(map, d))

then size(map)

else size(map) + 1

[A6] isempty(deleteLocation(addlocation(newmap, newlocation(d, p)), d)) = true

[A7] findlocation(addlocation(map, newlocation(d, p)), d) = p

[A8] findlocation(newmap, d) = undefined;

[A9] deletelocation(newmap, d) = undefined;

preconditions:

pre : deletelocation(map: Map, d: String) = containsdescription (map, d);

pre : findlocation(map: Map, d: String) = containsdescription (map, d);