

# SOEN331: Introduction to Formal Methods for Software Engineering

## Assignment 4 on algebraic specifications

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**Spec:** Location;

**Sort:** Location;

**Imports:**String, Point

**Description:** A location contains a description

**Operations:**

newLocation:  $\text{String} \times \text{Point} \rightarrow \text{Location}$ ;

setDescription:  $\text{String} \times \text{Location} \rightarrow \text{Location}$ ;

getDescription :  $\text{Location} \rightarrow \text{String}$ ;

setPoint :  $\text{Point} \times \text{Location} \rightarrow \text{Location}$ ;

getPoint :  $\text{Location} \rightarrow \text{Point}$ ;

**Variables:**

newDesc, d: String; newPoint, p: Point;

**Axioms:**

[A1] getDescription(newLocation(d, p)) = d;

[A2] getPoint(newLocation(d, p)) = p;

[A3] setDescription(newDesc, newLocation(d,p)) = newLocation(newDesc, p);

[A4] setPoint(newPoint, newLocation(d,p)) = newLocation(d, newPoint);

**Spec:** Map (Location);

**Sort:** Map;

**Imports:** String, Point, Boolean, Location;

**Description:** A map contains locations

**Operations:**

newmap:  $\rightarrow$  Map;  
addlocation: Map  $\times$  Location  $\rightarrow$  Map;  
deletelocation : Map  $\times$  String  $\rightarrow$  Map;  
containsdescription : Map  $\times$  String  $\rightarrow$  Boolean;  
containspoint : Map  $\times$  Point  $\rightarrow$  Boolean;  
findlocation : Map  $\times$  String  $\rightarrow$  Point;  
isempty : Map  $\rightarrow$  Boolean;  
clear : Map  $\rightarrow$  Map;  
size : Map  $\rightarrow$  N

**Variables:**

d: String; p, q: Point; loc: Location; map: Map

**Axioms:**

[A1] isempty(newmap) = true;  
[A2] isempty(clear(map)) = true;  
[A3] containsdescription(addlocation(map, loc), getDescription(loc)) = true;  
[A4] containsdescription(map,d)  $\rightarrow$  findlocation(addlocation(map, newlocation(d,q)), d)  
== q  
[A5] deletelocation(addlocation(addlocation(newmap, newLocation(d, p)),newLocation(d,q)),d)  
= newmap  
[A5] size (addlocation(addLocation(map, newLocation(d,q)), newLocation(d,p))) = size(map)  
[A6] isempty(deleteLocation(addlocation(newmap, newlocation(d,p)), d)) = true  
[A7] findlocation(addlocation(newmap, newlocation(d,p)), d) = p  
[A8] findlocation(newmap) = undefined;  
[A9] deletelocation(newmap) = undefined;

**preconditions:**

pre : deletelocation(map, d) = not isempty(map);

pre : findlocation(map, d) = not isempty(map);

**end:**