

$$\int R(\sin x, \cos x) \quad \text{ve} \quad \int R(\sin^2 x, \cos^2 x)$$

$$\tan \frac{x}{2} = t$$

$$dx = \frac{2}{1+t^2} dt$$

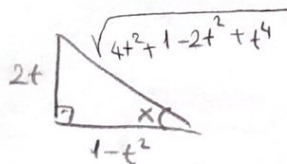
$$\sin x = \frac{2t}{1+t^2}$$

$$\cos x = \frac{1-t^2}{1+t^2}$$



$$\tan x = \frac{2 \tan \frac{x}{2}}{1 - \tan^2 \frac{x}{2}}$$

$$\tan x = \frac{2t}{1-t^2}$$

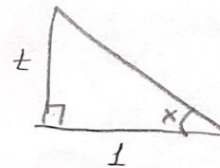


$$\tan x = t$$

$$dx = \frac{dt}{1+t^2}$$

$$\sin^2 x = \frac{t^2}{1+t^2}$$

$$\cos^2 x = \frac{1}{1+t^2}$$



Örnek




$$1) \int \frac{dx}{\sin^2 x \cos^4 x}$$

$$2) \int \frac{dx}{\cos x}$$

$$3) \int \frac{dx}{1 + \sin x - \cos x}$$

4) $\int \frac{1+\sin x}{1+\cos x} dx$

5) $\int \frac{dx}{\sin^3 x}$

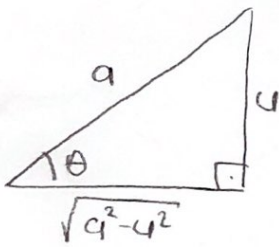
	$\sqrt{a^2 - u^2}$	$\sqrt{u^2 - a^2}$
$u = a \sin \theta$	$u = a \cos \theta$	$u = a \sec \theta$
		
$\sin \theta = \frac{u}{a}$	$\cos \theta = \frac{u}{a}$	$\sec \theta = \frac{u}{a}$
... kullan	... kullan	... kullan

Trigonometrik Dönüşümler

Radikal ifadeler içeren integralleri çözmek için trigonometrik dönüşümlerden yararlanınız.

$$\sqrt{a^2 - u^2}$$

$$u = a \sin \theta \text{ de.}$$

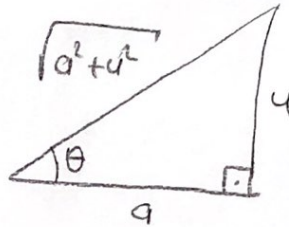


$$1 - \sin^2 \theta = \cos^2 \theta$$

özdeşliğini kullan.

$$\sqrt{a^2 + u^2}$$

$$u = a \tan \theta \text{ de.}$$

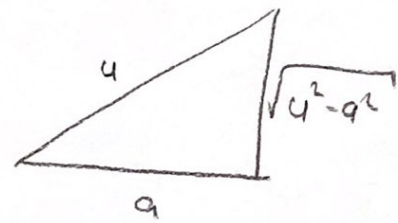


$$1 + \tan^2 \theta = \sec^2 \theta$$

özdeşliğini kullan.

$$\sqrt{u^2 - a^2}$$

$$u = a \sec \theta \text{ de.}$$



$$\sec^2 \theta - 1 = \tan^2 \theta$$

özdeşliğini kullan.

Örnekler

$$1) \int \frac{dx}{x^2 \sqrt{9-x^2}}$$

$$(2) \int \frac{\sqrt{9-x^2}}{x^2} dx$$

③

$$\int \frac{dx}{\sqrt{4x^2+1}}$$

$$(4) \int \frac{1}{x^2 \sqrt{x^2 + 4}} dx$$

$$(5) \int \frac{x}{\sqrt{x^2+4}} dx$$

$$(6) \int \frac{\sqrt{x^2-3}}{x} dx$$

⑦

$$\int \frac{dx}{\sqrt{x^2 - a^2}}$$

⑧

$$\int \frac{x^3}{(4x^2+9)^{3/2}} dx$$

9

$$\int \frac{x}{\sqrt{3-2x-x^2}} dx$$