

Decision Tree

- D.T Intuition
- Working D.T
- Entropy / Info. gain
- Code

→ Data Scientist Aintel

↳ Employee attrition

1. Find the chances of attrition of a Employee
 2. What are the Key factor responsible for Attrition
- ↪ Feature Importance

Age Overtime ✓

Age Overtime ✓
27 2

Overtime

Hours

3.5
3
2.5
2
1.5
1
0.5

18

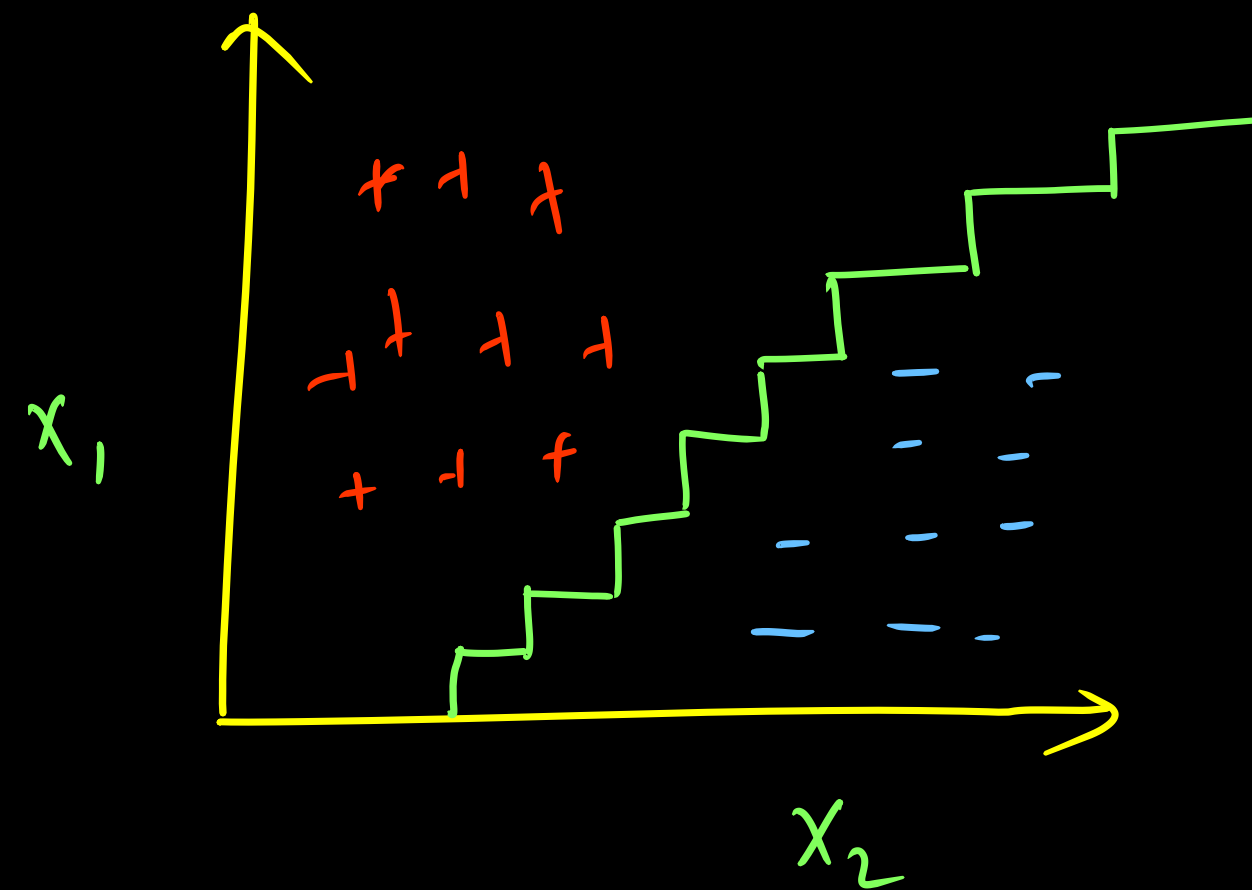
29 30 35 36

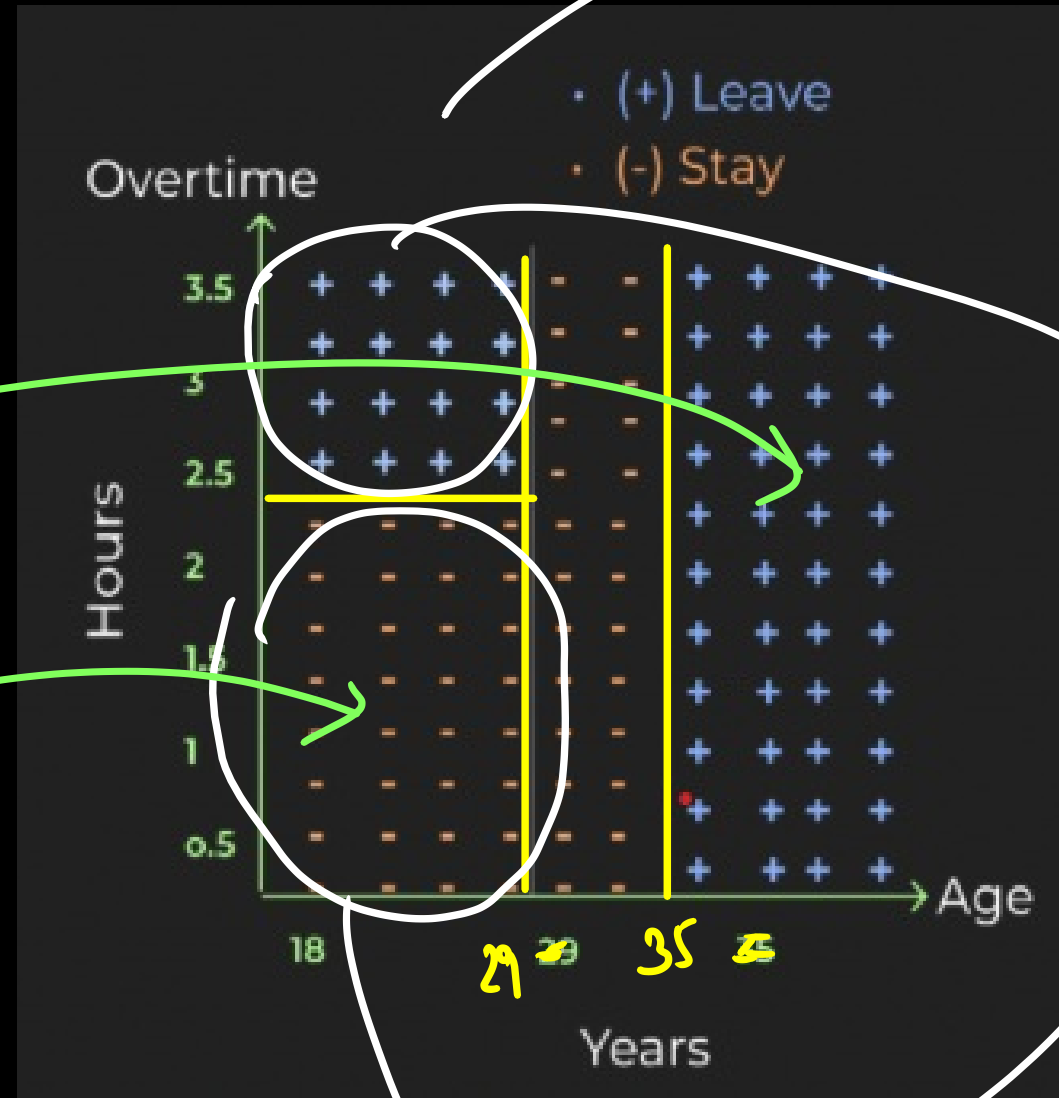
Years

- (+) Leave ✓
- (-) Stay ✓

→ Axis parallel
hyperplane

→ Non-linear
model





Training

If (Age < 29):

If (Overtime < 2.5):

Stay

else:

Leave

else

If (Age < 35):

else: Stay

Leave

If (Age < 29):

If (Overtime < 2.5):

Stay

else:

Leave

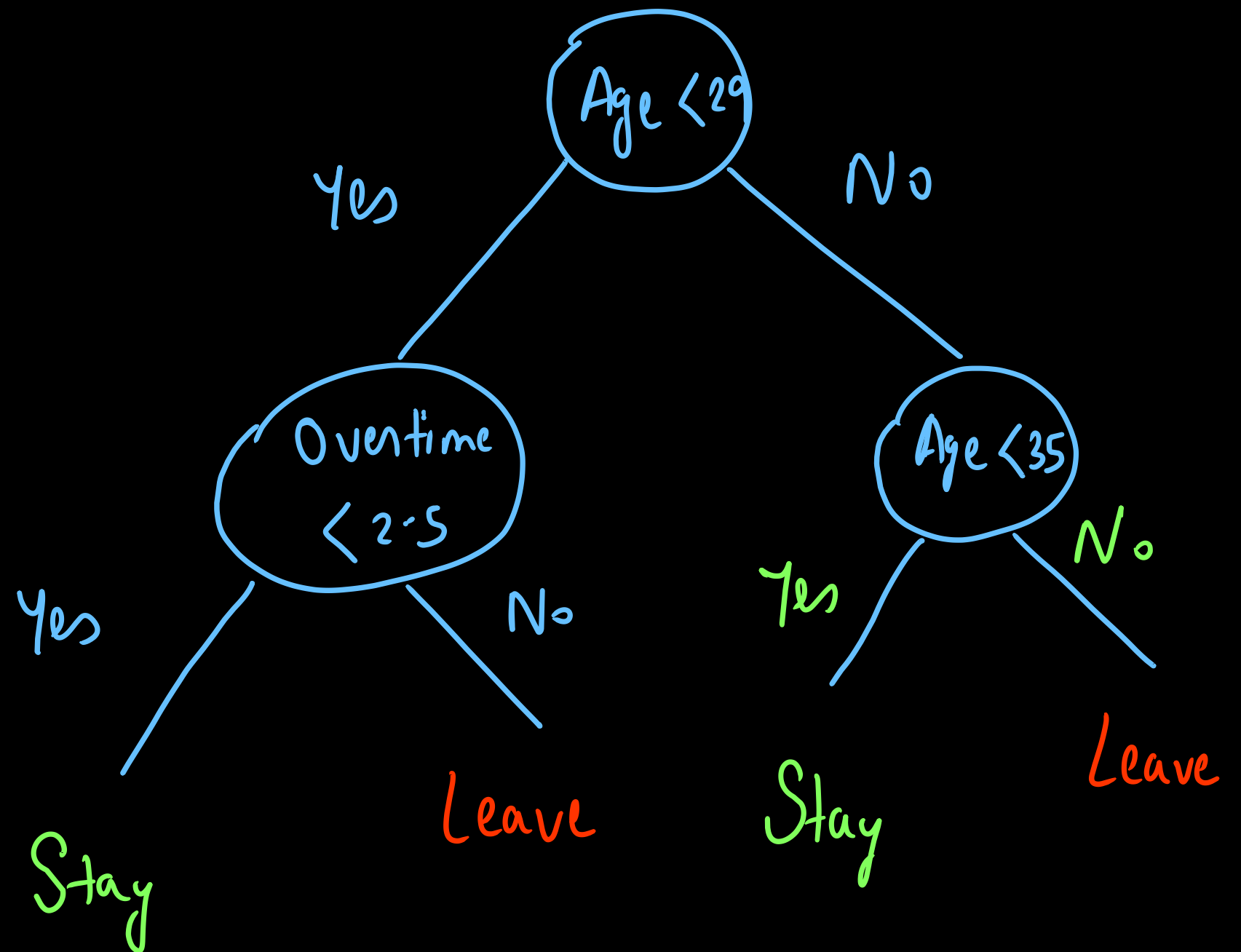
else

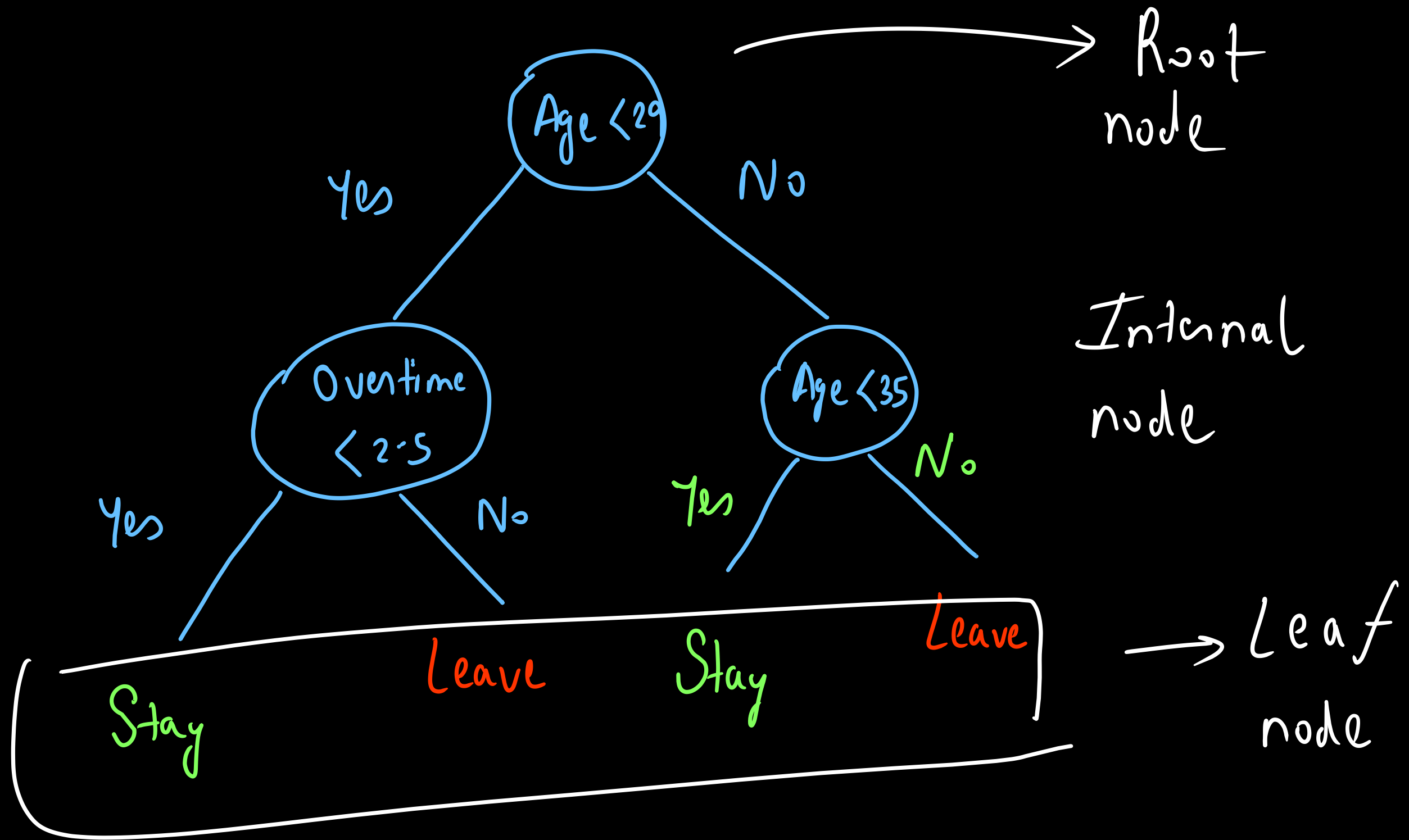
If (Age < 35):

Stay

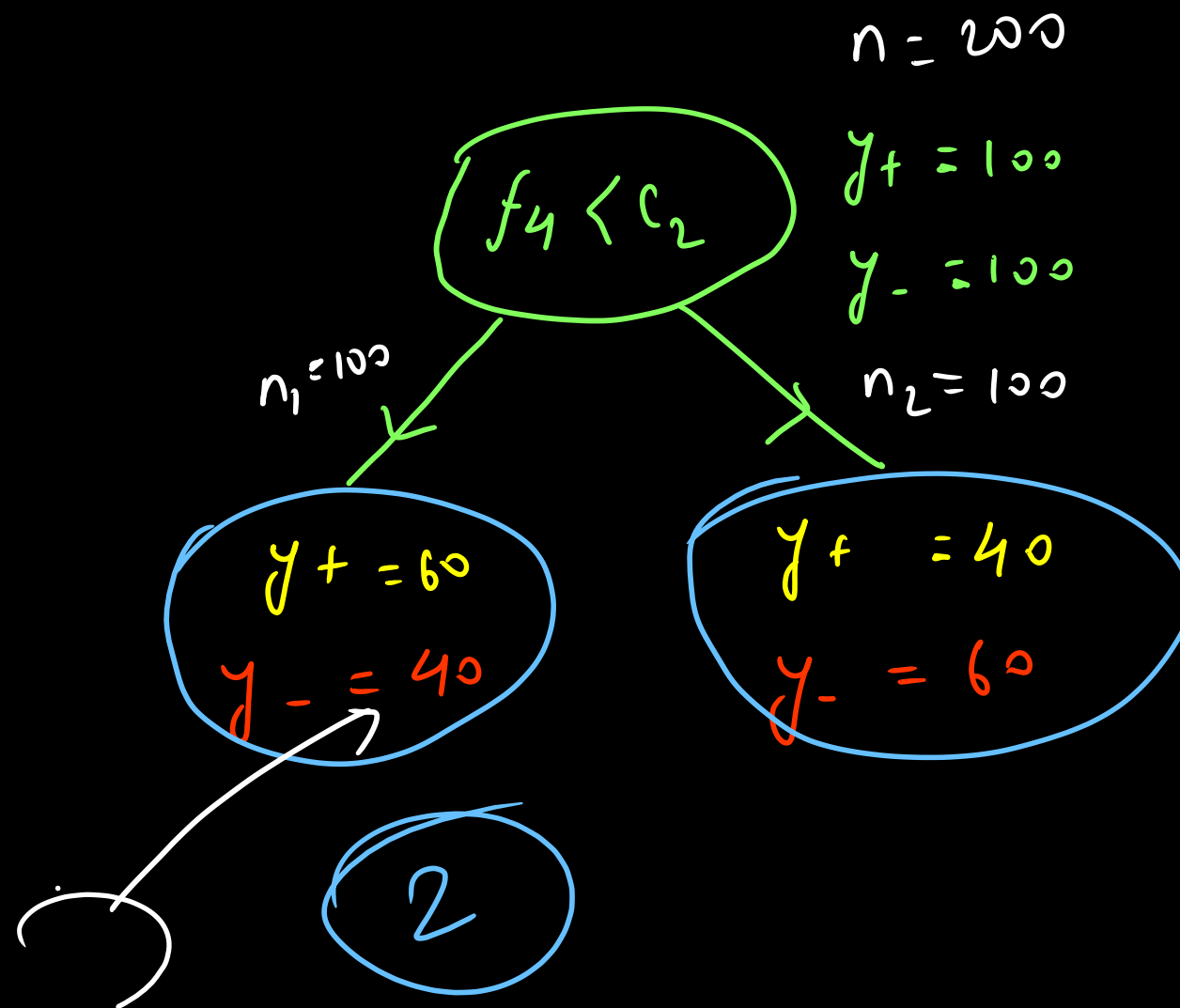
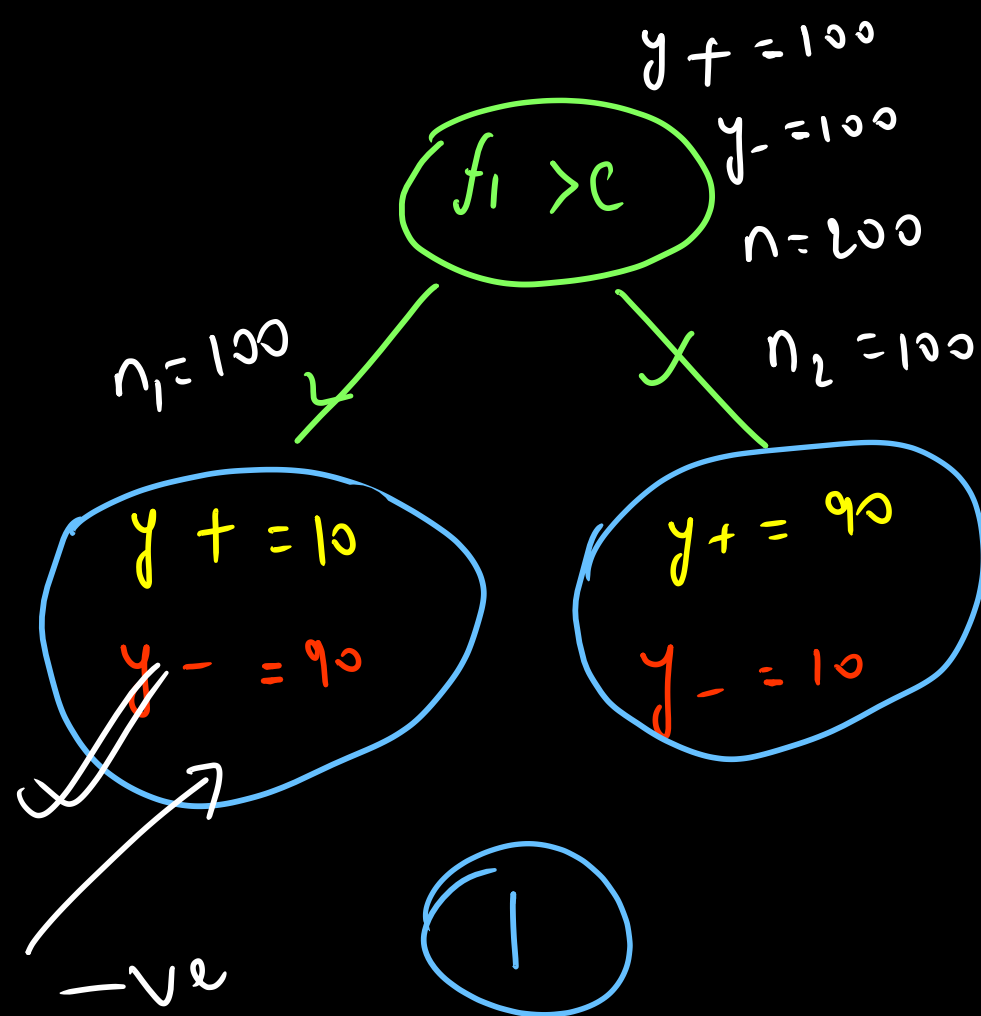
else:

Leave





→ Which options to choose



→ More homogeneous = More confidence in prediction

→ Entropy

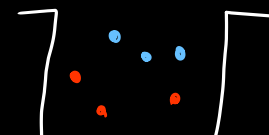
↳ Measures Randomness

↳ Impurity (Heterogeneity)

$$H(y) = - \sum_{i=1}^K p_i \log p_i$$

$$H(y) = - \sum_{i=1}^K p_i \log_2 p_i$$

$\xrightarrow{\text{No of classes}} K$
 $\xrightarrow{\text{Ranges } (0-1)}$
 $\xrightarrow{\text{Probab. of each class}} p_i$



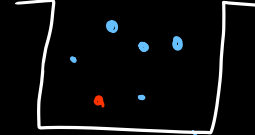
$$H(y) = - [p_{\text{blue}} \log_2 p_{\text{blue}} + p_{\text{red}} \log_2 p_{\text{red}}]$$

$$p(\text{blue}) = 3/6 = 1/2$$

$$p(\text{red}) = 3/6 = 1/2$$

$$= - \left[\frac{1}{2} \log_2 \left(\frac{1}{2} \right) + \frac{1}{2} \log_2 \left(\frac{1}{2} \right) \right]$$

$$= 1$$

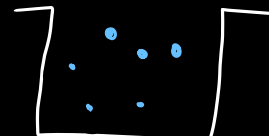


$$p_{\text{blue}} = 5/6$$

$$p_{\text{red}} = 1/6$$

$$H(y) = - [p_b \log_2 p_b + p_r \log_2 p_r]$$

$$= - \left[\frac{5}{6} \log_2 \left(\frac{5}{6} \right) + \frac{1}{6} \log_2 \left(\frac{1}{6} \right) \right]$$

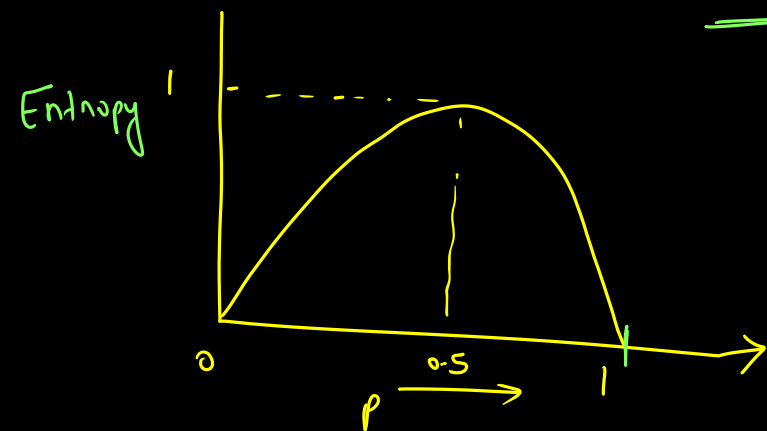


$$p_b = 1$$

$$p_r = 0$$

$$H(y) = - \left[1 \log_2 (1) + 0 \log_2 (0) \right]$$

$$= 0$$



→ Break until 22:19

.

Information Gain

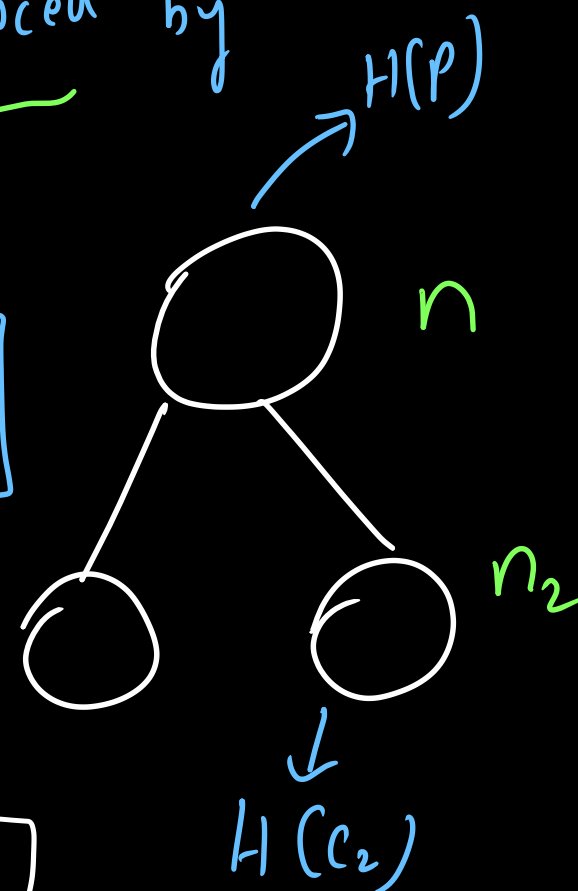
(Age, Gender)

→ Used to decide which feature to split on

→ Measure how much entropy is reduced by making a split

$$IG = H(P) - \left[\frac{n_1}{n} H(C_1) + \frac{n_2}{n} H(C_2) \right]$$

n_1
 $H(C_1)$



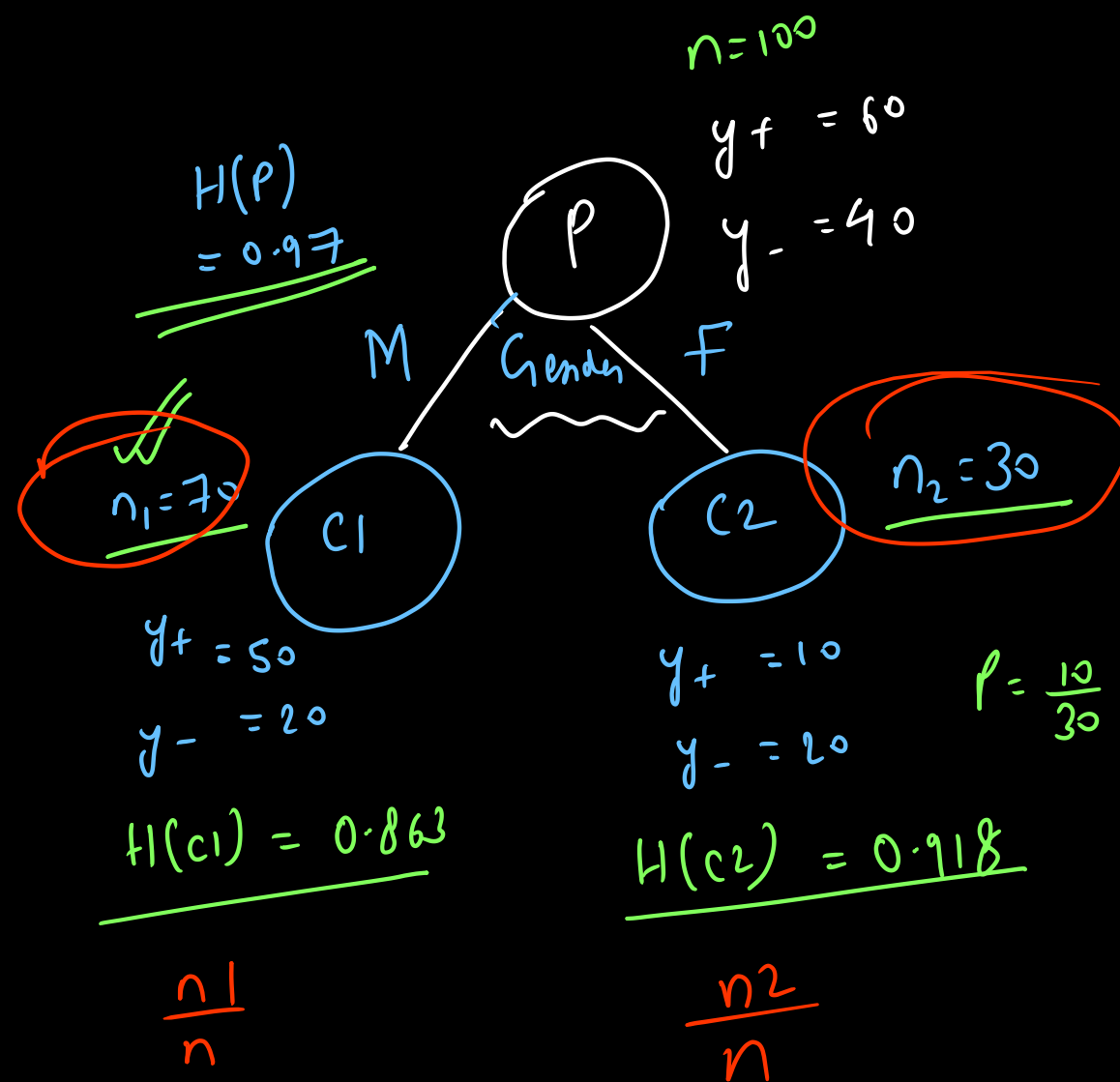
→ High $IG \rightarrow$ high reduction in entropy
(Heterogeneous)

More
homogeneous

✓ $n = 100$

$y_+ = 60$
 $y_- = 40$

Age	Gender	y
20	M	y_+
30	F	y_+
5	F	y_-

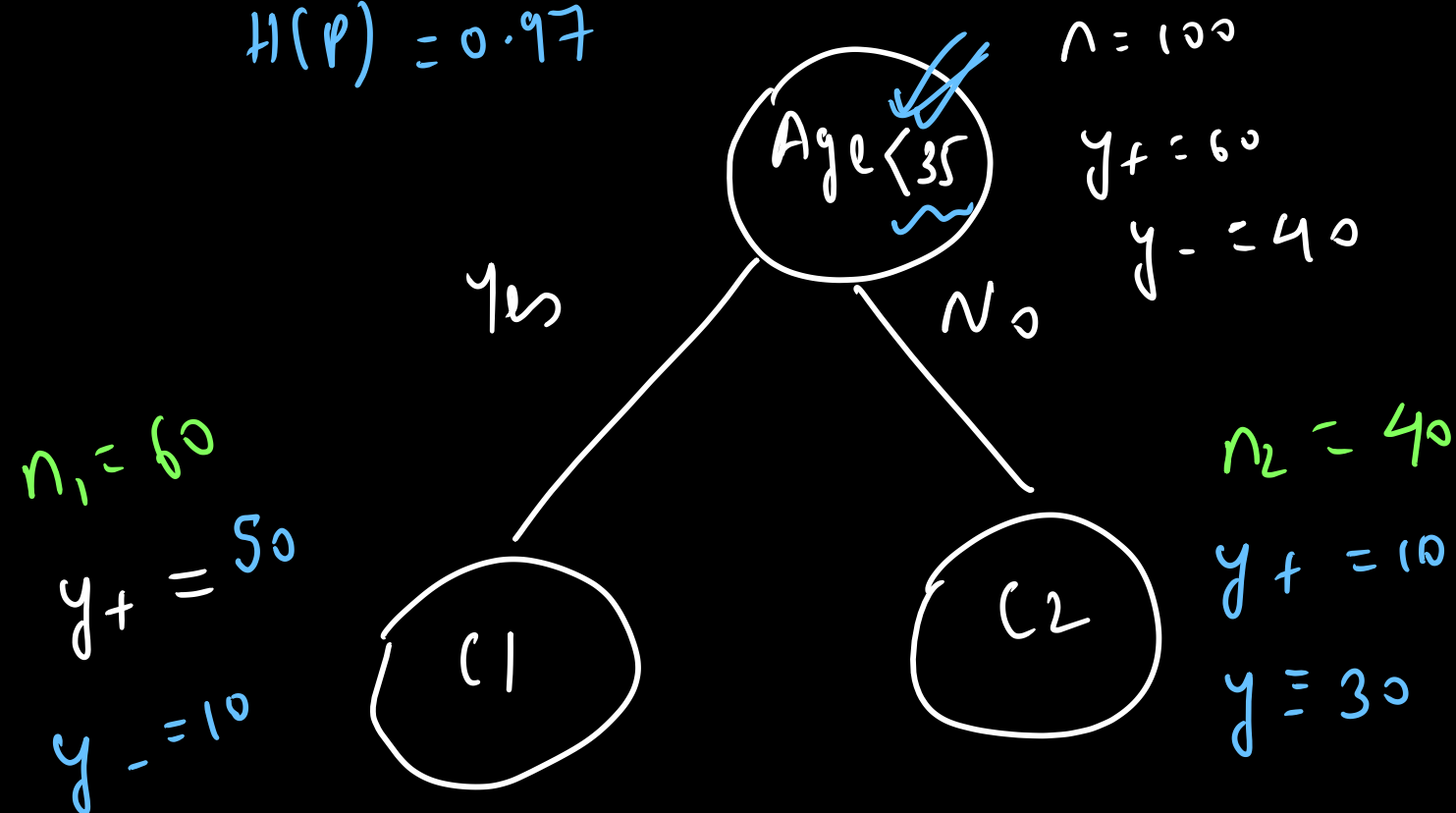


$I_C^{(Gender)} = H(P) - \left[\frac{n_1}{n} H(C_1) + \frac{n_2}{n} H(C_2) \right]$

$= 0.97 - [0.7 \times 0.863 + 0.3 \times 0.918]$

$= 0.0914$

$$H(P) = 0.97$$



$$H(C2) = 0.8112$$

$$H(C1) = 0.65$$

$$\begin{aligned}
 \checkmark \quad I_G(\text{Age} < 35) &= H(P) - \left[\frac{n_1}{n} H(C1) + \frac{n_2}{n} H(C2) \right] \\
 &= 0.97 - \left[\frac{60}{100} \times 0.65 + \frac{40}{100} \times 0.8112 \right] \\
 &= \underline{\underline{0.2565}}
 \end{aligned}$$

Age	Gender	y
10	M	y_+
20	F	y_-
15		
7		
35		
40		

7 → Age ≤ 7
 10 Age ≤ 10
 15 |
 20 |
 35 Age ≤ 35
 40

0 - 10

10 - 20

20 - 30

30 - 40

