

Ques 1 Assume weight vector of initial decision boundary w^T as $w^T = [1, 1]$

$$\Rightarrow x_1 + x_2 = 0$$

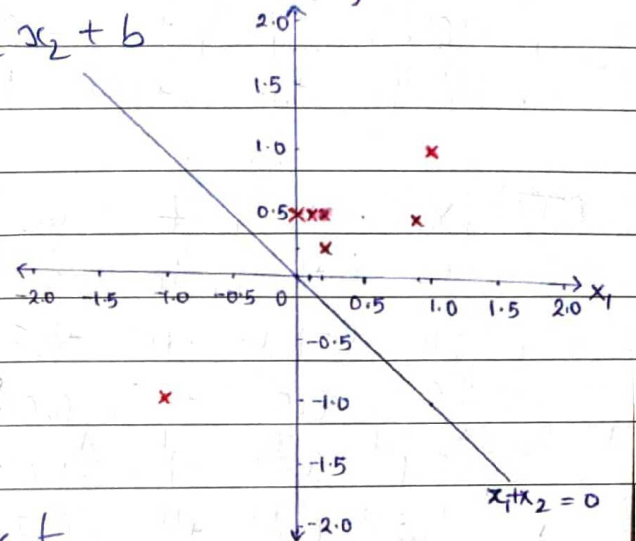
$$b = 0$$

$$y_{in} = w_i^T x_i + b = w_1 x_1 + w_2 x_2 + b$$

Initial decision boundary and samples

Assume learning rate as 1.

$$y = \begin{cases} 1 & \text{if } y_{in} > 0 \\ 0 & \text{if } y_{in} = 0 \\ -1 & \text{if } y_{in} < 0 \end{cases}$$



$$\Delta w_1 = \alpha t x_1 \quad \Delta b = \alpha t$$

$$\Delta w_2 = \alpha t x_2$$

(I)	x_1	x_2	class(t)	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
	1	1	+1	2	+1	0	0	0	1	1	0
	-1	-1	-1	-2	-1	0	0	0	1	1	0
	0	0.5	-1	0.5	+1	0	-0.5	-1	1	0.5	-1
	0.1	0.5	-1	-0.65	-1	0	0	0	1	0.5	-1
	0.2	0.2	+1	-0.4	-1	0.2	0.2	1	1.2	0.7	0
	0.9	0.5	+1	1.43	+1	0	0	0	1.2	0.7	0

(.II)	x_1	x_2	t	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
	1	1	+1	1.9	+1	0	0	0	1.2	0.7	0
	-1	-1	-1	-1.9	-1	0	0	0	1.2	0.7	0
	0	0.5	-1	0.35	+1	0	-0.5	-1	1.2	0.2	-1
	0.1	0.5	-1	-0.78	-1	0	0	0	1.2	0.2	-1
	0.2	0.2	+1	-0.72	-1	0.2	0.2	1	1.4	0.4	0
	0.9	0.5	+1	1.46	+1	0	0	0	1.4	0.4	0

(III)

x_1	x_2	t	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
1	1	+1	1.8	+1	0	0	0	1.4	0.4	0
-1	-1	-1	-1.8	-1	0	0	0	1.4	0.4	0
0	-1	-1	0.2	+1	0	-0.5	-1	1.4	-0.1	-1
0.1	-1	-1	-0.81	-1	0	0	0	1.4	-0.1	-1
0.2	+1	+1	-0.74	-1	0.2	0.2	1	1.6	0.1	0
0.9	+1	+1	1.44	+1	0	0	0	1.6	0.1	0

(IV)

x_1	x_2	t	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
1	+1	1	1.7	+1	0	0	0	1.6	0.1	0
-1	-1	-1	-1.7	-1	0	0	0	1.6	0.1	0
0	0.5	-1	0.05	+1	0	-0.5	-1	1.6	-0.4	-1
0.1	0.5	-1	-1.04	-1	0	0	0	1.6	-0.4	-1
0.2	0.2	+1	-0.76	-1	0.2	+0.2	1	1.8	-0.2	0
0.9	0.5	+1	1.52	+1	0	0	0	1.8	-0.2	0

(V)

x_1	x_2	t	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
1	1	+1	1.6	+1	0	0	0	1.8	-0.2	0
-1	-1	-1	-1.6	-1	0	0	0	1.8	-0.2	0
0	0.5	-1	-0.1	-1	0	0	0	1.8	-0.2	0
0.1	0.5	-1	0.08	+1	-0.1	-0.5	-1	1.7	-0.7	-1
0.2	0.2	+1	-0.8	-1	0.2	0.2	1	1.9	-0.5	0
0.9	0.5	+1	1.46	+1	0	0	0	1.9	-0.5	0

VI

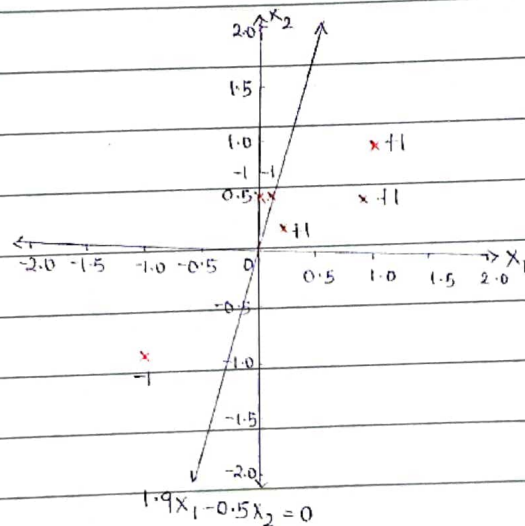
x_1	x_2	t	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
1	1	1	1.4	1	0	0	0	1.9	-0.5	0
-1	-1	-1	-1.4	-1	0	0	0	1.9	-0.5	0
0	0.5	-1	-0.25	-1	0	0	0	1.9	-0.5	0
0.1	0.5	-1	-0.06	-1	0	0	0	1.9	-0.5	0
0.2	0.2	+1	0.28	1	0	0	0	1.9	-0.5	0
0.9	0.5	+1	1.46	1	0	0	0	1.9	-0.5	0

The perceptron learning algorithm converged in 6 steps.
The final weight vector of the decision boundary is $w = [1.9, -0.5]$.

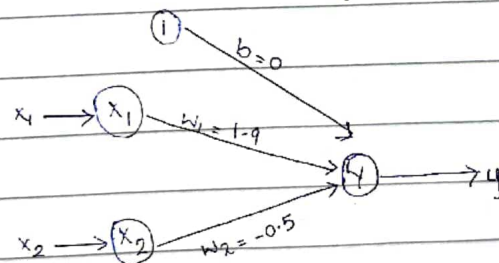
$$1.9x_1 + (-0.5)x_2 = 0 \Rightarrow 1.9x_1 - 0.5x_2 = 0$$

Let's plot the final ~~bx~~ decision boundary.

We can see that $1.9x_1 - 0.5x_2 = 0$ line separates the two classes correctly.



Final decision boundary



Neural network corresponding to the perceptron