

Antiamuny Code Library

tarjen

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第零章

- 安装 typst:
 - Linux, macOS, WSL

curl -fsSL https://typst.community/typst-install/install.sh | sh

► Windows

irm https://typst.community/typst-install/install.ps1 | iex

- 安装 VSCode 插件 tinymist:
 - ▸ 打开 VSCode
 - ► 搜索 tinymist 安装插件

赛前准备

```
测样例脚本(python 版)
1 import os
2 import sys
3 import zipfile
5 c = sys.argv[1]
6 code
测样例脚本(bash 版)
对拍(cpp 版本)
1 int t=10000, j=0;
2 while(t)
3 {
4
      cout<<"test:"<<++j<<"\n";
5
      system("testin.exe > data.txt");
7
      system("abiaocheng.exe < data.txt > biaoda.txt");
      system("nedtest.exe < data.txt > aatest.txt");
      if(system("fc aatest.txt biaoda.txt")){
9
10
           cout<<"error"<<"\n";</pre>
11
           break:
12
13 }
14 if(t==0) cout<<"no error"<<endl;</pre>
15 //system("pause");
16 return 0;
对拍(bat 版本)
1 @echo off
2 setlocal enabledelayedexpansion
3
4 set T=0
5 :loop
6 if %T% gtr 100000 (
      echo "Finished"
8
      exit /b
9)
10 set /a T+=1
11 echo T=!T!
12 testin.exe > data.txt
13 abiaocheng.exe < data.txt > biaoda.txt
14 nedtest.exe < data.txt > aatest.txt
15
16 fc aatest.txt biaoda.txt
17 if errorlevel 1 (
18
       echo "WA"
19
       exit /b
20 )
21
22 goto loop
```

杂项

rand

```
1 mt19937 64 rng(chrono::steady clock::now().time since epoch().count());
2 int myRand(int B) {
3 return (unsigned long long)rng() % B;
4 }
time
1 struct gettime{
2
      clock_t star,ends;
3
      gettime(){
4
          star = clock();
5
6
      ~gettime(){
7
          ends = clock();
8
          cout <<"Running Time : "<<(double)(ends - star)/ CLOCKS_PER_SEC << endl;</pre>
9
      }
10 } tim;
11 int main()
12 {
13
       tim.begin();
14
       tim.end();
15
       return 0;
16
17 }
子集枚举
1 for(int i=0;i<(1<<n);i++){</pre>
2
      for(int j=i;j;j=(j-1)&i){
3
4
      }
5 }
高维前缀和
1 for(int j = 0; j < n; j++)
2
      for(int i = 0; i < 1 << n; i++)
3
          if(i >> j \& 1) f[i] += f[i ^ (1 << j)];
三分
1 double f(double x){
2
      //something
3 }
4 const double eps=1e-8;
5 double sanfen(double l, double r){
      double mid,midr,ans;
6
7
      while (fabs(r-l)>eps) {
8
          mid=(l+r)/2;
9
          midr=(mid+r)/2;
10
           if(f(mid) < f(midr)) l=mid; else r=midr; //求最大值
11
       }
12
       ans=f(l);
13
       return ans;
14 }
```

bitset

```
1 template<int LEN>void solve(){
2
       sz=a.size();
3
       if (LEN<=b.size()){</pre>
4
           solve<min(N,LEN+10)>();
5
           return;
6
      }
7
      using Bitset=bitset<LEN>;
8
       Bitset is[sz+5];
9
       for(int i=0;i<sz;i++)for(int j=0;j<b.size();j++){</pre>
10
            auto&[x,l,r]=a[i];
11
            auto&[y,L,R]=b[j];
12
            if(l \le y \& y \le r \& L \le x \& x \le R) is[i][j]=1;
13
        }
14
        ll rs=0;
        for(int i=0,x;i<sz;i++)for(int j=i+1;j<sz;j++){}
15
16
            x=(is[i]\&is[j]).count();
17
            rs+=x*(x-1)/2;
18
        }
19
        cout<<rs<'\n';
20 }
bitset 手写
1 const int N=3000;
2 typedef unsigned long long ull;
4 int lim=N/64+3;
5 struct Bitset{
   ull v[N/64+5];
7 void init(){
8
     memset(v,0,sizeof(v));
9
      return;
10
    }
11
     void add(int x){
12
      v[x>>6] = (1ull << (x&63));
13
      return;
14
15
     void shift1(){
16
      int lst=0;
17
      for(int i=0;i<=lim;i++){</pre>
18
         int cur=v[i]>>63;
19
          v[i]<<=1;v[i]|=lst;
20
          lst=cur;
21
      }
22
      return;
23
24
     int count(){
25
      int res=0;
      for(int i=0;i<=lim;i++) res+=__builtin_popcountll(v[i]);</pre>
26
27
      return res;
28
      }
29
     Bitset operator | (const Bitset &x)const{
30
        Bitset res;
31
        for(int i=0;i<=lim;i++) res.v[i]=v[i]|x.v[i];</pre>
32
        return res;
33
      }
```

```
34
     Bitset operator&(const Bitset &x)const{
35
        Bitset res;
36
        for(int i=0;i<=lim;i++) res.v[i]=v[i]&x.v[i];</pre>
37
        return res;
38
39
     Bitset operator^(const Bitset &x)const{
40
        Bitset res;
41
        for(int i=0;i<=lim;i++) res.v[i]=v[i]^x.v[i];</pre>
42
        return res;
43
     }
44
     Bitset operator-(const Bitset &x)const{
45
        Bitset res;ull lst=0;
46
        for(int i=0;i<=lim;i++){</pre>
47
         ull cur=(v[i]<x.v[i]+lst);</pre>
48
         res.v[i]=v[i]-x.v[i]-lst;
49
         lst=cur;
50
      }
51
       return res;
52
53 }
lcslen(n2/w)
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int N=3010;
4 typedef unsigned long long ull;
5 const int lim=N/64+3;
6 struct Bitset{
7 ull v[N/64+5];
8 void init(){
    memset(v,0,sizeof(v));
10
     return;
11
     }
12
     void add(int x){
13
      v[x>>6] = (1ull << (x&63));
14
      return;
15
     }
16
     void shift1(){
17
      int lst=0;
18
      for(int i=0;i<=lim;i++){</pre>
19
        int cur=v[i]>>63;
20
          v[i]<<=1;v[i]|=lst;
21
          lst=cur;
22
      }
23
      return;
24
      }
25
      int count(){
26
      int res=0;
27
      for(int i=0;i<=lim;i++) res+=__builtin_popcountll(v[i]);</pre>
28
      return res;
29
      }
      Bitset operator | (const Bitset &x)const{
30
31
        Bitset res;
32
        for(int i=0;i<=lim;i++) res.v[i]=v[i]|x.v[i];</pre>
33
       return res;
34
     }
```

```
35
     Bitset operator&(const Bitset &x)const{
36
        Bitset res;
37
        for(int i=0;i<=lim;i++) res.v[i]=v[i]&x.v[i];</pre>
38
        return res;
39
40
     Bitset operator^(const Bitset &x)const{
41
42
        for(int i=0;i<=lim;i++) res.v[i]=v[i]^x.v[i];</pre>
43
        return res;
44
     }
45
     Bitset operator-(const Bitset &x)const{
46
        Bitset res;ull lst=0;
47
        for(int i=0;i<=lim;i++){</pre>
48
         ull cur=(v[i]<x.v[i]+lst);</pre>
49
         res.v[i]=v[i]-x.v[i]-lst;
50
          lst=cur;
51
      }
52
        return res;
53
      }
54 }ch[26],f,g;
55 auto getans = [&](int mid){
56
        int l1=mid, l2=n-mid;
57
        f.init();g.init();
58
        for(int i=0;i<26;i++){</pre>
59
            ch[i].init();
60
61
        for(int i=mid+1;i<=n;i++)ch[s[i]-'a'].add(i);</pre>
62
        for(int i=1;i<=mid;i++){</pre>
63
            q=f|ch[s[i]-'a'];
64
            f.shift1();
65
            f.add(1):
66
            f=g-f;
67
            f=f^g; f=f\&g;
68
        }
69
        return f.count();
70 };
wqs 二分
1 // 这里是 上凸 取 min
2 // 上凸取 max 二分的时候改变一下 mid 的变化方向
3 // 下凸取 min 改变 mid 算贡献的符号
4 //min max 指的是求的是最大值 还是最小值
5 int solve(int mid){
6
       k=mid;
7
       function<void(int,int)> dfs = [\&](int x,int h){
8
           info dp2[3];memset(dp2,0,sizeof(dp2));
9
           for(auto [it,w]:ve[x])if(it!=h){
10
                dfs(it,x);
11
                gmax(dp2[0],dp[x][0]+dp[it][0]);
12
                gmax(dp2[2],dp[x][0]+dp[it][1]);
13
                gmax(dp2[2],dp[x][2]+dp[it][0]);
14
                dp[x][0]=dp2[0];
15
                dp[x][1]=dp2[1];
16
                dp[x][2]=dp2[2];
17
18
            dp[x][0]=dp2[2];
```

```
19
            dp[x][1]=dp2[0]+info{a[x]+k,1};
20
       };
21
       dfs(1,0);
22
       return dp[1][0].second;
23 }
24 signed main()
25 {
26
       int l=-sum-10000000000000ll, r=sum+10000000000001;
27
       int ans=1e18;
28
       while(l<=r){</pre>
29
            int mid=(l+r)/2ll;
30
            if(solve(mid)>=m){
31
                ans=dp[1][0].first-m*mid;
32
                r=mid-1;
33
            }
34
            else l=mid+1;
35
       }
36
       if(ans!=(int)1e18)cout<<ans<<"\n";</pre>
37
        else cout<<"Impossible\n";</pre>
       return 0;
38
39 }
判断异或方程组是否有解
1 const int maxn=1e2+5;
2 //每个方程组一定是 xi1^xi2^xi3...=1/0 的形式
3 bitset<maxn>b[maxn];//1 表示这个方程组存在 Xi 比如 x3^x5=1 就应该是 3 和 5 的地方上是 1
4 //b[n+1]存方程右边等于 0/1
5 int sum[maxn];
6 bool check(int x)
7 {
8
       for(int i=1;i<=n;i++)if(b[x][i])return true;</pre>
9
       return !b[x][n+1];
10 }
11 bool solve()
12 {
13
       for(int i=1,p=1;i<=n;i++,p++)</pre>
14
15
            if(!b[p][i])
16
17
                int pos=0;
18
                for(int j=p+1; j<=n; j++)</pre>
19
                    if(b[j][i])
20
21
                        pos=j;
22
                        break;
23
24
                if(pos)swap(b[p],b[pos]);
25
            }
26
            int flag=b[p][i];
27
            for(int j=p+1; j<=n; j++) if(b[j][i]) b[j]^=b[p],flag=1;</pre>
28
            if(!flag) p--;
29
30
        for(int i=1; i<=n; i++) if(!check(i)) return false;</pre>
31
        return true;
32 }
```

可以判断不同或相同的并查集

```
1 int f[maxn];
2 int getf(int x){
3
       if(x<0)return -getf(-x);</pre>
4
       if(x==f[x])return x;
5
       else return f[x]=getf(f[x]);
6 }
7 bool merge(int x,int y){//如果是 x!=y 将 y 取反(x>0 y>0)
8
       x=getf(x),y=getf(y);
9
      if(x==-y)return false;
10
       if(x==y)return true;
11
        if(x<0)f[-x]=-y;
12
        else f[x]=y;
13
        return true;
14 }
Int128
1 #include <bits/stdc++.h>
2 using namespace std;
3 inline __int128 read()
4 {
5
        int128 x=0, f=1;
6
       char ch=getchar();
7
      while(ch<'0'||ch>'9')
8
       {
9
           if(ch=='-')
10
                f=-1;
11
            ch=getchar();
12
        while(ch>='0'&&ch<='9')</pre>
13
14
15
            x=x*10+ch-'0';
16
            ch=getchar();
17
18
        return x*f;
19 }
20 inline void write(__int128 x)
21 {
22
        if(x<0)
23
        {
24
            putchar('-');
25
            X=-X;
26
27
        if(x>9)
28
            write(x/10);
29
        putchar(x%10+'0');
30 }
31
32 istream& operator >> (istream& in, __int128& num) {
33
        string s;in>>s;
34
        num=0;
35
        for(auto it:s)num=num*10+it-'0';
36
        return in;
37 }
38
```

39 ostream& operator << (ostream& out, __int128 num) {

```
40
       string s;
41
       do{
42
           s.push_back(char(num%10+'0'));
43
           num/=10;
44
       }while(num>0);
45
       reverse(s.begin(),s.end());
46
       out<<s;
47
       return out;
48 }
树哈希
1 #include <cctype>
2 #include <chrono>
3 #include <cstdio>
4 #include <random>
5 #include <set>
6 #include <vector>
8 typedef unsigned long long ull;
10 const ull mask = std::chrono::steady_clock::now().time_since_epoch().count();
11
12 ull h(ull x) {
13
       return x * x * x * 1237123 + 19260817;
14 }
15 ull f(ull x) {
       ull cur = h(x \& ((1 << 31) - 1)) + h(x >> 31);
16
17
       return cur;
18 }
19 ull shift(ull x) {
x = mask;
x = x << 13;
22 x = x >> 7;
     x ^= x << 17;
23
     x ^= mask;
24
25
     return x;
26 }
27
28 const int N = 1e6 + 10;
29
30 int n;
31 ull hash[N];
32 std::vector<int> edge[N];
33 std::set<ull> trees;
34
35 void getHash(int x, int p) {
36 \quad hash[x] = 1;
37
     for (int i : edge[x]) {
38
       if (i == p) {
39
         continue;
40
       }
41
       getHash(i, x);
42
       hash[x] += shift(hash[i]);
43
44
     trees.insert(hash[x]);
45 }
```

```
46
47 int main() {
48
      scanf("%d", &n);
49
      for (int i = 1; i < n; i++) {
50
       int u, v;
51
       scanf("%d%d", &u, &v);
52
       edge[u].push back(v);
53
       edge[v].push_back(u);
54
55
     getHash(1, 0);
56
     printf("%lu", trees.size());
57 }
58
求 s 所有前缀对于 t 的所有子串的 lcs 长度
1 #include <bits/stdc++.h>
2 using namespace std;
3 struct PairLCS {
      vector<vector<int>> ih, iv;
5
      int n = 0, m = 0;
6
      PairLCS(string s, string t) : n(s.size()), m(t.size()) {
7
           ih = iv = vector<vector<int>>>(n + 1, vector<int>(m + 1));
8
           iota(ih[0].begin(),ih[0].end(), 0);
           for (int i = 1; i \le n; i++) {
9
10
                for (int j = 1; j \le m; j++) {
11
                    if (s[i - 1] == t[j - 1]) {
12
                        ih[i][j] = iv[i][j - 1];
13
                        iv[i][j] = ih[i - 1][j];
14
                    } else {
15
                        ih[i][j] = std::max(ih[i - 1][j], iv[i][j - 1]);
16
                        iv[i][j] = std::min(ih[i - 1][j], iv[i][j - 1]);
17
                    }
18
                }
19
           }
20
21
        int query(int a, int b, int c) const {
22
            int res = 0;
23
            for (int i = b + 1; i \le c; i++) res += ih[a][i] \le b;
24
            return res;
25
       } // s[0,a) t[b,c)
26 };
27
28
29
30 int cas;
31
32 void solution() {
33
     int q;
34
     std::string s, t;
35
      std::cin >> q >> s >> t;
36
37
     // int n = s.size(), m = t.size();
38
     PairLCS solver(s, t);
39
40
     for (int _ = 0; _ < q; _++) {
41
      int a, b, c;
```

```
42
       std::cin >> a >> b >> c;
43
      std::cout << solver.query(a, b, c) << '\n';</pre>
44
     }
45 }
46
47
48 int main() {
49
       ios::sync_with_stdio(false);
50
       cin.tie(0);
51
       int T = 1;
52
       // std::cin >> T;
53
       for (cas = 1; cas <= T; cas++) solution();</pre>
54
55
       return 0;
56 }
线性基
1 struct LinearBasis
2 {
3
      static const int maxbase = 35;
4
      bool flag = false;
5
      ll a[maxbase + 1];
      int tot;
6
7
      LinearBasis()
8
9
           memset(a, 0, sizeof a);
10
           tot=0;
11
       }
12
       LinearBasis(ll *x, int n)
13
14
           LinearBasis();
15
           build(x, n);
16
17
       void build(ll *x, int n)
18
19
            for(int i = 1; i <= n; ++i)</pre>
20
               insert(x[i]);
21
       }
22
       void clear()
23
24
           memset(a, 0, sizeof a);
25
26
       bool insert(ll t)
27
           //暴力插入一个数,维护的是一个上三角型的线性基矩阵,时间复杂度低,当待插入元素能插入时,返
28
□ true
29
            for(int i = maxbase; i \ge 0; --i)
30
31
                if(t & (1ll << i))</pre>
32
                {
33
                    if(!a[i])
34
                    {
35
                        a[i] = t;//这里表示插入成功
36
                        break;
37
38
                    t ^= a[i];
```

```
39
                }
40
41
            if(t == 0)flag = true;
42
            return t;
43
       }
44
       bool query(ll t)
45
46
            // 询问 t 是否可以被当前线性基表示,不插入
47
           if(t > queryMax())return false;
48
            if(t == 0)return true;
49
            for(int i = maxbase; i \ge 0; --i)
50
51
                if(t & (1ll << i))</pre>
52
                {
53
                    if(!a[i])
54
                    {
55
                        return false;
56
57
                    t ^= a[i];
58
                }
59
            }
60
            return true;
61
62
       void Insert(ll t)
63
            //插入一个线性基,利用高斯消元法维护一个对角矩阵
64
65
            for(int i = maxbase; i \ge 0; --i)
66
            {
67
                if(t >> i & 1)
68
                {
69
                    if(a[i])t ^= a[i];
70
                    else
71
                    {
72
                        a[i] = t;
73
                        for(int j = i - 1; j \ge 0; --j)if(a[j] && (a[i] >> j & 1))a[i]
^= a[j];
74
                        for(int j = i + 1; j \le maxbase; ++j)if(a[j] >> i & 1)a[j] ^=
a[i];
75
                        break;
76
                    }
77
                }
78
           }
79
       }
80
       LinearBasis merge(const LinearBasis &l1, const LinearBasis &l2)
81
82
            // 得到两个线性基的并
            LinearBasis ret = l1;
83
84
            for(int i = maxbase; i \ge 0; --i)
85
                if(l2.a[i])
86
                    ret.insert(l2.a[i]);
87
            return ret;
88
       }
89
       LinearBasis intersection(const LinearBasis &l1, const LinearBasis &l2)
90
            //得到两个线性基的交
91
92
            LinearBasis all, ret, full;
```

```
93
            ret.clear();
94
            for(int i = maxbase; i \ge 0; --i)
95
96
                 all.a[i] = l1.a[i];
97
                 full.a[i] = 1ll << i;</pre>
98
            }
            for(int i = maxbase; i \ge 0; --i)
99
100
             {
                  if(l2.a[i])
101
102
                  {
103
                      ll v = l2.a[i], k = 0;
104
                      bool flag = true;
105
                      for(int j = maxbase; j \ge 0; --j)
106
107
                          if(v & (1ll << j))</pre>
108
109
                               if(all.a[j])
110
                               {
111
                                   v ^= all.a[j];
112
                                   k ^= full.a[j];
113
                               }
114
                               else
115
                               {
116
                                   // l2's basis is not in l1's;
117
                                   flag = false;
                                   all.a[j] = v;
118
119
                                   full.a[j] = k;
120
                                   break;
121
                               }
                          }
122
123
                      }
124
                      if(flag)
125
126
                          ll v = 0; // get intersection by k;
127
                          for(int j = maxbase; j \ge 0; --j)
128
129
                               if(k & (1ll << j))</pre>
130
                               {
131
                                   v ^= l1.a[j];
132
                               }
133
                          }
134
                          ret.insert(v);
135
                      }
136
                  }
137
             }
138
             return ret;
139
         //询问最值
140
         ll queryMax()
141
142
143
             ll ret = 0;
144
              for(int i = maxbase; i \ge 0; --i)
                  if((ret ^ a[i]) > ret)
145
146
                      ret ^= a[i];
147
             return ret;
148
         }
```

```
149
        ll queryMin()
150
             for(int i = 0; i <= maxbase; ++i)</pre>
151
152
                 if(a[i])
153
                    return a[i];
154
            return 0;
155
        }
156
        ll Kth_Max(ll k)
157
158
            ll res=0;
159
             for(int i=62;i>=0;i--)
160
                if (k&(1LL<<i)) res^=a[i];</pre>
161
            return res;
162
        }
163 };
164
维护多个二维向量能够表示的范围
1 int gcd(int x,int y){
      if(y==0)return x;
3
      else return gcd(y,x%y);
4 }
5 struct vec{
      int a00,a01,a11;
7
      void clear(){
8
           a00=a01=a11=0;
9
      }
10
       void insert(int x,int y){
11
           while(x!=0){
12
                int t=a00/x;
13
                a00-=x*t;
14
                a01-=y*t;
15
                swap(a00,x);
16
                swap(a01,y);
17
18
            all=gcd(all,abs(y));
19
            if(a11!=0)a01%=a11;
20
21
       bool query(int x,int y){
22
            if(x!=0){
                if(a00==0||x%a00!=0)return false;
23
24
                int t=x/a00;
25
                y = a01 * t;
26
            }
27
            if(y==0)
28
               return true;
29
30
           else return all!=0&&y%all==0;
31
       }
32 };
```

字符串

AC 自动机

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=1e6+10;
4 int n;
5 char c[maxn];
6 struct AC{
7
      int trie[maxn][26],tot;
      int e[maxn],fail[maxn],old[maxn];
9
      void init(){
10
           memset(trie, 0, sizeof(trie));
11
           memset(e,0,sizeof(e));
12
           memset(fail,0,sizeof(fail));
13
           memset(old,0,sizeof(old));
14
           tot=0;
15
16
       void insert(char *t){
            int x=0;
17
            for(int i=1;t[i];i++){
18
19
                if(!trie[x][t[i]-'a']){
20
                    trie[x][t[i]-'a']=++tot;
21
                }
22
                x=trie[x][t[i]-'a'];
23
            }
24
           e[x] ++;
25
       }
       queue<int> qu;
26
27
        void build(){
28
            for(int i=0;i<26;i++){</pre>
29
                if(trie[0][i])qu.push(trie[0][i]);
30
            }
31
           while(!qu.empty()){
32
                int x=qu.front();
33
                qu.pop();
34
                for(int i=0;i<26;i++){
35
                    if(trie[x][i]){
36
                        fail[trie[x][i]]=trie[fail[x]][i];
37
                        qu.push(trie[x][i]);
38
39
                    else trie[x][i]=trie[fail[x]][i];
40
                          old[trie[x][i]]=e[fail[trie[x][i]]] ? fail[trie[x][i]] :
old[fail[trie[x][i]]];
41
                }
42
            }
43
44
       int query(char *t){//这里是统计有多少模板串出现在了文本串之中,所以统计到了就要变成-1
            int x=0, res=0;
46
            for(int i=1;t[i];i++){
47
                x=trie[x][t[i]-'a'];
48
                for(int j=x;j&&e[j]!=-1;j=old[j]){
49
                    res+=e[j];
50
                    e[j]=-1;
51
                }
52
            }
```

```
53
            return res;
54
       }
55 };
56 AC ac;
57 int main()
58 {
59
       scanf("%d",&n);
60
       for(int i=1;i<=n;i++){</pre>
61
            scanf("%s",c+1);
62
           ac.insert(c);
63
64
       ac.build();
65
       scanf("%s",c+1);
66
67
       cout<<ac.query(c)<<endl;</pre>
68
       return 0;
69 }
Dequehash
1 /*
2 严格 Obase, 不用管任何函数里面的东西, 用就可以了, 不要越界
3 pair<int,int> first 表示哈希 sum, second 表示当前位置的值
5 #define int long long
6 #define sz(a) (int)((a).size())
7 const int maxn=3e5+10;
8 const int mod=le9+7,base=1331;
9 int fpow(int n, int k, int p = mod) {int r = 1; for (; k; k >>= 1) {if (k & 1) r =
r * n % p; n = n * n % p;} return r;}
10 void add(int& a, int val, int p = mod) {if ((a = (a + val)) >= p) a -= p;}
11 void sub(int& a, int val, int p = mod) {if ((a = (a - val)) < 0) a += p;}
int mul(int a, int b, int p = mod) {return (int) a * b % p;}
int inv(int a, int p = mod) {return fpow(a, p - 2, p);}
14 int p[maxn],ip[maxn];
15 void init()
16 {
17
       p[0] = 1; for(int i=1;i<maxn;i++) p[i] = mul(p[i - 1], base, mod);
18
       for(int i=0;i<maxn;i++) ip[i] = inv(p[i], mod);</pre>
19 }
20 struct extendable_sequence {
21
       deque<pair<int,int>> dq;
22
       int pow_offset;
23
24
       extendable_sequence() {
25
            pow offset = 0;
26
           dq.push_back(make_pair(0, 0));
27
       }
28
29
       int size() {
30
           return sz(dq) - 1;
31
       }
32
       pair<int,int>& operator [] (int i) {
33
34
            return dq[i+1];
35
36
```

```
37
       void add back(vector<int> vals) {
38
            int t = dq.back().first;
39
            for(int i=0;i<sz(vals);i++) {</pre>
40
                add(t, mul(vals[i], mul(p[sz(dq) - 1], ip[pow_offset], mod), mod), mod);
41
                dq.push_back(make_pair(t, vals[i]));
42
           }
43
       }
44
45
        void add front(vector<int> vals) {
46
            pow_offset += sz(vals);
47
            int t = dq.front().first;
48
            for(int i=sz(vals)-1;i>=0;i--) {
49
                dq.front().second = vals[i];
50
                sub(t, mul(vals[i], mul(p[i], ip[pow_offset], mod), mod);
51
                dq.push_front(make_pair(t, 0));
52
           }
53
       }
54
55
       int calc(int l, int r) {
56
            l++, r++;
57
            if (l > r) return 0;
58
            int res = dq[r].first;
59
            sub(res, dq[l - 1].first, mod);
60
            res = mul(res, ip[l - 1], mod);
61
            res = mul(res, p[pow_offset], mod);
62
            return res;
63
       }
64 };
65 //返回(x+y)[l 到 r]的哈希值
66 int calc(extendable sequence& x, extendable sequence& y, int l, int r) {
        int res = x.calc(l, min(r, sz(x) - 1));
67
68
        add(res, mul(y.calc(max(Oll, l - sz(x)), r - sz(x)), p[sz(x)], mod), mod);
69
        return res;
70 }
71 //返回(x+y)[i]单个元素的值
72 int calc(extendable_sequence& x, extendable_sequence& y, int i) {
73
       if (i < sz(x)) {
74
            return x[i].second;
75
       }
76
        if (i - sz(x) < sz(y)) {
77
            return y[i - sz(x)].second;
78
79
       return -1;
80 }
Exkmp
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn = 1e6 + 1e3;
4 struct EXKMP
5 { // S里找T
7
      char S[maxn], T[maxn];
8
      int next[maxn], extend[maxn];
      void Get_Next()
10
       {
```

```
11
            int lenT = strlen(T + 1), p = 1, pos;
12
           next[1] = lenT; // 对于 next[1] 要特殊考虑
13
           while (p + 1 \le lenT \&\& T[p] == T[p + 1])
14
15
           next[pos = 2] = p - 1; // next[2] 是为了初始化
16
17
            for (int i = 3; i <= lenT; i++)</pre>
18
            { // 注意此时 k + 1 = i
19
               int len = next[i - pos + 1];
20
               if (len + i 
21
                   next[i] = len; // 对应上面第一种情况
22
               else
23
               {
24
                   int j = max(p - i + 1, 0); // 找到前面对于 子串 最靠后已经匹配的位置
25
                   while (i + j \le lenT \& T[j + 1] == T[i + j])
26
                                                    // 第二种需要暴力匹配
27
                   p = i + (next[pos = i] = j) - 1; // 记得更新 p, pos
28
               }
29
           }
30
       }
31
       void ExKMP()
32
33
           int lenS = strlen(S + 1), lenT = strlen(T + 1), p = 1, pos;
34
           Get_Next();
35
           while (p \le lenT \&\& S[p] == T[p])
36
               ++p;
37
           p = extend[pos = 1] = p - 1; // 初始化 extend[1]
38
39
           for (int i = 2; i <= lenS; i++)</pre>
40
           {
41
               int len = next[i - pos + 1];
42
               if (len + i 
43
                   extend[i] = len;
44
               else
45
               {
46
                   int j = max(p - i + 1, 0);
47
                   while (i + j \le lenS \& j \le lenT \& T[j + 1] == S[i + j])
48
49
                   p = i + (extend[pos = i] = j) - 1;
50
               }
51
           } // 和上面基本一模一样啦
52
53 } sol;
54 int main()
55 {
56
       scanf("%s", sol.S + 1);
57
       scanf("%s", sol.T + 1);
58
59
       sol.ExKMP();
60
       int len = strlen(sol.S + 1);
61
       for (int i = 1; i \le len; i++)
62
           printf("%d%c", sol.extend[i], i == len ? '\n' : ' ');
63
64
       return 0;
65 }
```

```
Hash
```

```
1 const int N=1e6+10;
2 typedef long long ll;
3 const ll p1=31,p2=131;
4 const ll mod1=1e9+7, mod2=1e9+9;
5 typedef pair<ll, ll> hs;
6 const hs p = make_pair(p1,p2);
7 hs &operator+=(hs &a, hs b) {
8
      a.first=(a.first+b.first)%mod1;
9
      a.second=(a.second+b.second)%mod2;
10
       return a;
11 }
12 hs operator+(hs a, hs b) { return a += b; }
13 hs &operator-=(hs &a, hs b) {
14
       a.first=(a.first-b.first+mod1)%mod1;
15
       a.second=(a.second-b.second+mod2)%mod2;
16
       return a;
17 }
18 hs operator-(hs a, hs b) { return a -= b; }
19 hs &operator*=(hs &a, hs b) {
20
       a.first=(a.first*b.first)%mod1;
21
       a.second=(a.second*b.second)%mod2;
22
       return a;
23 }
24 hs operator*(hs a, hs b) { return a *= b; }
25 struct Hash{
26
       int n:
27
       vector<hs>has1,has2,Pow;
28
       void Hash init(string &s){
29
           n=(int)s.size();
30
           Pow.resize(n+2);
31
           has1.resize(n+2);
32
           has2.resize(n+2);
33
           Pow[0]=make pair(111,111);
34
           for(int i=1;i<=n;i++)Pow[i]=Pow[i-1]*p;</pre>
35
            for(int i=1;i<=n;i++)has1[i]=has1[i-1]*p+hs{s[i-1]-'a'+1,s[i-1]-'a'+1};
36
            for(int i=n;i>=1;i--)has2[i]=has2[i+1]*p+hs{s[i-1]-'a'+1,s[i-1]-'a'+1};
37
38
       hs get1(int l,int r){
39
            return has1[r]-has1[l-1]*Pow[r-l+1];
40
41
       hs get2(int l,int r){
42
            return has2[l]-has2[r+1]*Pow[r-l+1];
43
       }
44 };
Kmp
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=1e6+10;
4 struct KMP{//lbase
      int len1,n,nxt[maxn];//nxt表示以i为结尾的前缀与后缀相同的长度
5
6
      char s1[maxn],s[maxn];
7
      void build()
8
          n=strlen(s+1);
```

```
10
            nxt[1]=0;
11
            int x=2, now=1; //x 是 s2 当前搜索到的位置, now 是前缀位置
12
            while(x<=n){</pre>
13
                if(s[x]==s[now]){
14
                     nxt[x]=now;
15
                     now++;
16
                     x++;
17
                }
18
                else{
19
                     if(now>1){
20
                         now=nxt[now-1]+1;
21
                     }
22
                     else{
23
                         nxt[x]=0;
24
                         now=1;
25
                         X++;
26
                     }
27
                }
28
            }
29
        }
30
        void find(){//sl 1base
31
            int now=1,tar=1;
32
            len1=strlen(s1+1);
33
            while(tar<=len1){</pre>
34
                if(s1[tar]==s[now]){
35
                     tar++;
36
                     now++;
37
                }
38
                else{
39
                     if(now>1){
40
                         now=nxt[now-1]+1;
41
                     }
42
                     else tar++;
43
                }
44
                if(now==n+1){
45
                     printf("%d\n",tar-now+1);
46
                }
47
            }
48
        }
49 };
50 KMP sol;
51 int main()
52 {
53
        scanf("%s%s",sol.s1+1,sol.s+1);
54
        sol.build();
55
        sol.find();
56
        for(int i=1;i<=sol.n;i++)cout<<sol.nxt[i]<<" ";</pre>
57
        return 0;
58 }
Manacher
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn = 1.1e7 + 5;
4 struct ST{
5 char s[maxn * 2], str[maxn * 2];
```

```
6 int Len[maxn * 2], len;
7
  void getstr() {//重定义字符串
8
      int k = 0;
9
     len = strlen(s);
10
      str[k++] = '@';//开头加个特殊字符防止越界
11
      for (int i = 0; i < len; i++) {
12
         str[k++] = '#';
13
         str[k++] = s[i];
14
15
      str[k++] = '#';
16
      len = k;
17
      str[k] = 0; // 字符串尾设置为 0, 防止越界
18 }
19
    int manacher() {
20
     int mx = 0, id;//mx 为最右边, id 为中心点
21
     int maxx = 0;
22
      for (int i = 1; i < len; i++) {
23
         if (mx > i) Len[i] = min(mx - i, Len[2 * id - i]);//判断当前点超没超过 mx
24
         else Len[i] = 1; //超过了就让他等于 1, 之后再进行查找
25
         while (str[i + Len[i]] == str[i - Len[i]]) Len[i]++;//判断当前点是不是最长回文子
串,不断的向右扩展
26
       if (Len[i] + i > mx) {//更新 mx
27
          mx = Len[i] + i;
28
          id = i;//更新中间点
29
         maxx = max(maxx, Len[i]);//最长回文字串长度
30
         }
31
       }
32
       return (maxx - 1);
33
    }
34
   void writ(){
35
      printf("%s\n",str);
36
         for(int i=0;i<len;i++){</pre>
37
             cout<<Len[i]<<" ";
38
        }
39
       cout<<"\n";
40
     }
41 };
42 ST s1,s2;
43 int main() {
44 scanf("%s", s1.s);
45 s1.getstr();
46 printf("%d\n",s1.manacher());
47
    return 0;
48 }
倍增 SA
1 #include<bits/stdc++.h>
2 using namespace std;
3 const int N = 1e6 + 10; //2*strlen
4 struct Suffix{
5
   int ht[N],rk[N],sa[N],y[N],c[N];
6
      int n,m;
7
      char s[N];
8 void init(){
          n=strlen(s+1);
10
          m = 300;
```

```
11
       for(int i=0;i<=m;i++) c[i]=0;</pre>
12
        for(int i=0; i<=2*n; i++) y[i]=0;
13
        for(int i=1;i<=n;i++) c[rk[i]=s[i]]++;</pre>
14
       for(int i=1;i<=m;i++) c[i]+=c[i-1];</pre>
15
        for(int i=n;i>=1;i--) sa[c[rk[i]]--]=i;
16
        for(int k=1; k<=n; k<<=1) {</pre>
17
         int p=0;
18
         for(int i=n-k+1;i<=n;i++) y[++p]=i;</pre>
19
          for(int i=1;i<=n;i++){</pre>
20
           if(sa[i]>k){
21
             y[++p]=sa[i]-k;
22
            }
23
          }
24
         for(int i=0;i<=m;i++) c[i]=0;</pre>
25
          for(int i=1;i<=n;i++) c[rk[i]]++;</pre>
26
          for(int i=1;i<=m;i++) c[i]+=c[i-1];
27
          for(int i=n;i>=1;i--) sa[c[rk[y[i]]]--]=y[i];
28
          for(int i=0;i<=n;i++) swap(rk[i],y[i]);</pre>
29
          rk[sa[1]]=p=1;
30
         for(int i=2;i<=n;i++){</pre>
31
           rk[sa[i]]=(y[sa[i]] == y[sa[i-1]] & y[sa[i]+k] == y[sa[i-1]+k] ? p : ++p);
32
          }
33
          if(p>=n) break;
34
          m=p;
35
       }
36
        for(int i=1, k=0; i<=n; i++) {</pre>
37
         if(k)k--;
38
          int j=sa[rk[i]-1];
39
         while(s[i+k] == s[j+k])k++;
40
         ht[rk[i]] = k;
41
       }
42
      }
43
        void writ()
44
45
             printf("%s\n",s+1);
            for(int i=1;i<=n;i++)cout<<sa[i]<<" ";;cout<<"\n";</pre>
46
             for(int i=1;i<=n;i++)cout<<ht[i]<<" ";;cout<<"\n";</pre>
47
48
             for(int i=1;i<=n;i++)cout<<rk[i]<<" ";;cout<<"\n";</pre>
49
        }
50
51 };
52 Suffix suf;
后缀自动机 SAM
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int N=2e6;
4 struct SAM {
5
       struct Node {
6
           int tr[26];
7
           int len, fa;
8
           Node() { memset(tr, 0, sizeof(tr)); len = fa = 0; }
9
       ep[N << 1];
10
        int last, tot, n;
11
        char base;
12
        vector<int> edg[N << 1];</pre>
```

```
13
        int siz[N << 1];</pre>
14
        void init(int _n) {
15
            last = tot = 1;
16
            base = 'a';
17
            for (int i = 0; i <= 2 * _n; i++) {
18
                ep[i] = Node();
19
                edg[i].clear();
20
                siz[i] = 0;
21
            }
22
        }
23
        void insert(char x) {
24
            int c = x - base;
            int p = last;
25
26
            int np = last = ++tot;
27
            siz[np] = 1;
28
            ep[np].len = ep[p].len + 1;
29
            for (; p && !ep[p].tr[c]; p = ep[p].fa)
30
                ep[p].tr[c] = np;
31
            if (!p) ep[np].fa = 1;
32
            else {
33
                int q = ep[p].tr[c];
34
                if (ep[q].len == ep[p].len + 1) ep[np].fa = q;
35
                else {
36
                    int nq = ++tot;
37
                    ep[nq] = ep[q];
38
                    ep[nq].len = ep[p].len + 1;
39
                    ep[q].fa = ep[np].fa = nq;
40
                    for (; p && ep[p].tr[c] == q; p = ep[p].fa)
41
                         ep[p].tr[c] = nq;
42
                }
43
            }
44
        }
45
        void construct() {
46
            for (int i = 2; i <= tot; i++) {
47
                edg[ep[i].fa].push_back(i);
48
            }
49
50
        void dfs(int u) {
51
            for (auto v : edg[u]) {
52
                dfs(v);
53
                siz[u] += siz[v];
54
            }
55
        }
56
        void build(string& s) {
57
            n = s.size();
58
            init(n);
59
            for (int i = 0; i < n; i++) {
60
                insert(s[i]);
61
            }
62
            construct();
63
            dfs(1);
64
        }
65
66 } sam;
67
```

回文自动机 PAM

```
1 #include<bits/stdc++.h>
2 using namespace std;
3 const int N=2e6+10;
4 struct PAM Trie
5 {
6 int ch[26];
7 int fail,len,num;
8 };
9 struct PAM
10 {
      PAM Trie b[N];
11
      int n,length,last,cnt;
12
13
      char s[N];
14
      PAM()
15
     {
16
        b[0].len = 0; b[1].len = -1;
17
        b[0].fail = 1; b[1].fail = 0;
18
      last = 0;
19
      cnt = 1;
20
21
      int get_fail(int x)
22
23
      while(s[n-b[x].len-1]!=s[n])
24
       {
25
          x=b[x].fail;
26
        }
27
        return x;
28
    }
29
     void insert()
30
      {
31
        int p=get_fail(last);
32
       if(!b[p].ch[s[n]-'a'])
33
34
          b[++cnt].len=b[p].len+2;
35
          int tmp=get_fail(b[p].fail);
36
          b[cnt].fail=b[tmp].ch[s[n]-'a'];
37
          b[cnt].num=b[b[cnt].fail].num+1;
38
          b[p].ch[s[n]-'a']=cnt;
39
40
        last=b[p].ch[s[n]-'a'];
41
       cout<<last<<"\n";</pre>
        //如果要统计出现次数 f[last]++;
42
43
     }
44
     void init()
45
      {
46
        length=strlen(s+1);
47
        for(n=1;n<=length;n++)</pre>
48
       {
          insert();
49
50
       }
51
    }
52 }pa;
53 int main()
54 {
   scanf("%s",pa.s+1);
```

```
56 pa.init();
57 return 0;
58 }
最小表示
1 int getMin(string s) {
      int i = 0, j = 1, k = 0;
3
      int len = s.length();
      while(i<len \&\& j<len \&\& k<len) {
4
5
          int tmp = s[(i + k) % len] - s[(j + k) % len];
6
          if(tmp==0) k++;
7
          else {
8
              if(tmp>0) i += k + 1;
9
              else j += k + 1;
10
               if(i==j) j++;
11
               k = 0;
12
           }
13
       }
14
       return min(i, j);
15 }
```

图论

```
johnson 全源最短路
```

```
1 struct graph {
2
    vector<vector<pair<int, ll>>> e;
    graph(int n) : e(n + 1) {}
4
    void adde(int u, int v, ll w) { e[u].push_back({v, w}); }
5
    vector<ll> h;
6
    // initialize h(u), return false if there exists a negative cycle
7
    bool init() {
      int n = e.size();
9
      h.assign(n, 0);
10
       queue<int> que;
11
        for (int u = 1; u < n; u++) que.push(u);
12
       vector<int> vis(n, 0), cnt(n, n + 1);
13
       while (que.size()) {
14
         auto u = que.front();
15
         que.pop();
16
         vis[u] = false;
17
         if (!cnt[u]--) return false; // exists a negative cycle
18
         for (auto &[v, w] : e[u])
19
            if (h[v] > h[u] + w) {
20
              h[v] = h[u] + w;
21
              if (!vis[v]) que.push(v), vis[v] = 1;
22
23
       }
24
       return true;
25
26
     // single source shortest path from given sink based on h(u)
27
     vector<ll> query(int s) {
28
       int n = e.size();
29
       vector<ll> dis(n, inf);
30
       priority_queue<pair<ll, int>, vector<pair<ll, int>>,
31
               greater<pair<ll, int>>>
32
           que;
33
       que.push(\{dis[s] = 0, s\});
34
       while (que.size()) {
35
         auto [du, u] = que.top();
36
         que.pop();
37
         if (dis[u] < du) continue;</pre>
38
         for (auto [v, w] : e[u]) {
39
            auto dv = du + w + h[u] - h[v];
40
            if (dis[v] > dv) que.push(\{dis[v] = dv, v\});
41
         }
42
43
       for (int i = 0; i < n; i++) dis[i] += h[i] - h[s];
       return dis;
45
     }
46 };
kosaraju
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn = 100010;
4 vector<int> ve[maxn], ve2[maxn];
5 vector<int> sta; // 存第一次 dfs1()的结果,即标记点的先后顺序,优先级小的点先进
```

```
6 int vis[maxn]; // vis[i]标记第一次 dfs1()点i是否访问过
7 int col[maxn]; // col[i]标记点 i 属于第几个强连通分量,同时记录 dfs2()过程中点 i 是否访问过
8 int cnt; //cnt 表示强连通分量的个数
9 void dfs1(int x){
10
      vis[x] = 1;
11
       for(auto it:ve[x])if(!vis[it])
12
          dfs1(it);
13
       sta.push back(x); //记录点的先后顺序,按照拓扑排序,优先级大的放在S的后面
14 }
15
16 void dfs2(int x){
17
      if(col[x])
                  return;
18
       col[x] = cnt;
19
       for(auto it:ve[x])if(!col[it])
20
          dfs2(it);
21 }
22 void Kosaraju(int n) {
23
      cnt = 0;
24
       sta.clear();
25
      memset(vis,0,sizeof(vis));
26
       memset(col, 0, sizeof(col));
27
      for(int i=1; i<=n; i++) //搜索所有点
28
          dfs1(i);
29
     for(int i=n-1; i>=0; i--){
30
         if(!col[sta[i]]){
31
              cnt++;
32
              dfs2(sta[i]);
33
          }
34
       }
35 }
36
K短路
1 //复杂度 nlogn +mlogm+klogk
2 #include <bits/stdc++.h>
3 #include <queue>
4
5 template <class T, class U>
6 inline bool smin(T &x, const U &y) {
7 return y < x ? x = y, 1 : 0;
8 }
9 template <class T, class U>
10 inline bool smax(T &x, const U &y) {
11 return x < y ? x = y, 1 : 0;
12 }
13
14 using LL = long long;
15 using PII = std::pair<int, int>;
16
17 constexpr int N(2.5e5 + 5);
18
19 using T = LL;
20 struct Edge {
21 int x, y; T z;
22 };
23 struct Heap {
```

```
24
     struct Node {
       int ls, rs, h, v;
25
26
       Tw;
     } t[N * 40];
27
28
     int cnt;
29
     int newNode(int v, T w) {
       t[++cnt] = \{0, 0, 1, v, w\};
31
        return cnt;
32
33
     int merge(int x, int y) {
34
       if (!x) return y;
35
        if (!y) return x;
36
        if (t[x].w > t[y].w) std::swap(x, y);
37
        t[++cnt] = t[x], x = cnt;
38
        t[x].rs = merge(t[x].rs, y);
39
        if (t[t[x].ls].h < t[t[x].rs].h) std::swap(t[x].ls, t[x].rs);
40
        t[x].h = t[t[x].rs].h + 1;
41
        return x;
42
     }
43 } h;
44
45
46 std::vector<T> kShortestPath(int n, int k, int s, int t, const std::vector<Edge>
&e) {
47
     int m = e.size();
     std::vector<int> deg(n + 1), g(m);
      for (auto \&[x, y, z] : e) deg[y]++;
49
50
      for (int i = 1; i \le n; i++) deg[i] += deg[i - 1];
51
     for (int i = 0; i < m; i++) g[--deg[e[i].y]] = i;
52
53
     std::vector<T> d(n, -1);
54
     std::vector<int> fa(n, -1), p;
55
56
     using Q = std::pair<T, int>;
57
     std::priority_queue<Q, std::vector<Q>, std::greater<Q>> q;
58
59
     {
60
        p.reserve(n);
61
        d[t] = 0, q.push(\{0, t\});
62
63
        std::vector<bool> vis(n);
64
        while (!q.empty()) {
65
         int x = q.top().second;
66
          q.pop();
67
          if (vis[x]) continue;
68
          vis[x] = true;
69
          p.push back(x);
70
          for (int i = deg[x]; i < deg[x + 1]; i++) {
71
            auto &[y, _, z] = e[g[i]];
72
            if (d[y] == -1 \mid \mid d[y] > d[x] + z) {
73
              d[y] = d[x] + z, fa[y] = g[i];
74
              q.push({d[y], y});
75
            }
76
          }
77
       }
78
     }
```

```
79
80
     if (d[s] == -1) std::vector<T>(k, -1);
81
     std::vector<int> heap(n);
82
     h.cnt = 0;
     for (int i = 0; i < m; i++) {
83
84
        auto \&[x, y, z] = e[i];
85
        if (d[x] != -1 \&\& d[y] != -1 \&\& fa[x] != i) {
86
          heap[x] = h.merge(heap[x], h.newNode(y, d[y] + z - d[x]));
87
88
     }
89
90
     for (int x : p) {
91
       if (x != t) heap[x] = h.merge(heap[x], heap[e[fa[x]].y]);
92
93
94
     if (heap[s]) q.push({d[s] + h.t[heap[s]].w, heap[s]});
95
     std::vector<T> res = {d[s]};
96
97
     for (int i = 1; i < k \&\& !q.empty(); i++) {
98
        auto [w, o] = q.top();
99
        q.pop();
100
101
         res.push back(w);
102
103
        int j = h.t[o].v;
         if (heap[j]) q.push({w + h.t[heap[j]].w, heap[j]});
105
         for (auto s : {h.t[o].ls, h.t[o].rs}) {
106
           if (s) q.push({w + h.t[s].w - h.t[o].w, s});
107
         }
108
109
      res.resize(k, -1);
110
      return res;
111 }
112
113 int a[N];
114 void solve() {
115
      int n, k;
116
      std::cin >> n >> k;
117
118
      std::vector<Edge> e;
119
      for (int i = 1; i <= n; i++) {
120
         std::cin >> a[i];
121
      }
122
      e.push_back({0, 1, a[1]});
123
      for (int i = 2; i \le n; i++) {
124
         if (i - 3 > 0) e.push_back(\{i - 3, i, a[i]\});
125
         e.push_back({i - 2, i, a[i]});
126
        e.push_back({i - 1, i, a[i]});
127
128
      if (n - 1 \ge 1) e.push_back(\{n - 1, n + 1, 0\});
129
       e.push_back(\{n, n + 1, 0\});
130
131
      auto res = kShortestPath(n + 2, k, 0, n + 1, e);
132
      for (auto x : res) std::cout << x << "\n";</pre>
133
134 }
```

```
135
136 int main() {
      // freopen("t.in", "r", stdin);
137
138
139
      std::ios::sync_with_stdio(false);
140
      std::cin.tie(nullptr);
141
142
     int t = 1;
143
144
      // std::cin >> t;
145
146
     while (t--) {
147
        solve();
148
      }
149
      return 0;
150 }
lca(o1)
1 #define int long long
2 const int maxn=1e5+10;//注意开两倍大小的空间 在 dp 上
3 vector<pair<int,int>>ve[maxn];
4 int dep[maxn];
5 pair<int,int>dp[21][maxn*3];
6 int red[maxn],d[maxn];
7 int Dep[maxn];
8 int dfn[maxn];
9 void dfs(int x,int fa,int l,int dis)
10 {
11
       if(red[x])dis=0;
12
       d[x]=dis;
13
   dep[x]=dep[fa]+1;
14
    Dep[x]=Dep[fa]+l;
15
       for(auto [it,len]:ve[x])
16 {
17
       if(it==fa) continue;
18
      dfs(it,x,len,dis+len);
19
   }
20 }
21 vector<int> sp;
22 void dfs2(int u, int fa)
23 {
24
25
       dfn[u] = sp.size();
26
       sp.push_back(u);
27
       for (auto& e : ve[u])if(e.first!=fa)
28
       {
29
           int& v = e.first;
30
           dfs2(v, u);
31
           sp.push_back(u);
32
       }
33 }
34 void initrmq()
35 {
36
       int n = sp.size();
37
       for (int i = 0; i < n; i++) dp[0][i] = {dfn[sp[i]], sp[i]};
38
       for (int i = 1; (1 << i) <= n; i++)
```

```
39
            for (int j = 0; j + (1 << i) - 1 < n; j++)
40
                dp[i][j] = min(dp[i - 1][j], dp[i - 1][j + (1 << (i - 1))]);
41 }
42 int lca(int u, int v)
43 {
44
        int l = dfn[u], r = dfn[v];
45
        if (l > r) swap(l, r);
        int k = _lg(r-l+1);
46
        return min(dp[k][l], dp[k][r - (1 << k) + 1]).second;
47
48 }
maxflow 只算值版本
1 struct dinic{
2
       struct E{
3
           int to,cap,inv;
4
      };
5
      vector <E> g[N];
6
      int dis[N],now[N];
7
      void addedge(int u,int v,int w){
8
           g[u].push_back({v,w,(int)g[v].size()});
9
           g[v].push_back({u,0,(int)g[u].size()-1});
10
        }
11
        void bfs(int st){
12
            queue<int>q;
13
            memset(dis,0,sizeof dis);
14
            q.push(st);dis[st]=1;
15
            while(q.size()){
16
                int u=q.front();q.pop();
17
                for(auto &[v,w,inv]:g[u]){
18
                    if(w\&\&!dis[v]){
19
                        dis[v]=dis[u]+1;
20
                        q.push(v);
21
                    }
22
                }
23
            }
24
25
        int dfs(int u,int t,int flow){
26
            if(u==t)return flow;
27
            for(int &i=now[u],sz=g[u].size(),d;i<sz;i++){</pre>
28
                auto &[v,w,inv]=g[u][i];
29
                if(w&&dis[v]>dis[u]){
30
                    d=dfs(v,t,min(flow,w));
31
                    if(d>0){
32
                        w-=d;
33
                        g[v][inv].cap+=d;
34
                         return d;
35
                    }
36
                }
37
            }
38
            return 0;
39
        }
40
        int maxflow(int st,int ed){
41
            for(int flow=0, res;;){
42
                bfs(st);
43
                if(!dis[ed])return flow;
44
                memset(now,0,sizeof now);
```

```
45
                while((res=dfs(st,ed,inf))>0){
46
                    flow+=res;
47
                }
48
            }
49
       }
50 };
maxflow 网络流最大流
1 // 用 givest 定源点汇点
2 // addedge 一次加了正反两条边
3 // init 慎用
4 // S必须是 0
5 // 输出方案注意是 head 开头
6 #include <bits/stdc++.h>
7 using namespace std;
8 const int N=2510, M=2510*10;
9 class Maxflow{
10 private:
int nedge=1,p[2*M],nex[2*M],head[N],c[2*M],cur[2*M];
12
       int dist[2*N];
13
        int S,T;
14
    void Addedge(int a,int b,int v){
15
      p[++nedge]=b;nex[nedge]=head[a];head[a]=nedge;
16
      c[nedge]=v;
17
18
       bool bfs(){
19
       queue<int>q;
20
       for(int i=S;i<=T;i++)dist[i]=-1;</pre>
21
      dist[S]=0;q.push(S);
22
      while(!q.empty()){
23
         int now=q.front();q.pop();
24
         for(int k=head[now]; k; k=nex[k])if(dist[p[k]]==-1\&\&c[k]>0){
25
           dist[p[k]]=dist[now]+1;
26
            q.push(p[k]);
27
          }
28
29
        return dist[T]>-1;
30
31
     int dfs(int x,int low){
32
       if(x==T) return low;
33
       if(low==0)return 0;
34
       int used=0;
35
        for(int &k=cur[x];k;k=nex[k])if(dist[p[k]]==dist[x]+1&&c[k]>0){
36
          int a=dfs(p[k],min(c[k],low-used));
37
          c[k] -= a; c[k^1] += a; used += a;
38
        if(low==used)break;
39
40
       if(used==0)dist[x]=-1;
41
      return used;
42
43 public:
44
     void init(int s,int t){
45
        for(int i=S;i<=T;i++)head[i]=0;</pre>
46
       S=s, T=t;
47
      nedge=1;
48
    }
```

```
49
       void addedge(int a,int b,int v){
50
            Addedge(a,b,v);
51
            Addedge(b,a,0);
52
53
     int dinic(){
54
      int flow=0;
55
       while(bfs()){
56
          for(int i=S;i<=T;i++)cur[i]=head[i];</pre>
57
         flow+=dfs(S, 1e9);
58
       }
59
        return flow;
60
   }
61 };
tarjan 缩点
1 stack<int>s;
2 vector<int>ve[maxn];
3 int col[maxn],num,dfn[maxn],low[maxn],dfstime;
4 void tarjan(int u)
5 {
6
       s.push(u);
7
      dfn[u]=low[u]=++dfstime;
8
       for(auto v:ve[u])
9
       {
10
            if(!dfn[v])
11
            {
12
                tarjan(v);
13
                low[u]=min(low[u],low[v]);
14
15
            else if(!col[v]) low[u]=min(low[u],dfn[v]);
16
       }
17
       if(dfn[u]==low[u])
18
19
            col[u]=++num;
20
           while(s.top()!=u)
21
            {
22
                col[s.top()]=num;
23
                s.pop();
24
            }
25
            s.pop();
26
       }
27 }
二分图匹配
1 #include <bits/stdc++.h>
2 using namespace std;
3 int const N = 1510 * 4, M = 75010;
4 int e[M], ne[M], h[N], idx;
5 int n, m, k, match[N], backup[N], st[N];
6 void add(int a, int b) {
7
      e[idx] = b, ne[idx] = h[a], h[a] = idx++;
8 }
9 int find(int x) {
10
       for (int i = h[x]; \sim i; i = ne[i]) {
11
            int j = e[i];
12
            if (!st[j]) {
```

```
13
                st[j] = 1;
14
                if (!match[j] || find(match[j])) {
15
                    match[j] = x;
16
                    return 1;
17
                }
18
           }
19
        }
20
        return 0;
21 }
22 int main() {
23
        cin >> n >> m >> k;
        memset(h, -1, sizeof h);
24
25
        for (int i = 1, a, b; i \le k; ++i) {
            scanf("%d%d", &a, &b);
26
27
            add(a, b + n);
28
29
        int maxMatch = 0;
30
        for (int i = 1; i <= n; ++i) {
31
            memset(st, 0, sizeof st);
32
            if (find(i)) maxMatch++;
33
34
        cout<<maxMatch<<endl;</pre>
35
        return 0;
36 }
37
二分图最优匹配
1 #include<bits/stdc++.h>
2 using namespace std;
3 const int maxn=110;
4 int n, m;
5 int a[maxn][maxn];
6 int lx[maxn], ly[maxn], link[maxn];
7 bool vx[maxn], vy[maxn];
8 int dfs(int x)
9 {
10
        if(x==-1)return 0;
11
        vx[x] = 1;
12
        for (int i = 1; i \le n; i++)
13
14
            if (!vy[i] \&\& lx[x] + ly[i] == a[x][i])
15
            {
16
                vy[i] = 1;
17
                if (link[i] == -1 || dfs(link[i]))
18
                {
19
                    link[i] = x;
20
                    return 1;
21
                }
22
            }
23
        }
24
        return 0;
25 }
26 bool deal()
27 {
28
        memset(ly, 0, sizeof(ly));
29
        memset(lx, 0xf7, sizeof(lx));
```

```
30
       memset(link, -1, sizeof(link));
31
        for (int i = 1; i <= n; i++)
32
        {
33
            for (int j = 1; j \le n; j++)
34
                lx[i] = max(lx[i], a[i][j]);
35
       }
36
        for(int i = 1; i <= n; i++)
37
38
            while(1)
39
            {
40
                memset(vx, 0, sizeof(vx));
41
                memset(vy, 0, sizeof(vy));
42
                if (dfs(i)) break;
43
                int delta = 0x7f7f7f7f;
44
                for (int j= 1; j <= n; j++)
45
46
                    if (vx[j] == 1)
47
                        for(int k = 1; k \le n; k++)
48
                            if (vy[k] == 0) delta = min(delta, lx[j] + ly[k] - a[j]
[k]);
49
                }
50
                if (delta == 0x7f7f7f7f) return 0;
51
                for (int j= 1; j <= n; j++)
52
                    if (vx[j] == 1) lx[j] -= delta;
53
                for(int k = 1; k \le n; k++)
54
                    if (vy[k] == 1) ly[k] += delta;
55
            }
56
57
       return 1;
58 }
59 int main()
60 {
61
               (deal() == 1) {
62
               int ans = 0;
63
               for(int i = 1; i <= n; i++)
64
               {
65
                   ans += a[link[i]][i];
66
67
               cout << ans <<'\n';//取最小就把所有边权取负再跑
68
           }
       return 0;
69
70 }
二分图染色
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=1010;
4 int n,m;
5 vector<int>ve[maxn];
6 int col[maxn][maxn],ans[maxn*2];
7 void dfs(int x,int y,int c1,int c2)
8 {
9
       if(col[y][c1]){
10
            dfs(y,col[y][c1],c2,c1);
11
            col[x][c1]=y;
12
            col[y][c1]=x;
```

```
13
        }
14
        else {
15
            col[x][c1]=y;
16
            col[y][c1]=x;
17
            col[y][c2]=0;
18
        }
19 }
20
   map<pair<int,int>,int>ma;
21
   int main()
22 {
23
        ios::sync_with_stdio(false);
24
        cin.tie(0);
25
        cin>>n>>m;
26
        int anss=0;
27
        for(int i=1;i<=m;i++){</pre>
28
            int x,y;
29
            cin>>x>>y;
30
            ve[x].push_back(y);
31
            ma[\{x,y\}]=i;
32
            int c1=1, c2=1;
33
            while(col[x][c1])c1++;
34
            while(col[y][c2])c2++;
35
            anss=\max(\{c1,c2,anss\});
36
            if(c1>c2){
37
                 swap(x,y); swap(c1,c2);
38
            }
39
            if(c1==c2){
40
                 col[x][c1]=y;
41
                 col[y][c1]=x;
42
            }
43
            else{
44
                 dfs(x,y,c1,c2);
45
            }
46
        }
47
        cout<<anss<<"\n";</pre>
48
        for(int i=1;i<=n;i++){</pre>
49
            for(int j=1;j<=anss;j++)if(col[i][j])ans[ma[{i,col[i][j]}]]=j;</pre>
50
51
        for(int i=1;i<=m;i++)cout<<ans[i]<<"\n";</pre>
52
        return 0;
53 }
圆方树
1
       vector<vector<int>> e1(n);
2
       int cnt = n;
3
4
       int now = 0;
5
       vector<int> dfn(n, -1), low(n);
6
       vector<int> stk;
7
       function<void(int)> tarjan = [&](int u) {
8
           stk.push_back(u);
9
           dfn[u] = low[u] = now++;
10
            for (auto v : ve[u]) {
11
                 if (dfn[v] == -1) {
12
                     tarjan(v);
13
                     low[u] = min(low[u], low[v]);
```

```
14
                    if (low[v] == dfn[u]) {
15
                         e1.push_back({});
16
                         int x;
17
                         do {
18
                             x = stk.back();
19
                             stk.pop_back();
20
                             el[cnt].push back(x);
21
                         } while (x != v);
22
                         el[u].push_back(cnt);
23
                         ++cnt;
24
                    }
25
                } else {
26
                    low[u] = min(low[u], dfn[v]);
27
                }
28
            }
29
        };
30
        tarjan(0);
基环树
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=2e5+10;
4 /*
5 1 init
6 2 addedge
7 3 Get
8 */
9 struct Graph{
10
        vector<int>ve[maxn];
11
        int base[maxn],id[maxn];
12
        bool Incircle[maxn];
13
        vector<int> Circle;
14
        int len=0;
15
        int dep[maxn],f[21][maxn];
16
        int n;
17
        void init(int _n){
18
            n=_n;
19
            for(int i=1;i<=n;i++){</pre>
20
                for(int j=0;j<21;j++)f[j][i]=0;</pre>
21
                ve[i].clear();
22
                Incircle[i]=false;
23
                id[i]=-1;
24
                base[i]=i;
                Circle.clear();
25
26
                len=0;
27
                dep[i]=0;
28
            }
29
        }
30
        void addedge(int x,int y){
31
            ve[x].push_back(y);
32
            ve[y].push_back(x);
33
34
        void dfs(int x,int fa)
35
36
            base[x]=base[fa];
37
            dep[x]=dep[fa]+1;
```

```
38
            for(int i=0;i<=19;i++)</pre>
39
                 f[i+1][x]=f[i][f[i][x]];
40
            for(auto it:ve[x])
41
42
                 if(it==fa) continue;
43
                 f[0][it]=x;
44
                 dfs(it,x);
45
            }
46
47
        void Get(){
48
            vector<int> sta;
49
            vector<bool> vis(n+1,false);
50
            function<br/><br/>bool(int,int)> dfs2 = [\&](int x,int h){
51
                 vis[x]=true;
52
                 sta.push_back(x);
53
                 for(auto it:ve[x])if(it!=h){
54
                     if(vis[it]){
55
                         Circle.push_back(it);
56
                         while(!sta.empty()&&sta.back()!=it){
57
                             Circle.push_back(sta.back());
58
                              sta.pop_back();
59
                         }
60
                         return true;
61
                     }
62
                     else{
63
                         if(dfs2(it,x))return true;
64
                     }
65
                 }
66
                 sta.pop_back();
67
                 return false;
68
            };
            dfs2(1,0);
69
70
            len=(int)Circle.size();
71
            for(auto it:Circle)Incircle[it]=true;
72
            for(auto it:Circle){
73
                 for(auto it2:ve[it])if(!Incircle[it2]){
74
                     f[0][it2]=it;
75
                     dfs(it2,it);
76
                 }
77
78
            for(int i=0;i<len;i++)id[Circle[i]]=i;</pre>
79
80
        int lca(int x,int y)
81
        {
82
            if(dep[x]<dep[y]) swap(x,y);</pre>
83
            for(int i=20;i>=0;i--)
84
            {
85
                 if(dep[f[i][x]]>=dep[y]) x=f[i][x];
86
                 if(x==y) return x;
87
            }
88
            for(int i=20;i>=0;i--)
                 if(f[i][x]!=f[i][y])
89
90
                     x=f[i][x],y=f[i][y];
91
            return f[0][x];
92
        }
93
        int dis(int x,int y){
```

```
94
           if(base[x]==base[y]){
95
                int l=lca(x,y);
96
                return dep[x]+dep[y]-2*dep[l];
97
           }
98
           else{
99
                int g=(id[base[x]]-id[base[y]]+len)%len;
100
                 return dep[x]+dep[y]+min(g,len-g);
101
            }
102
        }
103 };
104 Graph g;
带权并查集 dsu
1 const int maxn=1e5+10;
2 int f[maxn],dis[maxn];
3 int getf(int x){
      if(x==f[x])return x;
5
      int z=getf(f[x]);
      dis[x] += dis[f[x]];
7
      return f[x]=z;
8 }
9 void unit(int i,int j,int len){
10
       int x=getf(i),y=getf(j);
11
       f[x]=y;
       //在赋值之前因为 x 是头节点所以 dis 一定等于 0
12
13
       dis[x]=dis[j]-dis[i]+len;
14 }
带花树
1 #include <bits/stdc++.h>
2 using namespace std;
3 struct blossom {//0base
4
      int n, vis t;
5
      vector<vector<int>> E;
6
      vector<int> match, label, org, vis, parent;
7
      queue<int> 0;
8
      blossom(int _n) {
9
          n = n;
10
           E = vector<vector<int>>(n, vector<int>());
11
           match.assign(n, -1);
12
           label.resize(n);
13
           org.resize(n);
14
            iota(org.begin(), org.end(), 0);
15
            parent.assign(n, -1);
16
           vis.assign(n, 0);
17
           vis_t = 0;
18
19
       void addEdge(int u, int v) {
20
           E[u].emplace back(v);
21
           E[v].emplace_back(u);
22
23
       auto lca(int v, int u) {
24
           vis_t++;
25
           while (true) {
26
                if (v != -1) {
27
                    if (vis[v] == vis_t) {
```

```
28
                         return v;
29
                    }
30
                    vis[v] = vis_t;
31
                     if (match[v] == -1) {
32
                         v = -1;
33
                    } else {
34
                         v = org[parent[match[v]]];
35
36
                }
37
                swap(v, u);
38
            }
39
        }
40
        void agument(int v) {
41
            while (v != -1) {
42
                auto pv = parent[v];
43
                auto nxt = match[pv];
44
                match[v] = pv;
45
                match[pv] = v;
46
                v = nxt;
47
            }
48
        }
49
        void flower(int v, int u, int a) {
50
            while (org[v] != a) {
51
                parent[v] = u;
52
                u = match[v];
                if (label[u] == 1) {
53
54
                    label[u] = 0;
55
                     Q.emplace(u);
56
                }
57
                org[v] = org[u] = a;
58
                v = parent[u];
59
            }
60
        }
61
        auto bfs(int root) {
62
            fill(label.begin(), label.end(), -1);
63
            iota(org.begin(), org.end(), 0);
64
            while (!Q.empty()) {
65
                Q.pop();
66
            }
67
            Q.emplace(root);
68
            label[root] = 0;
69
            while (!Q.empty()) {
70
                auto u = Q.front();
71
                Q.pop();
72
                for (auto v : E[u]) {
73
                     if (label[v] == -1) {
74
                         label[v] = 1;
75
                         parent[v] = u;
76
                         if (match[v] == -1) {
77
                             agument(v);
78
                             return true;
79
80
                         label[match[v]] = 0;
81
                         Q.push(match[v]);
82
                         continue;
83
                     } else if (label[v] == 0 && org[v] != org[u]) {
```

```
84
                        auto a = lca(org[u], org[v]);
85
                        flower(v, u, a);
86
                        flower(u, v, a);
87
                    }
88
                }
89
            }
90
            return false;
91
        }
92
        void solve() {
93
            for (int i = 0; i < n; ++i) {
94
                if (match[i] == -1) {
95
                    bfs(i);
96
                }
97
            }
98
       }
99 };
100 int main()
101 {
         blossom G(n);
102
         for (int i = 0; i < n; ++i) {
103
             for (int j = i + 1; j < n; ++j) {
105
                 auto [xi, yi] = stone[i];
106
                 auto [xj, yj] = stone[j];
107
                 if (abs(xi - xj) + abs(yi - yj) \le L) {
108
                     G.addEdge(i, j);
109
                 }
110
             }
111
112
        G.solve();
113
         int num = 0;
         for (int i = 0; i < n; ++i) {
114
             if (G.match[i] != -1) {
115
116
                 num++;
117
             }
118
        }
119 }
带负环最小费用最大流
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int N = 200 + 5, M = 2e4 + N;
4 struct flow {
    int cnt = 1, hd[N], nxt[M << 1], to[M << 1], limit[M << 1], cst[M << 1];
    void add(int u, int v, int w, int c) {
7
      nxt[++cnt] = hd[u], hd[u] = cnt, to[cnt] = v, limit[cnt] = w, cst[cnt] = c;
8
      nxt[++cnt] = hd[v], hd[v] = cnt, to[cnt] = u, limit[cnt] = 0, cst[cnt] = -c;
9
10
     int fl[N], fr[N], dis[N], in[N];
11
     pair<int, int> mincost(int s, int t) {
12
       int flow = 0, cost = 0;
13
       while (1) {
14
         queue<int> q;
15
         memset(dis, 0x3f, sizeof(dis));
16
         q.push(s), fl[s] = 1e9, dis[s] = 0;
17
         while (!q.empty()) {
18
            int t = q.front();
```

```
19
            q.pop(), in[t] = 0;
20
            for (int i = hd[t]; i; i = nxt[i]) {
21
              int it = to[i], d = dis[t] + cst[i];
22
              if (limit[i] && d < dis[it]) {</pre>
                dis[it] = d, fl[it] = min(fl[t], limit[i]), fr[it] = i;
23
24
                if (!in[it]) in[it] = 1, q.push(it);
25
              }
26
            }
27
28
          if (dis[t] > 1e9) return make_pair(flow, cost);
29
          flow += fl[t], cost += dis[t] * fl[t];
30
          for (int u = t; u != s; u = to[fr[u] ^ 1])
31
            limit[fr[u]] \stackrel{-=}{=} fl[t], limit[fr[u] ^ 1] += fl[t];
32
        }
33
     }
34 };
35 struct bounded_flow {
36
     int e, u[M], v[M], lo[M], hi[M], cst[M];
37
     void add(int _u, int _v, int w, int c) {
38
        if (c < 0) {
39
          u[++e] = u, v[e] = v, lo[e] = w, hi[e] = w, cst[e] = c;
40
          u[++e] = v, v[e] = u, lo[e] = 0, hi[e] = w, cst[e] = -c;
41
        } else
42
          u[++e] = u, v[e] = v, lo[e] = 0, hi[e] = w, cst[e] = c;
43
44
      flow q;
45
     pair<int, int> mincost(int n, int s, int t, int ss, int tt) {
46
        static int w[N];
47
        memset(w, 0, sizeof(w));
48
        int flow = 0, cost = 0, tot = 0;
49
        for (int i = 1; i \le e; i++) {
          w[u[i]] = lo[i], w[v[i]] += lo[i];
50
51
          cost += lo[i] * cst[i];
52
          g.add(u[i], v[i], hi[i] - lo[i], cst[i]);
53
54
        for (int i = 1; i \le n; i++)
55
          if (w[i] > 0)
56
            g.add(ss, i, w[i], 0), tot += w[i];
57
          else if (w[i] < 0)
58
            g.add(i, tt, -w[i], 0);
59
        g.add(t, s, 1e9, 0);
60
        pair<int, int> res = g.mincost(ss, tt);
61
        cost += res.second;
62
        flow += g.limit[g.hd[s]];
63
        g.hd[s] = g.nxt[g.hd[s]], g.hd[t] = g.nxt[g.hd[t]];
64
        res = g.mincost(s, t);
65
        return make pair(flow + res.first, cost + res.second);
66
     }
67 } f;
68 int n, m, s, t;
69 int main() {
70
     cin >> n >> m >> t;
71
     for (int i = 1; i \le m; i++) {
72
       int u, v, w, c;
73
        cin >> u >> v >> w >> c, f.add(u, v, w, c);
74
     }
```

```
pair<int, int> res = f.mincost(n, s, t, 0, n + 1);
75
76
     cout << res.first << " " << res.second << endl;</pre>
77
     return 0;
78 }
79
支配树
1 /*
2 1base
3 注意 up 是数组需要外界导入
4 使用的时候直接 dtree::即可
5 */
6 namespace dtree{
7
   const int MAXN = 200020;
8 vector<int> E[MAXN], RE[MAXN], rdom[MAXN];
9
10
     int S[MAXN], RS[MAXN], cs;
11
   int par[MAXN], val[MAXN], sdom[MAXN], rp[MAXN], dom[MAXN];
12
13
     void clear(int n) {
14
       cs = 0;
15
       for(int i=0;i<=n;i++) {</pre>
16
         par[i] = val[i] = sdom[i] = rp[i] = dom[i] = S[i] = RS[i] = 0;
17
        E[i].clear(); RE[i].clear(); rdom[i].clear();
18
19
     }
20
     void add_edge(int x, int y) { E[x].push_back(y); }
21
    void Union(int x, int y) { par[x] = y; }
22 int Find(int x, int c = 0) {
23
      if(par[x] == x) return c ? -1 : x;
24
      int p = Find(par[x], 1);
25
      if(p == -1) return c ? par[x] : val[x];
26
       if(sdom[val[x]] > sdom[val[par[x]]]) val[x] = val[par[x]];
27
      par[x] = p;
28
       return c ? p : val[x];
29
    }
30
     void dfs(int x) {
31
       RS[S[x] = ++cs] = x;
32
      par[cs] = sdom[cs] = val[cs] = cs;
33
      for(int e : E[x]) {
34
         if(S[e] == 0) dfs(e), rp[S[e]] = S[x];
35
        RE[S[e]].push back(S[x]);
36
37
     }
38
     int solve(int s, int *up) {//s 是起点
39
       dfs(s);
40
       for(int i=cs;i;i--) {
         for(int e : RE[i]) sdom[i] = min(sdom[i], sdom[Find(e)]);
41
42
         if(i > 1) rdom[sdom[i]].push_back(i);
43
         for(int e : rdom[i]) {
44
          int p = Find(e);
45
          if(sdom[p] == i) dom[e] = i;
46
          else dom[e] = p;
47
48
         if(i > 1) Union(i, rp[i]);
49
      }
```

```
50
        for(int i=2;i<=cs;i++) if(sdom[i] != dom[i]) dom[i] = dom[dom[i]];</pre>
51
       for(int i=2;i<=cs;i++) up[RS[i]] = RS[dom[i]];</pre>
52
       return cs;
53 }
54 }
最小环
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=1e2+10;
4 const int inf=2e7+10;
5 int a[maxn][maxn],b[maxn][maxn];
6 int main()
7 {
8
       int n;cin>>n;
9
       int m;cin>>m;
10
        for(int i=1;i<=n;i++){</pre>
11
            for(int j=1;j<=n;j++)a[i][j]=b[i][j]=inf;</pre>
12
            a[i][i]=b[i][i]=0;
13
        }
14
        while(m--){
15
            int x,y;cin>>x>>y;
16
            int w;cin>>w;
17
            a[x][y]=min(a[x][y],w);
18
            a[y][x]=min(a[y][x],w);
19
            b[x][y]=min(b[x][y],w);
20
            b[y][x]=min(b[y][x],w);
21
22
        int ans=inf;
23
        for(int i=1;i<=n;i++){</pre>
24
            for(int j=1;j<i;j++){</pre>
25
                for(int k=j+1; k<i; k++){</pre>
26
                     ans=min(ans,a[i][j]+a[i][k]+b[j][k]);
27
                }
28
29
            for(int j=1; j<=n; j++){</pre>
30
                 for(int k=1;k<=n;k++)b[j][k]=min(b[j][i]+b[i][k],b[j][k]);</pre>
31
32
        }
33
        if(ans==inf)cout<<"No solution.";</pre>
34
        else cout<<ans;</pre>
35 }
最小费用最大流
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int N=1e4,M=1e6;
4 struct SSP {
5
       int cnt = 1, hd[N], nxt[M << 1], to[M << 1], limit[M << 1], cst[M << 1];
       void init(){
7
           memset(hd,0,sizeof(hd));
8
           cnt=1;
9
       }
10
        // w limit c cost
11
        void add(int u, int v, int w, int c) {
            nxt[++cnt] = hd[u], hd[u] = cnt, to[cnt] = v, limit[cnt] = w, cst[cnt] = c;
12
```

```
13
           nxt[++cnt] = hd[v], hd[v] = cnt, to[cnt] = u, limit[cnt] = 0, cst[cnt] = -
c;
14
       }
15
       int fr[N], fl[N], in[N], dis[N];
16
17
18
       pair<int, int> min cost(int s, int t) {
19
            int flow = 0, cost = 0;
20
           while (true) { // SPFA
21
                queue<int> q;
22
                memset(dis, 0x3f, sizeof(dis));
23
                memset(in, 0, sizeof(in));
24
                fl[s] = 1e9, dis[s] = 0, q.push(s);
25
                while (!q.empty()) {
26
                    int cur = q.front();
27
                    q.pop(), in[cur] = 0;
28
                    for (int i = hd[cur]; i; i = nxt[i]) {
29
                        int it = to[i], d = dis[cur] + cst[i];
30
                        if (limit[i] && d < dis[it]) {</pre>
31
                            fl[it] = min(limit[i], fl[cur]), fr[it] = i, dis[it] = d;
32
                            if (!in[it]) in[it] = 1, q.push(it);
33
                        }
34
                    }
35
                }
36
                if (dis[t] > 1e9) return {flow, cost};//改成>0 就是可行流
37
                flow += fl[t], cost += dis[t] * fl[t];
38
                  for (int u = t; u != s; u = to[fr[u] ^ 1]) limit[fr[u]] -= fl[t],
limit[fr[u] ^ 1] += fl[t];
39
           }
40
41 } Sol;
欧拉回路
1 #include<bits/stdc++.h>
2 using namespace std;
3 const int M=2333, N=666;
4 struct edge
5 {
6 int nxt,to;
7 \}e[M<<1];
8 int head[N],tot=1;
9 int cut[M<<1];</pre>
10 void add(int u,int v)
11 {
12
     e[++tot]=(edge){head[u],v},head[u]=tot;
13
     e[++tot]=(edge){head[v],u},head[v]=tot;
14 }
15 vector<int> st;
16 void dfs(int u)//欧拉回路
17 {
18
       for(int i=head[u];i!=0;i=e[i].nxt)
19
20
           if(cut[i]) continue;
21
           int v=e[i].to;
22
           cut[i]=cut[i^1]=1;
23
           dfs(v);
```

```
24 }
25 st.push(u);
26 }
27 int main()
28 {
29
30
31 return 0;
32 }
33
```

数据结构

SegmentSet

```
1 /*
2 every pair of pair<int,int> will not intersect
3 if i is true then it will be in the set
5 struct SegmentSet{
6
       set<pair<int,int>>s;
7
       void write(){
           for(auto [x,y]:s)cout<<x<"/"<<y<" ";;cout<<"\n";</pre>
8
9
10
        //make l...r to be true
11
        void insert(int l,int r)
12
        {
13
            int L=l,R=r;
14
            auto it=s.lower_bound(make_pair(L,(int)-2e9));
15
            while(it!=s.end()&&it->first<=R+1){</pre>
16
                R=max(it->second,R);
17
                it=s.erase(it);
18
            }
19
            if(it!=s.begin()){
20
                it--;
21
                if(it->second+1>=L){
22
                    L=min(L,it->first);
23
                    R=max(R,it->second);
24
                     s.erase(it);
25
                }
26
            }
27
            s.insert(make_pair(L,R));
28
29
        // if l...r all true return false
        bool query_no_full(int l,int r){
30
31
            auto it=s.lower_bound(make_pair(l,(int)-2e9));
32
            if(it!=s.end()){
33
                if(l==it->first&&r<=it->second)return false;
34
35
            if(it!=s.begin()){
36
                it--;
37
                if(it->second>=r)return false;
38
            }
39
            return true;
40
41
        //make l...r to be false
42
        void del(int l,int r){
            auto it=s.lower_bound(make_pair(l,(int)-2e9));
43
44
            while(it!=s.end()&&it->first<=r){</pre>
45
                if(it->second<=r){</pre>
46
                     it=s.erase(it);continue;
47
                }
48
                int R=it->second;
49
                s.erase(it);
50
                s.insert(make_pair(r+1,R));
51
                break;
52
            it=s.lower_bound(make_pair(l,(int)-2e9));
```

```
54
            if(it!=s.begin()){
55
56
                int L=it->first,R=it->second;
57
                if(R>=l){
58
                    s.erase(it);
59
                    if(L<=l-1)s.insert(make_pair(L,l-1));</pre>
60
                    if(R>=r+1)s.insert(make pair(r+1,R));
61
                }
62
            }
63
        }
64
        // if l...r all false return false
        bool query_at_least_one(int l,int r){
65
66
            auto it=s.lower_bound(make_pair(l,(int)-2e9));
67
            if(it!=s.end()){
68
                if(it->first<=r)return true;</pre>
69
            if(it!=s.begin()){
70
71
                it--;
72
                if(it->second>=l)return true;
73
            }
74
            return false;
75
        }
76 };
SegmentTree
1 //????????? ???????>=??sum??????
2 #include <bits/stdc++.h>
3 using namespace std;
4 const int maxn=1e6+10;
5 struct Node{
6
       int l,r,res,tag;
7 };
8 struct SegmentTree{
9
       Node a[maxn*4];
10
        void tag_init(int i){
11
            a[i].tag=0;
12
        }
13
        void tag_union(int fa,int i){
14
            a[i].tag+=a[fa].tag;
15
16
        void tag_cal(int i){
17
            a[i].res+=a[i].tag*(a[i].r-a[i].l+1);
18
        }
19
        void pushdown(int i){
20
            tag cal(i);
21
            if(a[i].l!=a[i].r){
22
                tag_union(i,i*2);
23
                tag_union(i,i*2+1);
24
            }
25
            tag init(i);
26
        }
        void pushup(int i){
27
28
            if(a[i].l==a[i].r)return;
29
            pushdown(i*2);
30
            pushdown(i*2+1);
31
            a[i].res=a[i*2].res+a[i*2+1].res;
```

```
32
        }
33
        void build(int i,int l,int r){
34
            a[i].l=l,a[i].r=r;tag_init(i);
35
            if(l>=r)return;
36
            int mid=(l+r)/2;
37
            build(i*2,l,mid);
38
            build(i*2+1, mid+1, r);
39
40
        void update(int i,int l,int r,int w){
41
            pushdown(i);
42
            if(a[i].r<l||a[i].l>r||l>r)return;
43
            if(a[i].l>=l\&\&a[i].r<=r){
44
                a[i].tag=w;
45
                 return;
46
            }
47
            update(i*2,l,r,w);
48
            update(i*2+1,l,r,w);
49
            pushup(i);
50
        }
51
        int query(int i,int l,int r){
52
            pushdown(i);
53
            if(a[i].r<l||a[i].l>r||l>r)return 0;
54
            if(a[i].l>=l\&\&a[i].r<=r){
55
                 return a[i].res;
56
            }
57
            return query(i*2,l,r)+query(i*2+1,l,r);
58
        }
59
        int min_right(int qL, int& nowsum,int querysum, int i) {//???????>=sum???
60
            pushdown(i);
61
            if (a[i].r < qL)return -1;</pre>
62
            if (qL <= a[i].l) {</pre>
63
                int ss = nowsum+a[i].res;
64
                if (ss<querysum) {</pre>
65
                     nowsum = ss;
66
                     return -1;
67
                }
68
                if (a[i].l == a[i].r)return a[i].l;
69
70
            int pos = min_right(qL, nowsum,querysum,i*2);
71
            if (pos != -1)return pos;
72
            return min_right(qL, nowsum,querysum,2*i+1);
73
74
        int max_left(int qR,int &nowsum,int querysum,int i){//???????>=sum???
75
            pushdown(i);
76
            if(a[i].l > qR)return -1;
77
            if(qR>=a[i].r){
78
                 int ss=nowsum+a[i].res;
79
                if(ss<querysum){</pre>
80
                     nowsum=ss;
81
                     return -1;
82
                }
83
                if(a[i].l==a[i].r)return a[i].r;
84
            }
85
            int pos=max left(qR,nowsum,querysum,i*2+1);
86
            if(pos!=-1)return pos;
87
            return max_left(qR,nowsum,querysum,i*2);
```

```
88
        }
89 };
90 SegmentTree tri;
91 int main()
92
93
        ios::sync_with_stdio(false);
94
        cin.tie(0);
95
        int n,q;cin>>n>>q;
96
        tri.build(1,1,n);
97
        for(int i=1;i<=n;i++){</pre>
98
            int x;cin>>x;tri.update(1,i,i,x);
99
        }
100
         while(q--){
101
             int ops;cin>>ops;
102
             if(ops==1){
103
                  int l,r,x;cin>>l>>r>>x;
                  tri.update(1,l,r,x);
104
105
             }
106
             if(ops==2){
107
                  int l,r;cin>>l>>r;
108
                  cout<<tri.query(1,l,r)<<"\n";</pre>
109
             }
110
             if(ops==3){
111
                  int x,sum;cin>>x>>sum;
112
                  int nowsum=0;
113
                  cout<<tri.min_right(x,nowsum,sum,1)<<"\n";</pre>
114
             }
115
             if(ops==4){
116
                  int x,sum;cin>>x>>sum;
117
                  int nowsum=0;
118
                  cout<<tri.max_left(x,nowsum,sum,1)<<"\n";</pre>
119
             }
120
         }
121 }
122
三维偏序 cdq
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=4e5+10;
4 struct Treearray{
5
       int c[maxn],n;
6
       void set_n(int _n){
7
           n=_n;
8
           for(int i=1;i<=n;i++)c[i]=0;</pre>
9
       }
10
        int lowbit(int x){
11
            return x&(-x);
12
13
        void update(int i,int k){
                                      //在i位置加上k
14
            while(i \leq n){
15
                c[i] += k;
16
                 i += lowbit(i);
17
            }
18
        }
19
        int getsum(int i){
                                   //求A[1 - i]的和
```

```
20
            int res = 0;
21
            while(i > 0){
22
                 res += c[i];
23
                 i -= lowbit(i);
24
25
            return res;
26
        }
27 };
28 Treearray tri;
29 int a[maxn],b[maxn],c[maxn];
30 int n,k;
31 int ans[maxn],id[maxn],cnt[maxn],t[maxn];
32 void subdiv(int l,int r){
33
        if(l==r)return;
34
        int mid=(l+r)/2;
35
        subdiv(l,mid);
36
        subdiv(mid+1, r);
37
        sort(id+l,id+mid+1,[&](int x,int y){
38
            if(b[x]==b[y])return c[x]<c[y];</pre>
39
            return b[x]<b[y];</pre>
40
        });
41
        sort(id+mid+1,id+r+1,[&](int x,int y){
42
            if(b[x]==b[y])return c[x]<c[y];</pre>
43
            return b[x]<b[y];</pre>
44
        });
45
46
        // for(int i=l;i<=r;i++)cout<<id[i]<<" \n"[i==r];
47
        assert(tri.getsum(tri.n)==0);
48
        for(int i=l,j=mid+1;i<=mid||j<=r;){</pre>
49
            if(j!=r+1&&(i==mid+1||b[id[i]]>b[id[j]])){
50
                 // cout<<"id="<<id[j]<<" +"<<tri.getsum(c[id[j]])<<"\n";
51
                 ans[id[j]]+=tri.getsum(c[id[j]]);
52
                 j++;
53
            }
54
            else{
                 tri.update(c[id[i]],t[id[i]]);
55
56
                 i++;
57
            }
58
        }
59
        for(int i=l;i<=mid;i++)tri.update(c[id[i]],-t[id[i]]);</pre>
60 }
61 int main()
62 {
63
        ios::sync_with_stdio(false);
64
        cin.tie(0);
65
        cin>>n>>k;
        tri.set n(200000);
66
67
        vector<tuple<int,int,int>> v(n);
68
        for(int i=0;i<n;i++){</pre>
69
            int x,y,z;cin>>x>>y>>z;v[i]=make_tuple(x,y,z);
70
71
        sort(v.begin(),v.end());
72
        int g=0;
73
        for(int i=0;i<n;i++){</pre>
74
            int j=i;
75
            while(j+1<n&v[i]==v[j+1])j++;
```

```
76
            g++;
77
            a[g]=get<0>(v[i]);
78
            b[g]=get<1>(v[i]);
79
            c[g]=get<2>(v[i]);
80
            t[g]=j-i+1;
81
            i=j;
82
            // cout<<"g="<<g<<" "<<a[g]<<" "<<b[g]<<" "<<c[g]<<"\n";
83
84
        for(int i=1;i<=q;i++)id[i]=i;</pre>
85
        subdiv(1,g);
86
        for(int i=1;i<=g;i++){</pre>
87
            cnt[ans[i]+t[i]-1]+=t[i];
88
            // cout<<"i="<<i<" ans="<<ans[i]<<"\n";
89
        }
90
        for(int i=0;i<n;i++)cout<<cnt[i]<<"\n";</pre>
91
        return 0;
92 }
93
主席树
1 //注意 Sum 和 cnt 的区别
2 #include <bits/stdc++.h>
3 using namespace std;
4 const int maxn = 1e5; // 数据范围
5 int n, m;
6 struct Persistent_SegmentTree
7 {
8
       int sum[(maxn << 5) + 10], root[maxn + 10], lch[(maxn << 5) + 10],
9
           rch[(maxn << 5) + 10], cnt[(maxn<<5)+10];
        int tot = 0;
10
11
        void init()
12
        {
13
            tot = 0;
14
        }
15
        int a[maxn + 10];
16
        void update(int &rot, int pr, int L, int R, int k)
17
        { // 插入操作
18
            rot = ++tot;
19
            lch[rot] = lch[pr];
20
            rch[rot] = rch[pr];
21
            sum[rot] = sum[pr] + k;
22
            cnt[rot] = cnt[pr] + 1;
23
            if (L == R)
24
                return;
25
            int mid = (L + R) \gg 1;
            if (k \le mid)
26
27
                update(lch[rot], lch[pr], L, mid,k);
28
            else
29
                update(rch[rot], rch[pr], mid + 1, R,k);
30
        }
        int getcnt(int s, int t, int L, int R, int l, int r) // s,t为root[l],root[r]的
根节点 中所有大小在[l,r]之间数字出现次数
32
        {
33
            if (l <= L && R <= r)
34
                return cnt[t] - cnt[s];
35
            int res = 0;
```

```
36
            int mid = (L + R) \gg 1;
37
            if (l <= mid)</pre>
38
                res += getcnt(lch[s], lch[t], L, mid, l, r);
39
            if (r > mid)
40
                res += getcnt(rch[s], rch[t], mid + 1, R, l, r);
41
            return res;
42
       }
43
44
        int getsum(int s, int t, int L, int R, int l, int r) // s,t为root[l],root[r]的
根节点 中所有大小在[l,r]之间数字的和
45
            if (l <= L && R <= r)
46
47
                return sum[t] - sum[s];
48
            int res = 0;
49
            int mid = (L + R) \gg 1;
50
            if (l <= mid)
51
                res += getsum(lch[s], lch[t], L, mid, l, r);
52
            if (r > mid)
53
                res += getsum(rch[s], rch[t], mid + 1, R, l, r);
54
            return res;
55
       }
56
       int get_Kth_min_Sum(int s,int t,int l,int r,int k,int &nowsum,int &ans){//return
第k小的值
57
            int ss = nowsum+cnt[t]-cnt[s];
58
            if (ss<k) {
59
                nowsum = ss;
60
                ans+=sum[t]-sum[s];
61
                return -1;
62
            }
63
            if (l == r){
64
                ans+=(k-nowsum)*l;
65
                return l;
66
            }
67
            int mid=(l+r)/2;
68
            int pos = get_Kth_min_Sum(lch[s],lch[t],l,mid,k,nowsum,ans);
69
            if (pos != -1)return pos;
70
            return get_Kth_min_Sum(rch[s],rch[t],mid+1,r,k,nowsum,ans);
71
72
       int get_Kth_max_Sum(int s,int t,int l,int r,int k,int &nowsum,int &ans){//return
第k大的值
73
            int ss = nowsum+cnt[t]-cnt[s];
74
            if (ss<k) {
75
                nowsum = ss;
76
                ans+=sum[t]-sum[s];
77
                return -1;
78
            if (l == r){
79
80
                ans+=(k-nowsum)*l;
81
                return l;
82
            }
83
            int mid=(l+r)/2;
84
            int pos = get Kth max Sum(rch[s],rch[t],mid+1,r,k,nowsum,ans);
85
            if (pos != -1)return pos;
86
            return get_Kth_max_Sum(lch[s],lch[t],l,mid,k,nowsum,ans);
87
        }
88
        int get_upper(int s,int t,int l,int r,int x){//第一个大于等于 x 的数
```

```
89
            if (r < x) return -1;
            if (x <= 1) {</pre>
90
91
                int ss = cnt[t]-cnt[s];
92
                if (ss==0) {
93
                     return -1;
94
                }
95
                if (l == r)return l;
96
            }
97
            int mid=(l+r)/2;
98
            int pos = get_upper(lch[s],lch[t],l,mid,x);
99
            if (pos != -1)return pos;
100
             return get_upper(rch[s],rch[t],mid+1,r,x);
101
102
         int get lower(int s,int t,int l,int r,int x){//第一个小于等于 x 的数
103
             if(l > x)return -1;
104
             if(x>=r){
105
                  int ss=cnt[t]-cnt[s];
106
                  if(ss==0){
107
                      return -1;
108
                 }
109
                  if(l==r)return r;
110
             }
             int mid=(l+r)/2;
111
112
             int pos=get_lower(rch[s],rch[t],mid+1,r,x);
113
             if(pos!=-1)return pos;
114
             return get_lower(lch[s],lch[t],l,mid,x);
115
         }
116 };
117 Persistent_SegmentTree tri;
118 int main()
119 {
120
         int n,q;
121
         cin >> n >> q;
122
123
         for (int i = 1; i <= n; i++)
124
         {
125
             int x;
126
             cin >> x;
127
             tri.update(tri.root[i], tri.root[i - 1], 1, n, x);
128
             assert (1 \le x \& x \le n);
129
         }
130
         while (q--)
131
         {
132
             int ops;cin>>ops;
133
             int l,r,k,L,R;
             if(ops==1){
134
135
                  cin>>l>>r>>L>>R;
136
                  cout<<tri.getsum(tri.root[l-1],tri.root[r],1,n,L,R)<<"\n";</pre>
137
             }
138
             if(ops==2){// get kth max no output -1
139
                 cin>>l>>r>>k;
140
                  int nowsum=0,ans=0;
141
cout<<tri.get Kth max Sum(tri.root[l-1],tri.root[r],1,n,k,nowsum,ans)<<"\n";</pre>
142
             }
143
             if(ops==3){// get kth max sum siz<k return allsum</pre>
```

```
144
                 cin>>l>>r>>k;
145
                 int nowsum=0,ans=0;
146
                 tri.get_Kth_max_Sum(tri.root[l-1],tri.root[r],1,n,k,nowsum,ans);
                 cout<<ans<<"\n";
147
148
             }
149
             if(ops==4){// get kth min no output -1
150
                 cin>>l>>r>>k;
151
                 int nowsum=0,ans=0;
152
cout<<tri.get_Kth_min_Sum(tri.root[l-1],tri.root[r],1,n,k,nowsum,ans)<<"\n";</pre>
153
154
             if(ops==5){// get kth min sum siz<k return allsum</pre>
155
                 cin>>l>>r>>k;
156
                 int nowsum=0,ans=0;
157
                 tri.get_Kth_min_Sum(tri.root[l-1],tri.root[r],1,n,k,nowsum,ans);
158
                 cout<<ans<<"\n";
159
             }
160
             if(ops==6){// get the min element >= k no return -1
161
                 cin>>l>>r>>k;
                 cout<<tri.get_upper(tri.root[l-1],tri.root[r],1,n,k)<<"\n";</pre>
162
163
             }
164
             if(ops==7){// get the max element <= k no return -1
165
                 cin>>l>>r>>k;
166
                 cout<<tri.get lower(tri.root[l-1],tri.root[r],1,n,k)<<"\n";</pre>
167
             }
168
         }
169 }
二维树状数组
1 const int maxn=1010;
2 struct treearray{
3
       int mkp1[maxn][maxn],mkp2[maxn][maxn],mkp3[maxn][maxn],mkp4[maxn][maxn];
4
       inline int lowbit(int x)
5
6
           return x&(-x);
7
       }
8
       inline void Update(int x,int y,int k)
9
       {
10
            for(int i=x;i<=n;i+=lowbit(i))</pre>
11
12
                for(int j=y;j<=m;j+=lowbit(j))</pre>
13
                {
14
                    mkp1[i][j]+=k;
15
                    mkp2[i][j]+=k*x;
16
                    mkp3[i][j]+=k*y;
17
                    mkp4[i][j]+=k*x*y;
18
                }
19
            }
20
21
        inline void update(int a,int b,int x,int y,int k)
22
        {
23
            Update(a,b,k);
24
            Update(a,y+1,-k);
25
            Update(x+1,b,-k);
26
            Update(x+1,y+1,k);
27
        }
```

```
28
       inline int Query(int x,int y)
29
30
           int ans=0;
31
           for(int i=x;i>=1;i-=lowbit(i))
32
33
               for(int j=y;j>=1;j-=lowbit(j))
34
35
                   ans+=(x+1)*(y+1)*mkp1[i][j]
36
                   -(y+1)*mkp2[i][j]-(x+1)*mkp3[i][j]+mkp4[i][j];
37
               }
38
           }
39
           return ans;
40
       }
41
       inline int query(int a,int b,int x,int y)
42
43
           return Query(x,y)+Query(a-1,b-1)-Query(x,b-1)-Query(a-1,y);
44
       }
45 };
46 treearray tri;
47 int main()
48 {
49
50 }
51
动态开点线段树
1 // root 表示整棵线段树的根结点; cnt 表示当前结点个数
2 const int maxn=1e5+10;
3 int n, cnt, root;
4 int sum[maxn*20], ls[maxn*20], rs[maxn*20];
6 // 用法: update(root, 1, n, x, f); 其中 x 为待修改节点的编号
7 void update(int& p, int L, int R, int x, int f) { // 引用传参
      if (!p) p = ++cnt; // 当结点为空时, 创建一个新的结点
9
      if (L == R) {
10
           sum[p] += f;
11
           return;
12
       }
13
       int m = L + ((R - L) >> 1);
14
       if (x \le m)
15
           update(ls[p], L, m, x, f);
16
       else
17
           update(rs[p], m + 1, R, x, f);
18
       sum[p] = sum[ls[p]] + sum[rs[p]]; // pushup
19 }
20 // 用法: query(root, 1, n, l, r);
21 int query(int p, int L, int R, int l, int r) {
       if (!p) return 0; // 如果结点为空,返回 0
22
23
       if (L >= l \&\& R <= r) return sum[p];
24
       int m = L + ((R - L) >> 1), ans = 0;
25
       if (l <= m) ans += query(ls[p], L, m, l, r);</pre>
26
       if (r > m) ans += query(rs[p], m + 1, R, l, r);
27
       return ans;
28 }
29 int merge(int a, int b, int l, int r) {
30
       if (!a) return b;
```

```
31
        if (!b) return a;
32
        if (l == r) {
            sum[a]+=sum[b];
33
34
            return a;
35
        }
36
        int mid = (l + r) \gg 1;
37
        ls[a] = merge(ls[a], ls[b], l, mid);
38
        rs[a] = merge(rs[a], rs[b], mid + 1, r);
39
        sum[a]=sum[ls[a]]+sum[rs[a]];
40
        return a;
41 }
   void split(int &p, int &q, int L, int R, int l, int r) {//p 原树 q 新树
42
43
        if (R < l || r < L) return;
44
        if (!p) return;
45
        if (l \le L \&\& R \le r) {
46
            q = p;
47
            p = 0;
48
            return;
49
        }
50
        if (!q) q = ++cnt;
51
        int m = L + R \gg 1;
52
        if (l <= m) split(ls[p], ls[q], L, m, l, r);</pre>
53
        if (m < r) split(rs[p], rs[q], m + 1, R, l, r);</pre>
54
        sum[p]=sum[ls[p]]+sum[rs[p]];
55
        sum[q]=sum[ls[q]]+sum[rs[q]];
56 }
57 int query1(int& Sum,int Up, int rt, int l, int r) {//min_x of f(x)+x>Up
        // cout<="Sum="<<Sum<" Up="<<Up<-" rt="<<rt<" l="<<!<<" r="<<r<"\n";
58
59
        if(!rt){
60
            if(r+Sum<=Up)return -1;</pre>
61
            else return r-(r+Sum-Up)+1;
62
        }
        if (true) {
63
64
            int ss = Sum+sum[rt];
65
            if (ss+r \le Up) {
66
                Sum = ss;
67
                return -1;
68
69
            if (l == r)return l;
70
        }
71
        int mid = (l + r) / 2;
72
        int pos = query1(Sum,Up,ls[rt], l, mid);
73
        if (pos != -1)return pos;
74
        return query1(Sum,Up,rs[rt], mid + 1, r);
75 }
可持久化 01trie
1 const int maxn=1e5+10;
2 struct Persistent_Trie
3 {
4
       int ch[maxn][2],tot,sum[maxn];
5
       void clear()
6
       {
7
           tot=0;
8
           return;
9
       }
```

```
10
        void cpy(int from,int to)
11
12
            ch[to][0]=ch[from][0];
13
            ch[to][1]=ch[from][1];
14
            sum[to]=sum[from];
15
            return;
16
        }
17
        void insert(int &root,int old,int num,int nowbit)
18
19
            root=++tot;
20
            cpy(old,root);
21
            sum[root]++;
22
            if(nowbit==-1)return;
23
            if(num&(1<<nowbit))</pre>
24
            {
25
                insert(ch[root][1],ch[root][1],num,nowbit-1);
26
            }
27
            else
28
            {
29
                insert(ch[root][0], ch[root][0], num, nowbit-1);
30
            }
31
        }
32
        int query(int s,int t,int x)
33
        {
34
            int ans=0;
35
            for(int i=30; i>=0; --i)
36
37
                if(sum[ch[t][!(x&(1<<i))]]-sum[ch[s][!(x&(1<<i))]])
38
                {
39
                    t=ch[t][!(x&(1<<i))];
40
                    s=ch[s][!(x&(1<<i))];
                    ans|=(1<<i);
41
42
                }
43
                else
44
                {
                    t=ch[t][!!(x&(1<<i))];
45
46
                    s=ch[s][!!(x&(1<<i))];
47
48
            }
49
            return ans;
50
        }
51 };
最近公共祖先 LCA
1 const int maxn=1e5+10;
2 vector<int>ve[maxn];
3 int dep[maxn],f[21][maxn];
4 void dfs(int x,int fa)
5 {
6
    dep[x]=dep[fa]+1;
7
    for(int i=0;i<=19;i++)
8
     f[i+1][x]=f[i][f[i][x]];
9
      for(auto it:ve[x])
10
11
        if(it==fa) continue;
12
      f[0][it]=x;
```

```
13
       dfs(it,x);
14 }
15 }
16 int lca(int x,int y)
17 {
18 if(dep[x]<dep[y]) swap(x,y);</pre>
19 for(int i=20;i>=0;i--)
20 {
21
       if(dep[f[i][x]]>=dep[y]) x=f[i][x];
22
       if(x==y) return x;
23 }
24
     for(int i=20;i>=0;i--)
25
      if(f[i][x]!=f[i][y])
26
        x=f[i][x], y=f[i][y];
27  return f[0][x];
28 }
点分治
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn = 100010;
4 const int inf =2e9;
5 int n, siz[maxn], dist[maxn], vis[maxn],maxx[maxn];
6 vector<pair<int, int>> ve[maxn];
7
8 void add_edge(int x, int y, int z)
9 {
10
       ve[x].emplace back(y, z);
11 }
12
13 void calcsiz(int x, int fa, int sum, int &rt)
14 {
15
       siz[x] = 1;
16
       \max x[x] = 0;
17
       for (auto &[to, len] : ve[x])
            if (to != fa && !vis[to])
18
19
            {
20
                calcsiz(to, x, sum, rt);
21
                \max x[x] = \max(\max x[x], siz[to]);
22
                siz[x] += siz[to];
23
            }
24
       \max x[x] = \max(\max x[x], \text{ sum - siz}[x]);
25
       if (\max x[x] < \max [rt])
26
            rt = x;
27 }
28
29
30 void calcdist(int x, int fa)
31 {
32
       for (auto &[to, len] : ve[x])
33
           if (to != fa && !vis[to])
34
            {
35
                dist[to] = dist[x] + len, calcdist(to, x);
36
37 }
38 void dfs(int x, int fa)
```

```
39 {
40
        vis[x] = true;
        for (auto &[to, len] : ve[x])
41
42
            if (to != fa && !vis[to])
43
            {
44
                dist[to] = len;
45
                calcdist(to, x);
46
            }
47
48
49
        for (auto &[to, len] : ve[x])
50
            if (to != fa && !vis[to])
51
            {
52
                int sum = siz[to];
53
                int rt = 0;
54
                calcsiz(to, x, sum, rt);
55
                calcsiz(rt, -1, sum, rt);
56
                dfs(rt, x);
57
            }
58 }
59
60 int main()
61 {
62
        ios::sync_with_stdio(false);
63
        cin.tie(0);
64
        cin >> n;
65
        for (int i = 1; i < n; i++)
66
67
            int a, b,c;
68
            cin >> a >> b>>c, add edge(a, b, c), add edge(b, a, c);
69
        }
70
        int rt = 0;
71
        maxx[rt] = inf;
72
        int sum = n;
73
        calcsiz(1, -1, sum, rt);
        calcsiz(rt, -1, sum, rt);
74
75
        dfs(rt, -1);
76
        return 0;
77 }
78
珂朵莉树
1 #include <bits/stdc++.h>
2 using namespace std;
  struct SegmentMap{
4
       map<int,int> ma;
5
       int sum=0;
6
      int n;
7
       SegmentMap(int _n=0){
8
           n=n;
9
           ma[1]=0;
10
            ma[n+1]=-1;
11
12
        void del(int l,int r,int x){//减去当前 (l,r,x) 的贡献
13
            sum = (r-l+1)*x;
14
        }
```

```
15
        void add(int l,int r,int x){//加上当前 (l,r,x) 的贡献
16
            sum += (r-l+1)*x;
17
        }
18
        void split(int x){
19
            auto t=prev(ma.upper_bound(x))->second;
20
            ma[x]=t;
21
        }
22
        void update(int l,int r,auto&& T){
23
            split(l);split(r+1);
24
            auto it=prev(ma.upper_bound(l));
25
            int pr=-1;
26
            while(it->first<=r){</pre>
27
                int nowl=it->first,nowr=next(it)->first-1;
28
                int x=it->second;
29
                del(nowl,nowr,x);
30
                add(nowl,nowr,T(x));
31
                if(l!=nowl&&pr==T(x))it=ma.erase(it);
32
                else {
33
                     it->second=T(x);
34
                    it=next(it);
35
                }
36
                pr=T(x);
37
38
            if(it->first!=n+1&&it->second==pr)ma.erase(it);
39
            if(l!=1){
40
                it=ma.lower_bound(l);
41
                if(prev(it)->second==it->second)ma.erase(it);
42
            }
43
        }
44 };
45 int main()
46 {
47
        ios::sync_with_stdio(false);
48
        cin.tie(0);
49
        int n,q;cin>>n>>q;
50
        SegmentMap sol(n);
51
        while(q--){
52
            int op;cin>>op;
53
            if(op==1){
54
                int l,r;cin>>l>>r;
55
                sol.update(l,r,[](int x){
56
                     return (int)sqrt(x);
57
                });
58
            }
59
            else{
60
                int l,r,x;cin>>l>>r>>x;
61
                sol.update(l,r,[x](int y){
62
                     return x;
63
                });
64
            }
65
            cout<<sol.sum<<"\n";</pre>
66
        }
67 }
```

笛卡尔树

```
1 const int maxn=2e5+10;
2 vector<int> ve[maxn];
3 int a[maxn];
4 int n;
5 int build(){
6
      int top=0;
7
      vector<int> Stack(n+1,0);
8
      for(int i=0;i<=n;i++){</pre>
9
           ve[i].clear();
10
           ve[i].resize(2,-1);
11
       }
12
    Stack[++top]=1;
13
     for(int i=2;i<=n;i++){</pre>
14
      while(top&&a[Stack[top]]>=a[i])top--;
15
       if(!top)ve[i][0]=Stack[top+1];
16
      else ve[i][0]=ve[Stack[top]][1],ve[Stack[top]][1]=i;
17
      Stack[++top]=i;
18
19
       return Stack[1];
20 }
线段树区间加区间历史最小值
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define int long long
4 const int maxn=1e6+10;
5 const int inf =2e9;
6 struct Node{
7
      int l,r,res,tag,tag2,res2;
8 };
9 struct SegmentTree{
10
       Node a[maxn*4];
11
        void tag init(int i){
12
            a[i].tag=a[i].tag2=0;
13
14
       void tag union(int fa,int i){
15
            if(a[fa].tag2<0)a[i].tag2=min(a[i].tag2,a[i].tag+a[fa].tag2);</pre>
16
            a[i].tag+=a[fa].tag;
17
       }
18
        void tag cal(int i){
19
            if(a[i].tag2<0)a[i].res2=min(a[i].res2,a[i].res+a[i].tag2);</pre>
20
           a[i].res+=a[i].tag;
21
22
       void pushdown(int i){
23
            tag cal(i);
24
            if(a[i].l!=a[i].r){
25
                tag_union(i,i*2);
26
                tag_union(i,i*2+1);
27
            }
28
            tag_init(i);
29
       }
30
       void pushup(int i){
31
            if(a[i].l==a[i].r)return;
32
            pushdown(i*2);
33
            pushdown(i*2+1);
34
            a[i].res=min(a[i*2].res,a[i*2+1].res);
```

```
35
            a[i].res2=min(a[i*2].res2,a[i*2+1].res2);
36
        }
37
        void build(int i,int l,int r){
38
            a[i].l=l,a[i].r=r;tag_init(i);
39
            if(l>=r)return;
40
            int mid=(l+r)/2;
41
            build(i*2,l,mid);
42
            build(i*2+1, mid+1, r);
43
44
        void update(int i,int l,int r,int w){
45
            if(a[i].r<l||a[i].l>r||l>r)return;
46
            pushdown(i);
47
            if(a[i].l>=l&&a[i].r<=r){</pre>
48
                a[i].tag+=w;
49
                a[i].tag2=min(a[i].tag2,a[i].tag);
50
                return:
51
            }
52
            update(i*2,l,r,w);
53
            update(i*2+1,l,r,w);
54
            pushup(i);
55
        }
56
        int query(int i,int l,int r){
57
            pushdown(i);
58
            if(a[i].r<l||a[i].l>r||l>r)return inf;
59
            if(a[i].l>=l\&\&a[i].r<=r){
60
                return a[i].res2;
61
            }
62
            return min(query(i*2,l,r),query(i*2+1,l,r));
63
        }
64 };
65 SegmentTree tri;
66 signed main()
67 {
68
        int n,m;
69
        cin>>n>>m;
70
        tri.build(1,1,n);
71
        for(int i=1;i<=m;i++){</pre>
72
            int ops;cin>>ops;
73
            if(ops==1){
74
                int l,r,x;cin>>l>>r>>x;
75
                tri.update(1,l,r,x);
76
            }
77
            else{
78
                int l,r;cin>>l>>r;
79
                cout<<tri.query(1,l,r)<<"\n";</pre>
80
            }
81
82
        return 0;
83 }
莫队
1 #include<bits/stdc++.h>
2 using namespace std;
3 const int N=1e6+5;
4 int n,m,a[N],block,ans[N],now,cnt[N];
5 struct node
```

```
6 {
7
      int l,r,i;
8
      friend bool operator<(const node a,const node b)</pre>
9
10
            if((a.l/block)==(b.l/block)) return ((a.l/block%2)?a.r>b.r:a.r<b.r);</pre>
11
            else return a.l<b.l;</pre>
12
       }
13 }q[N];
14 void add(int x)
15 {
16 }
17 void del(int x)
18 {
19 }
20 int main()
21 {
22
       block=max(1,n/sqrt(m));
23
       sort(q+1,q+1+m);
24
       int l=1, r=0;
25
       for(int i=1;i<=m;i++)</pre>
26
27
            while(l<q[i].l) del(l++);</pre>
28
            while(l>q[i].l) add(--l);
           while(r<q[i].r) add(++r);</pre>
29
           while(r>q[i].r) del(r--);
30
31
            ans[q[i].i]=now;
32
33
        for(int i=1;i<=m;i++)</pre>
34
            printf("%d\n",ans[i]);
35
        return 0;
36 }
37
虚树
1 //带边权的虚树
2 //ve2 是虚树, ve 是原树
3 //注意使用时 mlen 的意义需要修改 getlen 和 dfs 预处理的时候都要修改
4 //用的时候就 addintoxs(x)丢进去,每次 init 就全部删除
5 //add 是加原边, ADD 不用管它
6 //solve 里面是必备的几步,不能去除
7 #include <bits/stdc++.h>
8 using namespace std;
9 #define int long long
10 const int maxn=1e5+10;
11 const int inf =1e18;
12 int n,m;
13 struct XS{
14
       struct kkk{
15
            int to,len;
16
       };
17
       int dep[maxn],f[maxn][21],id[maxn];
18
       int mlen[maxn][21],ans[maxn][21];
19
       int state[maxn];
20
       int sum[maxn],all;
21
       vector<kkk> ve[maxn], ve2[maxn];
22
       int now;//统计 dfs 序
```

```
23
        void dfs(int u,int fa)
24
25
            id[u]=now++;
26
            dep[u]=dep[fa]+1;
27
            for(int i=0;i<=19;i++){</pre>
28
                f[u][i+1]=f[f[u][i]][i];
29
                mlen[u][i+1]=mlen[f[u][i]][i]+mlen[u][i];
30
31
            for(auto v:ve[u])
32
            {
33
                if(v.to==fa) continue;
34
                f[v.to][0]=u;
35
                mlen[v.to][0]=v.len;
36
                dfs(v.to,u);
37
            }
38
        }
39
        int lca(int x,int y)
40
41
            if(dep[x]<dep[y]) swap(x,y);</pre>
42
            for(int i=20;i>=0;i--)
43
            {
44
                if(dep[f[x][i]]>=dep[y]) x=f[x][i];
45
                if(x==y) return x;
46
47
            for(int i=20; i>=0; i--)
48
                if(f[x][i]!=f[y][i])
49
                    x=f[x][i], y=f[y][i];
50
            return f[x][0];
51
        }
52
        int getlen(int x,int y)
53
        {
54
            if(x==y)return 0;
55
            if(dep[x]<dep[y]) swap(x,y);</pre>
56
            int res=0;
57
            for(int i=20; i>=0; i--){
58
                if(dep[f[x][i]) >= dep[y]){
59
                     res=res+mlen[x][i];
60
                    x=f[x][i];
61
                }
62
                if(x==y)return res;
63
            }
64
            return inf;
65
66
        void add(int x,int y,int len){//加边
67
            ve[x].push back({y,len});
68
            ve[y].push_back({x,len});
69
70
        void ADD(int x,int y,int len){//虚树加边
71
            ve2[x].push_back({y,len});
72
            ve2[y].push_back({x,len});
73
        }
74
        vector<int> vis;//b vis 这两个用来初始化
75
        bool b[maxn];
        vector<int> v1;//用来表示加入虚树的点
76
77
        int sta[maxn];
78
        void init()//删除虚树
```

```
79
        {
            for(auto it:vis){
80
81
                 ve2[it].clear();
82
                 b[it]=false;
83
                 sum[it]=0;
84
85
            vis.clear();
86
            v1.clear();
87
88
        void makexs()
89
90
            sort(v1.begin(),v1.end(),[&](int x,int y){
91
                 return id[x]<id[y];</pre>
92
            });
93
            sta[0]=0;
            int top=1;
94
95
            sta[top]=1;
96
            vis.push_back(1);
97
            for(auto it:v1){
98
                 int l=lca(it,sta[top]);
99
                 if(l!=sta[top]){
100
                      while(id[l]<id[sta[top-1]]){</pre>
101
                           int w=getlen(sta[top],sta[top-1]);
102
                          ADD(sta[top-1],sta[top],w);
103
                          vis.push_back(sta[top--]);
104
105
                      if(id[l]>id[sta[top-1]]){
106
                          int w=getlen(sta[top],l);
107
                          ADD(l,sta[top],w);
108
                          vis.push back(sta[top]);
109
                          sta[top]=l;
                      }
110
111
                      else {
112
                          int w=getlen(sta[top],sta[top-1]);
113
                          ADD(sta[top],sta[top-1],w);
114
                          vis.push_back(sta[top--]);
115
                      }
116
117
                  sta[++top]=it;
118
             }
119
             for(int i=1;i<top;i++){</pre>
120
                  int w=getlen(sta[i],sta[i+1]);
121
                  ADD(sta[i],sta[i+1],w);
122
                  vis.push_back(sta[i+1]);
123
             }
124
125
         void addintoxs(int x){
126
             if(x==1)return;
127
             v1.push_back(x);
128
             b[x]=true;
129
         void solve(){
130
131
             now=0;
132
             dfs(1,0);
              for(int i=1;i<=n;i++){</pre>
133
134
                  makexs();
```

```
135
                 init();
136
             }
137
        }
138 };
139 XS xs;
LCT 维护联通性
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn = 10010;
5 struct LCT {
6
      int ch[maxn][2], fa[maxn], tag[maxn];
7
8
      void clear(int x) { ch[x][0] = ch[x][1] = fa[x] = tag[x] = 0; }
9
10
       int getch(int x) { return ch[fa[x]][1] == x; }
11
12
       int isroot(int x) { return ch[fa[x]][0] != x && ch[fa[x]][1] != x; }
13
       void pushdown(int x) {
14
15
            if (tag[x]) {
16
            if (ch[x][0]) swap(ch[ch[x][0]][0], ch[ch[x][0]][1]), tag[ch[x][0]] ^= 1;
17
            if (ch[x][1]) swap(ch[ch[x][1]][0], ch[ch[x][1]][1]), tag[ch[x][1]] ^= 1;
18
            tag[x] = 0;
19
            }
20
       }
21
22
       void update(int x) {
23
            if (!isroot(x)) update(fa[x]);
24
            pushdown(x);
25
       }
26
27
       void rotate(int x) {
28
            int y = fa[x], z = fa[y], chx = getch(x), chy = getch(y);
29
            fa[x] = z;
30
            if (!isroot(y)) ch[z][chy] = x;
31
            ch[y][chx] = ch[x][chx ^ 1];
32
            fa[ch[x][chx ^ 1]] = y;
33
            ch[x][chx ^ 1] = y;
34
            fa[y] = x;
35
       }
36
37
       void splay(int x) {
38
            update(x);
39
            for (int f = fa[x]; f = fa[x], !isroot(x); rotate(x))
40
            if (!isroot(f)) rotate(getch(x) == getch(f) ? f : x);
41
       }
42
43
       void access(int x) {
44
            for (int f = 0; x; f = x, x = fa[x]) splay(x), ch[x][1] = f;
45
46
47
       void makeroot(int x) {
48
            access(x);
49
            splay(x);
```

```
50
          swap(ch[x][0], ch[x][1]);
51
          tag[x] \stackrel{\sim}{=} 1;
52
       }
53
54
     int find(int x) {
55
        access(x);
56
          splay(x);
57
          while (ch[x][0]) x = ch[x][0];
58
          splay(x);
59
          return x;
60
      }
61 /*----*/
62
      bool query(int x,int y){//查询是否为同一颗树
63
       return find(x)==find(y);
64
65
       void addedge(int x,int y){
          if (find(x) != find(y)) makeroot(x), fa[x] = y;
66
67
68
      void deledge(int x,int y){
69
         makeroot(x);
70
          access(y);
71
          splay(y);
72
          if (ch[y][0] == x && !ch[x][1]) ch[y][0] = fa[x] = 0;
73
       }
74 } st;
75
76 int n, q, x, y;
77 char op[maxn];
78
79 int main() {
80
      scanf("%d%d", &n, &q);
81
       while (q--) {
82
          scanf("%s%d%d", op, &x, &y);
83
          if (op[0] == 'Q') {
84
             if (st.query(x,y))
              printf("Yes\n");
85
86
          else
87
              printf("No\n");
88
          }
89
          if (op[0] == 'C')st.addedge(x,y);
90
          if (op[0] == 'D')st.deledge(x,y);
91
92
      return 0;
93 }
```

数学

组合数

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define int long long
4 const int maxn=100010;
5 const int mod=1e9+7;
6 int ksm(int x,int k){
7
      int res=1;
8
      while(k){
9
           if(k&1)res=res*x%mod;
10
           x=x*x%mod;
11
           k/=2;
12
       }
13
       return res;
14 }
15 int ny(int x){
       return ksm(x,mod-2);
16
17 }
18 void add(int &x,int y){
19
       if((x+=y)>=mod)x-=mod;
20 }
21 void del(int &x,int y){
22
       if((x-=y)<0)x+=mod;
23 }
24 int inv[maxn],fac[maxn];
25 int C(int n,int m){return n==0?1:fac[n]*inv[n-m]%mod*inv[m]%mod;}
26 int A(int n,int m){return n==0?1:fac[n]*inv[n-m]%mod;}
27 void init(){
28
       inv[0]=fac[0]=1;
29
       inv[1]=1;
30
       for(int i=1;i<maxn;i++){</pre>
31
            fac[i]=fac[i-1]*i%mod;
32
       }
33
       inv[1]=1;
34
       for(int i=2;i<maxn;i++){</pre>
35
            inv[i]=(int)(mod-mod/i)*inv[mod%i]%mod;
36
       inv[0]=1;
37
38
        for(int i=1;i<maxn;i++){</pre>
39
            inv[i]=inv[i-1]*inv[i]%mod;
40
       }
41 }
42 signed main()
43 {
44
       init();
45
       if(mod==(int)(1e9+7))assert(C(2000,1000)==72475738);
        if(mod==9982444353)assert(C(2000,1000)==472799582);
47 }
BSGS 指数方程余数问题(求 a^x=b%p)
1 #include <cstdio>
2 #include <cstring>
3 #include <cmath>
4 #include <algorithm>
```

```
5 #include <unordered_map>
7 using namespace std;
9 typedef long long LL;
10
11 const int INF = 0x3f3f3f3f;
12
13 int a, b, p;
14 unordered_map<int, int> hs;
15
16 int exgcd(int a, int b, int &x, int &y) {
17
        if (!b) {
18
           x = 1, y = 0;
19
            return a;
20
        }
21
        int d = exgcd(b, a % b, y, x);
22
        y -= a / b * x;
23
        return d;
24 }
25
26 int BSGS(int a, int b, int p) {
27
        if (1 % p == b % p) return 0;
28
        int k = sqrt(p) + 1;
29
        hs.clear();
        for (int y = 0, r = b % p; y < k; y++) {
30
31
            hs[r] = y;
32
            r = (LL)r * a % p;
33
        }
34
        int ak = 1;
35
        for (int i = 1; i <= k; i++) ak = (LL)ak * a % p;</pre>
36
        for (int x = 1, l = ak; x \le k; x++) {
37
            if (hs.count(l)) return k * x - hs[l];
38
            l = (LL)l * ak % p;
39
40
        return -INF;
41 }
42
43 int exBSGS(int a, int b, int p) {
44
        b = (b \% p + p) \% p;
45
        if (1 % p == b % p) return 0;
46
        int x, y;
47
        int d = exgcd(a, p, x, y);
48
        if (d > 1) {
            if (b % d) return -INF;
            exgcd(a / d, p / d, x, y);
50
51
            return exBSGS(a, (LL)b / d * x % (p / d), p / d) + 1;
52
53
        return BSGS(a, b, p);
54 }
55
56 int main() {
57
        while (~scanf("%d%d%d", &a, &p, &b), a || b || p) {
58
            int res = exBSGS(a, b, p);
59
            if (res < 0) puts("No Solution");</pre>
60
            else printf("%d\n", res);
```

```
61
       }
62
       return 0;
63 }
EXGCD
1 int exgcd(int a, int b, int \&x, int \&y){//x ax+by=gcd(a,b) !(a==0&&b==0)
       if(b==0){
3
           x=1;
4
           y=0;
5
           return a;
6
      }
7
      int d=exgcd(b,a%b,x,y);
8
      int t=x;
9
      x=y;
10
       y=t-(a/b)*y;
11
       return d;
12 }
FFT
1 //当 vector 用就可以了
2 #include <bits/stdc++.h>
3 #define fp(i, a, b) for (int i = (a), i##_{-} = (b) + 1; i < i##_{-}; ++i)
4 #define fd(i, a, b) for (int i = (a), i##_{=} = (b) - 1; i > i##_{=}; --i)
5 using namespace std;
6 using ll = int64_t;
7 using db = double;
8 /*-----
9 struct cp {
10
       db x, y;
       cp(db real = 0, db imag = 0) : x(real), y(imag){};
11
12
        cp operator+(cp b) const { return {x + b.x, y + b.y}; }
13
       cp operator-(cp b) const { return {x - b.x, y - b.y}; }
14
       cp operator*(cp b) const { return \{x * b.x - y * b.y, x * b.y + y * b.x\}; }
15 };
16 using vcp = vector<cp>;
17 using Poly = vector<int>;
18 namespace FFT {
19
       const db pi = acos(-1);
20
       vcp Omega(int L) {
21
            vcp \ w(L); \ w[1] = 1;
22
            for (int i = 2; i < L; i <<= 1) {
23
                auto w\theta = w.begin() + i / 2, w1 = w.begin() + i;
24
                cp wn(cos(pi / i), sin(pi / i));
25
                for (int j = 0; j < i; j += 2)
26
                    w1[j] = w0[j >> 1], w1[j + 1] = w1[j] * wn;
27
            }
28
            return w;
29
30
       auto W = Omega(1 << 21); // NOLINT</pre>
31
        void DIF(cp *a, int n) {
32
            cp x, y;
33
            for (int k = n >> 1; k; k >>= 1)
34
                for (int i = 0; i < n; i += k << 1)
35
                    for (int j = 0; j < k; ++j)
36
                        x = a[i + j], y = a[i + j + k],
37
                        a[i + j + k] = (a[i + j] - y) * W[k + j], a[i + j] = x + y;
```

```
38
       }
39
       void IDIT(cp *a, int n) {
40
           cp x, y;
41
           for (int k = 1; k < n; k <<= 1)
               for (int i = 0; i < n; i += k << 1)
42
43
                   for (int j = 0; j < k; ++j)
44
                       x = a[i + j], y = a[i + j + k] * W[k + j],
45
                       a[i + j + k] = x - y, a[i + j] = x + y;
46
           const db Inv = 1. / n;
47
           fp(i, 0, n - 1) a[i].x *= Inv, a[i].y *= Inv;
48
           reverse(a + 1, a + n);
49
       }
50 }
51
52 namespace Polynomial {
53
       // basic operator
54
       void DFT(vcp &a) { FFT::DIF(a.data(), a.size()); }
55
       void IDFT(vcp &a) { FFT::IDIT(a.data(), a.size()); }
56
       int norm(int n) { return 1 << (__lg(n - 1) + 1); }</pre>
57
58
       // Poly mul
59
       vcp \& dot(vcp \& a, vcp \& b) \{ fp(i, 0, a.size() - 1) a[i] = a[i] * b[i]; return
a; }
60
       Poly operator+(Poly a, Poly b) {
61
           int maxlen = max(a.size(), b.size());
62
           Poly ans(maxlen + 1);
63
           a.resize(maxlen + 1), b.resize(maxlen + 1);
64
           for (int i = 0; i < maxlen; i++)
65
               ans[i] = a[i] + b[i];
66
           return ans;
67
       }
68
       Poly operator*(ll k, Poly a) {
69
           Poly ans;
70
           for(auto i:a)
71
               ans.push_back(k * i);
72
           return ans;
73
74
       Poly operator*(Poly a, Poly b) {
75
           int n = a.size() + b.size() - 1;
76
           vcp c(norm(n));
77
           fp(i, 0, a.size() - 1) c[i].x = a[i];
           fp(i, 0, b.size() - 1) c[i].y = b[i];
78
79
           DFT(c), dot(c, c), IDFT(c), a.resize(n);
80
           fp(i, 0, n - 1) a[i] = int(c[i].y * .5 + .5);
81
           return a;
82
       }
84 /*-----*/
85 using namespace Polynomial;
FWT
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int mod = 998244353;
4 void add(int &x, int y) {
if ((x += y) >= mod) x -= mod;
```

```
6 }
7 void del(int &x, int y) {
8 if ((x -= y) < 0) x += mod;
9 }
10 void fwtor(int a[], int m, int opt) //(1,-1)
11 {
12
     for (int len = 2; len <= m; len <<= 1)</pre>
13
       for (int p = len >> 1, i = 0; i < m; i += len)
14
          for (int j = i; j < i + p; j++)
15
            if (opt > 0)
16
              add(a[j + p], a[j]);
17
            else
18
              del(a[j + p], a[j]);
19 }
20 void fwtand(int a[], int m, int opt) //(1,-1)
21 {
22
     for (int len = 2; len <= m; len <<= 1)</pre>
23
       for (int p = len >> 1, i = 0; i < m; i += len)
24
         for (int j = i; j < i + p; j++)
25
            if (opt > 0)
26
              add(a[j], a[j + p]);
27
            else
28
              del(a[j], a[j + p]);
29 }
30 void fwtxor(int a[], int m, int opt) //(1,1/2)
31 {
32
     for (int len = 2; len <= m; len <<= 1)</pre>
33
       for (int p = len >> 1, i = 0; i < m; i += len)
34
         for (int j = i; j < i + p; j++) {
35
            add(a[j], a[j + p]);
36
            a[j + p] = (a[j] - 2ll * a[j + p] % mod + mod) % mod;
            a[j] = 111 * a[j] * opt % mod;
37
38
            a[j + p] = 111 * a[j + p] * opt % mod;
39
         }
40 }
41 int a[1 << 17], b[1 << 17], c[1 << 17];
42 void mul(int a[], int b[], int c[], int m) {
     for (int i = 0; i < m; i++) c[i] = 1ll * a[i] * b[i] % mod;
43
44 }
45 void print(int a[], int m) {
     for (int i = 0; i < m; i++) cout << a[i] << " \n"[i == m - 1];
47 }
48 int main() {
49
     int n;
50
     cin >> n;
51
     int m = 1 \ll n;
52
     for (int i = 0; i < m; i++) cin >> a[i];
53
     for (int i = 0; i < m; i++) cin >> b[i];
54
55
      fwtor(a, m, 1), fwtor(b, m, 1), mul(a, b, c, m);
56
      fwtor(a, m, -1), fwtor(b, m, -1), fwtor(c, m, -1), print(c, m);
57
58
      fwtand(a, m, 1), fwtand(b, m, 1), mul(a, b, c, m);
59
      fwtand(a, m, -1), fwtand(b, m, -1), fwtand(c, m, -1), print(c, m);
60
61
      fwtxor(a, m, 1), fwtxor(b, m, 1), mul(a, b, c, m);
```

```
62 fwtxor(c, m, (mod + 1) / 2), print(c, m);
63 }
莫比乌斯反演
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=1e5+10;
4 int pr[maxn],tot,mul[maxn],phi[maxn];
5 bool vis[maxn];
6 void init(int n)
7 {
8
      mul[1]=phi[1]=1;
9
      for(int i=2;i<=n;i++)</pre>
10
11
           if(!vis[i])
12
13
               mul[i]=-1;
14
               pr[++tot]=i;
15
               phi[i]=i-1;
16
17
           for(int j=1; j \le tot \&\& (long long)pr[j]*i \le n; <math>j++)
18
           {
19
               int num=pr[j]*i;
20
               vis[num]=1;
21
               mul[num]=-mul[i];
22
               phi[num]=phi[i]*phi[pr[j]];
23
               if(i%pr[j]==0)
24
               {
25
                   phi[num]=pr[j]*phi[i];
26
                   mul[num] = 0;
27
                   break;
28
               }
29
           }
30
       }
31 }
NTT
1 #include <bits/stdc++.h>
2
3 #define fp(i, a, b) for (int i = (a), i##_{=} = (b) + 1; i < i##_{=}; ++i)
4 #define fd(i, a, b) for (int i = (a), i## = (b) - 1; i > i## ; --i)
5 #define file(s) freopen(s".in","r",stdin),freopen(s".out","w",stdout)
6 using namespace std;
7 const int maxn = 2e5 + 5, P = 998244353;
8 using arr = int[maxn];
9 using ll = int64 t;
10 /*----
                         */
11 class Cipolla {
12
       int P, I2{};
13
       using pll = pair<ll, ll>;
14 #define X first
15 #define Y second
       ll mul(ll a, ll b) const { return a * b % P; }
16
17
        pll mul(pll a, pll b) const { return {(a.X * b.X + I2 * a.Y % P * b.Y) % P,
(a.X * b.Y + a.Y * b.X) % P}; }
       template<class T> T POW(T a, int b, T x) { for (; b; b >>= 1, a = mul(a, a)) if
```

```
(b & 1) x = mul(x, a); return x; }
19 public:
20
       Cipolla(int p = 0) : P(p) {}
21
       pair<int, int> sqrt(int n) {
22
           int a = rand(), x;
23
            if (!(n %= P))return {0, 0};
24
            if (POW(n, (P-1) >> 1, (int)1) == P-1) return \{-1, -1\};
25
            while (POW(I2 = ((ll) a * a - n + P) % P, (P - 1) >> 1, (int)1) == 1) a =
rand();
           x = (int) POW(pll{a, 1}, (P + 1) >> 1, {1, 0}).X;
26
27
           if (2 * x > P) x = P - x;
28
           return {x, P - x};
29
       }
30 #undef X
31 #undef Y
32 };
34 #define ADD(a, b) (((a) += (b)) >= P ? (a) -=P : 0) // (a += b) %= P
35 #define SUB(a, b) (((a) -= (b)) < 0 ? (a) += P: 0) // ((a -= b) += P) %= P
36 #define MUL(a, b) ((ll) (a) * (b) % P)
37 //vector<int> getInv(int L) {
38 //
         vector<int> inv(L); inv[1] = 1;
         fp(i, 1, L - 1) inv[i] = MUL((P - P / i), inv[P % i]);
39 //
40 //
         return inv;
41 //}
42 //auto inv = getInv(maxn); // NOLINT
43 int POW(ll a, int b = P - 2, ll x = 1) { for (; b; b >>= 1, a = a * a % P) if (b &
1) x = x * a % P; return x; }
44 //int INV(int a) { return a < maxn ? inv[a] : POW(a); }
45 namespace NTT {
46
       const int q = 3;
47
        vector<int> Omega(int L) {
            int wn = POW(g, P / L);
48
49
           vector<int> w(L); w[L >> 1] = 1;
50
            fp(i, L / 2 + 1, L - 1) w[i] = MUL(w[i - 1], wn);
51
            fd(i, L / 2 - 1, 1) w[i] = w[i << 1];
52
            return w;
53
54
       auto W = Omega(1 << 21); // NOLINT
55
        void DIF(int *a, int n) {
56
            for (int k = n >> 1; k; k >>= 1)
57
                for (int i = 0, y; i < n; i += k << 1)
58
                    fp(j, 0, k - 1)
59
                         y = a[i + j + k], a[i + j + k] = MUL(a[i + j] - y + P, W[k + j])
j]), ADD(a[i + j], y);
60
       }
        void IDIT(int *a, int n) {
61
62
            for (int k = 1; k < n; k <<= 1)
63
                for (int i = 0, x, y; i < n; i += k << 1)
64
                    fp(j, 0, k - 1)
65
                        x = a[i + j], y = MUL(a[i + j + k], W[k + j]),
66
                       a[i + j + k] = x - y < 0 ? x - y + P : x - y, ADD(a[i + j], y);
67
            int Inv = P - (P - 1) / n;
68
            fp(i, 0, n - 1) a[i] = MUL(a[i], Inv);
69
            reverse(a + 1, a + n);
70
       }
```

```
71 }
72 namespace Polynomial {
73
        using Poly = std::vector<int>;
74
75
        // mul/div int
76
        Poly & operator*=(Poly &a, int b) { for (auto &x : a) x = MUL(x, b); return a; }
77
        Poly operator*(Poly a, int b) { return a *= b; }
78
        Poly operator*(int a, Poly b) { return b * a; }
79
        Poly &operator/=(Poly &a, int b) { return a *= POW(b); }
80
        Poly operator/(Poly a, int b) { return a /= b; }
81
82
        // Poly add/sub
83
        Poly &operator+=(Poly &a, Poly b) {
84
            a.resize(max(a.size(), b.size()));
85
            fp(i, 0, b.size() - 1) ADD(a[i], b[i]);
86
            return a;
87
88
        Poly operator+(Poly a, Poly b) { return a += b; }
89
        Poly &operator-=(Poly &a, Poly b) {
90
            a.resize(max(a.size(), b.size()));
91
            fp(i, 0, b.size() - 1) SUB(a[i], b[i]);
92
            return a;
93
94
        Poly operator-(Poly a, Poly b) { return a -= b; }
95
96
        // Poly mul
97
        void DFT(Poly &a) { NTT::DIF(a.data(), a.size()); }
98
        void IDFT(Poly &a) { NTT::IDIT(a.data(), a.size()); }
99
        int norm(int n) { return 1 << (32 - __builtin_clz(n - 1)); }</pre>
100
         void norm(Poly \&a) { if (!a.empty()) a.resize(norm(a.size()), 0); }
101
         Poly &dot(Poly &a, Poly &b) {
             fp(i, 0, a.size() - 1) a[i] = MUL(a[i], b[i]);
102
103
             return a;
104
105
         Poly operator*(Poly a, Poly b) {
106
             int n = a.size() + b.size() - 1, L = norm(n);
107
             if (a.size() <= 8 || b.size() <= 8) {
108
                 Poly c(n);
109
                 fp(i, 0, a.size() - 1) fp(j, 0, b.size() - 1)
110
                     c[i + j] = (c[i + j] + (ll) a[i] * b[j]) % P;
111
                 return c;
112
             }
113
             a.resize(L), b.resize(L);
114
             DFT(a), DFT(b), dot(a, b), IDFT(a);
115
             return a.resize(n), a;
116
         }
117
118
         // Poly inv
119
         Poly Inv2k(Poly a) { // a.size() = 2^k
120
             int n = a.size(), m = n >> 1;
121
             if (n == 1) return \{POW(a[0])\};
122
             Poly b = Inv2k(Poly(a.begin(), a.begin() + m)), c = b;
123
             b.resize(n), DFT(a), DFT(b), dot(a, b), IDFT(a);
124
             fp(i, 0, n - 1) a[i] = i < m?0 : P - a[i];
125
             DFT(a), dot(a, b), IDFT(a);
126
             return move(c.begin(), c.end(), a.begin()), a;
```

```
127
128
         Poly Inv(Poly a) {
129
             int n = a.size();
130
             norm(a), a = Inv2k(a);
131
             return a.resize(n), a;
132
         }
133
134
         // Poly div/mod
135
         Poly operator/(Poly a, Poly b){
136
             int k = a.size() - b.size() + 1;
137
             if (k < 0) return \{0\};
138
             reverse(a.begin(), a.end());
139
             reverse(b.begin(), b.end());
140
             b.resize(k), a = a * Inv(b);
141
             a.resize(k), reverse(a.begin(), a.end());
142
             return a;
143
         }
144
         pair<Poly, Poly> operator%(Poly a, const Poly& b) {
145
             Poly c = a / b;
146
             a -= b * c, a.resize(b.size() - 1);
147
             return {c, a};
148
         }
149
150
         // Poly sqrt
151
         Poly Sqrt(Poly a) {
152
             int n = a.size(), k = norm(n);
153
             Poly b = {(new Cipolla(P))->sqrt(a[0]).first}, c;
154
             a.resize(k * 2, 0);
155
             for (int L = 2; L <= k; L <<= 1) {
156
                 b.resize(2 * L, 0), c = Poly(a.begin(), a.begin() + L) * Inv(b);
157
                 fp(i, 0, 2 * L - 1) b[i] = MUL(b[i] + c[i], (P + 1) / 2);
158
             }
159
             return b.resize(n), b;
160
         }
161
162
        // Poly calculus
163
         void Derivative(Poly &a) {
164
             fp(i, 1, a.size() - 1) a[i - 1] = MUL(i, a[i]);
165
             a.pop back();
166
         }
167 }
任意模数 NTT
1 const long long mod =1e18;
  namespace polynomial {
3
       typedef complex<long double> cplx;
4
       const long double pi = acos((long double)-1.0);
5
      const int len = 15, mask = (1 << len) - 1;
6
      struct UnitRoot {
7
           static vector<cplx> w;
8
           static vector<cplx> get_root(int n) {
9
               n = 1 << 32 - __builtin_clz(n);</pre>
10
                if (n > w.size()) {
11
                    w.resize(n);
                    for (int i = 0; i < n; i++)
12
13
                        w[i] = cplx(cos(2 * i * pi / n), sin(2 * i * pi / n));
```

```
14
                                                    }
15
                                                    int m = w.size() / n;
16
                                                    vector<cplx> res(n);
17
                                                    for (int i = 0, j = 0; i < n; i++, j += m) res[i] = w[j];
                                                     return res;
18
19
                                       }
20
                          };
21
                          vector<cplx> UnitRoot::w;
22
23
                         void fft(vector<cplx> &p, const vector<cplx> &w) {
24
                                        int n = w.size();
25
                                        for (int i = 1, j = 0; i < n - 1; ++i) {
26
                                                    int s = n;
27
                                                    do {
28
                                                                  s >>= 1;
29
                                                                  j ^= s;
30
                                                    } while (~j & s);
31
                                                    if (i < j) {
32
                                                                  swap(p[i], p[j]);
33
                                                    }
34
                                       }
                                       for (int d = 0; (1 << d) < n; ++d) {
35
                                                     int m = 1 \ll d, m2 = m * 2, rm = n >> (d + 1);
36
37
                                                     for (int i = 0; i < n; i += m2) {
38
                                                                  for (int j = 0; j < m; ++j) {
39
                                                                               auto &p1 = p[i + j + m], &p2 = p[i + j];
40
                                                                               auto t = w[rm * j] * p1;
41
                                                                               p1 = p2 - t;
42
                                                                               p2 = p2 + t;
43
                                                                  }
44
                                                    }
                                       }
45
46
47
                          vector<long long> conv(const vector<long long> &a,const vector<long long> &b)
{
48
                                       vector<cplx> w = UnitRoot::get_root(a.size() + b.size() - 1);
49
                                        int n = w.size();
50
                                       vector<cplx> A(n), B(n), C(n), D(n);
51
                                       for (int i = 0; i < a.size(); ++i) A[i] = cplx(a[i] >> len, a[i] & mask);
52
                                        for (int i = 0; i < b.size(); ++i) B[i] = cplx(b[i] >> len, b[i] & mask);
53
                                        fft(A, w), fft(B, w);
54
                                        for (int i = 0; i < n; ++i) {
55
                                                    int j = (n - i) % n;
                                                    cplx da = (A[i] - conj(A[j])) * cplx(0, -0.5), db = (A[i] + conj(A[j]))
* cplx(0.5, 0), dc = (B[i] - conj(B[j])) * cplx(0, -0.5), dd = (B[i] + conj(B[j])) *
cplx(0.5, 0);
                                                   C[j] = da * dd + da * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = db * dd + db * dc * cplx(0, 1); D[j] = dc * c
57
1);
58
59
                                       fft(C, w), fft(D, w);
60
                                       vector<long long> res(a.size() + b.size() - 1);
                                       for (int i = 0; i < res.size(); ++i) {</pre>
                                                  long long da = (long long)(C[i].imag() / n + 0.5) % mod,db = (long long)
 (C[i].real() / n + 0.5) % mod,dc = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0.5) % mod,dd = (long long)(D[i].imag() / n + 0
long)(D[i].real() / n + 0.5) % mod;
63
                                                     res[i] = ((dd << (len * 2)) + ((db + dc) << len) + da) % mod;
```

```
64
           }
65
           return res;
66
       }
67 };
68 using namespace polynomial;
Pollard Rho
1 typedef long long ll;
2 map<ll, bool>P;
3 mt19937_64 rnd(time(0));
4 namespace Pollard_Rho
6 #define ldb long double
7 ll mul(ll x, ll y, ll mod)
9 return ((x * y - (ll)((ldb)x / mod * y) * mod) + mod) % mod;
10 }
11 ll gcd(ll a, ll b)
13
   return (b == 0 ? a : gcd(b, a % b));
14 }
15 ll ksm(ll a, ll b, ll mod)
16 {
17
     ll ans = 1; a %= mod;
18
     while (b) {if (b & 1)ans = mul(ans, a, mod); b >>= 1; a = mul(a, a, mod);}
19 return ans;
20 }
21 int pr[15] = \{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37\};
22 bool Miller_Rabin(ll n)
23 {
24
    if (n == 2 || n == 3)return 1;
25 if (n \% 2 == 0 || n == 1) return 0;
26 ll d = n - 1;
27
    int s = 0;
28
    while (d \% 2 == 0)s ++, d >>= 1;
29
    for (int i = 0; i \le 11; i ++)
30 {
31
       if (pr[i] >= n)break;
32
       ll a = pr[i];
33
       ll x = ksm(a, d, n);
34
      ll y = 0;
35
       for (int j = 0; j \le s - 1; j ++)
36
37
         y = mul(x, x, n);
38
         if (y == 1 \&\& x != 1 \&\& x != (n - 1)) return 0;
39
        x = y;
40
41
       if (y != 1)return 0;
42 }
43
    return 1;
44 }
45 ll Pollard Rho(ll n)
46 {
47
   ll now, pre, g;
48
    while (true)
49 {
```

```
50
       now = pre = rnd() % (n - 1) + 1;
51
      q = 1;
52
      ll c = rnd() % (n - 1) + 1;
53
       for (int i = 1, fst = 1;; i ++)
54
55
         now = (mul(now, now, n) + c) % n;
56
         g = mul(g, abs(now - pre), n);
57
        if (now == pre || !g)break;
58
         if (!(i & 127) || i == fst)
59
         {
60
           g = gcd(g, n);
61
         if (g > 1) return g;
62
           if (i == fst)pre = now, fst <<= 1;</pre>
63
        }
64
       }
     }
65
66 }
67 void Find(ll n)
68 {
69
     if (n == 1)return ;
70
   if (Miller_Rabin(n))
71 {
72
       P[n] = 1;
73
       return ;
74 }
75
    ll p = Pollard_Rho(n);
76 int c = 0;
77
    while (!(n % p))
78
    {
79
       n /= p, c ++;
80
     }
81
     Find(p);
82
   Find(n);
83 }
84 }
85 void solve(int x,set<int> &s){
86
       Pollard_Rho :: Find(x);
87
       for (auto [x, _] : P)s.insert(x);
88
       P.clear();
89 }
扩展中国剩余定理
1 #define int long long
2 int mul(int a,int b,int mod){//0(1)取模快速乘,不会爆 long long
    return (a*b-(int)((long double)a/mod*b)*mod+mod)%mod;
4 }
5 int exgcd(int a, int b, int& x, int& y){
6
  if(!b){
7
      x = 1, y = 0;
8
      return a;
9
    }
10
   int d = exgcd(b,a%b,y,x);
11
     y = a/b*x;
12
     return d;
13 }
14 int solve(int n,vector<int>&mo,vector<int>&res){
```

```
15
    int a1,m1;
16
       a1=res[0], m1=mo[0];
17
    bool ok = 1;
18
    for(int i=1;i<n;i++){</pre>
19
       int a2,m2,k1,k2;
20
            m2=mo[i],a2=res[i];
21
      int d = exgcd(m1, m2, k1, k2);
22
       if((a2-a1)%d) ok = 0;
23
       else{
24
          k1=mul(k1,(a2-a1)/d,m2/d);//这个地方必须要用取模快速乘
25
         a1=a1+k1*m1;
26
        m1=abs(m1/d*m2);
27
      }
28
29
     if(ok)return (a1%m1+m1)%m1;
30
       else return -1;
31 }
拉格朗日插值
1 #define int long long
2 const int N=1e6+10, mod=998244353;
3 int ksm(int a,int n,int m=mod){int s=1;while(n){if(n&1) s=s*a%m;a=a*a%m;n>>=1;}
return s;}
4 int fac[N+5], facinv[N+5], inv[N+5];
5 struct LR{
    int Inv(int n){return ksm(n,mod-2);}
7
   void init(){ //预处理阶乘和阶乘逆元,逆元.
8
     fac[0]=inv[0]=inv[1]=1;
9
           for(int i=1;i<=N;i++)</pre>
10
                fac[i]=fac[i-1]*i%mod;
11
       facinv[N]=Inv(fac[N]);
12
       for(int i=N-1;~i;i--)
13
                facinv[i]=facinv[i+1]*(i+1)%mod;
14
       for(int i=2;i<N+5;i++)</pre>
15
         inv[i]=(mod-mod/i)*inv[mod%i]%mod;
16
17
     int cal(vector<int>&x, vector<int>&y, int k){ //离散点 n 个点[0, n-1] x[i], y[i] 插 f(k)
18
            int n=x.size();
19
       int s=0;
20
            for(int i=0; i< n; i++) if(x[i]==k) return y[i];
21
      for(int i=0;i<n;i++){</pre>
22
         int p=y[i]%mod,q=1;
23
          for(int j=0;j<n;j++){</pre>
24
            if(i==j) continue;
25
           p=p*((k-x[i])%mod+mod)%mod;
            q=q*((x[i]-x[j])\mod+mod)\mod;
26
27
28
          s=(s+p*Inv(q)*mod)*mod;
29
       }return (s%mod+mod)%mod;
30
31
     int inpo(vector<int>&f,int x){ //给定 连续i属于[0,n] f(i) 拉插f(x)
32
            int n=f.size()-1;
33
            if(x>=0\&\&x<=n) return f[x];
34
      int p,s=0;
35
            vector<int>pre(n+1), suf(n+1);
36
            pre[0]=x-0;
```

```
37
            for(int i=1;i<=n;i++)pre[i]=pre[i-1]*(x-i)%mod;</pre>
38
            suf[n]=x-n;
39
            for(int i=n-1;i>=0;i--)suf[i]=suf[i+1]*(x-i)%mod;
40
      for(int i=0;i<=n;i++){</pre>
41
        p=facinv[n-i]%mod*facinv[i]%mod;
42
               if(i>0)p=p*pre[i-1]%mod;
43
               if(i<n)p=p*suf[i+1]%mod;</pre>
44
        if ((n-i)\&1) s=(s-p*f[i]%mod+mod)%mod;
45
        else s=(s+p*f[i]%mod)%mod;
46
      }
47
       return (s%mod+mod)%mod;
     }
48
49 }sol;
拉格朗日插值没有模数
1 struct LR{
2
   int inter(std::vector <int> vec, int x){
3
      int n = vec.size() - 1;
      int ans = 0;
5
      for (int i = 0; i \le n; ++ i){
6
          int div = 1;
7
          for (int j = 0; j \le n; ++ j){
8
              if (i != j) div *= (i - j);
9
          }
10
           bool flag = div < 0;</pre>
11
           div = std::abs(div);
12
           int prod = vec[i];
13
           for (int j = 0; j \le n; ++ j){
14
               if (i == j) continue;
15
               int gcd = std::abs(std::_gcd(x - j, div));
16
               prod *= (x - j) / gcd;
17
               div /= gcd;
18
           }
19
           ans += flag ? -prod : prod;
20
21
       return ans:
22 }
杜教筛
1 const int maxn=3e6+10;
2 int sumf[maxn];
3 int Sum(int n){// 这是 f * g 的 n 项前缀和
5 }
6 int Sumg(int n){// g 的 n 项前缀和
7
8 }
9 map<int,int> f;
10 int F (int n) {
11 if (n <= 3000'000) return sumf[n]; // 预处理出 n 较小时的前缀和
   if (f.find(n)!=f.end()) return f[n]; // 记忆化,如果求过这个值,就不需要再递归一遍了
12
13
    int ans = Sum(n);
14
    for (int l = 2, r; l <= n; l = r + 1) // 整除分块
15
       r = n / (n / l), ans -= (Sumg(r) - Sumg(l-1)) * F (n / l);
16
       // [l,r] 的 F (n / l) 是一样的,对 g(x) 求个和即可
    return f[n] = ans / Sumg(1); // 别忘了除上 g(1)
17
```

```
18 }
19
线性筛质数
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int maxn=1e6+10;
4 bool v[maxn];
5 int n,pr;
6 vector<int> p;
7 void init()
8 {
9
      v[1]=true;
10
       for(int i=2;i<maxn;i++)</pre>
11
12
        if(!v[i])p.push_back(i);
13
        for(int j=0;j< p.size()&&i*p[j]< maxn;++j) {v[i*p[j]]=true;if(i*p[j]==0)break;}
14
15 }
16
线性递推
1 #include<bits/stdc++.h>
2 using namespace std;
3 #define rep(i,a,n) for (int i=a;i<n;i++)</pre>
4 #define per(i,a,n) for (int i=n-1;i>=a;i--)
5 #define all(x) (x).begin(),(x).end()
6 #define siz(x) ((int)(x).size())
7 typedef vector<int> VI;
8 typedef long long ll;
9 typedef pair<int,int> PII;
10 const ll mod=1000000007;
11 ll
        powmod(ll
                    a,ll
                            b)
                                 {ll}
                                       res=1;a%=mod; assert(b>=0); for(;b;b>>=1)
{if(b&1)res=res*a%mod;a=a*a%mod;}return res;}
12 ll n;
13 namespace linear seq {
14
       const int N=10010;
       ll res[N],base[N],_c[N],_md[N];
15
16
17
       vector<int> Md;
18
       void mul(ll *a,ll *b,int k) {
19
            rep(i,0,k+k) _c[i]=0;
20
            rep(i,0,k) if (a[i]) rep(j,0,k) _c[i+j]=(_c[i+j]+a[i]*b[j])*mod;
21
           for (int i=k+k-1;i>=k;i--) if (_c[i])
22
                rep(j,0,siz(Md)) _c[i-k+Md[j]]=(_c[i-k+Md[j]]-_c[i]*_md[Md[j]])%mod;
23
            rep(i,0,k) a[i]=_c[i];
24
25
       int solve(ll n, VI a, VI b) {
26
           ll ans=0,pnt=0;
27
            int k=siz(a);
28
            assert(siz(a)==siz(b));
29
            rep(i,0,k) _md[k-1-i]=-a[i];_md[k]=1;
           Md.clear();
30
31
            rep(i,0,k) if (_md[i]!=0) Md.push_back(i);
32
            rep(i,0,k) res[i]=base[i]=0;
33
            res[0]=1;
```

```
34
            while ((1ll<<pnt)<=n) pnt++;</pre>
35
             for (int p=pnt;p>=0;p--) {
36
                 mul(res, res, k);
37
                 if ((n>>p)\&1) {
38
                     for (int i=k-1;i>=0;i--) res[i+1]=res[i];res[0]=0;
39
                     \label{eq:rep} rep(j,0,siz(Md)) \ res[Md[j]] = (res[Md[j]] - res[k] * \_md[Md[j]]) %mod;
40
                 }
41
42
             rep(i,0,k) ans=(ans+res[i]*b[i])%mod;
43
             if (ans<0) ans+=mod;</pre>
44
             return ans;
45
        }
46
        VI BM(VI s) {
47
            VI C(1,1), B(1,1);
48
             int L=0, m=1, b=1;
49
             rep(n, 0, siz(s)) {
50
                 ll d=0;
51
                 rep(i,0,L+1) d=(d+(ll)C[i]*s[n-i])%mod;
52
                 if (d==0) ++m;
53
                 else if (2*L \le n) {
54
                     VI T=C;
55
                     ll c=mod-d*powmod(b,mod-2)%mod;
56
                     while (siz(C)<siz(B)+m) C.push back(0);</pre>
57
                     rep(i,0,siz(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
58
                     L=n+1-L; B=T; b=d; m=1;
59
                 } else {
60
                     ll c=mod-d*powmod(b,mod-2)%mod;
61
                     while (siz(C)<siz(B)+m) C.push back(0);</pre>
62
                     rep(i,0,siz(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
63
                     ++m;
                 }
64
65
             }
66
             return C;
67
        }
68
        int gao(VI a,ll n) {
69
            VI c=BM(a);
70
             c.erase(c.begin());
71
             rep(i, 0, siz(c)) c[i] = (mod-c[i])%mod;
72
             return solve(n,c,VI(a.begin(),a.begin()+siz(c)));
73
        }
74 };
75
76 int main() {
77
        vector<int>v;
78
        v.push back(2);
79
        v.push_back(24);
80
        v.push back(96);
81
        v.push_back(416);
82
        v.push_back(1536);
83
        v.push_back(5504);
84
        v.push_back(18944);
85
        v.push back(64000);
86
        v.push_back(212992);
87
        v.push back(702464);
88
      scanf("%lld", &n);
89
        printf("%lld\n",1LL * linear_seq::gao(v,n-1) % mod);
```

```
90 }
91
辛普森积分
1 double simpson(double l, double r) {
    double mid = (l + r) / 2;
    return (r - l) * (f(l) + 4 * f(mid) + f(r)) / 6; // 辛普森公式
4 }
6 double asr(double l, double r, double eps, double ans, int step) {//step 是递归的下限
    double mid = (l + r) / 2;
8
    double fl = simpson(l, mid), fr = simpson(mid, r);
9
    if (abs(fl + fr - ans) \le 15 * eps && step < 0)
10
       return fl + fr + (fl + fr - ans) / 15; // 足够相似的话就直接返回
11
     return asr(l, mid, eps / 2, fl, step - 1) +
           asr(mid, r, eps / 2, fr, step - 1); // 否则分割成两段递归求解
12
13 }
14
15 double calc(double l, double r, double eps) {
16
     return asr(l, r, eps, simpson(l, r), 12);
17 }
18
高斯消元(模意义)
1 #define int long long
2 const int eps=0;
3 const int maxn=220;
4 const int mod=1e6+3;
5 int ksm(int x,int k){
6
      int res=1;
7
      while(k){
8
          if(k&1)res=res*x%mod;
9
          x=x*x%mod;
10
           k/=2;
11
       }
12
       return res;
13 }
14 int ny(int x){
15
       return ksm(x,mod-2);
16 }
17 void add(int &x,int y){
18
       if((x+=y)>=mod)x-=mod;
19 }
20 void del(int &x,int y){
21
       if ((x-=y)<0)x+=mod;
22 }
23 int a[maxn], x[maxn]; // 方程左边的矩阵和方程右边的值,求解之后 x 存的就是结果
24 int Gauss(int equ,int var){//equ 方程数 var 未知数个数 return 1表示有解
25
       int i,j,k,col,max r;
26
       for(k=0, col=0; k < equ&col < var; k++, col++) {
27
           max_r=k;
28
           for(i=k+1;i<equ;i++)</pre>
29
               if((a[i][col])>(a[max_r][col]))
30
                   max r=i;
31
           if((a[max_r][col])==0)return 0;
32
           if(k!=max_r){
```

```
33
                for(j=col;j<var;j++)</pre>
34
                     swap(a[k][j],a[max_r][j]);
35
                swap(x[k],x[max_r]);
36
            }
37
            x[k]=x[k]*ny(a[k][col])%mod;
38
            for(j=col+1; j<var; j++)a[k][j]=a[k][j]*ny(a[k][col])%mod;</pre>
39
            a[k][col]=1;
40
            for(i=0;i<equ;i++)</pre>
41
                if(i!=k){
42
                     del(x[i],x[k]*a[i][col]%mod);
43
                     for(j=col+1;j<var;j++)del(a[i][j],a[k][j]*a[i][col]%mod);</pre>
44
                     a[i][col]=0;
45
                }
46
        }
47
        return 1;
48 }
高斯消元(浮点数)
1 #define lf double
2 //0 base
3 const lf eps=1e-9;
4 const int maxn=220;
5 lf a[maxn],x[maxn];//方程左边的矩阵和方程右边的值,求解之后x存的就是结果
6 int Gauss(int equ,int var){//equ 方程数 var 未知数个数 return 1表示有解
7
       int i,j,k,col,max_r;
8
       for(k=0, col=0; k<equ&col<var; k++, col++) {
9
           max_r=k;
10
            for(i=k+1;i<equ;i++)</pre>
11
                if(fabs(a[i][col])>fabs(a[max_r][col]))
12
                     max r=i;
13
            if(fabs(a[max_r][col])<eps)return 0;</pre>
14
            if(k!=max_r){
15
                for(j=col;j<var;j++)</pre>
16
                     swap(a[k][j],a[max_r][j]);
17
                swap(x[k],x[max r]);
18
19
            x[k]/=a[k][col];
20
            for(j=col+1; j<var; j++)a[k][j]/=a[k][col];</pre>
21
            a[k][col]=1;
22
            for(i=0;i<equ;i++)</pre>
23
                if(i!=k){
24
                     x[i] = x[k] * a[i][col];
25
                     for(j=col+1; j < var; j++)a[i][j]-=a[k][j]*a[i][col];</pre>
26
                     a[i][col]=0;
27
                }
28
        }
29
        return 1;
30 }
```

计算几何

```
开头
```

```
1 #include <bits/stdc++.h>
2 using namespace std;
4 using point_t=long double; //全局数据类型,可修改为 long long 等
6 constexpr point_t eps=le-8;
7 constexpr long double PI=3.1415926535897932384l;
点与向量
1 // 点与向量
2 template<typename T> struct point
3 {
4
      T x, y;
5
        bool operator==(const point &a) const {return (abs(x-a.x)<=eps && abs(y-
a.y)<=eps);}
       bool operator<(const point &a) const {if (abs(x-a.x)<=eps) return y<a.y-eps;
return x<a.x-eps;}</pre>
      bool operator>(const point &a) const {return !(*this<a || *this==a);}</pre>
9
      point operator+(const point &a) const {return {x+a.x,y+a.y};}
10
       point operator-(const point &a) const {return {x-a.x,y-a.y};}
       point operator-() const {return {-x,-y};}
11
12
       point operator*(const T k) const {return {k*x,k*y};}
13
       point operator/(const T k) const {return {x/k,y/k};}
14
       T operator*(const point &a) const {return x*a.x+y*a.y;} // 点积
15
       T operator^(const point &a) const {return x*a.y-y*a.x;} // 叉积,注意优先级
16
       int toleft(const point &a) const {const auto t=(*this)^a; return (t>eps)-(t<-
eps);} // to-left 测试
       T len2() const {return (*this)*(*this);} // 向量长度的平方
17
18
       T dis2(const point &a) const {return (a-(*this)).len2();} // 两点距离的平方
19
20
       // 涉及浮点数
       long double len() const {return sqrtl(len2());} // 向量长度
21
22
       long double dis(const point &a) const {return sqrtl(dis2(a));} // 两点距离
          long double ang(const point &a) const {return acosl(max(-1.0l,min(1.0l,
((*this)*a)/(len()*a.len()))));} // 向量夹角
              point rot(const long double
                                                     const {return {x*cos(rad)-
24
                                              rad)
y*sin(rad),x*sin(rad)+y*cos(rad)};} // 逆时针旋转(给定角度)
       point rot(const long double cosr, const long double sinr) const {return {x*cosr-
y*sinr,x*sinr+y*cosr};} // 逆时针旋转(给定角度的正弦与余弦)
26 };
27
28 using Point=point<point t>;
极角排序
1 // 极角排序
2 struct argcmp
3 {
4
      bool operator()(const Point &a,const Point &b) const
5
      {
          const auto quad=[](const Point &a)
```

```
7
          {
8
              if (a.y<-eps) return 1;
9
              if (a.y>eps) return 4;
10
               if (a.x<-eps) return 5;</pre>
11
               if (a.x>eps) return 3;
12
               return 2;
13
           };
14
           const int qa=quad(a),qb=quad(b);
15
           if (qa!=qb) return qa<qb;</pre>
16
           const auto t=a^b;
17
           // if (abs(t)<=eps) return a*a<b*b-eps; // 不同长度的向量需要分开
18
           return t>eps;
19
       }
20 };
直线
1 // 直线
2 template<typename T> struct line
4
      point<T> p,v; // p 为直线上一点,v 为方向向量
5
6
       bool operator==(const line &a) const {return v.toleft(a.v)==0 && v.toleft(p-
a.p) == 0;
      int toleft(const point<T> &a) const {return v.toleft(a-p);} // to-left 测试
8
      bool operator<(const line &a) const // 半平面交算法定义的排序
9
      {
10
           if (abs(v^a.v) \le b \le v^a.v = -eps) return toleft(a.p) = -1;
11
           return argcmp()(v,a.v);
12
       }
13
14
       // 涉及浮点数
15
        point<T> inter(const line &a) const {return p+v*((a.v^(p-a.p))/(v^a.v));} //
直线交点
       long double dis(const point<T> &a) const {return abs(v^(a-p))/v.len();} // 点
到直线距离
17
       point<T> proj(const point<T> &a) const {return p+v*((v*(a-p))/(v*v));} // 点在
直线上的投影
18 };
19
20 using Line=line<point t>;
线段
1 //线段
2 template<typename T> struct segment
3 {
4
      point<T> a,b;
5
6
      bool operator<(const segment &s) const {return make_pair(a,b)<make_pair(s.a,s.b);}</pre>
7
      // 判定性函数建议在整数域使用
8
9
10
       // 判断点是否在线段上
       // -1 点在线段端点 | 0 点不在线段上 | 1 点严格在线段上
11
12
       int is on(const point<T> &p) const
13
       {
           if (p==a || p==b) return -1;
14
```

```
15
           return (p-a).toleft(p-b)==0 && (p-a)*(p-b)<-eps;
16
       }
17
18
       // 判断线段直线是否相交
       // -1 直线经过线段端点 | 0 线段和直线不相交 | 1 线段和直线严格相交
19
20
       int is_inter(const line<T> &l) const
21
22
           if (l.toleft(a)==0 || l.toleft(b)==0) return -1;
23
           return l.toleft(a)!=l.toleft(b);
24
       }
25
       // 判断两线段是否相交
26
27
       // -1 在某一线段端点处相交 | 0 两线段不相交 | 1 两线段严格相交
28
       int is inter(const segment<T> &s) const
29
30
           if (is_on(s.a) || is_on(s.b) || s.is_on(a) || s.is_on(b)) return -1;
31
           const line<T> l{a,b-a},ls{s.a,s.b-s.a};
32
           return l.toleft(s.a)*l.toleft(s.b)==-1 && ls.toleft(a)*ls.toleft(b)==-1;
33
       }
34
35
       // 点到线段距离
36
       long double dis(const point<T> &p) const
37
38
           if ((p-a)*(b-a)<-eps || (p-b)*(a-b)<-eps) return min(p.dis(a),p.dis(b));
39
           const line<T> l{a,b-a};
40
           return l.dis(p);
41
       }
42
43
       // 两线段间距离
44
       long double dis(const segment<T> &s) const
45
46
           if (is_inter(s)) return 0;
47
           return min({dis(s.a),dis(s.b),s.dis(a),s.dis(b)});
48
       }
49 };
50
51 using Segment=segment<point_t>;
多边形
1 // 多边形
2 template<typename T> struct polygon
3 {
      vector<point<T>> p; // 以逆时针顺序存储
4
5
6
      size_t nxt(const size_t i) const {return i==p.size()-1?0:i+1;}
7
      size_t pre(const size_t i) const {return i==0?p.size()-1:i-1;}
8
      // 回转数
9
10
       // 返回值第一项表示点是否在多边形边上
       // 对于狭义多边形, 回转数为 0 表示点在多边形外, 否则点在多边形内
11
12
       pair<bool,int> winding(const point<T> &a) const
13
14
           int cnt=0;
15
           for (size_t i=0;i<p.size();i++)</pre>
16
17
               const point<T> u=p[i],v=p[nxt(i)];
```

```
18
                if (abs((a-u)^(a-v)) \le eps \& (a-u)*(a-v) \le eps) return \{true, 0\};
19
                if (abs(u.y-v.y)<=eps) continue;</pre>
20
                const Line uv={u,v-u};
21
                if (u.y<v.y-eps && uv.toleft(a)<=0) continue;
22
                if (u.y>v.y+eps && uv.toleft(a)>=0) continue;
23
                if (u.y<a.y-eps && v.y>=a.y-eps) cnt++;
                if (u.y>=a.y-eps && v.y<a.y-eps) cnt--;</pre>
24
25
26
            return {false,cnt};
27
       }
28
29
       // 多边形面积的两倍
30
        // 可用于判断点的存储顺序是顺时针或逆时针
31
       T area() const
32
33
            T sum=0;
34
            for (size_t i=0;i<p.size();i++) sum+=p[i]^p[nxt(i)];</pre>
35
            return sum;
36
       }
37
38
       // 多边形的周长
39
       long double circ() const
40
41
            long double sum=0;
            for (size_t i=0;i<p.size();i++) sum+=p[i].dis(p[nxt(i)]);</pre>
42
43
            return sum;
44
45 };
46
47 using Polygon=polygon<point t>;
凸多边形
1 //凸多边形
2 template<typename T> struct convex: polygon<T>
3
  {
4
       // 闵可夫斯基和
5
      convex operator+(const convex &c) const
6
       {
7
           const auto &p=this->p;
8
           vector<Segment> e1(p.size()),e2(c.p.size()),edge(p.size()+c.p.size());
9
           vector<point<T>> res; res.reserve(p.size()+c.p.size());
            const auto cmp=[](const Segment &u,const Segment &v) {return argcmp()(u.b-
u.a,v.b-v.a);};
11
            for (size t i=0;i<p.size();i++) e1[i]={p[i],p[this->nxt(i)]};
12
            for (size_t i=0;i<c.p.size();i++) e2[i]={c.p[i],c.p[c.nxt(i)]};</pre>
13
            rotate(e1.begin(),min_element(e1.begin(),e1.end(),cmp),e1.end());
14
            rotate(e2.begin(),min_element(e2.begin(),e2.end(),cmp),e2.end());
15
           merge(e1.begin(),e1.end(),e2.begin(),e2.end(),edge.begin(),cmp);
16
            const auto check=[](const vector<point<T>> &res,const point<T> &u)
17
            {
18
                const auto back1=res.back(),back2=*prev(res.end(),2);
19
                 return (back1-back2).toleft(u-back1)==0 && (back1-back2)*(u-back1)>=-
eps;
20
21
            auto u=e1[0].a+e2[0].a;
22
            for (const auto &v:edge)
```

```
23
           {
24
               while (res.size()>1 && check(res,u)) res.pop back();
25
                res.push_back(u);
26
               u=u+v.b-v.a;
27
            }
28
            if (res.size()>1 && check(res,res[0])) res.pop_back();
29
            return {res};
30
       }
31
32
       // 旋转卡壳
33
       // func 为更新答案的函数,可以根据题目调整位置
34
       template<typename F> void rotcaliper(const F &func) const
35
36
            const auto &p=this->p;
            const auto area=[](const point<T> &u,const point<T> &v,const point<T> &w)
37
{return (w-u)^(w-v);};
38
            for (size_t i=0,j=1;i<p.size();i++)</pre>
39
40
                const auto nxti=this->nxt(i);
41
               func(p[i],p[nxti],p[j]);
42
               while (area(p[this->nxt(j)],p[i],p[nxti])>=area(p[j],p[i],p[nxti]))
43
44
                    j=this->nxt(j);
45
                    func(p[i],p[nxti],p[j]);
46
               }
47
           }
48
       }
49
50
       // 凸多边形的直径的平方
51
       T diameter2() const
52
       {
53
            const auto &p=this->p;
54
           if (p.size()==1) return 0;
55
           if (p.size()==2) return p[0].dis2(p[1]);
56
           T ans=0;
               auto func=[&](const point<T> &u,const point<T> &v,const point<T> &w)
57
\{ans=max(\{ans,w.dis2(u),w.dis2(v)\});\};
58
            rotcaliper(func);
59
            return ans;
60
       }
61
62
       // 判断点是否在凸多边形内
63
       // 复杂度 O(logn)
64
       // -1 点在多边形边上 | 0 点在多边形外 | 1 点在多边形内
65
       int is in(const point<T> &a) const
66
       {
67
            const auto &p=this->p;
68
           if (p.size()==1) return a==p[0]?-1:0;
69
            if (p.size()==2) return segment<T>{p[0],p[1]}.is_on(a)?-1:0;
70
           if (a==p[0]) return -1;
71
             if ((p[1]-p[0]).toleft(a-p[0])==-1 \mid | (p.back()-p[0]).toleft(a-p[0])==1)
return 0;
72
           const auto cmp=[&](const Point &u,const Point &v){return (u-p[0]).toleft(v-
p[0])==1;;
73
            const size_t i=lower_bound(p.begin()+1,p.end(),a,cmp)-p.begin();
74
           if (i==1) return segment<T>{p[0],p[i]}.is_on(a)?-1:0;
```

```
75
            if (i==p.size()-1 \&\& segment<T>\{p[0],p[i]\}.is on(a)) return -1;
76
            if (segment<T>{p[i-1],p[i]}.is on(a)) return -1;
77
            return (p[i]-p[i-1]).toleft(a-p[i-1])>0;
78
       }
79
80
       // 凸多边形关于某一方向的极点
81
       // 复杂度 O(logn)
82
       // 参考资料: https://codeforces.com/blog/entry/48868
       template<typename F> size t extreme(const F &dir) const
83
84
       {
85
           const auto &p=this->p;
          const auto check=[&](const size_t i){return dir(p[i]).toleft(p[this->nxt(i)]-
p[i])>=0;};
            const auto dir0=dir(p[0]); const auto check0=check(0);
88
           if (!check0 && check(p.size()-1)) return 0;
89
           const auto cmp=[&](const Point &v)
90
            {
91
               const size_t vi=&v-p.data();
92
               if (vi==0) return 1;
93
               const auto checkv=check(vi);
94
               const auto t=dir0.toleft(v-p[0]);
95
               if (vi==1 \&\& checkv==check0 \&\& t==0) return 1;
96
               return checkv^(checkv==check0 && t<=0);</pre>
97
           };
98
            return partition_point(p.begin(),p.end(),cmp)-p.begin();
99
       }
100
101
        // 过凸多边形外一点求凸多边形的切线,返回切点下标
102
        // 复杂度 O(logn)
103
        // 必须保证点在多边形外
        pair<size_t, size_t> tangent(const point<T> &a) const
104
105
106
            const size_t i=extreme([&](const point<T> &u){return u-a;});
107
            const size_t j=extreme([&](const point<T> &u){return a-u;});
108
            return {i,j};
109
        }
110
111
        // 求平行于给定直线的凸多边形的切线,返回切点下标
112
        // 复杂度 O(logn)
113
        pair<size_t, size_t> tangent(const line<T> &a) const
114
115
            const size_t i=extreme([&](...){return a.v;});
            const size_t j=extreme([&](...){return -a.v;});
116
117
            return {i,j};
118
        }
119 };
120
121 using Convex=convex<point_t>;
员
1 // 圆
2 struct Circle
3 {
4
      Point c;
      long double r;
5
6
```

```
7
      bool operator==(const Circle &a) const {return c==a.c && abs(r-a.r)<=eps;}
8
       long double circ() const {return 2*PI*r;} // 周长
9
       long double area() const {return PI*r*r;} // 面积
10
       // 点与圆的关系
11
12
       // -1 圆上 | 0 圆外 | 1 圆内
13
        int is in(const Point &p) const {const long double d=p.dis(c); return abs(d-
r)<=eps?-1:d<r-eps;}
14
15
       // 直线与圆关系
16
       // 0 相离 | 1 相切 | 2 相交
17
       int relation(const Line &l) const
18
19
            const long double d=l.dis(c);
20
            if (d>r+eps) return 0;
21
            if (abs(d-r)<=eps) return 1;</pre>
22
            return 2;
23
       }
24
25
       // 圆与圆关系
26
       // -1 相同 | 0 相离 | 1 外切 | 2 相交 | 3 内切 | 4 内含
27
       int relation(const Circle &a) const
28
29
            if (*this==a) return -1;
30
            const long double d=c.dis(a.c);
31
            if (d>r+a.r+eps) return 0;
32
           if (abs(d-r-a.r)<=eps) return 1;</pre>
33
            if (abs(d-abs(r-a.r))<=eps) return 3;</pre>
34
            if (d<abs(r-a.r)-eps) return 4;</pre>
35
            return 2;
36
       }
37
38
       // 直线与圆的交点
39
       vector<Point> inter(const Line &l) const
40
            const long double d=l.dis(c);
41
42
            const Point p=l.proj(c);
43
            const int t=relation(l);
44
            if (t==0) return vector<Point>();
45
            if (t==1) return vector<Point>{p};
46
            const long double k=sqrt(r*r-d*d);
47
            return vector<Point>{p-(l.v/l.v.len())*k,p+(l.v/l.v.len())*k};
48
       }
49
50
       // 圆与圆交点
51
       vector<Point> inter(const Circle &a) const
52
53
            const long double d=c.dis(a.c);
54
            const int t=relation(a);
55
            if (t==-1 || t==0 || t==4) return vector<Point>();
56
           Point e=a.c-c; e=e/e.len()*r;
57
           if (t==1 || t==3)
58
           {
59
                if (r*r+d*d-a.r*a.r>=-eps) return vector<Point>{c+e};
60
                return vector<Point>{c-e};
61
            }
```

```
62
           const long double costh=(r*r+d*d-a.r*a.r)/(2*r*d),sinth=sqrt(1-costh*costh);
63
           return vector<Point>{c+e.rot(costh,-sinth),c+e.rot(costh,sinth)};
64
       }
65
       // 圆与圆交面积
66
67
       long double inter_area(const Circle &a) const
68
69
           const long double d=c.dis(a.c);
70
           const int t=relation(a);
71
           if (t==-1) return area();
72
           if (t<2) return 0;
           if (t>2) return min(area(),a.area());
73
74
             r*r)/(2*a.r*d);
           const long double sinth1=sqrt(1-costh1*costh1),sinth2=sqrt(1-costh2*costh2);
75
76
           const long double th1=acos(costh1), th2=acos(costh2);
77
           return r*r*(th1-costh1*sinth1)+a.r*a.r*(th2-costh2*sinth2);
78
79
80
       // 过圆外一点圆的切线
81
       vector<Line> tangent(const Point &a) const
82
83
           const int t=is in(a);
84
           if (t==1) return vector<Line>();
85
           if (t==-1)
86
           {
87
               const Point v=\{-(a-c).y,(a-c).x\};
88
               return vector<Line>{{a,v}};
89
90
           Point e=a-c; e=e/e.len()*r;
91
           const long double costh=r/c.dis(a),sinth=sqrt(1-costh*costh);
92
           const Point t1=c+e.rot(costh,-sinth),t2=c+e.rot(costh,sinth);
93
           return vector<Line>{{a,t1-a},{a,t2-a}};
94
       }
95
96
       // 两圆的公切线
97
       vector<Line> tangent(const Circle &a) const
98
       {
99
           const int t=relation(a);
100
            vector<Line> lines;
            if (t==-1 || t==4) return lines;
101
102
            if (t==1 || t==3)
103
104
                const Point p=inter(a)[0], v=\{-(a.c-c).y, (a.c-c).x\};
105
                lines.push back({p,v});
106
            }
107
            const long double d=c.dis(a.c);
108
            const Point e=(a.c-c)/(a.c-c).len();
109
            if (t<=2)
110
            {
111
                const long double costh=(r-a.r)/d,sinth=sqrt(1-costh*costh);
112
                const Point dl=e.rot(costh,-sinth),d2=e.rot(costh,sinth);
113
                const Point u1=c+d1*r,u2=c+d2*r,v1=a.c+d1*a.r,v2=a.c+d2*a.r;
114
                lines.push back({u1,v1-u1}); lines.push back({u2,v2-u2});
115
            }
            if (t==0)
116
```

```
117
            {
118
                 const long double costh=(r+a.r)/d,sinth=sqrt(1-costh*costh);
119
                 const Point dl=e.rot(costh,-sinth),d2=e.rot(costh,sinth);
120
                 const Point u1=c+d1*r, u2=c+d2*r, v1=a.c-d1*a.r, v2=a.c-d2*a.r;
121
                 lines.push_back({u1,v1-u1}); lines.push_back({u2,v2-u2});
122
            }
123
             return lines;
124
        }
125
        // 圆的反演
126
127
        tuple<int, Circle, Line> inverse(const Line &l) const
128
        {
129
             const Circle null_c={{0.0,0.0},0.0};
130
             const Line null_l={{0.0,0.0},{0.0,0.0}};
131
             if (l.toleft(c)==0) return {2,null_c,l};
132
             const Point v=l.toleft(c)==1?Point{l.v.y,-l.v.x}:Point{-l.v.y,l.v.x};
133
             const long double d=r*r/l.dis(c);
134
             const Point p=c+v/v.len()*d;
135
             return {1,{(c+p)/2,d/2},null_l};
136
        }
137
138
        tuple<int,Circle,Line> inverse(const Circle &a) const
139
140
             const Circle null_c={{0.0,0.0},0.0};
141
             const Line null_l={{0.0,0.0},{0.0,0.0}};
             const Point v=a.c-c;
143
            if (a.is_in(c)==-1)
144
            {
145
                 const long double d=r*r/(a.r+a.r);
146
                 const Point p=c+v/v.len()*d;
147
                 return {2,null_c,{p,{-v.y,v.x}}};
148
            }
149
             if (c==a.c) return {1,{c,r*r/a.r},null_l};
150
             const long double d1=r*r/(c.dis(a.c)-a.r), d2=r*r/(c.dis(a.c)+a.r);
151
             const Point p=c+v/v.len()*d1,q=c+v/v.len()*d2;
152
             return {1,{(p+q)/2,p.dis(q)/2},null_l};
153
        }
154 };
155
156 // 圆与多边形面积交
157 long double area_inter(const Circle &circ,const Polygon &poly)
158 {
159
        const auto cal=[](const Circle &circ,const Point &a,const Point &b)
160
        {
            if ((a-circ.c).toleft(b-circ.c)==0) return 0.0l;
161
162
             const auto ina=circ.is_in(a),inb=circ.is_in(b);
163
             const Line ab={a,b-a};
164
             if (ina && inb) return ((a-circ.c)^(b-circ.c))/2;
165
            if (ina && !inb)
166
            {
167
                 const auto t=circ.inter(ab);
                 const Point p=t.size()==1?t[0]:t[1];
168
169
                 const long double ans=((a-circ.c)^(p-circ.c))/2;
170
                 const long double th=(p-circ.c).ang(b-circ.c);
171
                 const long double d=circ.r*circ.r*th/2;
172
                 if ((a-circ.c).toleft(b-circ.c)==1) return ans+d;
```

```
173
                 return ans-d;
174
            }
175
            if (!ina && inb)
176
                 const Point p=circ.inter(ab)[0];
177
178
                 const long double ans=((p-circ.c)^(b-circ.c))/2;
179
                 const long double th=(a-circ.c).ang(p-circ.c);
                 const long double d=circ.r*circ.r*th/2;
180
181
                 if ((a-circ.c).toleft(b-circ.c)==1) return ans+d;
182
                 return ans-d;
183
            }
             const auto p=circ.inter(ab);
184
185
            if (p.size()==2 && Segment{a,b}.dis(circ.c)<=circ.r+eps)</pre>
186
187
                 const long double ans=((p[0]-circ.c)^(p[1]-circ.c))/2;
188
                           const long double th1=(a-circ.c).ang(p[0]-circ.c),th2=(b-
circ.c).ang(p[1]-circ.c);
189
                 const long double d1=circ.r*circ.r*th1/2,d2=circ.r*circ.r*th2/2;
190
                 if ((a-circ.c).toleft(b-circ.c)==1) return ans+d1+d2;
191
                 return ans-d1-d2;
192
            }
193
            const long double th=(a-circ.c).ang(b-circ.c);
194
             if ((a-circ.c).toleft(b-circ.c)==1) return circ.r*circ.r*th/2;
195
             return -circ.r*circ.r*th/2;
196
         };
197
198
         long double ans=0;
199
         for (size t i=0;i<poly.p.size();i++)</pre>
200
         {
201
             const Point a=poly.p[i],b=poly.p[poly.nxt(i)];
             ans+=cal(circ.a.b):
202
203
         }
204
         return ans;
205 }
判断多条线段是否有交点
1 // 判断多条线段是否有交点
2 // 扫描线, 复杂度 0(nlogn)
3 bool segs_inter(const vector<Segment> &segs)
4 {
5
      if (segs.empty()) return false;
6
      using seq t=tuple<point t,int,Segment>;
7
      const auto segcmp=[](const seg t &u, const seg t &v)
8
      {
9
           const auto [u0,u1,u2]=u;
10
            const auto [v0,v1,v2]=v;
11
            if (abs(u0-v0)<=eps) return make_pair(u1,u2)<make_pair(v1,v2);</pre>
12
            return u0<v0-eps;</pre>
13
       };
14
       vector<seq t> seq;
15
       for (auto seg:segs)
16
17
            if (seg.a.x>seg.b.x+eps) swap(seg.a,seg.b);
18
            seq.push_back({seg.a.x,0,seg});
19
            seq.push_back({seg.b.x,1,seg});
20
       }
```

```
21
        sort(seq.begin(),seq.end(),seqcmp);
22
        point t x now;
23
        auto cmp=[&](const Segment &u, const Segment &v)
24
25
            if (abs(u.a.x-u.b.x) \le eps \mid abs(v.a.x-v.b.x) \le eps) return u.a.y \le v.a.y = eps;
26
                     return ((x_now-u.a.x)*(u.b.y-u.a.y)+u.a.y*(u.b.x-u.a.x))*(v.b.x-
v.a.x < ((x now-v.a.x)*(v.b.y-v.a.y)+v.a.y*(v.b.x-v.a.x))*(u.b.x-u.a.x)-eps;
27
        };
28
        multiset<Segment,decltype(cmp)> s{cmp};
29
        for (const auto [x,o,seg]:seq)
30
31
            x_now=x;
32
            const auto it=s.lower_bound(seg);
33
            if (o==0)
34
35
                if (it!=s.end() && seg.is inter(*it)) return true;
36
                if (it!=s.begin() && seg.is_inter(*prev(it))) return true;
37
                s.insert(seg);
38
            }
39
           else
40
            {
41
              if (next(it)!=s.end() && it!=s.begin() && (*prev(it)).is inter(*next(it)))
return true:
42
                s.erase(it);
43
           }
44
        }
45
        return false;
46 }
半平面交
1 // 半平面交
2 // 排序增量法, 复杂度 O(nlogn)
3 // 输入与返回值都是用直线表示的半平面集合
4 vector<Line> halfinter(vector<Line> l, const point_t lim=1e9)
5 {
         const auto check=[](const Line &a,const Line &b,const Line &c){return
a.toleft(b.inter(c))<0;};</pre>
      // 无精度误差的方法,但注意取值范围会扩大到三次方
8
      /*const auto check=[](const Line &a,const Line &b,const Line &c)
9
      {
10
                 const Point p=a.v*(b.v^c.v), q=b.p*(b.v^c.v)+b.v*(c.v^(b.p-c.p))-
a.p*(b.v^c.v);
11
            return p.toleft(q)<0;</pre>
12
       };*/
13
        l.push\_back(\{\{-lim,0\},\{0,-1\}\}); l.push\_back(\{\{0,-lim\},\{1,0\}\});
14
        l.push_back({{lim,0},{0,1}}); l.push_back({{0,lim},{-1,0}});
15
        sort(l.begin(),l.end());
16
       deque<Line> q;
17
        for (size_t i=0;i<l.size();i++)</pre>
18
19
            if (i>0 \&\& l[i-1].v.toleft(l[i].v)==0 \&\& l[i-1].v*l[i].v>eps) continue;
20
           while (q.size()>1 && check(l[i],q.back(),q[q.size()-2])) q.pop back();
21
           while (q.size()>1 && check(l[i],q[0],q[1])) q.pop_front();
22
            if (!q.empty() && q.back().v.toleft(l[i].v)<=0) return vector<Line>();
23
            q.push back(l[i]);
24
       }
```

```
25
       while (q.size()>1 \&\& check(q[0],q.back(),q[q.size()-2])) q.pop back();
26
        while (q.size()>1 \&\& check(q.back(),q[0],q[1])) q.pop_front();
27
        return vector<Line>(q.begin(),q.end());
28 }
圆面积并
1 // 圆面积并
2 // 轮廓积分, 复杂度 0(n^2logn)
3 // ans[i] 表示被至少覆盖了 i+1 次的区域的面积
4 vector<long double> area_union(const vector<Circle> &circs)
5 {
6
       const size_t siz=circs.size();
7
      using arc t=tuple<Point,long double,long double,long double>;
8
      vector<vector<arc t>> arcs(siz);
9
       const auto eq=[](const arc_t &u,const arc_t &v)
10
11
            const auto [u1,u2,u3,u4]=u;
12
            const auto [v1,v2,v3,v4]=v;
13
            return u1==v1 && abs(u2-v2)<=eps && abs(u3-v3)<=eps && abs(u4-v4)<=eps;
14
       };
15
16
       auto cut_circ=[&](const Circle &ci,const size_t i)
17
18
            vector<pair<long double,int>> evt;
19
            evt.push_back({-PI,0}); evt.push_back({PI,0});
20
            int init=0;
21
            for (size_t j=0;j<circs.size();j++)</pre>
22
23
                if (i==j) continue;
24
                const Circle &cj=circs[j];
25
                if (ci.r<cj.r-eps && ci.relation(cj)>=3) init++;
26
                const auto inters=ci.inter(cj);
             if (inters.size()==1) evt.push_back({atan2l((inters[0]-ci.c).y,(inters[0]-
ci.c).x),0});
28
                if (inters.size()==2)
29
                {
30
                    const Point dl=inters[0]-ci.c,dr=inters[1]-ci.c;
31
                    long double argl=atan2l(dl.y,dl.x),argr=atan2l(dr.y,dr.x);
32
                    if (abs(argl+PI)<=eps) argl=PI;</pre>
33
                    if (abs(argr+PI)<=eps) argr=PI;</pre>
34
                    if (argl>argr+eps)
35
                        evt.push_back({argl,1}); evt.push_back({PI,-1});
36
37
                        evt.push back({-PI,1}); evt.push back({argr,-1});
38
                    }
39
                    else
40
                    {
41
                        evt.push_back({argl,1});
42
                        evt.push_back({argr,-1});
43
                    }
44
                }
45
46
            sort(evt.begin(),evt.end());
47
            int sum=init;
48
            for (size_t i=0;i<evt.size();i++)</pre>
49
            {
```

```
50
                sum+=evt[i].second;
51
                                           if
                                                 (abs(evt[i].first-evt[i+1].first)>eps)
arcs[sum].push_back({ci.c,ci.r,evt[i].first,evt[i+1].first});
52
                if (abs(evt[i+1].first-PI)<=eps) break;</pre>
53
            }
54
       };
55
56
        const auto oint=[](const arc t &arc)
57
58
            const auto [cc,cr,l,r]=arc;
59
            if (abs(r-l-PI-PI)<=eps) return 2.0l*PI*cr*cr;</pre>
            return cr*cr*(r-l)+cc.x*cr*(sin(r)-sin(l))-cc.y*cr*(cos(r)-cos(l));
60
61
       };
62
63
       for (size_t i=0;i<circs.size();i++)</pre>
64
65
            const auto &ci=circs[i];
66
            cut_circ(ci,i);
67
        }
68
        vector<long double> ans(siz);
69
        for (size_t i=0;i<siz;i++)</pre>
70
71
            long double sum=0;
72
            sort(arcs[i].begin(),arcs[i].end());
73
            int cnt=0;
74
            for (size_t j=0;j<arcs[i].size();j++)</pre>
75
76
              if (j>0 && eq(arcs[i][j],arcs[i][j-1])) arcs[i+(++cnt)].push_back(arcs[i]
[j]);
77
                else cnt=0,sum+=oint(arcs[i][j]);
78
            }
79
            ans[i]=sum/2;
80
81
        return ans;
82 }
多边形面积并
1 // 多边形面积并
2 // 轮廓积分, 复杂度 O(n^2logn), n 为边数
3 // ans[i] 表示被至少覆盖了 i+1 次的区域的面积
4 vector<long double> area_union(const vector<Polygon> &polys)
5 {
6
       const size t siz=polys.size();
7
      vector<vector<pair<Point,Point>>> segs(siz);
       const auto check=[](const Point &u,const Segment &e){return !((u<e.a && u<e.b)
|| (u>e.a && u>e.b));};
10
       auto cut_edge=[&](const Segment &e,const size_t i)
11
12
            const Line le{e.a,e.b-e.a};
13
            vector<pair<Point,int>> evt;
14
            evt.push_back({e.a,0}); evt.push_back({e.b,0});
15
            for (size_t j=0;j<polys.size();j++)</pre>
16
17
                if (i==j) continue;
18
                const auto &pj=polys[j];
```

```
19
                 for (size_t k=0; k<pj.p.size(); k++)</pre>
20
21
                     const Segment s={pj.p[k],pj.p[pj.nxt(k)]};
22
                     if (le.toleft(s.a)==0 \&\& le.toleft(s.b)==0)
23
24
                         evt.push_back({s.a,0});
25
                         evt.push back({s.b,0});
26
                     }
27
                     else if (s.is_inter(le))
28
                     {
29
                         const Line ls{s.a,s.b-s.a};
30
                         const Point u=le.inter(ls);
31
                         if (le.toleft(s.a)<0 \&\& le.toleft(s.b)>=0) evt.push_back(\{u,-1\});
32
                         else if (le.toleft(s.a)>=0 & le.toleft(s.b)<0) evt.push back(\{u,1\});
33
                     }
                 }
34
35
            }
36
            sort(evt.begin(),evt.end());
37
            if (e.a>e.b) reverse(evt.begin(),evt.end());
38
            int sum=0;
39
            for (size_t i=0;i<evt.size();i++)</pre>
40
            {
41
                 sum+=evt[i].second;
42
                 const Point u=evt[i].first,v=evt[i+1].first;
43
                 if (!(u==v) \& check(u,e) \& check(v,e)) segs[sum].push_back({u,v});
44
                 if (v==e.b) break;
45
            }
46
        };
47
48
        for (size t i=0;i<polys.size();i++)</pre>
49
50
            const auto &pi=polys[i];
51
            for (size_t k=0; k<pi.p.size(); k++)</pre>
52
53
                 const Segment ei={pi.p[k],pi.p[pi.nxt(k)]};
54
                 cut_edge(ei,i);
55
            }
56
57
        vector<long double> ans(siz);
58
        for (size_t i=0;i<siz;i++)</pre>
59
60
            long double sum=0;
61
            sort(segs[i].begin(),segs[i].end());
62
            int cnt=0;
63
            for (size t j=0;j<segs[i].size();j++)</pre>
64
65
                 if (j>0 \&\& segs[i][j]==segs[i][j-1]) segs[i+(++cnt)].push_back(segs[i])
[j]);
66
                 else cnt=0,sum+=segs[i][j].first^segs[i][j].second;
67
            }
68
            ans[i]=sum/2;
69
        }
70
        return ans;
71 }
```

点集形成的最小最大三角形

```
1 // 点集形成的最小最大三角形
2 // 极角序扫描线,复杂度 O(n^2logn)
3 // 最大三角形问题可以使用凸包与旋转卡壳做到 0(n^2)
4 pair<point_t,point_t> minmax_triangle(const vector<Point> &vec)
5 {
6
              if (vec.size()<=2) return {0,0};</pre>
7
              vector<pair<int,int>> evt;
8
              evt.reserve(vec.size()*vec.size());
9
              point t maxans=0, minans=numeric limits<point t>::max();
10
                for (size_t i=0;i<vec.size();i++)</pre>
11
12
                         for (size_t j=0;j<vec.size();j++)</pre>
13
14
                                 if (i==j) continue;
15
                                 if (vec[i]==vec[j]) minans=0;
16
                                 else evt.push back({i,j});
17
                         }
18
19
                sort(evt.begin(),evt.end(),[&](const pair<int,int> &u,const pair<int,int> &v)
20
21
                         const Point du=vec[u.second]-vec[u.first],dv=vec[v.second]-vec[v.first];
22
                         return argcmp()({du.y,-du.x},{dv.y,-dv.x});
23
                });
24
                vector<size_t> vx(vec.size()),pos(vec.size());
25
                for (size_t i=0;i<vec.size();i++) vx[i]=i;</pre>
26
                sort(vx.begin(),vx.end(),[&](int x,int y){return vec[x]<vec[y];});</pre>
27
                for (size_t i=0;i<vx.size();i++) pos[vx[i]]=i;</pre>
28
                for (auto [u,v]:evt)
29
                {
30
                         const size t i=pos[u], j=pos[v];
31
                         const size_t l=min(i,j),r=max(i,j);
32
                         const Point vecu=vec[u],vecv=vec[v];
33
                         if (l>0) minans=min(minans,abs((vec[vx[l-1]]-vecu)^(vec[vx[l-1]]-vecv)));
34
                        if (r<vx.size()-1) minans=min(minans,abs((vec[vx[r+1]]-vecu)^(vec[vx[r+1]]-</pre>
vecv)));
                                                                      \max = \max(\{\max, abs((vec[vx[0]] - vecu)^(vec[vx[0]] - vecu)^(vec[vx[0]] - vecu)^(vec[vx[0]]) - vecu)^(vec[vx[0]] - vecu)^(vec[vx[0
vecv)),abs((vec[vx.back()]-vecu)^(vec[vx.back()]-vecv))});
                         if (i<j) swap(vx[i],vx[j]),pos[u]=j,pos[v]=i;</pre>
36
37
                }
38
                return {minans,maxans};
39 }
点集的凸包
1 // 点集的凸包
2 // Andrew 算法, 复杂度 O(nlogn)
3 Convex convexhull(vector<Point> p)
4 {
5
              vector<Point> st;
6
              if (p.empty()) return Convex{st};
7
              sort(p.begin(),p.end());
8
              const auto check=[](const vector<Point> &st,const Point &u)
9
10
                         const auto back1=st.back(),back2=*prev(st.end(),2);
11
                         return (back1-back2).toleft(u-back1)<=0;</pre>
12
                };
13
                for (const Point &u:p)
```

```
14
       {
15
           while (st.size()>1 && check(st,u)) st.pop_back();
16
           st.push_back(u);
17
18
       size_t k=st.size();
19
       p.pop_back(); reverse(p.begin(),p.end());
20
       for (const Point &u:p)
21
22
           while (st.size()>k && check(st,u)) st.pop_back();
23
           st.push_back(u);
24
25
       st.pop_back();
26
       return Convex{st};
27 }
给定三点求圆心
1 void cal(Point& a, Point& b, Point& c){ //圆上三点定圆心
2
      double al=b.x-a.x, bl=b.y-a.y, cl=(al*al+b1*b1)/2;
3
      double a2=c.x-a.x, b2=c.y-a.y, c2=(a2*a2+b2*b2)/2;
4
      double d = a1*b2-a2*b1;
5
      X = a.x + (c1*b2-c2*b1)/d;
6
      Y = a.y + (a1*c2-a2*c1)/d;
7
      r=dis2(a);
8 }
```