

WODEN: A CUDA-enabled package to simulate low-frequency radio interferometric data

Jack L. B. Line^{1, 2}

¹ International Centre for Radio Astronomy Research, Curtin University, Perth, WA 6845, Australia
² ARC Centre of Excellence for All Sky Astrophysics in 3 Dimensions (ASTRO 3D)

DOI: [10.21105/joss.03676](https://doi.org/10.21105/joss.03676)

Software

- [Review](#) ↗
- [Repository](#) ↗
- [Archive](#) ↗

Editor: [Dan Foreman-Mackey](#) ↗

Reviewers:

- [@plapant](#)
- [@mkolopanis](#)

Submitted: 21 July 2021

Published: 14 December 2021

License

Authors of papers retain copyright and release the work under a Creative Commons Attribution 4.0 International License ([CC BY 4.0](#)).

Summary

WODEN is designed to simulate the response of a class of telescope known as an interferometer, producing output “visibilities” for a given astrophysical sky model. Simulated observations allow us to test other software packages that are designed to calibrate and analyse real interferometric data, including verifying expected behaviour with known inputs, and trialling new sky modelling techniques. The WODEN sky model can be specified in dirac-delta like functions on the sky (known in the field as “point sources”) elliptical Gaussian models, or built out of “shapelet” basis functions (allowing complicated morphologies to be created). Users are able to input a bespoke layout for the interferometer, vary a number of observational parameters including time of day, length of observation and frequency coverage, and select from a number of predefined primary beams which encode the response of the receiving elements of an interferometer. This allows simulations of a number of telescopes to be undertaken. WODEN works with all Stokes I, Q, U, V sky polarisations, simulating telescopes with dual linear polarisations.

The core functionality of WODEN is written in CUDA as interferometric simulations are computationally intensive but embarrassingly parallel. The compute performance of CUDA allows for large-scale simulations to be run including emission from all directions in the sky. This is paramount for interferometers with a widefield of view such as the Murchison Widefield Array (MWA, [Tingay et al. \(2013\)](#)). A Python wrapper is used to take advantage of community packages such as [astropy](#) [Astropy Collaboration et al. \(2018\)](#), and to present a user-friendly interface to WODEN. Those simulating MWA observations can use the MWA `metafits` file to quickly feed in observational parameters to WODEN to match real data.

Statement of need

An interferometer creates visibilities V by cross-correlating signals detected between pairs of antennas or dishes (baselines), described by coordinates u, v, w . Each visibility is sensitive to the entire sky, directions of which we describe by the direction cosines l, m, n . The full integral can be discretised as

$$V(u_i, v_i, w_i) = \sum_j \mathcal{B}(l_j, m_j) I(l_j, m_j) \exp[-2\pi i(u_i l_j + v_i m_j + w_i(n_j - 1))],$$

where u_i, v_i, w_i are the visibility coordinates of the i^{th} baseline, l_j, m_j, n_j is the sky position of the j^{th} component in the sky model, $I(l_j, m_j)$ is the flux density of that component, and $\mathcal{B}(l_j, m_j)$ the instrument beam pattern.

36 For a telescope like the MWA, the primary beam $\mathcal{B}(l, m)$ is a complicated pattern on the sky,
37 which is sensitive to emission from directly overhead to all the way down to the horizon. To
38 truly capture the effects of astrophysical foregrounds we therefore have to simulate the entire
39 sky. The MWA Fully Embedded Element (FEE, [Sokolowski et al. \(2017\)](#)) model is currently
40 the most accurate representation of the MWA primary beam, and is incorporated into WODEN.

41 Under a formalism like the above, that splits the sky into discrete points, pushing $j \geq 25 \times 10^6$
42 can be required to achieve the angular resolution required. Furthermore, u, v, w are time
43 and frequency dependent, so to sample in frequency of order 500 times and 100 samples in
44 time, there are of order 10^{12} visibility calculations to make. This makes CUDA acceleration
45 paramount.

46 Alternative approaches to interferometric simulations exist, such as [pyuvsim](#) (which sacrifices
47 speed for excellent precision), and [RIMEz](#) (which decomposes the sky into spherical harmonics
48 rather than discrete points). WODEN was designed with the Australian MWA Epoch of Reion-
49 isation (EoR) processing pipeline in mind, which uses a calibration and foreground removal
50 software called the RTS ([Mitchell et al., 2008](#)) in search of signals from the very first stars
51 (see [Yoshiura et al. \(2021\)](#) for a recent use of this pipeline). The RTS creates a sky model
52 using the same formalism above, however the code is not optimised enough to handle the
53 volume of sources to simulate the entire sky. To test the RTS method of sky generation,
54 we therefore needed a fast and discretised method. Another excellent CUDA accelerated
55 simulation package, [OSKAR](#), addresses these two points. However, the RTS also generates
56 parts of the sky model via shapelets (see [Line et al. \(2020\)](#) for an overview), which OSKAR
57 cannot. Furthermore, in real data, the precession of the Earth's rotational axis causes sources
58 to move from the sky coordinates as specified in the RA, DEC J2000 coordinate system. The
59 RTS is designed to undo this precession, and so a simulation fed into the RTS should *contain*
60 precession. WODEN adds in this precession using the same method as the RTS to be consistent.
61 This unique combination of CUDA, shapelet foregrounds, the MWA FEE primary beam, along
62 with source precession, created the need for WODEN. These effects should not preclude other
63 calibration packages from using WODEN outputs however, meaning WODEN is not limited to
64 feeding data into the RTS alone.

65 Example application

66 In [Line et al. \(2020\)](#), we compared two methods to model Fornax A: a combination of point
67 and elliptical Gaussians, compared to shapelets (see [Figure 1](#)). We were able to quickly
68 compare the computational efficiency of the methods using a desktop, and comment on
69 their respective strengths and weaknesses in regard to foreground removal for EoR purposes.
70 Furthermore, as we could control the simulations, we could compare the methods in the
71 absence of other processing systematics that are present in the real data from the MWA,
72 which dominated the comparison when using the RTS alone.

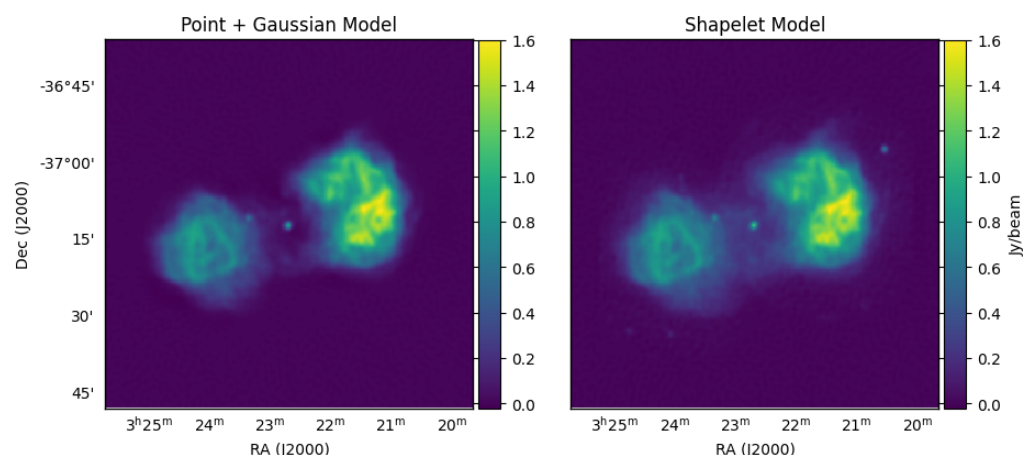


Figure 1: Two methods to simulate Fornax A visibilities are compared here (both imaged using WSClean (Offringa et al., 2014; Offringa & Smirnov, 2017)), with point and elliptical Gaussians on the left, and shapelets on the right.

Documentation

The documentation for WODEN can be found [here on readthedocs](#), including a detailed installation guide, ways to test a local installation, details of the calculations WODEN makes under the hood, and worked examples, which are also included in the github repo.

Acknowledgements

I acknowledge direct contributions from Tony Farlie (who taught me how pointer arithmetic works in C) and indirect contributions from Bart Pindor and Daniel Mitchell (through their work in the RTS and through advising me on CUDA). I'd like to thank Chris Jordan who acted as a sounding board as I learnt C and CUDA.

This research was supported by the Australian Research Council Centre of Excellence for All Sky Astrophysics in 3 Dimensions (ASTRO 3D), through project number CE170100013.

References

- Astropy Collaboration, Price-Whelan, A. M., Sipőcz, B. M., Günther, H. M., Lim, P. L., Crawford, S. M., Conseil, S., Shupe, D. L., Craig, M. W., Dencheva, N., Ginsburg, A., VanderPlas, J. T., Bradley, L. D., Pérez-Suárez, D., de Val-Borro, M., Aldcroft, T. L., Cruz, K. L., Robitaille, T. P., Tollerud, E. J., ... Astropy Contributors. (2018). The Astropy Project: Building an Open-science Project and Status of the v2.0 Core Package. *156*(3), 123. <https://doi.org/10.3847/1538-3881/aabc4f>
- Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., Greenfield, P., Droettboom, M., Bray, E., Aldcroft, T., Davis, M., Ginsburg, A., Price-Whelan, A. M., Kerzendorf, W. E., Conley, A., Crighton, N., Barbary, K., Muna, D., Ferguson, H., Grollier, F., Parikh, M. M., Nair, P. H., ... Streicher, O. (2013). Astropy: A community Python package for astronomy. *558*, A33. <https://doi.org/10.1051/0004-6361/201322068>

- 96 Line, J. L. B., Mitchell, D. A., Pindor, B., Riding, J. L., McKinley, B., Webster, R. L., Trott,
97 C. M., Hurley-Walker, N., & Offringa, A. R. (2020). Modelling and peeling extended
98 sources with shapelets: A Fornax A case study. *Publications of the Astronomical Society*
99 *Australia*, 37, 15. <https://doi.org/10.1017/PASA.2020.18>
- 100 Mitchell, D. A., Greenhill, L. J., Wayth, R. B., Sault, R. J., Lonsdale, C. J., Cappallo,
101 R. J., Morales, M. F., & Ord, S. M. (2008). Real-Time Calibration of the Murchison
102 Widefield Array. *IEEE Journal of Selected Topics in Signal Processing*, 2(5), 707–717.
103 <https://doi.org/10.1109/JSTSP.2008.2005327>
- 104 Offringa, A. R., McKinley, B., Hurley-Walker, N., Briggs, F. H., Wayth, R. B., Kaplan, D. L.,
105 Bell, M. E., Feng, L., Neben, A. R., Hughes, J. D., Rhee, J., Murphy, T., Bhat, N. D. R.,
106 Bernardi, G., Bowman, J. D., Cappallo, R. J., Corey, B. E., Deshpande, A. A., Emrich,
107 D., ... Williams, C. L. (2014). Wsclean: An implementation of a fast, generic wide-field
108 imager for radio astronomy. *Monthly Notices of the Royal Astronomical Society*, 444(1),
109 606–619. <https://doi.org/10.1093/mnras/stu1368>
- 110 Offringa, A. R., & Smirnov, O. (2017). An optimized algorithm for multiscale wideband
111 deconvolution of radio astronomical images. *Monthly Notices of the Royal Astronomical*
112 *Society*, 471(1), 301–316. <https://doi.org/10.1093/mnras/stx1547>
- 113 Sokolowski, M., Colegate, T., Sutinjo, A. T., Ung, D., Wayth, R., Hurley-Walker, N., Lenc, E.,
114 Pindor, B., Morgan, J., Kaplan, D. L., Bell, M. E., Callingham, J. R., Dwarakanath, K. S.,
115 For, B.-Q., Gaensler, B. M., Hancock, P. J., Hindson, L., Johnston-Hollitt, M., Kapińska,
116 A. D., ... Zheng, Q. (2017). Calibration and Stokes Imaging with Full Embedded Element
117 Primary Beam Model for the Murchison Widefield Array. *Publications of the Astronomical*
118 *Society Australia*, 34, e062. <https://doi.org/10.1017/pasa.2017.54>
- 119 Tingay, S. J., Goeke, R., Bowman, J. D., Emrich, D., Ord, S. M., Mitchell, D. A., Morales,
120 M. F., Booler, T., Crosse, B., Wayth, R. B., Lonsdale, C. J., Tremblay, S., Pallot, D.,
121 Colegate, T., Wicenec, A., Kudryavtseva, N., Arcus, W., Barnes, D., Bernardi, G., ...
122 Wyithe, J. S. B. (2013). The Murchison Widefield Array: The Square Kilometre Array
123 Precursor at Low Radio Frequencies. *Publications of the Astronomical Society Australia*,
124 30, e007. <https://doi.org/10.1017/pasa.2012.007>
- 125 Yoshiura, S., Pindor, B., Line, J. L. B., Barry, N., Trott, C. M., Beardsley, A., Bowman, J.,
126 Byrne, R., Chokshi, A., Hazelton, B. J., Hasegawa, K., Howard, E., Greig, B., Jacobs, D.,
127 Jordan, C. H., Joseph, R., Kolopanis, M., Lynch, C., McKinley, B., ... Zheng, Q. (2021).
128 A new MWA limit on the 21 cm power spectrum at redshifts 13–17. *Monthly Notices*
129 *to the Royal Astronomical Society*, 505(4), 4775–4790. <https://doi.org/10.1093/mnras/stab1560>
130