

PySDM v1: particle-based cloud modelling package for warm-rain microphysics and aqueous chemistry

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Introduction

PySDM is an open-source Python package for simulating the dynamics of particles undergoing condensational and collisional growth, interacting with a fluid flow and subject to chemical composition changes. It is intended to serve as a building block for process-level as well as computational-fluid-dynamics simulation systems involving representation of a continuous phase (air) and a dispersed phase (aerosol), with PySDM being responsible for representation of the dispersed phase. As of the major version 1 (v1), the development has been focused on atmospheric cloud physics applications, in particular on modelling the dynamics of particles immersed in moist air using the particle-based approach to represent the evolution of the size spectrum of aerosol/cloud/rain particles. The particle-based approach contrasts the more commonly used bulk and bin methods in which atmospheric particles are segregated into multiple categories (aerosol, cloud, rain) and their evolution is governed by deterministic dynamics solved on the same Eulerian grid as the dynamics of the continuous phase. Particle-based methods employ discrete computational (super) particles for modelling the dispersed phase. Each super particle is associated with a set of continuously-valued attributes evolving in Lagrangian manner. Such approach is particularly well suited for using probabilistic representation of particle collisional growth (coagulation) and for representing processes dependent on numerous particle attributes which helps to overcome the limitations of bulk and bin methods ([Morrison et al., 2020](#)).

The PySDM package core is a Pythonic high-performance implementation of the Super-Droplet Method (SDM) Monte-Carlo algorithm for representing collisional growth ([Shima et al., 2009](#)), hence the name. The SDM is a probabilistic alternative to the mean-field approach embodied by the Smoluchowski equation, for a comparative outline of both approaches see [Bartman & Arabas \(2021\)](#). In atmospheric aerosol-cloud interactions, particle collisional growth is responsible for formation of rain drops through collisions of smaller cloud droplets (warm-rain process) as well as for aerosol washout.

Besides collisional growth, PySDM includes representation of condensation/evaporation of water vapour on/from the particles. Furthermore, representation of dissolution and, if applicable, dissociation of trace gases (sulfur dioxide, ozone, hydrogen peroxide, carbon dioxide, nitric acid and ammonia) is included to model the subsequent aqueous-phase oxidation of the dissolved sulfur dioxide. Representation of the chemical processes follows the particle-based formulation of [Jaruga & Pawlowska \(2018\)](#).

43 The usage examples are built on top of four different environment classes included in PySDM
44 v1 and implementing common simple atmospheric cloud modelling frameworks: box, adiabatic
45 parcel, single-column and 2D prescribed flow kinematic models.

46 In addition, the package ships with tutorial code depicting how PySDM can be used from Julia
47 and Matlab using the PyCall.jl and the Matlab-bundled Python interface, respectively. Two
48 exporter classes are available as of time of writing enabling storage of particle attributes in
49 the VTK format and storage of gridded products in netCDF format.

50 Dependencies and supported platforms

51 PySDM essential dependencies are: NumPy, SciPy, Numba, Pint and ChemPy which are all
52 free and open-source software available via the PyPI platform. PySDM ships with a setup.py
53 file allowing installation using the pip package manager (i.e., `pip install git+https://`
54 `github.com/atmos-cloud-sim-uj/PySDM.git`).

55 PySDM has two alternative parallel number-crunching backends available: multi-threaded CPU
56 backend based on Numba (Lam et al., 2015) and GPU-resident backend built on top of Thru
57 stRTC (Yang, 2020). The optional GPU backend relies on proprietary vendor-specific CUDA
58 technology, the accompanying non-free software and drivers; ThrustRTC and CURandRTC
59 packages are released under the Anti-996 license.

60 The usage examples for Python were developed embracing the Jupyter interactive platform
61 allowing control of the simulations via web browser. All Python examples are ready for use
62 with the mybinder.org and the Google Colab platforms.

63 Continuous integration infrastructure used in the development of PySDM assures the targeted
64 full usability on Linux, macOS and Windows environments. Compatibility with Python versions
65 3.7 through 3.9 is maintained as of time of writing. Test coverage for PySDM is reported
66 using the codecov.io platform. Coverage analysis of the backend code requires execution
67 with JIT-compilation disabled for the CPU backend (e.g., using the `NUMBA_DISABLE_JIT=1`
68 environment variable setting). For the GPU backend, a purpose-built FakeThrust class is
69 shipped with PySDM which implements a subset of the ThrustRTC API and translates C++
70 kernels into equivalent Numba parallel Python code for debugging and coverage analysis.

71 The Pint dimensional analysis package is used for unit testing. It allows asserting on the
72 dimensionality of arithmetic expressions representing physical formulae. In order to enable JIT
73 compilation of the formulae for simulation runs, a purpose-built FakeUnitRegistry class
74 that mocks the Pint API reducing its functionality to SI prefix handling is used by default
75 outside of tests.

76 API in brief

77 In order to depict PySDM API with a practical example, the following listings provide sample
78 code roughly reproducing the Figure 2 from the Shima et al. (2009) paper in which the SDM
79 algorithm was introduced.

80 It is a coalescence-only set-up in which the initial particle size spectrum is exponential and
81 is deterministically sampled to match the condition of each super-droplet having equal initial
82 multiplicity, with the multiplicity denoting the number of real particles represented by a single
83 computational particle referred to as a super-droplet:

```
from PySDM.physics import si
from PySDM.initialisation.spectral_sampling import ConstantMultiplicity
```

```
from PySDM.physics.spectra import Exponential

n_sd = 2 ** 17
initial_spectrum = Exponential(
    norm_factor=8.39e12, scale=1.19e5 * si.um ** 3)
attributes = {}
spectral_sampling = ConstantMultiplicity(spectrum=initial_spectrum)
attributes['volume'], attributes['n'] = spectral_sampling.sample(n_sd=n_sd)
```

84 In the above snippet, the `si` is an instance of the `FakeUnitRegistry` class. The exponential
 85 distribution of particle volumes is sampled at 2^{17} points in order to initialise two key attributes
 86 of the super-droplets, namely their volume and multiplicity. Subsequently, a `Builder` object
 87 is created to orchestrate dependency injection while instantiating the `Particulator` class of
 88 `PySDM`:

```
import numpy as np
from PySDM.builder import Builder
from PySDM.environments import Box
from PySDM.dynamics import Coalescence
from PySDM.physics.coalescence_kernels import Golovin
from PySDM.backends import CPU
from PySDM.products import ParticlesVolumeSpectrum

radius_bins_edges = np.logspace(
    np.log10(10 * si.um), np.log10(5e3 * si.um), num=32)

builder = Builder(n_sd=n_sd, backend=CPU())
builder.set_environment(Box(dt=1 * si.s, dv=1e6 * si.m ** 3))
builder.add_dynamic(Coalescence(kernel=Golovin(b=1.5e3 / si.s)))
products = [ParticlesVolumeSpectrum(radius_bins_edges)]
particulator = builder.build(attributes, products)
```

89 The backend argument may be set to an instance of either `CPU` or `GPU` what translates to
 90 choosing the multi-threaded Numba-based backend or the ThrustRTC-based GPU-resident
 91 computation mode, respectively. The employed `Box` environment corresponds to a zero-
 92 dimensional framework (particle positions are neglected). The `SDM` Monte-Carlo coalescence
 93 algorithm is added as the only dynamic in the system (other dynamics available as of v1.3
 94 represent condensational growth, particle displacement, aqueous chemistry, ambient thermo-
 95 dynamics and Eulerian advection). Finally, the `build()` method is used to obtain an instance
 96 of the `Particulator` class which can then be used to control time-stepping and access sim-
 97 ulation state through the products registered with the builder. A minimal simulation example
 98 is depicted below with a code snippet and a resultant plot (Figure 1):

```
from PySDM.physics.constants import rho_w
from matplotlib import pyplot

for step in [0, 1200, 2400, 3600]:
    particulator.run(step - particulator.n_steps)
    pyplot.step(
        x=radius_bins_edges[:-1] / si.um,
        y=particulator.products['dv/dlnr'].get()[0] * rho_w/si.g,
        where='post', label=f"t = {step}s")

pyplot.xscale('log')
```

```
pyplot.xlabel('particle radius [ $\mu\text{m}$ ']')
pyplot.ylabel("dm/dlnr [g/m3/(unit dr/r)]")
pyplot.legend()
pyplot.show()
```

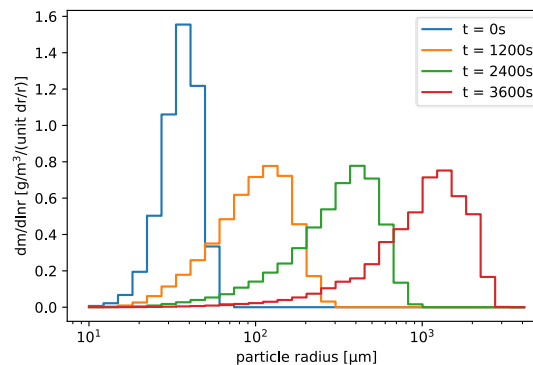


Figure 1: Sample plot generated with the code snippets included in the paper.

Usage examples

The PySDM examples are shipped in a separate package that can be installed with pip (pip install git+https://github.com/atmos-cloud-sim-uj/PySDM-examples.git) or conveniently experimented with using Colab or mybinder.org platforms (single-click launching badges included in the PySDM README file). The examples are based on setups from literature, and the package is structured using bibliographic labels (e.g., PySDM_examples.Shima_et_al_2009).

All examples feature a settings.py file with simulation parameters, a simulation.py file including logic analogous to the one presented in the code snippets above for handling composition of PySDM components using the Builder class, and a Jupyter notebook file with simulation launching code and basic result visualisation.

Box environment examples

The Box environment is the simplest one available in PySDM and the PySDM_examples package ships with two examples based on it. The first, is an extension of the code presented in the snippets in the preceding section and reproduces Fig. 2 from the seminal paper of Shima et al. (2009). Coalescence is the only process considered, and the probabilities of collisions of particles are evaluated using the Golovin additive kernel, which allows to compare the results with analytical solution of the Smoluchowski equation (included in the resultant plots).

The second example based on the Box environment, also featuring collision-only setup reproduces several figures from the work of Berry (1966) involving more sophisticated collision kernels representing such phenomena as the geometric sweep-out and the influence of electric field on the collision probability.

Adiabatic parcel examples

The Parcel environment shares the zero-dimensionality of Box (i.e., no particle physical coordinates considered), yet provides a thermodynamic evolution of the ambient air mimicking

124 adiabatic displacement of an air parcel in hydrostatically stratified atmosphere. Adiabatic cool-
125 ing during the ascent results in reaching supersaturation what triggers activation of aerosol
126 particles (condensation nuclei) into cloud droplets through condensation. All examples based
127 on the Parcel environment utilise the Condensation and AmbientThermodynamics dy-
128 namics.

129 The simplest example uses a monodisperse particle spectrum represented with a single super-
130 droplet and reproduces simulations described in Arabas & Shima (2017) where an ascent-
131 descent scenario is employed to depict hysteretic behaviour of the activation/deactivation
132 phenomena.

133 A polydisperse lognormal spectrum represented with multiple super-droplets is used in the
134 example based on the work of Yang et al. (2018). Presented simulations involve repeated
135 ascent-descent cycles and depict the evolution of partitioning between activated and unacti-
136 vated particles. Similarly, polydisperse lognormal spectra are used in the example based on
137 Lowe et al. (2019), where additionally each lognormal mode has a different hygroscopicity.
138 The Lowe et al. (2019) example additionally features representation of droplet surface tension
139 reduction by organics.

140 Finally, there are two examples featuring adiabatic parcel simulations involving representa-
141 tion of the dynamics of chemical composition of both ambient air and the droplet-dissolved
142 substances, in particular focusing on the oxidation of aqueous-phase sulfur. The examples
143 reproduce the simulations discussed in Kreidenweis et al. (2003) and in Jaruga & Pawlowska
144 (2018).

145 Kinematic (prescribed-flow) examples

146 Coupling of PySDM with fluid-flow simulation is depicted with both 1D and 2D prescribed-flow
147 simulations, both dependent on the PyMPDATA package (Bartman et al., 2021) implementing
148 the MPDATA advection algorithm. For a review on MPDATA, see e.g., Smolarkiewicz (2006).

149 Usage of the kinematic_1d environment is depicted in an example based on the work of
150 Shipway & Hill (2012), while the kinematic_2d environment is showcased with a Jupyter
151 notebook featuring an interactive user interface and allowing studying aerosol-cloud interac-
152 tions in drizzling stratocumulus setup based on the work of Arabas et al. (2015).

153 Figure 2 presents a snapshot from the 2D simulation described in detail in Arabas et al.
154 (2015) and works cited therein. Each plot depicts a 1.5 km by 1.5 km vertical slab of an
155 idealised atmosphere in which a prescribed single-eddy non-divergent flow is forced (updraft
156 in the left-hand part of the domain, downdraft in the right-hand part). The left plot shows
157 the distribution of aerosol particles in the air. The upper part of the domain is covered with a
158 stratocumulus-like cloud which formed on the aerosol particles above the flat cloud base at the
159 level where relative humidity goes above 100%. Within the cloud, the aerosol concentration is
160 thus reduced. The middle plot depicts the sizes of particles. Particles larger than 1 micrometre
161 in diameter are considered as cloud droplets, particles larger than 50 micrometres in diameter
162 are considered as drizzle (unlike in bin or bulk models, such categorisation is employed for
163 analysis only and not within the particle-based model formulation). Concentration of drizzle
164 particles forming through collisions is depicted in the right panel. A rain shaft forms in the
165 right part of the domain where the downward flow direction amplifies particle sedimentation.
166 Precipitating drizzle drops collide with aerosol particles washing out the sub-cloud aerosol.
167 Most of the drizzle drops evaporate before reaching the bottom of the domain depicting the
168 virga phenomenon and the resultant aerosol resuspension.

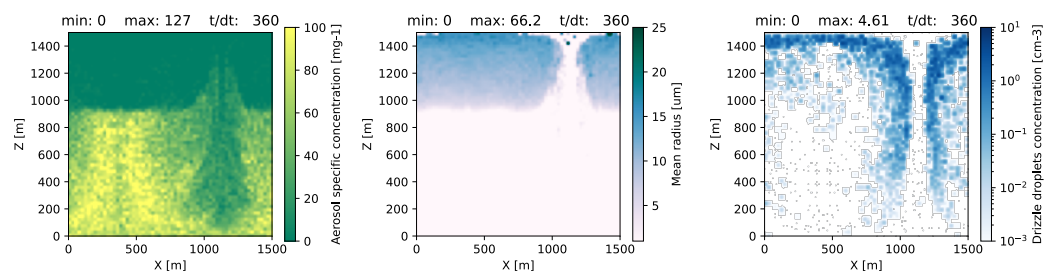


Figure 2: Results from a 2D prescribed-flow simulation using the Arabas et al. (2015) example.

Selected relevant recent open-source developments

The SDM algorithm implementations are part of the following open-source packages (of otherwise largely differing functionality):

- libcloudph++ in C++ (Arabas et al., 2015; Jaruga & Pawlowska, 2018) with Python bindings (Jarecka et al., 2015);
- SCALE-SDM in Fortran, (Sato et al., 2018);
- PALM LES in Fortran, (Maronga et al., 2020);
- LCM1D in Python/C, (Unterstrasser et al., 2020);
- Pencil Code in Fortran, (Brandenburg et al., 2021);
- NTLP in Fortran, (Richter et al., 2021).
- superdroplet in Python (Cython and Numba), C++, Fortran and Julia (<https://github.com/darochen/superdroplet>);

List of links directing to SDM-related files within the above projects' repositories is included in the PySDM README file.

Python packages for solving the dynamics of aerosol particles with discrete-particle (moving-sectional) representation of the size spectrum include (both depend on the Assimulo package for solving ODEs):

- pyrcel, (Rothenberg & Wang, 2017);
- PyBox, (Topping et al., 2018).

Summary

The key goal of the reported endeavour was to equip the cloud modelling community with a solution enabling rapid development and paper-review-level reproducibility of simulations (i.e., technically feasible without contacting the authors and possible to be set up within minutes) while being free from the two-language barrier commonly separating prototype and high-performance research code. The key advantages of PySDM stem from the characteristics of the employed Python language which enables high performance computational modelling without trading off such features as:

succinct syntax – the snippets presented in the paper are arguably close to pseudo-code;

portability depicted in PySDM with continuous integration Linux, macOS and Windows;

interoperability depicted in PySDM with Matlab and Julia usage examples requiring minimal amount of binding-specific code;

200 **multifaceted ecosystem** depicted in PySDM with one-click execution of Jupyter notebooks
 201 on mybinder.org and colab.research.google.com platforms;

202 **availability of tools for modern hardware** depicted in PySDM with the GPU backend.

203 PySDM together with a set of developed usage examples constitutes a tool for research on
 204 cloud microphysical processes, and for testing and development of novel modelling methods.
 205 PySDM is released under the GNU GPL v3 license.

206 Author contributions

207 PB had been the architect and lead developer of PySDM v1 with SA taking the role of main
 208 developer and maintainer over the time. PySDM 1.0 release accompanied PB's MSc thesis
 209 prepared under the mentorship of SA. MO contributed to the development of the condensation
 210 solver and led the development of relevant examples. GŁ contributed the initial draft of
 211 the aqueous-chemistry extension which was refactored and incorporated into PySDM under
 212 guidance from AJ. KG and BP contributed to the GPU backend. CS and AT contributed to
 213 the examples. OB contributed the VTK exporter. The paper was composed by SA and PB
 214 and is partially based on the content of the PySDM README file and PB's MSc thesis.

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