



# LEGWORK: A python package for computing the evolution and detectability of stellar-origin gravitational-wave sources with space-based detectors

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## Software

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## Summary

LEGWORK (LISA Evolution and Gravitational Wave Orbit Kit) is an open-source Python package for making predictions about stellar-origin gravitational wave sources and their detectability in LISA or other space-based gravitational wave detectors. LEGWORK can be used to evolve the orbits of sources due to gravitational wave emission, calculate gravitational wave strains (using post-Newtonian approximations), compute signal-to-noise ratios and visualise the results. It can be applied to a variety of potential sources, including binaries consisting of white dwarfs, neutron stars and black holes. Although we focus on double compact objects, in principle LEGWORK can be used for any system with a user-specified orbital evolution, such as those affected by a third object or gas drag. We optimised the package to make it efficient for use in population studies which can contain tens-of-millions of sources. We hope that LEGWORK will enable and accelerate future studies triggered by the rapidly growing interest in gravitational wave sources.

## Statement of need

The planned space-based gravitational wave detector LISA (Laser Interferometer Space Antenna) will present an entirely new view of gravitational waves by focusing on lower frequencies ( $10^{-5} < f/\text{Hz} < 10^{-1}$ ) than ground-based detectors. This will enable the study of many new source classes including mergers of supermassive black holes e.g.([Begelman et al., 1980](#); [Bellovary et al., 2019](#); [Klein et al., 2016](#)), extreme mass ratio inspirals e.g.([Babak et al., 2017](#); [Barack & Cutler, 2007](#); [Berti et al., 2006](#); [Christopher J. Moore et al., 2017](#)), and cosmological GW backgrounds e.g.([Bartolo et al., 2016](#); [Caldwell et al., 2019](#); [Caprini et al., 2016](#)). However, this frequency regime is also of interest for the detection of local stellar-mass binaries during their inspiral phase. LISA is expected to detect Galactic stellar-origin binaries containing combinations of white dwarfs, neutron stars, and black holes, ranging from the numerous double white dwarf population, to the rare but loud double black hole population.

The potential to detect stellar-origin sources with LISA has been studied in the past e.g.([Belczynski et al., 2010](#); [Liu, 2009](#); [Liu & Zhang, 2014](#); [Nelemans et al., 2001](#); [Nissanke et al., 2012](#); [Ruiter et al., 2010](#)). More recently, the direct detection of gravitational waves with ground-based detectors has led to renewed interest in this topic with many recent papers addressing the issue e.g.[[Christian & Loeb \(2017\)](#); [Kremer et al. \(2017\)](#); [Kremer et](#)

41 al. (2018); Korol et al. (2017); Korol et al. (2018); Korol et al. (2019); Korol et al. (2020);  
42 Lamberts et al. (2018); Lamberts et al. (2019); Fang et al. (2019); Andrews et al. (2020);  
43 Lau et al. (2020); Breivik, Coughlin, et al. (2020); Breivik, Mingarelli, et al. (2020); Roebber  
44 et al. (2020); Chen et al. (2020); Sesana et al. (2020); Shao+2021].

45 Each of these studies require making estimates of the signal-to-noise ratio of individual bi-  
46 nary systems and possibly the slow gravitational wave inspiral that lead to the present-day  
47 parameters. So far, most studies made use of custom made codes which have not been made  
48 publicly available.

49 We believe that the large renewed interest in LISA and the stellar-origin sources it may detect  
50 will lead to many more studies in the near future that would need similar computations.  
51 This leads to a significant amount of redundancy which, at best results in extra work for each  
52 individual and at worst leads to an increased chance of introducing mistakes and inconsistencies  
53 when translating the necessary expressions to software.

54 LEGWORK is a Python package designed to streamline the process of making predictions of  
55 LISA detection rates for stellar-origin binaries such that it is as fast, reliable and simple as  
56 possible. This goal makes LEGWORK unique among other implementations of gravitational-  
57 wave tools in the literature, which focus on a more broad coverage of the gravitational-wave  
58 spectrum and source classes, rather than an optimised approach for certain sources e.g.(C. J.  
59 Moore et al., 2015; Yi et al., 2021). With LEGWORK one can evolve the orbits of a binary  
60 or a collection of binaries and calculate their strain amplitudes for any range of frequency  
61 harmonics. One can compute the sensitivity curve for LISA or other future gravitational wave  
62 detectors (e.g. TianQin's curve, or that of a custom instrument) and use it to compute the  
63 signal-to-noise ratio of a collection of sources. Furthermore, LEGWORK provides tools to  
64 visualise all of the results with easy-to-use plotting functions. Finally, LEGWORK is fully  
65 tested to check for consistency in the derivations described below.

66 Specifically, we implement the expressions by Peters & Mathews (1963) and Peters (1964)  
67 for the evolution of binary orbits due to the emission of gravitational waves, equations for the  
68 strain amplitudes and signal-to-noise ratios of binaries from various papers (Barack & Cutler,  
69 2004; Cornish & Larson, 2003; Finn & Thorne, 2000; e.g. Flanagan & Hughes, 1998; C. J.  
70 Moore et al., 2015) and approximations for the LISA and TianQin sensitivity curves given in  
71 Robson et al. (2019) and Huang et al. (2020) respectively.

72 The open-source nature of the project means that new users as well as seasoned experts in the  
73 field can work together in a collaborative setting to consider new features and enhancements to  
74 the package as well as check the implementation. At the same time, with our thorough online  
75 documentation, derivations and tutorials, we hope LEGWORK can make this functionality  
76 more accessible to the broader scientific community.

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