

SISSO++: A C++ Implementation of the (Sure-Independence Screening and Sparsifying Operator Approach

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DOI: [10.21105/joss.03960](https://doi.org/10.21105/joss.03960)

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Submitted: 01 October 2021
Published: 09 December 2021

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Summary

The sure independence screening and sparsifying operator (SISSO) approach ([Ouyang et al., 2018](#)) is an algorithm belonging to the field of artificial intelligence and more specifically a combination of symbolic regression and compressed sensing. As a symbolic regression method, SISSO is used to identify mathematical functions, i.e. the descriptors, that best predict the target property of a data set. Furthermore, the compressed sensing aspect of SISSO, allows it to find sparse linear models using tens to thousands of data points. SISSO is introduced for both regression and classification tasks. In practice, SISSO first constructs a large and exhaustive feature space of trillions of potential descriptors by taking in a set of user-provided *primary features* as a dataframe, and then iteratively applying a set of unary and binary operators, e.g. addition, multiplication, exponentiation, and squaring, according to a user-defined specification. From this exhaustive pool of candidate descriptors, the ones most correlated to a target property are identified via sure-independence screening, from which the low-dimensional linear models with the lowest error are found via an ℓ_0 regularization.

Because symbolic regression generates an interpretable equation, it has become an increasingly popular concept across scientific disciplines ([Wang et al., 2019](#)), ([Neumann et al., 2020](#)), ([Udrescu & Tegmark, 2020](#)). A particular advantage of these approaches are their capability to model complex phenomena using relatively simple descriptors. SISSO has been used successfully in the past to model, explore, and predict important material properties, including the stability of different phases ([Bartel et al., 2018](#)), and ([Schleder et al., 2020](#)); the catalytic activity and reactivity ([Han et al., 2021](#)), ([W. Xu et al., 2021](#)), ([Andersen et al., 2019](#)), and ([Andersen & Reuter, 2021](#)); and glass transition temperatures ([Pilania et al., 2019](#)). Beyond regression problems, SISSO has also been used successfully to classify materials into different crystal prototypes ([Ouyang et al., 2019](#)), or whether a material crystallizes in its ground state as a perovskite ([Bartel et al., 2019](#)), or to determine whether a material is a topological insulator or not ([Cao et al., 2020](#)).

The SISSO++ package is an open-source (Apache-2.0 licence), modular, and extensible C++ implementation of the SISSO method with Python bindings. Specifically, SISSO++ applies this methodology for regression, log regression, and classification problems. Additionally, the library includes multiple Python functions to facilitate the post-processing, analyzing, and visualizing of the resulting models.

Statement of need

The main goal of the SISSO++ package is to provide a user-friendly, easily extendable version of the SISSO method for the scientific community. While both a FORTRAN (Ouyang, n.d.) and a Matlab (Gasper, n.d.) implementation of SISSO exist, their lack of native Python interfaces led to the development of multiple separate Python wrappers (C. Xu, n.d.), (Waroquiers, n.d.). This package looks to rectify this situation by providing an implementation that has native Python bindings and can be used both in a massively parallel environment for discovering the descriptors and on personal computing devices for analyzing and visualizing the results. For this reason, all computationally intensive tasks are written in C++ and support parallelization via MPI and OpenMP. Additionally, the Python bindings allow one to easily incorporate the methods into computational workflows and postprocess results. Furthermore, this enables integration of SISSO into existing machine-learning frameworks, e.g. scikit-learn (Pedregosa et al., 2011). The code is designed in a modular fashion, which simplifies the process of extending the code for other applications. Finally the project's extensive documentation and tutorials provide a good access point for new users of the method.

Features

The following features are implemented in SISSO++:

- A C++ library for using SISSO to find analytical models for a given problem
- Python bindings to be able to interface with the C++ objects in a Python environment
- Postprocessing tools for visualizing models and analyzing results using Matplotlib (Hunter, 2007)
- Access to solve an n -dimensional classification model using a combination of calculating the convex-hull overlap and a linear-support vector machine solver
- The ability to include non-linear parameters within features (e.g. $\exp(\alpha x)$ and $\ln(x + \beta)$) (Purcell et al., 2021)
- Complete API documentation defining all functions of the code
- Tutorials and Quick-Start Guides describing the basic functionality of the code

Code Dependencies

The following libraries are used by SISSO++:

- NLOpt (Johnson, n.d.) is used to optimize the non-linear bias and scale parameters within features
- The CLP library from Coin-OR (Forrest et al., n.d.) is used to find the number of points in the convex hull overlap region for classification problems
- LIBSVM (Chang & Lin, 2011) is used to find the linear-SVM model for classification problems
- Scikit-learn (Pedregosa et al., 2011), (Buitinck et al., 2013) is used to update the SVM model for classification problems within Python

- NumPy (Harris et al., 2020) and pandas (team, 2020), (McKinney, 2010) are used to represent the data structures within Python and perform array operations.
- seaborn (Waskom, 2021) and Matplotlib (Hunter, 2007) are used to generate the plots during postprocessing

Acknowledgements

The authors would like to thank Markus Rampp and Meisam Tabriz of the MPCDF for technical support. We would also like to thank Lucas Foppa, Jingkai Quan, Aakash Naik, James Dean, Timur Bazhurov, and Luigi Sbailò for testing and providing valuable feedback. T.P. would like to thank the Alexander von Humboldt Foundation for their support through the Alexander von Humboldt Postdoctoral Fellowship Program. This project was supported by TEC1p (the European Research Council (ERC) Horizon 2020 research and innovation programme, grant agreement No. 740233), BiGmax (the Max Planck Society's Research Network on Big-Data-Driven Materials-Science), and the FAIRmat consortium of the NFDI and FAIR-DI e.V. association.

References

- Andersen, M., Levchenko, S. V., Scheffler, M., & Reuter, K. (2019). Beyond Scaling Relations for the Description of Catalytic Materials. *ACS Catal.*, 9(4), 2752–2759. <https://doi.org/10.1021/acscatal.8b04478>
- Andersen, M., & Reuter, K. (2021). Adsorption Enthalpies for Catalysis Modeling through Machine-Learned Descriptors. *Acc. Chem. Res.*, 54(12), 2741–2749. <https://doi.org/10.1021/acs.accounts.1c00153>
- Bartel, C. J., Millican, S. L., Deml, A. M., Rumptz, J. R., Tumas, W., Weimer, A. W., Lany, S., Stevanović, V., Musgrave, C. B., & Holder, A. M. (2018). Physical descriptor for the Gibbs energy of inorganic crystalline solids and temperature-dependent materials chemistry. *Nat. Commun.*, 9(1), 1–10. <https://doi.org/10.1038/s41467-018-06682-4>
- Bartel, C. J., Sutton, C., Goldsmith, B. R., Ouyang, R., Musgrave, C. B., Ghiringhelli, L. M., & Scheffler, M. (2019). New tolerance factor to predict the stability of perovskite oxides and halides. *Sci. Adv.*, 5(2). <https://doi.org/10.1126/sciadv.aav0693>
- Buitinck, L., Louppe, G., Blondel, M., Pedregosa, F., Mueller, A., Grisel, O., Niculae, V., Prettenhofer, P., Gramfort, A., Grobler, J., Layton, R., VanderPlas, J., Joly, A., Holt, B., & Varoquaux, G. (2013). API design for machine learning software: Experiences from the scikit-learn project. *ECML PKDD Workshop: Languages for Data Mining and Machine Learning*, 108–122.
- Cao, G., Ouyang, R., Ghiringhelli, L. M., Scheffler, M., Liu, H., Carbogno, C., & Zhang, Z. (2020). Artificial intelligence for high-throughput discovery of topological insulators: The example of alloyed tetradymites. *Phys. Rev. Mater.*, 4(3), 034204. <https://doi.org/10.1103/PhysRevMaterials.4.034204>
- Chang, C.-C., & Lin, C.-J. (2011). LIBSVM: A library for support vector machines. *ACM Transactions on Intelligent Systems and Technology*, 2, 27:1–27:27.
- Forrest, J. J., Vigerske, S., Ralphs, T., Hafer, L., Fasano, J. P., Santos, H. G., Saltzman, M., Gassmann, H. I., Kristjansson, B., & King, A. (n.d.). *Coin-or/clp: Version 1.17.6*. <http://dx.doi.org/10.5281/zenodo.3748677>
- Gaspar, P. (n.d.). https://github.com/NREL/SISSORRegressor_MATLAB

- 119 Han, Z. K., Sarker, D., Ouyang, R., Mazheika, A., Gao, Y., & Levchenko, S. V. (2021). Single-
120 atom alloy catalysts designed by first-principles calculations and artificial intelligence. *Nat.*
121 *Commun.*, 12(1), 1–9. <https://doi.org/10.1038/s41467-021-22048-9>
- 122 Harris, C. R., Millman, K. J., Walt, S. J. van der, Gommers, R., Virtanen, P., Cournapeau,
123 D., Wieser, E., Taylor, J., Berg, S., Smith, N. J., Kern, R., Picus, M., Hoyer, S., Kerkwijk,
124 M. H. van, Brett, M., Haldane, A., Río, J. F. del, Wiebe, M., Peterson, P., ... Oliphant,
125 T. E. (2020). Array programming with NumPy. *Nature*, 585(7825), 357–362. <https://doi.org/10.1038/s41586-020-2649-2>
- 126
- 127 Hunter, J. D. (2007). Matplotlib: A 2D graphics environment. *Computing in Science &*
128 *Engineering*, 9(3), 90–95. <https://doi.org/10.1109/MCSE.2007.55>
- 129 Hunter, J. D. (2007). Matplotlib: A 2D graphics environment. *Computing in Science &*
130 *Engineering*, 9(3), 90–95. <https://doi.org/10.1109/MCSE.2007.55>
- 131 Johnson, S. G. (n.d.). *The NLOpt nonlinear-optimization package*. <http://github.com/stevengj/nlopt>
- 132
- 133 McKinney, Wes. (2010). Data Structures for Statistical Computing in Python. In Stéfan van
134 der Walt & Jarrod Millman (Eds.), *Proceedings of the 9th Python in Science Conference*
135 (pp. 56–61). <https://doi.org/10.25080/Majora-92bf1922-00a>
- 136 Neumann, P., Cao, L., Russo, D., Vassiliadis, V. S., & Lapkin, A. A. (2020). A new formulation
137 for symbolic regression to identify physico-chemical laws from experimental data. *Chem.*
138 *Eng. J.*, 387, 123412. <https://doi.org/10.1016/j.cej.2019.123412>
- 139 Ouyang, R. (n.d.). *GitHub - rouyang2017/SISSO: A data-driven method combining symbolic*
140 *regression and compressed sensing toward accurate & interpretable models*. Retrieved
141 September 2, 2021, from <https://github.com/rouyang2017/SISSO>
- 142 Ouyang, R., Ahmetcik, E., Carbogno, C., Scheffler, M., & Ghiringhelli, L. M. (2019). Simul-
143 taneous learning of several materials properties from incomplete databases with multi-task
144 SISSO. *J. Phys. Mater.*, 2(2), 024002. <https://doi.org/10.1088/2515-7639/ab077b>
- 145 Ouyang, R., Curtarolo, S., Ahmetcik, E., Scheffler, M., & Ghiringhelli, L. M. (2018). SISSO:
146 A compressed-sensing method for identifying the best low-dimensional descriptor in an
147 immensity of offered candidates. *Phys. Rev. Mater.*, 2(8), 083802. <https://doi.org/10.1103/PhysRevMaterials.2.083802>
- 148
- 149 Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., Blondel,
150 M., Prettenhofer, P., Weiss, R., Dubourg, V., Vanderplas, J., Passos, A., Cournapeau,
151 D., Brucher, M., Perrot, M., & Duchesnay, E. (2011). Scikit-learn: Machine learning in
152 Python. *Journal of Machine Learning Research*, 12, 2825–2830.
- 153 Pilania, G., Iverson, C. N., Lookman, T., & Marrone, B. L. (2019). Machine-Learning-Based
154 Predictive Modeling of Glass Transition Temperatures: A Case of Polyhydroxyalkanoate
155 Homopolymers and Copolymers. *J. Chem. Inf. Model.*, 59(12), 5013–5025. <https://doi.org/10.1021/acs.jcim.9b00807>
- 156
- 157 Purcell, T. A. R., Scheffler, M., Ghiringhelli, L. M., & Carbogno, C. (2021). Accelerating
158 Material-Space Exploration by Mapping Materials Properties via Artificial Intelligence:
159 The Case of the Lattice Thermal Conductivities. *In Preparation*.
- 160 Schleder, G. R., Acosta, C. M., & Fazzio, A. (2020). Exploring Two-Dimensional Materials
161 Thermodynamic Stability via Machine Learning. *ACS Appl. Mater. Interfaces*, 12(18),
162 20149–20157. <https://doi.org/10.1021/acsami.9b14530>
- 163 team, T. pandas development. (2020). *Pandas-dev/pandas: pandas (latest)* [Computer
164 software]. Zenodo. <https://doi.org/10.5281/zenodo.3509134>
- 165 Udrescu, S. M., & Tegmark, M. (2020). AI Feynman: A physics-inspired method for symbolic
166 regression. *Sci. Adv.*, 6(16). <https://doi.org/10.1126/sciadv.aay2631>

- 167 Wang, Y., Wagner, N., & Rondinelli, J. M. (2019). Symbolic regression in materials science.
168 *MRS Commun.*, 9(3), 793–805. <https://doi.org/10.1557/mrc.2019.85>
- 169 Waroquiers, D. (n.d.). *Python interface to the SISSO (sure independence screening and*
170 *sparsifying operator) method*. <https://github.com/Matgenix/pysisso>
- 171 Waskom, M. L. (2021). Seaborn: Statistical data visualization. *Journal of Open Source*
172 *Software*, 6(60), 3021. <https://doi.org/10.21105/joss.03021>
- 173 Xu, C. (n.d.). *SISSOkit*. <https://github.com/chuanqixu/SISSOkit>
- 174 Xu, W., Andersen, M., & Reuter, K. (2021). Data-Driven Descriptor Engineering and Refined
175 Scaling Relations for Predicting Transition Metal Oxide Reactivity. *ACS Catal.*, 11(2),
176 734–742. <https://doi.org/10.1021/acscatal.0c04170>

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