




medoutcon: Nonparametric efficient causal mediation analysis with machine learning in R

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Summary

Science is most often concerned with questions of *mechanism*. In myriad applications, only the portion of the causal effect of an exposure on an outcome through a particular pathway under study is of interest. The study of such path-specific, or mediation, effects has a rich history, first undertaken scientifically by [Wright \(1921\)](#) and [Wright \(1934\)](#). Today, the study of such effects has attracted a great deal of attention in statistics and causal inference, inspired by applications in disciplines ranging from epidemiology and vaccinology to psychology and economics. Examples include understanding the biological mechanisms by which vaccines causally alter infection risk ([Benkeser et al., 2021](#); [Hejazi et al., 2020](#)), assessing the effect of novel pharmacological therapies on substance abuse disorder relapse ([Hejazi et al., 2021](#); [Rudolph et al., 2020](#)), and evaluating the effects of housing vouchers on adolescent development ([Rudolph et al., 2021](#)). The `medoutcon` R package provides researchers in each of these disciplines, and in others, with the tools necessary to implement statistically efficient estimators of the *interventional* direct and indirect effects ([Díaz et al., 2020](#)) (for brevity, henceforth, (in)direct effects), a recently formulated set of causal effects robust to the presence of confounding of the mediator-outcome relationship by the exposure. In cases where such confounding is a nonissue, the interventional (in)direct effects ([VanderWeele et al., 2014](#)) reduce to the well-studied *natural* (in)direct effects ([Pearl, 2001](#); [Robins & Greenland, 1992](#)), for which `medoutcon` provides efficient estimators similar to those of [Zheng & van der Laan \(2012\)](#). By readily incorporating the use of machine learning in the estimation of nuisance parameters (through integration with the `s3` R package ([Coyle, Hejazi, Malenica, Phillips, & Sofrygin, 2021](#)) of the `tlverse` ecosystem ([van der Laan et al., 2022](#))), `medoutcon` incorporates state-of-the-art non/semi-parametric estimation techniques, facilitating their adoption in a vast array of settings.

Statement of Need

While there is demonstrable interest in causal mediation analysis in a large variety of disciplines, thoughtfully implementing data analysis strategies based on recent developments in this area is challenging. Contributions in the causal inference and statistics literature largely fall into two key areas. Broadly, the study of identification outlines novel causal effect parameters with properties desirable in real-world settings (e.g., the interventional effects, which can be learned under mediator-outcome confounding) and untestable assumptions under which a statistical functional corresponds to a causal estimand of interest. A complementary line of study develops non/semi-parametric efficiency theory for the statistical functionals outlined in the causal identification literature, allowing for their robust estimation with modern techniques from machine learning. Neither concerns itself with opening the door to applying these estimators in real-world data analyses. Moreover, the implementation of open source software

for efficient estimators of causal effects is complex – for such a task, the data scientist must be knowledgeable of causal inference, semiparametric statistical theory, machine learning, and the intersection of these disciplines, and that is to forego mention of research software engineering best practices, including, for example, unit/regression testing and automated continuous integration. The `medoutcon` R package is a free, open source implementation of non/semi-parametric efficient estimators of the natural and interventional (in)direct effects, providing data scientists in research and in industry with access to state-of-the-art statistical methodology for causal mediation analysis. Its estimators have been interrogated in simulation studies and applied in real-world data analyses. To the best of our knowledge, no other R package provides similarly convenient access to multiply robust, non/semi-parametric efficient estimators of causal mediation effects with a flexible interface to accommodate machine learning of nuisance parameters.

Natural and Interventional Causal Mediation Effects

To evaluate the causal effects of an exposure on an outcome through mediating pathways, let's consider a dataset of n units, where the observed data on a single unit is assumed to have been generated by a nonparametric structural equation model (NPSEM) (Pearl, 2009):

$$\begin{aligned} W &= f_W(U_W); A = f_A(W, U_A); Z = f_Z(W, A, U_Z); \\ M &= f_M(W, A, Z, U_M); Y = f_Y(W, A, Z, M, U_Y), \end{aligned}$$

where W are baseline (pre-exposure) covariates, $A \in \{0, 1\}$ is the (binary) exposure of interest, Z is an intermediate confounder of the mediator-outcome relationship and is affected by exposure A , M represents mediating variables, and Y is the outcome. This NPSEM admits an equivalent representation as a directed acyclic graph (or DAG), in which each variable is a node and dependencies are represented by directed paths between the nodes. The natural (in)direct effects cannot generally be identified (i.e., learned from the observed data) in the presence of intermediate confounding, so, for now, we make the simplifying assumption that the intermediate variable Z is absent. In this simple case, the population average treatment effect (ATE) – that is, the total effect of A on Y , comparing two exposure contrasts $\{a', a^*\}$ – may be decomposed into the natural direct effect (NDE) and the natural indirect effect (NIE) as

$$\mathbb{E}[Y(a') - Y(a^*)] = \underbrace{\mathbb{E}[Y(a', M(a')) - Y(a', M(a^*))]}_{\text{Indirect effect (through } M)} + \underbrace{\mathbb{E}[Y(a', M(a^*)) - Y(a^*, M(a^*))]}_{\text{Direct effect (not through } M)},$$

where the *counterfactual* variables $Y(\cdot)$ are *potential outcomes* (Hernán & Robins, 2021; Imbens & Rubin, 2015) – that is, $Y(a')$ is the value that the outcome would take when the exposure is set to level a' , possibly contrary to fact. Similarly, $M(a^*)$ is the value that the mediators would take when the exposure is set to level a^* , as the result of an intervention, for example. The NIE captures the effect of the exposure A on Y through the mediating variables M while the NDE captures the effect of A on Y through all other pathways. Robins & Greenland (1992) and Pearl (2001) independently studied this decomposition within the potential outcomes and NPSEM frameworks, respectively. In both cases, the NDE and NIE are derived from the ATE by introducing a decomposition term that deterministically sets the values of the exposure and mediators to differing values by the application of *static* interventions. As regards estimation, Tchetgen Tchetgen & Shpitser (2012) and Zheng & van der Laan (2012) outlined non/semi-parametric efficiency theory for developing estimators of the NDE and NIE and proposed efficient estimators of these causal quantities.

The presence of intermediate confounders Z often cannot be ruled out in real-world data analysis scenarios. Such post-exposure variables, which are affected by A and affect both M and Y , complicate efforts to disentangle the effect of A on Y through paths involving

M and other paths. Recognizing the limitations of the natural effects in these settings, [Didelez et al. \(2006\)](#), [Petersen et al. \(2006\)](#), [VanderWeele et al. \(2014\)](#), and [Rudolph et al. \(2017\)](#), among others, contributed to the development of the interventional (in)direct effects. Unlike the decomposition strategy that delineates the NDE and NIE, these effects require a more sophisticated approach to identification, relying upon *stochastic* interventions on the mediator(s), which require random draws from the mediators post-intervention distribution rather than the setting of fixed counterfactual values. Specifically, for the two exposure contrasts $\{a', a^*\}$, the effect of A on Y can be defined as the difference in expected outcome in the hypothetical worlds in which $(A, M) = (a', G_{a'})$ versus $(A, M) = (a^*, G_{a^*})$. Here, G_a denotes a random draw from the conditional distribution of M_a conditional on W , as defined by a stochastic intervention. The direct and indirect effects are defined as follows

$$\mathbb{E}[Y(a', G_{a'}) - Y(a^*, G_{a^*})] = \underbrace{\mathbb{E}[Y(a', G_{a'}) - Y(a', G_{a^*})]}_{\text{Indirect effect (through } M)} + \underbrace{\mathbb{E}[Y(a', G_{a^*}) - Y(a^*, G_{a^*})]}_{\text{Direct effect (not through } M)}.$$

Like the NDE, this interventional direct effect measures the effects through all paths avoiding the mediating variables. Analogous to the NIE, the interventional indirect effect measures the effect through paths involving the mediators. Note, however, that natural and interventional mediation effects have different interpretations. That is, the interventional indirect effect measures the effect of fixing the exposure at a' while setting the mediator to a random draw G_{a^*} (i.e., under an intervention setting the exposure to a^*) versus a random draw $G_{a'}$ (i.e., after setting the exposure to a'), given covariates W . Intuitively, the interventional effects remain identifiable under intermediate confounding since the stochastic intervention on the mediators breaks the relationship between Z and M . Prior to the work of [Díaz et al. \(2020\)](#), and contemporaneous developments by [Benkeser & Ran \(2021\)](#), non/semi-parametric efficiency theory for the interventional (in)direct effects was unavailable. Recently, a novel family of interventional effects, accommodating flexible stochastic interventions on the exposure, have been formulated ([Hejazi et al., 2021](#)).

medoutcon's Scope

Development of the medoutcon package began as a software accompaniment to the theoretical developments of [Díaz et al. \(2020\)](#) – where the investigations of these authors outlined efficient estimators of the interventional (in)direct effects, medoutcon implements these efficient estimators. Implemented in the R language and environment for statistical computing ([R Core Team, 2021](#)), medoutcon aims to provide a simple application user interface (API) for convenience in a variety of data analytic applications. Specifically, medoutcon – via a single, user-facing eponymous function medoutcon() – provides access to both one-step and targeted minimum loss (TML) estimators of these causal (in)direct effects. State-of-the-art machine learning algorithms, including ensemble modeling ([van der Laan et al., 2007](#)), may readily be used for the estimation of relevant nuisance parameters, through a design that tightly couples medoutcon with the s13 R package ([Coyle, Hejazi, Malenica, Phillips, & Sofrygin, 2021](#)). Cross-fitting is automatically incorporated, via the origami R package ([Coyle, Hejazi, Malenica, & Phillips, 2021](#); [Coyle & Hejazi, 2018](#)), in computing the efficient estimators, allowing for some common but restrictive regularity conditions to be relaxed ([Bickel et al., 1993](#); [Chernozhukov et al., 2017](#); [Zheng & van der Laan, 2011](#)).

Beyond implementing the interventional (in)direct effects, medoutcon additionally allows for the natural (in)direct effects to be estimated when intermediate confounders are omitted from the call to the medoutcon() function (i.e., by setting $Z = \text{NULL}$). This feature is based on a correspondence between the identifying statistical functionals of the natural and interventional (in)direct effects in the absence of intermediate confounding. In this simplified case, the efficient estimators of the interventional (in)direct effects formulated by [Díaz et al. \(2020\)](#) are analogous to the efficient estimators of the natural (in)direct effects formulated

104 by Zheng & van der Laan (2012). By supporting this case, medoutcon serves as a one-stop
105 tool for estimating these classical and popular causal mediation effects, allowing for practicing
106 data scientists and applied statisticians to deploy cutting-edge estimators of the natural and
107 interventional (in)direct effects through a unified API.

108 Availability

109 The medoutcon package is publicly available via [GitHub](#), with plans for submission to the
110 Comprehensive R Archive Network, pending the inclusion of its dependencies (sl3, in par-
111 ticular) in that repository. Use of the medoutcon package has been extensively documented
112 in the package's README, a vignette, and its [documentation website](#). Ongoing development
113 of the package incorporates research and data science software engineering best practices,
114 including a suite of unit tests and automated continuous integration checking.

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