

1. Common Types of Cubic Unit Cells

The main cubic unit cells in crystallography are:

1. Simple Cubic (SC)
2. Body-Centered Cubic (BCC)
3. Face-Centered Cubic (FCC)

There are also other unit cells in different crystal systems (tetragonal, hexagonal, etc.), but we'll focus on cubic cells first.

A. Simple Cubic (SC)

Easy Example

Think of SC as a stack of small marbles in a box:

- 1 marble at each corner
- No center or face marbles

Counting marbles (atoms):

$$8 \text{ corners} \times \frac{1}{8} = 1$$

Total atoms per SC unit cell = 1

Packing efficiency analogy: Only 52% of the box is filled, the rest is empty space.

◆ Theory / Formulas

1. Atoms in SC:

$$N_{\text{atoms}} = 8 \times \frac{1}{8} = 1$$

2. Edge length (a) vs. atomic radius (r):

$$a = 2r$$

3. Packing efficiency (APF):

$$\text{APF} = \frac{1 \cdot \frac{4}{3}\pi r^3}{(2r)^3} = 0.52 = 52\%$$

4. Examples: Polonium (Po), some simple metals

B. Body-Centered Cubic (BCC)

Easy Example

Think of BCC as a **cube-shaped gift box**:

- 1 gift at each corner → shared with 8 neighboring boxes → counts as 1/8 each
- 1 gift in the center → belongs entirely to your box

Counting gifts (atoms):

$$8 \times \frac{1}{8} + 1 = 2$$

Total atoms per BCC unit cell = 2

Packing efficiency analogy: 68% of the box is filled.

◆ Theory / Formulas

1. Atoms in BCC:

$$N_{\text{atoms}} = 8 \times \frac{1}{8} + 1 = 2$$

2. Edge length (a) vs. atomic radius (r):

Atoms touch along the **body diagonal**:

$$4r = a\sqrt{3} \quad \Rightarrow \quad a = \frac{4r}{\sqrt{3}}$$

3. Packing efficiency (APF): 68%

4. Examples: Fe, Cr, W

C. Face-Centered Cubic (FCC)

Easy Example

Think of FCC as **stacking oranges in a grocery box**:

- 1 orange at each corner → shared with 8 boxes → counts as 1/8 each
- 1 orange in the center of each face → shared with 2 boxes → counts as 1/2 each

Counting oranges (atoms):

$$8 \times \frac{1}{8} + 6 \times \frac{1}{2} = 4$$

Total atoms per FCC unit cell = 4

Packing efficiency analogy: 74% of the cube is filled with atoms, the rest is empty space.

◆ Theory / Formulas

1. Atoms in FCC:

$$N_{\text{atoms}} = 8 \times \frac{1}{8} + 6 \times \frac{1}{2} = 4$$

2. Edge length (a) vs. atomic radius (r):

Atoms touch along the face diagonal:

$$4r = a\sqrt{2} \quad \Rightarrow \quad a = 2\sqrt{2}r$$

3. Packing efficiency (APF): 74%

4. Examples: Cu, Al, Ag

2. Quick Comparison Table

Unit Cell	Atoms per Cell	Packing Efficiency	Touching Direction	Everyday Analogy	Examples
SC	1	52%	Edge	Single marbles	Po
BCC	2	68%	Body diagonal	Gift in box	Fe, Cr, W
FCC	4	74%	Face diagonal	Oranges in box	Cu, Al, Ag

3. Additional Theory

1. Packing Efficiency (APF):

$$\text{APF} = \frac{\text{Volume of atoms in the unit cell}}{\text{Volume of the unit cell}} \times 100$$

2. Relationship between edge length (a) and atomic radius (r):

Unit Cell	Formula
SC	$a = 2r$
BCC	$a = \frac{4r}{\sqrt{3}}$
FCC	$a = 2\sqrt{2}r$

3. Atoms sharing rules:

- Corner atom → 1/8th per cell
- Face atom → 1/2 per cell

- Body-center atom → 1 per cell

4. Packing efficiency significance:

- Higher APF → atoms are tightly packed → more stable structure
 - FCC > BCC > SC in packing efficiency and stability
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🌟 4. Everyday Analogies Recap

- SC → 1 marble in a box → 52% filled
 - BCC → gift in the center of a box → 68% filled
 - FCC → oranges stacked tightly → 74% filled
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✓ FCC Unit Cell Summary

- 8 corners × 1/8 = 1 atom
 - 6 faces × 1/2 = 3 atoms
 - Total = 4 atoms per unit cell
 - Packing efficiency = 74%
 - Example analogy: oranges stacked tightly
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✓ BCC Unit Cell Summary

- 8 corners × 1/8 = 1 atom
- 1 body-center atom = 1 atom
- Total = 2 atoms per unit cell
- Packing efficiency = 68%
- Example analogy: gift in a box