

# ☀ 1. Common Types of Cubic Unit Cells

The main cubic unit cells in crystallography are:

1. Simple Cubic (SC)
2. Body-Centered Cubic (BCC)
3. Face-Centered Cubic (FCC)

There are also other unit cells in different crystal systems (tetragonal, hexagonal, etc.), but we'll focus on cubic cells first.

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## A. Simple Cubic (SC)

### 🍊 Easy Example

Think of SC as a stack of small marbles in a box:

- 1 marble at each corner
- No center or face marbles

Counting marbles (atoms):

$$8 \text{ corners} \times \frac{1}{8} = 1$$

Total atoms per SC unit cell = 1

Packing efficiency analogy: Only 52% of the box is filled, the rest is empty space.

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### ◆ Theory / Formulas

1. Atoms in SC:

$$N_{\text{atoms}} = 8 \times \frac{1}{8} = 1$$

2. Edge length (a) vs. atomic radius (r):

$$a = 2r$$

3. Packing efficiency (APF):

$$\text{APF} = \frac{1 \cdot \frac{4}{3}\pi r^3}{(2r)^3} = 0.52 = 52\%$$

4. Examples: Polonium (Po), some simple metals
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## B. Body-Centered Cubic (BCC)

## 🍊 Easy Example

Think of BCC as a **cube-shaped gift box**:

- 1 gift at each corner → shared with 8 neighboring boxes → counts as 1/8 each
- 1 gift in the center → belongs entirely to your box

Counting gifts (atoms):

$$8 \times \frac{1}{8} + 1 = 2$$

Total atoms per BCC unit cell = 2

Packing efficiency analogy: 68% of the box is filled.

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### ◆ Theory / Formulas

#### 1. Atoms in BCC:

$$N_{\text{atoms}} = 8 \times \frac{1}{8} + 1 = 2$$

#### 2. Edge length (a) vs. atomic radius (r):

Atoms touch along the **body diagonal**:

$$4r = a\sqrt{3} \quad \Rightarrow \quad a = \frac{4r}{\sqrt{3}}$$

#### 3. Packing efficiency (APF): 68%

#### 4. Examples: Fe, Cr, W

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## C. Face-Centered Cubic (FCC)

## 🍊 Easy Example

Think of FCC as **stacking oranges in a grocery box**:

- 1 orange at each corner → shared with 8 boxes → counts as 1/8 each
- 1 orange in the center of each face → shared with 2 boxes → counts as 1/2 each

Counting oranges (atoms):

$$8 \times \frac{1}{8} + 6 \times \frac{1}{2} = 4$$

Total atoms per FCC unit cell = 4

Packing efficiency analogy: 74% of the cube is filled with atoms, the rest is empty space.

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### ◆ Theory / Formulas

### 1. Atoms in FCC:

$$N_{\text{atoms}} = 8 \times \frac{1}{8} + 6 \times \frac{1}{2} = 4$$

### 2. Edge length (a) vs. atomic radius (r):

Atoms touch along the **face diagonal**:

$$4r = a\sqrt{2} \quad \Rightarrow \quad a = 2\sqrt{2}r$$

### 3. Packing efficiency (APF): 74%

### 4. Examples: Cu, Al, Ag

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## 2. Quick Comparison Table

Unit Cell	Atoms per Cell	Packing Efficiency	Touching Direction	Everyday Analogy	Examples
SC	1	52%	Edge	Single marbles	Po
BCC	2	68%	Body diagonal	Gift in box	Fe, Cr, W
FCC	4	74%	Face diagonal	Oranges in box	Cu, Al, Ag

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## 3. Additional Theory

### 1. Packing Efficiency (APF):

$$\text{APF} = \frac{\text{Volume of atoms in the unit cell}}{\text{Volume of the unit cell}} \times 100$$

### 2. Relationship between edge length (a) and atomic radius (r):

Unit Cell	Formula
SC	$a = 2r$
BCC	$a = \frac{4r}{\sqrt{3}}$
FCC	$a = 2\sqrt{2}r$

### 3. Atoms sharing rules:

- Corner atom → 1/8th per cell
- Face atom → 1/2 per cell

- Body-center atom → 1 per cell
  - 4. **Packing efficiency significance:**
  - Higher APF → atoms are tightly packed → more stable structure
  - FCC > BCC > SC in packing efficiency and stability
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## 🌟 4. Everyday Analogies Recap

- SC → 1 marble in a box → 52% filled
  - BCC → gift in the center of a box → 68% filled
  - FCC → oranges stacked tightly → 74% filled
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## ✅ FCC Unit Cell Summary

- 8 corners  $\times$   $1/8$  = 1 atom
  - 6 faces  $\times$   $1/2$  = 3 atoms
  - Total = 4 atoms per unit cell
  - Packing efficiency = 74%
  - Example analogy: oranges stacked tightly
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## ✅ BCC Unit Cell Summary

- 8 corners  $\times$   $1/8$  = 1 atom
- 1 body-center atom = 1 atom
- Total = 2 atoms per unit cell
- Packing efficiency = 68%
- Example analogy: gift in a box