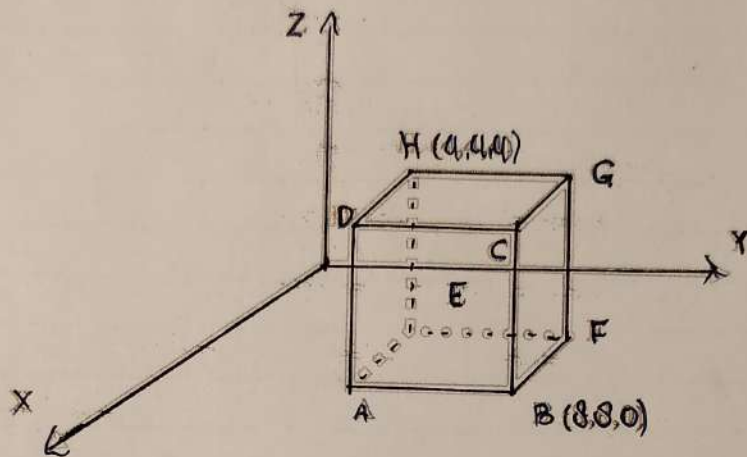


Tugas M9



Diketahui suatu kubus  $ABCD - EFGH$  sebagaimana tampak pada gambar diatas, dilakukan transformasi secara berkesinambungan dengan urutan sebagai berikut :

- Diputar  $90^\circ$  searah jarum jam sepanjang sumbu  $Y$ , kemudian
- Digeser 4 satuan ke bawah dan 4 satuan ke kiri, lalu
- Dilakukan perbesaran 2 kali keatas

maka tentukanlah

- Matriks Rotasi, Translasi, Dilatasi dan komposisinya
- Titik - titik sudut dari bangun hasil akhir proses transformasi berdasarkan perhitungan matriks komposisinya
- Gambarkan bangun dari hasil akhir transformasi tersebut

$$A(0,0,0)$$

$$B(8,0,0)$$

$$C(8,0,4)$$

$$D(8,4,4)$$

$$E(4,4,0)$$

$$F(4,0,0)$$

$$G(4,0,4)$$

$$H(4,4,4)$$

A. Rotasi

$$R = \begin{bmatrix} \cos 90 & 0 & -\sin 90 \\ 0 & 1 & 0 \\ \sin 90 & 0 & \cos 90 \end{bmatrix} = \begin{bmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

M. Translasi

$$T = \begin{bmatrix} 1 & 0 & 0 & T_x \\ 0 & 1 & 0 & T_y \\ 0 & 0 & 1 & T_z \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -4 \\ 0 & 0 & 1 & -4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

M. Dilatasi

$$D = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & s_z \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$

Komposisi

D.T.R

$$K = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -4 \\ 0 & 0 & 1 & -4 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$K = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -4 \\ 0 & 0 & 2 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



$$A' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 8 \\ 4 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 8 \\ 1 \end{bmatrix} = (0, 0, 8)$$

$$B' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 8 \\ 8 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \\ 8 \\ 1 \end{bmatrix} = (0, 4, 8)$$

$$C' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 8 \\ 8 \\ 4 \\ 1 \end{bmatrix} = \begin{bmatrix} -4 \\ 4 \\ 8 \\ 1 \end{bmatrix} = (-4, 4, 8)$$

$$D' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 8 \\ 4 \\ 4 \\ 1 \end{bmatrix} = \begin{bmatrix} -4 \\ 0 \\ 8 \\ 1 \end{bmatrix} = (-4, 0, 8)$$

$$E' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 4 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = (0, 0, 0)$$

$$F' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 8 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \\ 0 \\ 1 \end{bmatrix} = (0, 4, 0)$$

$$G' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 8 \\ 4 \\ 1 \end{bmatrix} = \begin{bmatrix} -4 \\ 4 \\ 0 \\ 1 \end{bmatrix} = (-4, 4, 0)$$

$$H' = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & -4 \\ 2 & 0 & 0 & -8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 4 \\ 4 \\ 1 \end{bmatrix} = \begin{bmatrix} -4 \\ 0 \\ 0 \\ 1 \end{bmatrix} = (-4, 0, 0)$$

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5/12/2024

