

MEAN SQUARE ERROR

Mean Squared Error Definition

- The **mean squared error** (MSE) tells you how close a regression line is to a set of points. It does this by taking the distances from the points to the regression line (these distances are the “errors”) and squaring them.
- The squaring is necessary to remove any negative signs. It also gives more weight to larger differences. It’s called the **mean** squared error as you’re finding the average of a set of errors.
- The lower the MSE, the better the Prediction.

Mean Squared Error Example

- MSE formula = $(1/n) * \Sigma(\text{actual} - \text{predicted})^2$

Where:

- n = number of items,
- Σ = summation notation,
- Actual = original or observed y-value,
- Prediction = y-value from regression.

General steps to calculate the MSE from a set of X and Y values:

- Find the regression line.
- Insert your X values into the linear regression equation to find the new Y values (Y').
- Subtract the new Y value from the original to get the error.
- Square the errors.
- Add up the errors (the Σ in the formula is summation notation).
- Find the mean.

Example Problem:

Find the MSE for the following set of values: (43,41), (44,45), (45,49), (46,47), (47,44).

Step 1: Find the regression line.

I used online calculator and got the regression line $y = 9.2 + 0.8x$.

Step 2: Find the new Y' values:

$$9.2 + 0.8(43) = 43.6$$

$$9.2 + 0.8(44) = 44.4$$

$$9.2 + 0.8(45) = 45.2$$

$$9.2 + 0.8(46) = 46$$

$$9.2 + 0.8(47) = 46.8$$

Step 3: Find the error ($Y - Y'$):

$$41 - 43.6 = -2.6$$

$$45 - 44.4 = 0.6$$

$$49 - 45.2 = 3.8$$

$$47 - 46 = 1$$

$$44 - 46.8 = -2.8$$

Step 4: Square the Errors:

$$-2.62 = 6.76$$

$$0.62 = 0.36$$

$$3.82 = 14.44$$

$$12 = 1$$

$$-2.82 = 7.84$$

Height (X)	Weight (Y)	Estimated (Y')	Error (Y-Y')	Error Squared
43	41	43.6	-2.6	6.76
44	45	44.4	0.6	0.36
45	49	45.2	3.8	14.44
46	47	46	1	1
47	44	46.8	-2.8	7.84
Regression line = $y=9.2+0.8x$				

Step 5: Add all of the squared errors up:

$$6.76 + 0.36 + 14.44 + 1 + 7.84 = 30.4$$

Step 6: Find the mean squared error:

$$30.4 / 5 = 6.08$$