

## ME 318M Homework #7

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### Problem 1:

Code:

```
function I = inverse2(M)
[rows, columns] = size(M); %check if input matrix is a square matrix
if rows ~= columns %if not square, end function/script
    disp('Input matrix is not a square matrix')
    I = [];
    return
end
%make an identity matrix, a, that is same size as the input matrix
for j = 1:columns
    for i = 1:rows
        if i == j
            out(i,j) = 1;
        else
            out(i,j) = 0;
        end
    end
end
%actual math part
M = [M, out];
for k = 1:rows
    A = M(k, k:end); %first row
    B = A/(M(k,k)); %first row/diag
    M(k, k:end) = B; %reassign first row
    C = M([1:k-1, k+1:end], k:end); %rest of M
    factor = M([1:k-1, k+1:end], k); %get the shit under the 1
    sub = factor*B;
    NewRest = C - sub;
    M([1:k-1, k+1:end], k:end) = NewRest;
end
I = M(1:end, rows+1:end);
```

To find if inverse found is actually inverse, I multiplied the inverse by matrix M and obtained the 20x20 identity matrix.

## Command Window:

```
>> M*I
```

```
ans =
```

```
Columns 1 through 4
```

1.0000	0.0000	0.0000	-0.0000
0.0000	1.0000	-0.0000	0.0000
0.0000	0.0000	1.0000	0.0000
0.0000	0.0000	-0.0000	1.0000
-0.0000	0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	-0.0000	-0.0000
0.0000	0.0000	-0.0000	0.0000
-0.0000	-0.0000	0.0000	-0.0000
0.0000	-0.0000	0.0000	-0.0000
0.0000	0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	-0.0000	0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	0.0000	0.0000	-0.0000

```
Columns 5 through 8
```

-0.0000	0.0000	0.0000	-0.0000
-0.0000	0.0000	0.0000	-0.0000
-0.0000	0.0000	-0.0000	-0.0000
-0.0000	-0.0000	0.0000	0.0000
1.0000	0.0000	0.0000	0.0000
0.0000	1.0000	0.0000	0.0000
0.0000	-0.0000	1.0000	-0.0000
-0.0000	0.0000	-0.0000	1.0000
0.0000	-0.0000	0.0000	0.0000
0.0000	-0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	-0.0000	-0.0000
0.0000	-0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	-0.0000
0.0000	-0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	0.0000	0.0000
0.0000	-0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	-0.0000
0.0000	0.0000	0.0000	0.0000

```
Columns 9 through 12
```

0.0000	0.0000	-0.0000	-0.0000
-0.0000	0.0000	0.0000	-0.0000
-0.0000	0.0000	0.0000	-0.0000
0.0000	-0.0000	0.0000	-0.0000
0.0000	0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
-0.0000	0.0000	0.0000	-0.0000
1.0000	-0.0000	-0.0000	0.0000
0.0000	1.0000	-0.0000	0.0000
-0.0000	0.0000	1.0000	-0.0000
-0.0000	0.0000	0.0000	1.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	0.0000	-0.0000	0.0000

Columns 13 through 16

-0.0000	0.0000	0.0000	-0.0000
-0.0000	-0.0000	0.0000	-0.0000
-0.0000	0.0000	0.0000	-0.0000
0.0000	-0.0000	-0.0000	-0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	0.0000	-0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	-0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	0.0000	-0.0000
-0.0000	0.0000	0.0000	-0.0000
1.0000	-0.0000	-0.0000	0.0000
-0.0000	1.0000	-0.0000	0.0000
0.0000	-0.0000	1.0000	0.0000
0.0000	-0.0000	-0.0000	1.0000
0.0000	0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	0.0000

Columns 17 through 20

0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000
-0.0000	-0.0000	-0.0000	0.0000
0.0000	-0.0000	-0.0000	-0.0000
0.0000	-0.0000	-0.0000	-0.0000

0.0000	0.0000	0.0000	-0.0000
-0.0000	0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	-0.0000
-0.0000	-0.0000	-0.0000	-0.0000
-0.0000	-0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	-0.0000
0.0000	0.0000	-0.0000	-0.0000
0.0000	-0.0000	-0.0000	-0.0000
0.0000	-0.0000	-0.0000	-0.0000
1.0000	-0.0000	-0.0000	-0.0000
0.0000	1.0000	-0.0000	-0.0000
0.0000	0.0000	1.0000	-0.0000
0.0000	-0.0000	-0.0000	1.0000

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	-0.0471	0.1105	-0.0397	0.0800	-0.4511	-0.2751	-0.6318	-0.6245	-0.3219	-0.2665	0.2344	-0.5122	-1.5596	0.5085	0.7293	-0.5160	0.3952	0.7494	0.3951	0.1016
2	0.3848	0.1683	-0.1117	0.3348	-0.7261	0.6019	0.0261	-0.1414	-0.6172	0.7452	0.2468	-0.3748	-0.6651	0.0235	0.4068	-0.5001	-0.5168	0.3190	0.1420	0.2691
3	-0.3114	0.0734	0.1659	-0.1678	0.2808	-0.4237	-0.3603	-0.5512	-0.0972	-0.5672	0.0695	-0.1488	-0.5428	0.4356	0.3391	-0.2711	0.5667	0.3506	0.0039	-0.0208
4	-0.0340	-0.0628	0.1013	0.0486	-0.0693	-0.0685	-0.1280	-0.1726	0.0190	-0.1882	0.1107	0.0199	-0.1783	0.1892	0.0461	-0.0396	0.0279	0.1755	0.0517	0.1028
5	0.8684	-0.0307	-0.2231	0.6074	-0.7846	1.4565	0.8719	1.3296	-0.7965	1.5774	-0.1063	0.3680	1.9321	-0.9102	-0.7832	0.3807	-1.6336	-1.0001	-0.7166	0.7030
6	0.6177	0.4356	-0.3070	0.4567	-1.2441	0.7252	-0.3852	-0.5876	-1.0355	0.8282	0.6716	-0.6143	-1.4341	0.4621	0.5983	-0.8852	-0.3994	0.7767	0.2182	0.6148
7	0.9398	0.3564	-0.3166	0.7630	-1.4836	1.2166	-0.0549	0.1076	-1.3136	1.4514	0.3625	-0.5002	-0.7218	-0.0312	0.4412	-0.7121	-1.1609	0.0713	-0.1772	0.6800
8	0.4934	0.2836	-0.3541	0.6076	-1.3673	0.7788	-0.5165	-0.6683	-1.1112	0.7681	0.4573	-0.6830	-1.4289	0.5089	0.6008	-0.9078	-0.4356	0.8313	0.0872	0.6392
9	1.2760	0.3666	-0.4800	1.0163	-2.1902	1.4661	-0.5219	-0.3598	-1.6070	1.7956	0.7712	-0.8988	-1.6724	0.1512	1.0029	-1.1968	-1.1172	0.7552	0.3496	0.8083
10	-0.6411	-0.3240	0.2840	-0.4791	0.5735	-0.8284	-0.2598	-0.1376	0.6330	-0.8534	-0.1284	0.3060	-0.0296	0.0804	-0.1855	0.2559	0.9773	-0.0795	0.1701	-0.3441
11	0.8645	0.4601	-0.2757	0.6567	-1.5633	1.0832	-0.3476	-0.5878	-1.2268	1.1191	0.5490	-0.6741	-1.3870	0.2478	0.6496	-0.8565	-0.7621	0.7416	0.3348	0.5006
12	0.3144	0.1255	-0.1861	0.3142	-0.8392	0.3288	-0.5074	-0.4910	-0.6046	0.3408	0.3152	-0.4242	-1.0560	0.1953	0.3997	-0.5556	-0.2232	0.5521	0.0824	0.4387
13	-0.2436	-0.0807	0.0266	-0.3349	0.7066	-0.3771	0.3367	0.2705	0.5272	-0.5971	-0.0979	0.4147	0.8559	-0.2114	-0.3830	0.3827	0.3004	-0.2868	-0.1112	-0.2993
14	1.5164	0.2196	-0.4456	0.9097	-1.1493	2.3303	0.9830	1.7189	-1.0886	2.4713	0.0327	0.1054	1.9581	-1.2040	-0.6197	-0.1341	-2.2747	-1.0972	-0.5495	0.5642
15	-1.5003	-0.5011	0.4989	-1.3707	2.3392	-2.1070	0.0136	-0.2389	1.9838	-2.4520	-0.7375	0.7961	0.6131	0.2985	-0.5332	1.0425	1.8747	-0.2684	0.0325	-0.9723
16	-0.6166	-0.5154	0.2280	-0.5873	1.5411	-0.7582	0.6123	0.6867	1.1346	-1.0359	-0.3919	0.6209	1.7549	-0.3885	-1.0020	0.9638	0.5603	-0.9113	-0.2855	-0.5810
17	-0.2815	0.0718	0.0962	-0.4844	0.4054	-0.4101	-0.3102	-0.2306	0.2433	-0.5160	-0.1083	-0.0382	-0.3232	0.3382	0.0734	0.0034	0.3409	0.2042	-0.0242	-0.2495
18	-1.5063	-0.5493	0.6292	-1.4388	2.7448	-2.3626	0.3332	0.0987	2.3450	-2.5818	-0.8404	0.9290	1.3599	0.0682	-0.8106	1.2312	1.9373	-0.5018	0.0058	-1.2494
19	0.9318	0.4931	-0.4179	0.7519	-1.6970	1.2930	-0.2387	-0.2322	-1.3708	1.5301	0.5841	-0.7179	-1.1052	0.0657	0.7379	-0.9382	-1.1213	0.3736	0.2855	0.6152

## Problem 2:

Problem 2

#1) 
$$\left[ \begin{array}{ccc|ccc} 1 & 2 & 5 & 1 & 0 & 0 \\ 3 & 7 & 4 & 0 & 1 & 0 \\ 1 & 4 & 2 & 0 & 0 & 1 \end{array} \right]$$

$R_1 - 2R_2 \rightarrow R_1$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & -2 & 1 & 0 \\ 3 & 7 & 4 & 0 & 1 & 0 \\ 1 & 4 & 2 & 0 & 0 & 1 \end{array} \right]$$

$R_2 + 11R_3 \rightarrow R_2$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & -2 & 1 & 0 \\ 0 & 1 & 0 & -2 & -3 & 11 \\ 1 & 4 & 2 & 0 & 0 & 1 \end{array} \right]$$

$R_1 - 2R_3 \rightarrow R_1$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & -2 & 1 & 0 \\ 0 & 1 & 0 & -2 & -3 & 11 \\ 1 & 4 & 2 & 0 & 0 & 1 \end{array} \right]$$

$R_3 - R_1 \rightarrow R_3$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & -2 & 1 & 0 \\ 0 & 1 & 0 & -2 & -3 & 11 \\ 0 & 2 & -2 & 2 & -1 & 1 \end{array} \right]$$

$R_1 - 2R_2 \rightarrow R_1$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 7 & -2 & 0 \\ 0 & 1 & 0 & -2 & -3 & 11 \\ 0 & 2 & -2 & 2 & -1 & 1 \end{array} \right]$$

$R_3 - 2R_2 \rightarrow R_3$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 7 & -2 & 0 \\ 0 & 1 & 0 & -2 & -3 & 11 \\ 0 & 0 & 1 & 5 & -2 & 1 \end{array} \right]$$

$R_2 \times \frac{1}{19} \rightarrow R_2$  
$$\left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 7 & -2 & 0 \\ 0 & 1 & 0 & -\frac{2}{19} & -\frac{3}{19} & \frac{11}{19} \\ 0 & 0 & 1 & \frac{5}{19} & -\frac{2}{19} & \frac{1}{19} \end{array} \right]$$

#2) 
$$\begin{bmatrix} -\frac{2}{19} & \frac{11}{19} & -\frac{27}{19} \\ -\frac{2}{19} & -\frac{3}{19} & \frac{11}{19} \\ \frac{5}{19} & -\frac{2}{19} & \frac{1}{19} \end{bmatrix} \begin{bmatrix} -1 \\ 2 \\ -2 \end{bmatrix} = \begin{bmatrix} (-\frac{2}{19})(-1) + (\frac{11}{19})(2) + (-\frac{27}{19})(-2) \\ (-\frac{2}{19})(-1) + (-\frac{3}{19})(2) + (\frac{11}{19})(-2) \\ (\frac{5}{19})(-1) + (-\frac{2}{19})(2) + (\frac{1}{19})(-2) \end{bmatrix} = \begin{bmatrix} \frac{38}{19} \\ -\frac{30}{19} \\ -\frac{11}{19} \end{bmatrix}$$

## 3) MATLAB Command Window

```
>> A = [1 2 5; 3 7 4; 1 4 2];
```

```
>> inverse2(A)
```

```
ans =
```

```
-0.1053    0.8421   -1.4211
-0.1053   -0.1579    0.5789
 0.2632   -0.1053    0.0526
```

```
>> ans*[-1; 2; -2]
```

```
ans =
```

```
4.6316
-1.3684
-0.5789
```

### Problem 3:

Problem 3

$$A = \begin{bmatrix} 1 & 2 & 5 & | & 1 & 0 & 0 \\ 3 & 4 & 6 & | & 0 & 1 & 0 \\ 1 & 0 & -4 & | & 0 & 0 & 1 \end{bmatrix}$$

$\Rightarrow$  not an invertible matrix

$$\det A = 1(-16) + 2(6+12) + 5(-4)$$
$$= -16 + 36 - 20 = 0 \quad \checkmark$$

$R_2 - 3R_1 \rightarrow R_2$

$$\begin{bmatrix} 1 & 2 & 5 & | & 1 & 0 & 0 \\ 0 & -2 & -9 & | & -3 & 1 & 0 \\ 0 & -2 & -9 & | & -1 & 0 & 1 \end{bmatrix}$$

$R_3 - R_1 \rightarrow R_3$

$$\begin{bmatrix} 1 & 2 & 5 & | & 1 & 0 & 0 \\ 0 & -2 & -9 & | & -3 & 1 & 0 \\ 0 & -2 & -9 & | & -1 & 0 & 1 \end{bmatrix}$$

$R_1 + R_2 \rightarrow R_1$

$$\begin{bmatrix} 1 & 0 & -4 & | & -2 & 1 & 0 \\ 0 & -2 & -9 & | & -3 & 1 & 0 \\ 0 & 0 & 0 & | & 2 & -1 & 1 \end{bmatrix}$$

$R_3 - R_2 \rightarrow R_3$

$$\begin{bmatrix} 1 & 0 & -4 & | & -2 & 1 & 0 \\ 0 & 1 & \frac{9}{2} & | & \frac{3}{2} & -\frac{1}{2} & 0 \\ 0 & 0 & 0 & | & 2 & -1 & 1 \end{bmatrix}$$

Interesting MATLAB output:

```
>> A = [1 2 5; 3 4 6; 1 0 -4]
```

A =

1	2	5
3	4	6
1	0	-4

While trying to find the inverse of A, the third row became all zeroes. This meant that the Gauss-Jordan method could not be completed because there was no way to change the left side to the identity matrix.