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```
% lab2.m
% Please place lab2.m in your working directory
% Provide the print-out from running this function
% using 'publish lab2'
%
% T. Holton 10 Sept 08

test_lab2;
```

## Convolution, Part I

### Convolution #1

```
x = sequence([1 2 6 -3 5], 1);
h = sequence([4 -1 5 3 2], -3);
test_lab2(x, h);

% Convolution #2
test_lab2(h, x);

% Convolution #3
h = sequence(1, 0);
test_lab2(x, h);

% Convolution #4
test_lab2(h, x);

% Convolution #5
x = sequence(cos(2 * pi * (1:50000) / 16), -5); % nice, big sequence
h = sequence(ones(1, 10), 10);
test_lab2(x, h);

% Convolution #6
test_lab2(h, x);

% Convolution #7
x = sequence(1, 2);
h = sequence(1, -1);
test_lab2(x, h);

% Convolution #8
```

---

```
test_lab2(h, x);
```

*Problem #1*

*Your data are correct  
Your offset is correct  
Your elapsed time is 116.6 usecs  
which is 3.63 times Holton's elapsed time (32.1 usecs)  
and 5.3 times Matlab's elapsed time (22 usecs)*

*Problem #2*

*Your data are correct  
Your offset is correct  
Your elapsed time is 103 usecs  
which is 3.67 times Holton's elapsed time (28.1 usecs)  
and 11.4 times Matlab's elapsed time (9 usecs)*

*Problem #3*

*Your data are correct  
Your offset is correct  
Your elapsed time is 101.6 usecs  
which is 0.338 times Holton's elapsed time (300.6 usecs)  
and 0.276 times Matlab's elapsed time (368.1 usecs)*

*Problem #4*

*Your data are correct  
Your offset is correct  
Your elapsed time is 66.6 usecs  
which is 0.623 times Holton's elapsed time (106.9 usecs)  
and 3.42 times Matlab's elapsed time (19.5 usecs)*

*Problem #5*

*Your data are correct  
Your offset is correct  
Your elapsed time is 16618.8 usecs  
which is 1.39 times Holton's elapsed time (11978.8 usecs)  
and 31.9 times Matlab's elapsed time (520.5 usecs)*

*Problem #6*

*Your data are correct  
Your offset is correct  
Your elapsed time is 15675 usecs  
which is 1.1 times Holton's elapsed time (14234.5 usecs)  
and 9.96 times Matlab's elapsed time (1573.8 usecs)*

*Problem #7*

*Your data are correct  
Your offset is correct  
Your elapsed time is 121.4 usecs  
which is 5.32 times Holton's elapsed time (22.8 usecs)  
and 4.58 times Matlab's elapsed time (26.5 usecs)*

*Problem #8*

*Your data are correct  
Your offset is correct*

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*Your elapsed time is 62.5 usecs  
which is 1.41 times Holton's elapsed time (44.3 usecs)  
and 8.33 times Matlab's elapsed time (7.5 usecs)*

## Real-time Convolution

Real-time convolution #1

```
x = [1 4 2 6 5];  
h = [4 -1 3 -5 2];  
test_lab2a;  
test_lab2a(x, h);
```

```
% Real-time convolution convolution #2  
test_lab2a(h, x);
```

```
% Real-time convolution #3  
x = cos(2 * pi * (1:50000) / 16); % nice, big sequence  
h = ones(1, 10);  
test_lab2a(x, h);
```

*Real-time convolution #1  
Your data are correct*

*Real-time convolution #2  
Your data are correct*

*Real-time convolution #3  
Your data are correct*

## Deconvolution

Deconvolution #1

```
h = sequence([1 3 2], 2);  
y = sequence([1 6 15 20 15 7 2], -1);  
test_lab2b;  
test_lab2b(y, h);
```

```
% Deconvolution #1  
y = sequence([-1 -2 0 0 0 0 1 2], 2);  
test_lab2b(y, h);
```

*Deconvolution problem #1  
Your data are correct  
Your offset is correct*

*Deconvolution problem #2  
Your data are correct  
Your offset is correct*

---

# Code

```
disp('-----')
disp('                Code')
disp('-----')
type sequence
type conv_rt

-----
                        Code
-----

classdef sequence
    properties
        data
        offset
    end

    methods(Static)

        function [a,b] = padData(x,y)
            Lx = length(x.data) + x.offset;
            Ly = length(y.data) + y.offset;
            a = [zeros(1,x.offset-y.offset), x.data, zeros(1,Ly-Lx)];
            b = [zeros(1,y.offset-x.offset), y.data, zeros(1,Lx-Ly)];
        end

%           % My Original Implementation
%           %
%           % Pads the input sequences so that they are of the same
length.
%           % Sequence with the lower offset will not have front
padding. This
%           % returns the data portion of the sequences only.
%           function [a,b] = padData(x,y)
%               % Find which sequence has the lower offset (furthest to
the
%               % left).
%               lo = sequence([],0);
%               hi = sequence([],0);
%               if(x.offset<y.offset)
%                   lo = x;
%                   hi = y;
%               else
%                   lo = y;
%                   hi = x;
%               end
%               % Define ints for left and right padding of zeros.
%               leftPad = hi.offset-lo.offset;
%               rightPad = (length(lo.data)+lo.offset)-
(length(hi.data)+hi.offset);
%               % Padding the left side of the sequence with the higher
offset
end
end
```

---

```

%           % is easiest.
%           hi.data = [zeros(1,leftPad),hi.data];
%           % Pad the right side of either the lower or higher
offset
%           % sequence depending on whether rightPad is
%           % positive or negative.
%           if(rightPad>0)
%               hi.data = [hi.data, zeros(1,rightPad)];
%           elseif(rightPad<0)
%               lo.data = [lo.data, zeros(1,abs(rightPad))];
%           end
%           % Map lo and hi back to the order in which they came
i.e. a = x
%           % and b = y.
%           if(x.offset<y.offset)
%               a=lo.data;
%               b=hi.data;
%           else
%               a=hi.data;
%               b=lo.data;
%           end
%           end
%       end

methods
function s = sequence(data, offset)
% SEQUENCE    Sequence object
%           S = SEQUENCE(DATA, OFFSET) creates sequence S
%           using DATA and OFFSET
%
%           Your Name    1 Jan 2014
s.data = data;
s.offset = offset;
end

function display(s)
var = inputname(1);
if (isempty(var))
    disp('ans =');
else
    disp([var '=']);
end
switch length(s.data)
case 0
    disp('    data: []')
case 1
    disp(['    data: ', num2str(s.data)])
otherwise
    disp(['    data: [' num2str(s.data) ']'])
end
disp([' offset: ' num2str(s.offset)])
end

function y = flip(x)

```

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```

        ofs = -(x.offset+length(x.data)-1);
    y = sequence(x.data(end:-1:1),ofs);
end

function y = shift(x, n0)
    y = sequence(x.data, x.offset+n0);
end

function z = plus(x, y)
    if(isa(x,'double'))
        z = sequence(x+y.data,y.offset);
    elseif(isa(y,'double'))
        z = sequence(x.data+y,x.offset);
    else
        [a, b] = sequence.padData(x,y);
        z = sequence(a+b,min(x.offset,y.offset));
    end
    %trim(z);
end

function z = minus(x, y)
    if(isa(x,'double'))
        z = sequence(x-y.data,y.offset);
    elseif(isa(y,'double'))
        z = sequence(x.data-y,x.offset);
    else
        [a, b] = sequence.padData(x,y);
        z = sequence(a-b,min(x.offset,y.offset));
    end
    %trim(z);
end

function z = times(x, y)
    if(isa(x,'double'))
        z = sequence(x.*y.data,y.offset);
    elseif(isa(y,'double'))
        z = sequence(x.data.*y,x.offset);
    else
        [a, b] = sequence.padData(x,y);
        z = sequence(a.*b,min(x.offset,y.offset));
    end
    %trim(z);
end

function y = conv(x,h)
    lx = length(x.data);
    lh = length(h.data);
    if(lx>lh)
        y = convol(h,x,lh,lx);
    else
        y = convol(x,h,lx,lh);
    end
end

```

---

---

```

function H = getConvMatrix(h,lx,lh)
    widthH = lx + lh - 1;
    H=zeros( lx, widthH );
    for n = 1:lx
        zerosLeftLength    = n-1;
        dataStart           = 1;
        dataEnd             = min( lh, widthH -
zerosLeftLength );
        zerosRightLength    = widthH - dataEnd - dataStart -
zerosLeftLength + 1;
        left                = zeros( 1, zerosLeftLength );
        mid                 = h.data( dataStart : dataEnd );
        right               = zeros( 1, zerosRightLength );
        H(n,:)              = [left, mid, right];
    end
end

% Convolution
function y = convol( x,h,lx,lh )
    H = getConvMatrix(h,lx,lh);
    y = sequence( x.data*H, x.offset+h.offset );
end

function x = deconv(y,h)
    ly = length(y.data);
    lh = length(h.data);
    lx = ly-lh+1;
    x_data = zeros(1,lx);
    for n=1:lx
        sub = 0;
        for k=1:(min(n,lh))
            sub = sub + x_data(n-k+1)*h.data(k);
        end
        x_data(n)=(y.data(n)-sub)/h.data(1);
    end
    x=sequence(x_data,y.offset-h.offset);
end

function x = trim(x)
    while(x.data(1) == 0 && length(x.data)>1)
        x.data(1) = [];
    end
    while(x.data(end) == 0 && length(x.data)>1)
        x.data(end) = [];
    end
end

function stem(x)
    % STEM Display a Matlab sequence, x, using a stem plot.
    data_length = length(x.data);
    n_axis_indeces = linspace(1,data_length,data_length);
    n_axis_vals = n_axis_indeces
+linspace(x.offset,x.offset,data_length)-1;

```

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