

# Assignment - 1

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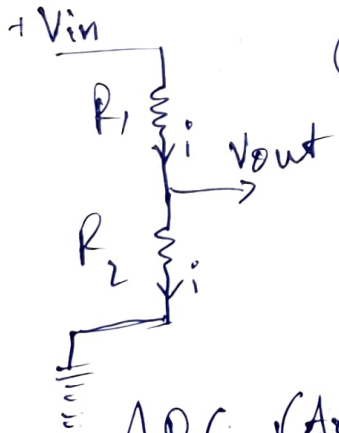
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## Introduction:

Objectives  $\rightarrow$  to study the circuits learnt in theory and practice applied engineering using tinkercad Simulated Circuits.

Theory includes voltage dividers, RC circuits and Ohmmeter used to measure unknown resistances.

Task A). A simple Voltage divider is needed in measurement systems to measure the voltages based on theory. This is important because some measurement devices have limited ranges and sometimes we need to reduce the voltage.



$$\text{(Ohm's law)} \quad i = \frac{V_{in}}{R_1 + R_2}$$

$$V_{out} = i R_2 = V_{in} \cdot \left( \frac{R_2}{R_1 + R_2} \right)$$

ADC (Arduino) is used to measure the  $V_{out}$  in the circuit, conversion formula:

$$V_{out} = (\text{ADC reading}) \times \frac{5}{1023}$$



As seen in the measurements, due to the noise, and the unavoidable possibility of an error of  $\pm \frac{1}{2}$  LSB, (LSB =  $\frac{5}{1023}$ ) measurement do not exactly match

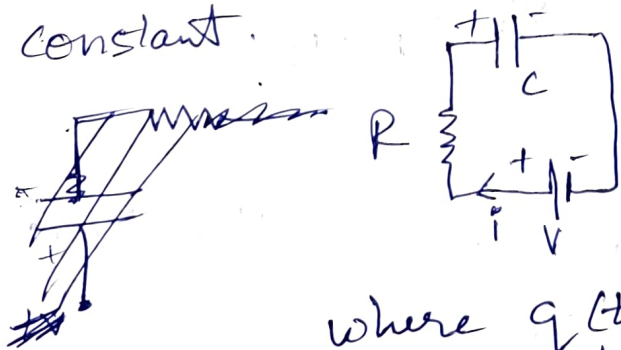
theoretical values.

for  $V_{in} = 3V$

$R_1$	$R_2$	$V_{in}$ (V)	Theoretical $V_{out}(V)$	measured $V_{out}(V)$
1	1	3	1.5	1.491
6	3	3	1	0.997
15	25	3	1.875	1.877
27	23	3	1.380	1.378
20	60	3	2.250	2.248

~~Task A~~) code reads the analog pin values & converts them to digital code using the conversion formula. `void setup` function has `serial.begin(9600)` - which is used to output the values to serial monitor. `Serial.print(value)` → prints the value in the serial monitor.

Task B) The simulated RC circuit is used to measure the capacitance by measuring time constant.



Using the Kirchhoff's law at time  $t$ ,

$$V - iR - \frac{q(t)}{C} = 0$$

where  $q(t)$  is the charge in capacitor plate at time  $t$ .

as  $i = \text{current at time } t = \frac{dq}{dt}$ ,

$$V - \frac{q}{C} = R \cdot \frac{dq}{dt} \Rightarrow \frac{dq}{CV - q} = \frac{dt}{RC}$$

integrating both sides, assuming at  $t=0, q=0$ ,

$$\int_0^q \frac{dq}{CV - q} = \int_0^t \frac{dt}{RC} \Rightarrow \ln\left(\frac{CV}{CV - q}\right) = \frac{t}{RC}$$

$$\Rightarrow q = CV(1 - e^{-t/RC}) \Rightarrow \frac{q}{C} = V(1 - e^{-t/RC})$$

i.e., potential difference across  $C$  is

$$V_c(t) = V(1 - e^{-t/RC})$$

$$\text{for } t = RC, V_c(t) = V(1 - e^{-1}) \approx V(0.63)$$

i.e., when the voltage  $V_c$  is 63% of battery, the time taken is  $\tau = RC$

Voltage supply = 3V   63% of V ≈ 1.90V	measured time	expected time
1) $R = 50k\Omega$ $C = 1000\mu F$ → $\tau = 50s$	49996ms	50000ms
2) $R = 50k\Omega$ $C = 1200\mu F$ → $\tau = 60s$	59958ms	60000ms
3) $R = 50k\Omega$ $C = 1400\mu F$ → $\tau = 70s$	69919ms	70000ms





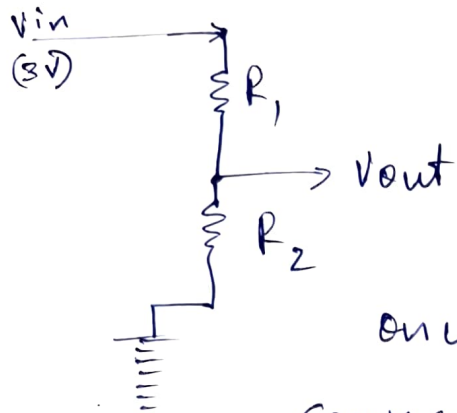
~~The~~ The measured time does not perfectly correspond to theoretical time constant because the voltage gets added with noise and then ADC has limitation in measurement, ~~and so there is~~ a systematic error of  $\pm \frac{1}{2} \text{ LSB} \approx \pm \frac{1}{2} (4.88 \text{ mV})$

code:

```
unsigned long startTime;  
void setup() function does the same work with  
then using an extra a reference time from  
which the time measurement starts.
```

the millis()  $\rightarrow$  increments time every one millisecond, and we finally need ~~time - reference~~ (starting ~~time~~) final incremented time - starting time, which is the duration taken to reach a voltage printed along with it in the serial monitor.

Task c) For a given Resistor  $R_1 = 5k\Omega$ , we can measure the Voltage  $V_{out}$  of the Voltage Divider consisting the unknown Resistance  $R_2$  and  $R_1 = 5k\Omega$ .



$$V_{out} = V_{in} \frac{R_2}{R_1 + R_2}$$

once we know  $V_{out}$  using the ADC connected, we can find  $R_2$ .

$$(R_1 + R_2) V_{out} = V_{in} R_2$$

$$\left[ \frac{R_1 V_{out}}{V_{in} - V_{out}} = R_2 \right] \quad \left[ \begin{array}{l} \text{Known Resistor} \\ R_1 = 5k\Omega \end{array} \right]$$

$R_2$ (used) ( $k\Omega$ )	$V_{out}$ (measured) (volts)	$R_2$ (measured) = $\frac{R_1 V_{out}}{V_{in} - V_{out}}$ ( $k\Omega$ )
5k $\Omega$	1.500	$R_2 = \frac{5(1.5)}{3 - 1.5} = 5k\Omega$
10k $\Omega$	1.999	$R_2 = \frac{5(1.999)}{3 - 1.999} \approx 9.985k\Omega$
7k $\Omega$	1.750	$R_2 = \frac{5(1.75)}{(3 - 1.75)} = 7k\Omega$
11k $\Omega$	2.063	$R_2 = \frac{5(2.063)}{3 - 2.063} = 11.008k\Omega$

The screenshot shows the Arduino IDE interface. At the top right, there's a dropdown menu set to "1 (Arduino Uno R3)". Below it are icons for uploading, saving, and compiling. The main editor area contains C++ code for setting up a serial connection and reading an analog pin.

```
Text          ↕      📁      ⚙️      A ▾        1 (Arduino Uno R3) ▾  
1 const int analogPin = A0;  
2 const float Vref = 5.0; // Arduino default reference  
3  
4 void setup() {  
5     Serial.begin(9600);  
6 }  
7  
8 void loop() {  
9     int adcValue = analogRead(analogPin);  
10    float voltage = adcValue * Vref / 1023.0;  
11  
12    Serial.print("ADC = ");  
13    Serial.print(adcValue);  
14    Serial.print(" Voltage = ");  
15    Serial.println(voltage, 3);  
16    Serial.println(" V");  
17  
18    delay(500);  
19 }  
20
```