

Assignment 1

Date: _____
Page: _____

* Section A

- 1) True
- 2) True
- 3) False
- 4) True
- 5) True
- 6) False
- 7) False
- 8) True
- 9) True
- 10) True

* SECTION - B.

- 2) A: Squared loss
B: Absolute loss
C: Hinge loss
D: Logistic loss
E: 0-1 loss

3)(a) They are continuous and differentiable, allowing gradient.

(b) Loss function that are twice differentiable and convex,
~~thus~~. can be optimised using Newton's Method because
the Method requires computation of both gradients.

* SECTION C

- 1) Underfitting happens when a model is too simple to capture the underlying pattern in the data

- 2) High training and test errors indicate high ~~loss~~, bias, meaning the model is unable to capture the true relationship in the data.
- 3) Bagging reduces variances by averaging predictions from multiple models trained on different subsets of data.
- 4) Boosting reduce bias by improving model complexity; while variance depends on noise and regularization.

* SECTION - D

- 1) To reduce KNN computation time
 - i) Reduce data size
 - ii) Fewer dimensions
 - iii) Reduce search time to $O(\log n)$
- 2) Square euclidian distance does not change KNN predictions and does not solve the curse of dimensionality.
- 3) KNN fails in high dimensions because.
 - data looks scattered, distance lose meaning.
- 4) $K \uparrow \Rightarrow \text{Bias} \uparrow \Rightarrow \text{Variance} \downarrow$
 $K \downarrow \Rightarrow \text{Bias} \downarrow \Rightarrow \text{Variance} \uparrow$

5) KNN is preferred over linear SVM when data has complex local structure & ~~large~~ limited size.

* SECTION - E

1) Constant value $\rightarrow c$

$$L(c) = \sum_{y_i} (y_i - c)^2$$

Differentiate w.r.t. c .

$$\frac{dL}{dc} = \sum 2(c - y_i) = 0$$

$$c = \frac{1}{n} \sum y_i$$

2) $G = 1 - \sum_{i=1}^k p_i^2$

Min: $p = (1, 0, 0)$

$$G = 1 - (1)^2 + 0 + 0 = 0 \rightarrow \text{Min.}$$

Max: $p = (1/3, 1/3, 1/3)$

$$= 1 - 3\left(\frac{1}{3}\right)^2 = 2/3 \rightarrow \text{Max.}$$

3) Decision trees are myopic because they greedily select splits based on local impurity reduction without considering future splits.

- 4) ~~avif~~ Overfitting in decision ~~tree~~ trees,
- 1) Pruning
- 2) Restrict Tree complexity.

* SECTION-F

- 1) Random forest cannot use the same data for training and testing,
- 2) Random forest should not use the same data for training and testing, but they estimate generalisation error using out-of-bag samples.

Bagging reduces variance

Boosting reduces bias.