

Assignment - 1

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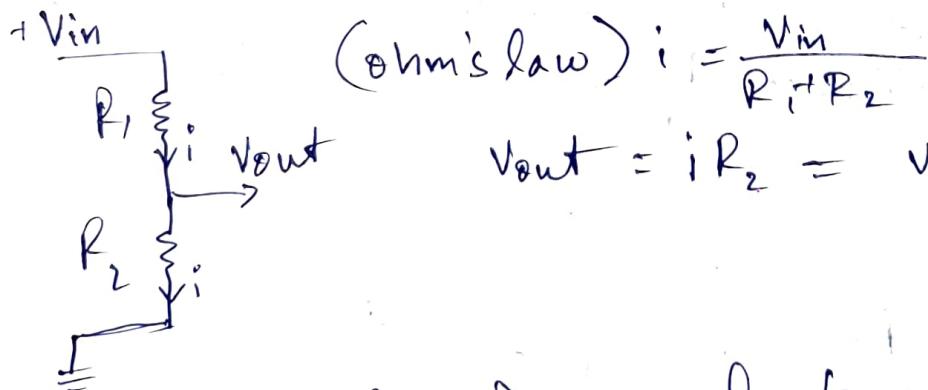
Y85 EE student.

Introduction :

Objectives : → to study the circuits learnt in theory and practice applied engineering using tinker cad Simulated Circuits.

Theory includes voltage dividers, ~~as~~ RC circuits and ohmmeter used to measure unknown resistances.

Task A). A simple Voltage divider is needed in measurement systems to measure the voltages based on theory. This is important because some measurement devices have limited ranges and sometimes we need to reduce the voltage.

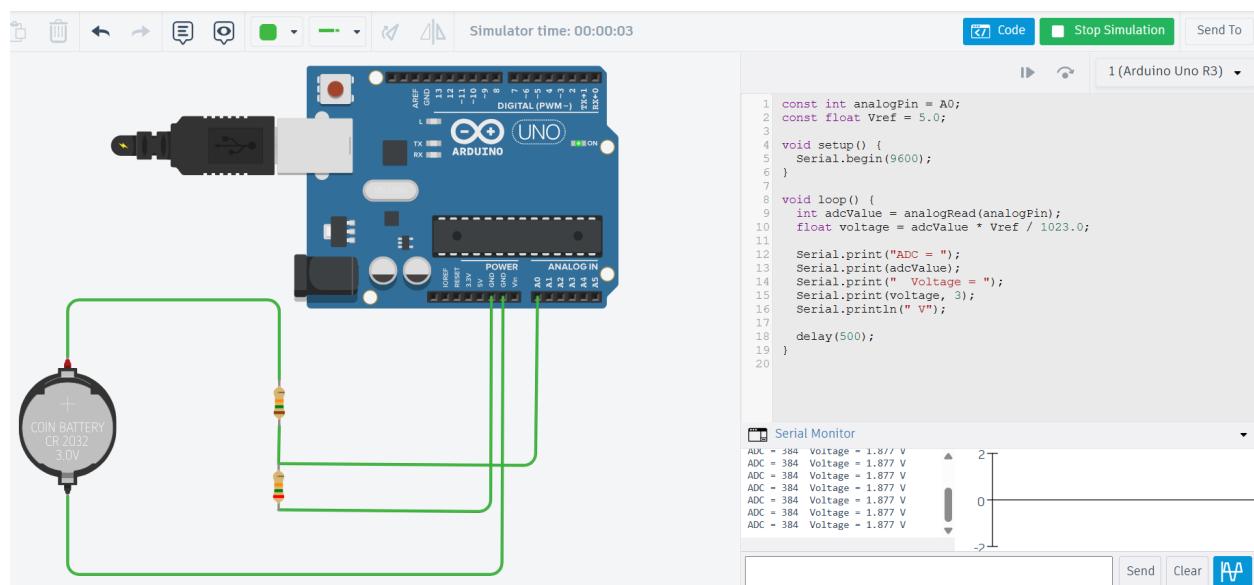
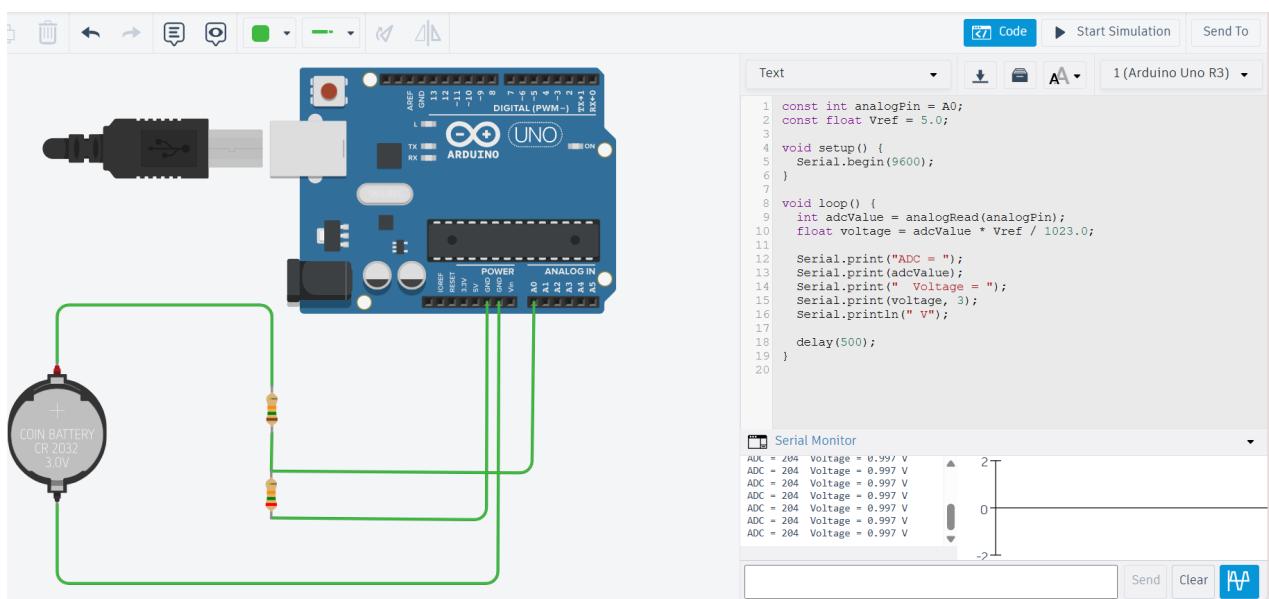
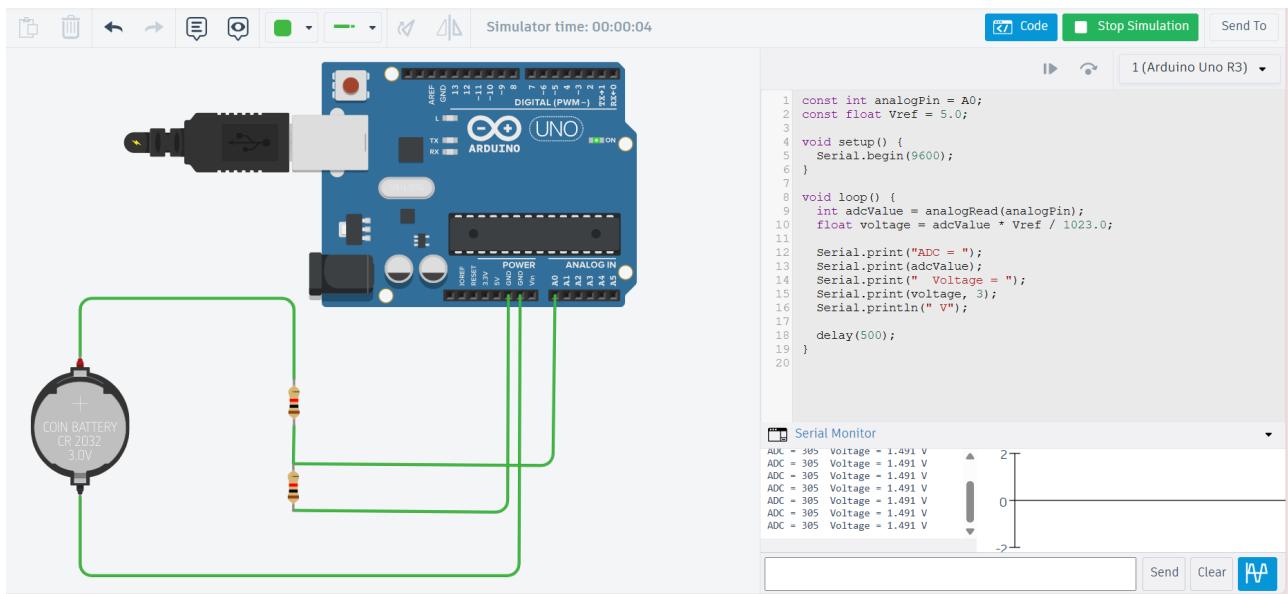


$$(\text{Ohm's law}) i = \frac{V_{in}}{R_1 + R_2}$$

$$V_{out} = i R_2 = V_{in} \cdot \left(\frac{R_2}{R_1 + R_2} \right)$$

ADC (Arduino) is used to measure the V_{out} in the circuit, conversion formula:

$$V_{out} = (\text{ADC reading}) \times \frac{5}{1023}$$

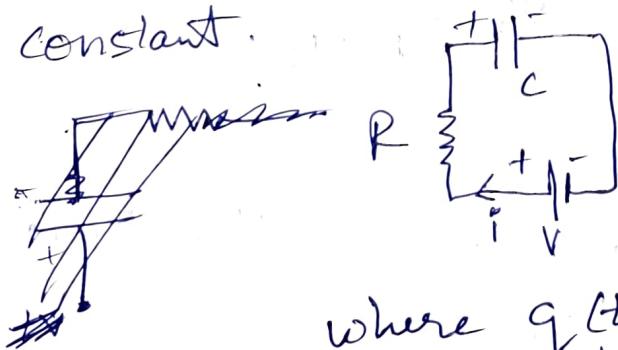


As seen in the measurements, due to the noise, and the unavoidable possibility of an error of $\pm \frac{1}{2}$ LSB,
 $(LSB = \frac{5}{1023})$ measurement does not exactly match theoretical values.
 for $V_{in} = 3V$

R_1	R_2	V_{in} (V)	Theoretical $V_{out}(V)$	measured $V_{out}(V)$
1	1	3	1.5	1.491
6	3	3	1	0.997
15	25	3	1.875	1.877
21	23	3	1.380	1.378
20	60	3	2.250	2.248

Task A) code reads the analog pin values & converts them to digital code using the conversion formula.
 void setup function has serial.begin(9600) - which is used to output the values to serial monitor.
 Serial.print(value) → prints the value in the serial monitor.

Task B) The simulated RC circuit is used to measure the capacitance by measuring time constant.



Using the Kirchoff's law at time t ,

$$V - iR - \frac{q(t)}{C} = 0$$

where $q(t)$ is the charge in capacitor plate at time t .

as $i = \text{current at time } t = \frac{dq}{dt}$,

$$V - \frac{q}{C} = R \cdot \frac{dq}{dt} \Rightarrow \frac{dq}{CV - q} = \frac{dt}{RC}$$

integrating both sides, assuming at $t=0, q=0$,

$$\int_0^q \frac{dq}{CV - q} = \int_0^t \frac{dt}{RC} \Rightarrow \ln\left(\frac{CV}{CV - q}\right) = \frac{t}{RC}$$

$$\Rightarrow q = CV(1 - e^{-t/RC}) \Rightarrow \frac{q}{C} = V(1 - e^{-t/RC})$$

i.e., potential difference across C is

$$V_C(t) = V(1 - e^{-t/RC})$$

$$\text{for } t = RC, V_C(t) = V(1 - e^{-1}) \approx V(0.63)$$

i.e., when the voltage V_C is 63% of battery,
the time taken is $\tau = RC$

Voltage supply	Measured time	Expected time
$3V$ 63% of $V \approx 1.90V$		

$$1) R = 50K\Omega \quad C = 1000\mu F \rightarrow \tau = 50s \quad 49996ms \quad 50000ms$$

$$2) R = 50K\Omega \quad C = 1200\mu F \rightarrow \tau = 60s \quad 59958ms \quad 60000ms$$

$$3) R = 50K\Omega \quad C = 1400\mu F \rightarrow \tau = 70s \quad 69919ms \quad 70000ms.$$

The circuit diagram shows an Arduino Uno connected to a CR2032 coin cell battery. A 50 kΩ resistor is connected between the Arduino's 3.3V pin and one terminal of the battery. The other terminal of the battery is connected to ground. The Arduino's A0 pin is connected to the junction point between the resistor and the battery. A digital multimeter is connected to the A0 pin to measure the voltage.

Resistor

- Name: 1
- Resistance: 50 kΩ

```

1 unsigned long startTime;
2
3 void setup() {
4   Serial.begin(9600);
5   startTime = millis(); // start timing
6 }
7
8 void loop() {
9   int adc = analogRead(A0);
10  float V = adc * (5.0 / 1023.0);
11
12  unsigned long t = millis() - startTime;
13
14  Serial.print(t);
15  Serial.print(" ms, ");
16  Serial.println(V);
17
18  delay(100);
19 }
20

```

Serial Monitor

49691 ms, 1.89
49793 ms, 1.89
49894 ms, 1.89
49996 ms, 1.90
50098 ms, 1.90
50199 ms, 1.90
50300 ms, 1.90

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```

Serial Monitor

59653 ms, 1.89
59754 ms, 1.89
59855 ms, 1.89
59958 ms, 1.90
60059 ms, 1.90
60161 ms, 1.90
60262 ms, 1.90

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Serial Monitor

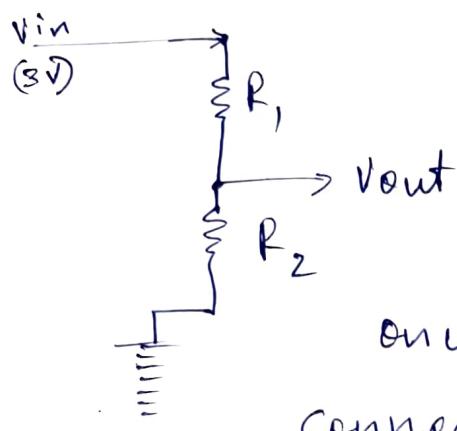
69715 ms, 1.89
69817 ms, 1.89
69919 ms, 1.90
70021 ms, 1.90
70122 ms, 1.90
70223 ms, 1.90
70326 ms, 1.90

The measured time does not perfectly correspond to theoretical time constant because the voltage gets added with noise and then ADC has limitation in measurement, and so there is a systematic error of $\pm \frac{1}{2} \text{ LSB} \approx \pm \frac{1}{2} (4.88 \text{ mV})$

Code:

```
unsigned long startTime;  
void setup() function does the same work with  
then using as extra a reference time from  
which the time measurement starts.  
the millis() → increments time every one millisecond,  
and we finally need time - reference starting  
time final incremented time - starting time,  
which is the duration taken to reach a  
voltage printed along with it in the serial  
monitor.
```

Task c) For a given Resistor $R_{1,2} = 5\text{k}\Omega$, $5\text{k}\Omega$, we can measure the Voltage ~~as~~ V_{out} of the Voltage Divider consisting the unknown Resistance R_2 and $R_1 = 5\text{k}\Omega$.



$$V_{out} = V_{in} \frac{R_2}{R_1 + R_2}$$

Once we know V_{out} , using the ADC connected, we can find R_2 .

$$(R_1 + R_2) V_{out} = V_{in} R_2$$

$$\left[\frac{R_1 V_{out}}{V_{in} - V_{out}} = R_2 \right] \quad \left[\begin{array}{l} \text{Known Resistor} \\ R_1 = 5\text{k}\Omega \end{array} \right]$$

$R_2(\text{used})$ $(\text{k}\Omega)$	$V_{out}(\text{measured})$ (Volts)	$R_2(\text{measured}) = \frac{R_1 V_{out}}{V_{in} - V_{out}}$
$5\text{k}\Omega$	1.500	$R_2 = \frac{5(1.5)}{3 - 1.5} = 5\text{k}\Omega$
$10\text{k}\Omega$	1.999	$R_2 = \frac{5(1.999)}{3 - 1.999} \approx 9.985\text{k}\Omega$
$7\text{k}\Omega$	1.750	$R_2 = \frac{5(1.75)}{3 - 1.75} = 7\text{k}\Omega$
$11\text{k}\Omega$	2.063	$R_2 = \frac{5(2.063)}{3 - 2.063} = 11.008\text{k}\Omega$

Due to uncertainty in V_{out} , there is an uncertainty in R_2 measured as well.

