

Assignment - 1

Section - A

- | | |
|----------|-----------|
| (1) True | (6) False |
| (2) True | (7) False |
| (3) True | (8) True |
| (4) True | (9) True |
| (5) True | (10) True |

Section - B

Model	Loss function	Regularizer
SVM	Hinge Loss	$ W ^2$ (L2 norm)
LASSO	Squared Loss (L2 loss)	$ W ^2$ (L2 norm)
RIDGE	Squared Loss (L2 loss)	$ W ^2$ (L2 norm)

- (2) A: 0-1 Loss
B: Hinge Loss
C: Squared Loss
D: Absolute Loss (L1 Loss)
E: Logistic Loss

- (3) (a) Squared Loss, Logistic Loss, Absolute Loss are optimizable using gradient descent because they are differentiable and their gradient exists.

- ⑥ Squared loss and logistic loss are optimizable using Newton's method because they are twice differentiable.

Section - C

- ① Under-fitting occurs when the model is too simple to capture the underlying pattern in the data.
- ② This means that model has high bias and is underfitting the data.
- ③ Bagging reduces variance by averaging predictions from multiple models trained on different bootstrap samples, which cancels out individual model fluctuations.
- ④ Boosting reduces bias significantly by focusing on hard-to-predict samples, but it can increase variance if overfitting occurs.

Section - E

- ① To reduce KNN computation time we should
- use efficient data structure (Ball-tree)
 - reduce dimensionality
 - use approximate nearest neighbours
 - reduce dataset size

Q 2 (a) No,

Squaring perm distance ordering, so nearest neighbors remain the same.

Q 2 (b) No,

Curse of Dimensionality remains unchanged since relative distances are unaffected.

(3) Distances become less discriminative and data becomes sparse, making nearest neighbors unreliable

(4) $K \downarrow$ bias \downarrow variance \uparrow

OR, $K \uparrow$ bias \uparrow variance \downarrow

(5) When the decision boundary is highly non-linear and sufficient data is available, KNN is preferred over linear SVM

Section E

(1) Say leaf n nodes y_1, y_2, \dots, y_n

Squared loss:

$$L(\hat{y}) = \sum_{i=1}^n (y_i - \hat{y})^2$$

$$\frac{\partial L}{\partial \hat{y}} = \sum_{i=1}^n 2(\hat{y} - y_i)$$

for minimum loss

$$\frac{\partial L}{\partial \hat{y}} = 0$$

$$\rightarrow \boxed{\hat{y} = \frac{1}{n} \sum_{i=1}^n y_i} = \text{mean value}$$

② Minimum = 0 (pure node)

$$\text{Maximum} = 1 - \sum_{i=1}^2 (y_i)^2 = 2/3$$

③ They make greedy, locally optimal ~~split~~ splits without considering feature splits.

- ④ 1) Limit on tree depth
2) Post-pruning using validation data

Section-F

①

No, trees are trained on bootstrap samples while feature is done using out-of-bag (OOB) samples or separate test data.

②

Bagging

Trains models independently to reduce variance

Boosting

Trains model sequentially, focusing on previous errors to reduce bias