5.1

Introduction

From the earliest days of computing, programmers have wanted unlimited amounts of fast memory. The topics in this chapter aid programmers by creating that illusion. Before we look at creating the illusion, let's consider a simple analogy that illustrates the key principles and mechanisms that we use.

Suppose you were a student writing a term paper on important historical developments in computer hardware. You are sitting at a desk in a library with a collection of books that you have pulled from the shelves and are examining. You find that several of the important computers that you need to write about are described in the books you have, but there is nothing about the EDSAC. Therefore, you go back to the shelves and look for an additional book. You find a book on early British computers that covers the EDSAC. Once you have a good selection of books on the desk in front of you, there is a good probability that many of the topics you need can be found in them, and you may spend most of your time just using the books on the desk without going back to the shelves. Having several books on the desk in front of you saves time compared to having only one book there and constantly having to go back to the shelves to return it and take out another.

The same principle allows us to create the illusion of a large memory that we can access as fast as a very small memory. Just as you did not need to access all the books in the library at once with equal probability, a program does not access all of its code or data at once with equal probability. Otherwise, it would be impossible to make most memory accesses fast and still have large memory in computers, just as it would be impossible for you to fit all the library books on your desk and still find what you wanted quickly.

This *principle of locality* underlies both the way in which you did your work in the library and the way that programs operate. The principle of locality states that programs access a relatively small portion of their address space at any instant of time, just as you accessed a very small portion of the library's collection. There are two different types of locality:

- Temporal locality (locality in time): if an item is referenced, it will tend to be referenced again soon. If you recently brought a book to your desk to look at, you will probably need to look at it again soon.
- Spatial locality (locality in space): if an item is referenced, items whose addresses are close by will tend to be referenced soon. For example, when you brought out the book on early English computers to find out about the EDSAC, you also noticed that there was another book shelved next to it about early mechanical computers, so you also brought back that book and, later on, found something useful in that book. Libraries put books on the same topic together on the same shelves to increase spatial locality. We'll see how memory hierarchies use spatial locality a little later in this chapter.

temporal locality The principle stating that if a data location is referenced then it will tend to be referenced again soon.

spatial locality The locality principle stating that if a data location is referenced, data locations with nearby addresses will tend to be referenced soon.

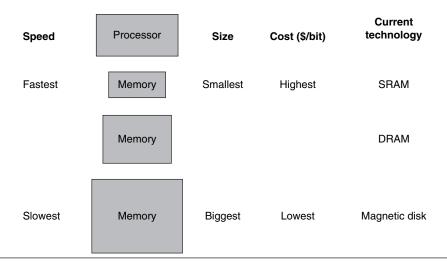


FIGURE 5.1 The basic structure of a memory hierarchy. By implementing the memory system as a hierarchy, the user has the illusion of a memory that is as large as the largest level of the hierarchy, but can be accessed as if it were all built from the fastest memory. Flash memory has replaced disks in many personal mobile devices, and may lead to a new level in the storage hierarchy for desktop and server computers; see Section 5.2.

Just as accesses to books on the desk naturally exhibit locality, locality in programs arises from simple and natural program structures. For example, most programs contain loops, so instructions and data are likely to be accessed repeatedly, showing high amounts of temporal locality. Since instructions are normally accessed sequentially, programs also show high spatial locality. Accesses to data also exhibit a natural spatial locality. For example, sequential accesses to elements of an array or a record will naturally have high degrees of spatial locality.

We take advantage of the principle of locality by implementing the memory of a computer as a **memory hierarchy**. A memory hierarchy consists of multiple levels of memory with different speeds and sizes. The faster memories are more expensive per bit than the slower memories and thus are smaller.

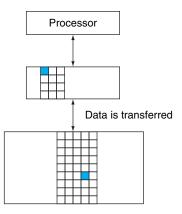
Figure 5.1 shows the faster memory is close to the processor and the slower, less expensive memory is below it. The goal is to present the user with as much memory as is available in the cheapest technology, while providing access at the speed offered by the fastest memory.

The data is similarly hierarchical: a level closer to the processor is generally a subset of any level further away, and all the data is stored at the lowest level. By analogy, the books on your desk form a subset of the library you are working in, which is in turn a subset of all the libraries on campus. Furthermore, as we move away from the processor, the levels take progressively longer to access, just as we might encounter in a hierarchy of campus libraries.

A memory hierarchy can consist of multiple levels, but data is copied between only two adjacent levels at a time, so we can focus our attention on just two levels.

memory hierarchy

A structure that uses multiple levels of memories; as the distance from the processor increases, the size of the memories and the access time both increase.



block (or line) The minimum unit of information that can be either present or not present in a cache.

hit rate The fraction of memory accesses found in a level of the memory hierarchy.

miss rate The fraction of memory accesses not found in a level of the memory hierarchy.

hit time The time required to access a level of the memory hierarchy, including the time needed to determine whether the access is a hit or a miss.

miss penalty The time required to fetch a block into a level of the memory hierarchy from the lower level, including the time to access the block, transmit it from one level to the other, insert it in the level that experienced the miss, and then pass the block to the requestor.

FIGURE 5.2 Every pair of levels in the memory hierarchy can be thought of as having an **upper and lower level.** Within each level, the unit of information that is present or not is called a *block* or a *line*. Usually we transfer an entire block when we copy something between levels.

The upper level—the one closer to the processor—is smaller and faster than the lower level, since the upper level uses technology that is more expensive. Figure 5.2 shows that the minimum unit of information that can be either present or not present in the two-level hierarchy is called a **block** or a **line**; in our library analogy, a block of information is one book.

If the data requested by the processor appears in some block in the upper level, this is called a *hit* (analogous to your finding the information in one of the books on your desk). If the data is not found in the upper level, the request is called a *miss*. The lower level in the hierarchy is then accessed to retrieve the block containing the requested data. (Continuing our analogy, you go from your desk to the shelves to find the desired book.) The **hit rate**, or *hit ratio*, is the fraction of memory accesses found in the upper level; it is often used as a measure of the performance of the memory hierarchy. The **miss rate** (1–hit rate) is the fraction of memory accesses not found in the upper level.

Since performance is the major reason for having a memory hierarchy, the time to service hits and misses is important. **Hit time** is the time to access the upper level of the memory hierarchy, which includes the time needed to determine whether the access is a hit or a miss (that is, the time needed to look through the books on the desk). The **miss penalty** is the time to replace a block in the upper level with the corresponding block from the lower level, plus the time to deliver this block to the processor (or the time to get another book from the shelves and place it on the desk). Because the upper level is smaller and built using faster memory parts, the hit time will be much smaller than the time to access the next level in the hierarchy, which is the major component of the miss penalty. (The time to examine the books on the desk is much smaller than the time to get up and get a new book from the shelves.)

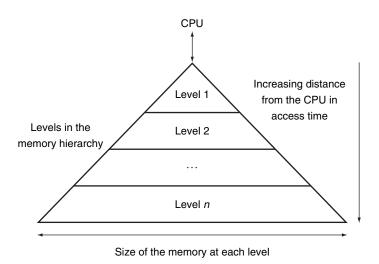


FIGURE 5.3 This diagram shows the structure of a memory hierarchy: as the distance from the processor increases, so does the size. This structure, with the appropriate operating mechanisms, allows the processor to have an access time that is determined primarily by level 1 of the hierarchy and yet have a memory as large as level n. Maintaining this illusion is the subject of this chapter.

hierarchy and yet have a memory as large as level n. Maintaining this illusion is the subject of this chapter. Although the local disk is normally the bottom of the hierarchy, some systems use tape or a file server over a local area network as the next levels of the hierarchy.

5.2

Memory Technologies

There are four primary technologies used today in memory hierarchies. Main memory is implemented from DRAM (dynamic random access memory), while levels closer to the processor (caches) use SRAM (static random access memory). DRAM is less costly per bit than SRAM, although it is substantially slower. The price difference arises because DRAM uses significantly less area per bit of memory, and DRAMs thus have larger capacity for the same amount of silicon; the speed difference arises from several factors described in Section B.9 of Appendix B. The third technology is flash memory. This nonvolatile memory is the secondary memory in Personal Mobile Devices. The fourth technology, used to implement the largest and slowest level in the hierarchy in servers, is magnetic disk. The access time and price per bit vary widely among these technologies, as the table below shows, using typical values for 2012:

| Memory technology | Typical access time | \$ per GiB in 2012 |
|----------------------------|-------------------------|--------------------|
| SRAM semiconductor memory | 0.5–2.5 ns | \$500-\$1000 |
| DRAM semiconductor memory | 50–70 ns | \$10-\$20 |
| Flash semiconductor memory | 5,000-50,000 ns | \$0.75-\$1.00 |
| Magnetic disk | 5,000,000-20,000,000 ns | \$0.05-\$0.10 |

We describe each memory technology in the remainder of this section.

references. This locality arises both because of successive accesses to the same file and because the operating system tries to schedule such accesses together.

Once the head has reached the correct track, we must wait for the desired sector to rotate under the read/write head. This time is called the **rotational latency** or **rotational delay**. The average latency to the desired information is halfway around the disk. Disks rotate at 5400 RPM to 15,000 RPM. The average rotational latency at 5400 RPM is

Average rotational latency =
$$\frac{0.5 \text{ rotation}}{5400 \text{ RPM}} = \frac{0.5 \text{ rotation}}{5400 \text{ RPM/} \left(60 \frac{\text{seconds}}{\text{minute}}\right)}$$

= $0.0056 \text{ seconds} = 5.6 \text{ ms}$

The last component of a disk access, *transfer time*, is the time to transfer a block of bits. The transfer time is a function of the sector size, the rotation speed, and the recording density of a track. Transfer rates in 2012 were between 100 and 200 MB/sec.

One complication is that most disk controllers have a built-in cache that stores sectors as they are passed over; transfer rates from the cache are typically higher, and were up to 750 MB/sec (6 Gbit/sec) in 2012.

Alas, where block numbers are located is no longer intuitive. The assumptions of the sector-track-cylinder model above are that nearby blocks are on the same track, blocks in the same cylinder take less time to access since there is no seek time, and some tracks are closer than others. The reason for the change was the raising of the level of the disk interfaces. To speed-up sequential transfers, these higher-level interfaces organize disks more like tapes than like random access devices. The logical blocks are ordered in serpentine fashion across a single surface, trying to capture all the sectors that are recorded at the same bit density to try to get best performance. Hence, sequential blocks may be on different tracks.

In summary, the two primary differences between magnetic disks and semiconductor memory technologies are that disks have a slower access time because they are mechanical devices—flash is 1000 times as fast and DRAM is 100,000 times as fast—yet they are cheaper per bit because they have very high storage capacity at a modest cost—disk is 10 to 100 time cheaper. Magnetic disks are nonvolatile like flash, but unlike flash there is no write wear-out problem. However, flash is much more rugged and hence a better match to the jostling inherent in personal mobile devices.

5.3

The Basics of Caches

In our library example, the desk acted as a cache—a safe place to store things (books) that we needed to examine. *Cache* was the name chosen to represent the level of the memory hierarchy between the processor and main memory in the first commercial computer to have this extra level. The memories in the datapath in Chapter 4 are simply replaced by caches. Today, although this remains the dominant

rotational latency Also called rotational delay. The time required for the desired sector of a disk to rotate under the read/write head; usually assumed to be half the rotation time.

Cache: a safe place for hiding or storing things.

Webster's New World Dictionary of the American Language, Third College Edition, 1988 use of the word *cache*, the term is also used to refer to any storage managed to take advantage of locality of access. Caches first appeared in research computers in the early 1960s and in production computers later in that same decade; every general-purpose computer built today, from servers to low-power embedded processors, includes caches.

In this section, we begin by looking at a very simple cache in which the processor requests are each one word and the blocks also consist of a single word. (Readers already familiar with cache basics may want to skip to Section 5.4.) Figure 5.7 shows such a simple cache, before and after requesting a data item that is not initially in the cache. Before the request, the cache contains a collection of recent references $X_1, X_2, ..., X_{n-1}$, and the processor requests a word X_n that is not in the cache. This request results in a miss, and the word X_n is brought from memory into the cache.

In looking at the scenario in Figure 5.7, there are two questions to answer: How do we know if a data item is in the cache? Moreover, if it is, how do we find it? The answers are related. If each word can go in exactly one place in the cache, then it is straightforward to find the word if it is in the cache. The simplest way to assign a location in the cache for each word in memory is to assign the cache location based on the *address* of the word in memory. This cache structure is called **direct mapped**, since each memory location is mapped directly to exactly one location in the cache. The typical mapping between addresses and cache locations for a direct-mapped cache is usually simple. For example, almost all direct-mapped caches use this mapping to find a block:

(Block address) modulo (Number of blocks in the cache)

If the number of entries in the cache is a power of 2, then modulo can be computed simply by using the low-order \log_2 (cache size in blocks) bits of the address. Thus, an 8-block cache uses the three lowest bits (8 = 2^3) of the block address. For example, Figure 5.8 shows how the memory addresses between 1_{ten} (00001_{two}) and 29_{ten} (11101_{two}) map to locations 1_{ten} (001_{two}) and 1_{ten} (101_{two}) in a direct-mapped cache of eight words.

Because each cache location can contain the contents of a number of different memory locations, how do we know whether the data in the cache corresponds to a requested word? That is, how do we know whether a requested word is in the cache or not? We answer this question by adding a set of tags to the cache. The tags contain the address information required to identify whether a word in the cache corresponds to the requested word. The tag needs only to contain the upper portion of the address, corresponding to the bits that are not used as an index into the cache. For example, in Figure 5.8 we need only have the upper 2 of the 5 address bits in the tag, since the lower 3-bit index field of the address selects the block. Architects omit the index bits because they are redundant, since by definition the index field of any address of a cache block must be that block number.

We also need a way to recognize that a cache block does not have valid information. For instance, when a processor starts up, the cache does not have good data, and the tag fields will be meaningless. Even after executing many instructions,

direct-mapped cache

A cache structure in which each memory location is mapped to exactly one location in the cache.

tag A field in a table used for a memory hierarchy that contains the address information required to identify whether the associated block in the hierarchy corresponds to a requested word.

| X ₄ |
|------------------|
| X ₁ |
| X _{n-2} |
| |
| X _{n-1} |
| X ₂ |
| X _n |
| X ₃ |

a. Before the reference to X_n

b. After the reference to X_n

FIGURE 5.7 The cache just before and just after a reference to a word X_n that is not initially in the cache. This reference causes a miss that forces the cache to fetch X_n from memory and insert it into the cache.

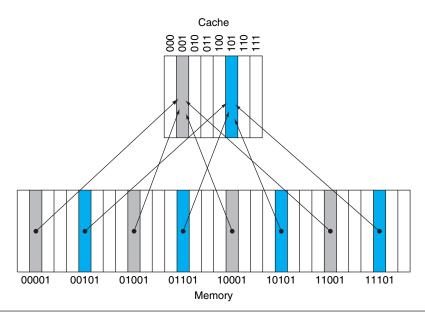


FIGURE 5.8 A direct-mapped cache with eight entries showing the addresses of memory words between 0 and 31 that map to the same cache locations. Because there are eight words in the cache, an address X maps to the direct-mapped cache word X modulo 8. That is, the low-order $\log_2(8) = 3$ bits are used as the cache index. Thus, addresses 00001_{two} , 01001_{two} , 10001_{two} , and 11001_{two} all map to entry 1001_{two} of the cache, while addresses 100101_{two} , 101011_{two} , 101011_{two} , and 111011_{two} all map to entry 1011_{two} of the cache.

valid bit A field in the tables of a memory hierarchy that indicates that the associated block in the hierarchy contains valid data. some of the cache entries may still be empty, as in Figure 5.7. Thus, we need to know that the tag should be ignored for such entries. The most common method is to add a **valid bit** to indicate whether an entry contains a valid address. If the bit is not set, there cannot be a match for this block.

For the rest of this section, we will focus on explaining how a cache deals with reads. In general, handling reads is a little simpler than handling writes, since reads do not have to change the contents of the cache. After seeing the basics of how reads work and how cache misses can be handled, we'll examine the cache designs for real computers and detail how these caches handle writes.



Caching is perhaps the most important example of the big idea of **prediction**. It relies on the principle of locality to try to find the desired data in the higher levels of the memory hierarchy, and provides mechanisms to ensure that when the prediction is wrong it finds and uses the proper data from the lower levels of the memory hierarchy. The hit rates of the cache prediction on modern computers are often higher than 95% (see Figure 5.47).

Accessing a Cache

Below is a sequence of nine memory references to an empty eight-block cache, including the action for each reference. Figure 5.9 shows how the contents of the cache change on each miss. Since there are eight blocks in the cache, the low-order three bits of an address give the block number:

| Decimal address of reference | Binary address of reference | Hit or miss in cache | Assigned cache block (where found or placed) |
|------------------------------|--------------------------------|-------------------------|--|
| 22 | 10110 _{two} | miss (5.6b) | $(10110_{two} \mod 8) = 110_{two}$ |
| 26 | 11010 _{two} | miss (5.6c) | $(11010_{\text{two}} \text{ mod } 8) = 010_{\text{two}}$ |
| 22 | 10110 _{two} | hit | $(10110_{two} \text{ mod } 8) = 110_{two}$ |
| 26 | 11010 _{two} | hit | $(11010_{\text{two}} \text{ mod } 8) = 010_{\text{two}}$ |
| 16 | 10000 _{two} | miss (5.6d) | $(10000_{\text{two}} \text{ mod } 8) = 000_{\text{two}}$ |
| 3 | 00011 _{two} | miss (5.6e) | $(00011_{two} \text{ mod } 8) = 011_{two}$ |
| 16 | 10000 _{two} | hit | $(10000_{\text{two}} \text{ mod } 8) = 000_{\text{two}}$ |
| 18 | 10010 _{two} | miss (5.6f) | $(10010_{\text{two}} \text{ mod } 8) = 010_{\text{two}}$ |
| 16 | 10000 _{two} | hit | $(10000_{\text{two}} \text{ mod } 8) = 000_{\text{two}}$ |

Since the cache is empty, several of the first references are misses; the caption of Figure 5.9 describes the actions for each memory reference. On the eighth reference

| Index | V | Tag | Data |
|-------|---|-----|------|
| 000 | N | | |
| 001 | N | | |
| 010 | N | | |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | N | | |
| 111 | N | | |

a. The initial state of the cache after power-on

| Index | V | Tag | Data |
|-------|---|-------------------|--------------------------------|
| 000 | N | | |
| 001 | N | | |
| 010 | Υ | 11 _{two} | Memory (11010 _{two}) |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | Υ | 10 _{two} | Memory (10110 _{two}) |
| 111 | N | | |

c. After handling a miss of address (11010_{two})

| Index | V | Tag | Data |
|-------|---|-------------------|--------------------------------|
| 000 | Υ | 10 _{two} | Memory (10000 _{two}) |
| 001 | N | | |
| 010 | Υ | 11 _{two} | Memory (11010 _{two}) |
| 011 | Υ | 00 _{two} | Memory (00011 _{two}) |
| 100 | N | | |
| 101 | N | | |
| 110 | Υ | 10 _{two} | Memory (10110 _{two}) |
| 111 | N | | |

e. After handling a miss of address (00011_{two})

| Index | V | Tag | Data |
|-------|---|-------------------|--------------------------------|
| 000 | N | | |
| 001 | N | | |
| 010 | N | | |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 _{two} | Memory (10110 _{two}) |
| 111 | N | | |

b. After handling a miss of address (10110_{two})

| Index | V | Tag | Data |
|-------|---|-------------------|--------------------------------|
| 000 | Υ | 10 _{two} | Memory (10000 _{two}) |
| 001 | N | | |
| 010 | Υ | 11 _{two} | Memory (11010 _{two}) |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | Υ | 10 _{two} | Memory (10110 _{two}) |
| 111 | N | | |

d. After handling a miss of address (10000_{two})

| Index | V | Tag | Data |
|-------|---|-------------------|--------------------------------|
| 000 | Υ | 10 _{two} | Memory (10000 _{two}) |
| 001 | N | | |
| 010 | Υ | 10 _{two} | Memory (10010 _{two}) |
| 011 | Υ | 00 _{two} | Memory (00011 _{two}) |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 _{two} | Memory (10110 _{two}) |
| 111 | N | | |

f. After handling a miss of address (10010_{two})

FIGURE 5.9 The cache contents are shown after each reference request that misses, with the index and tag fields shown in binary for the sequence of addresses on page 386. The cache is initially empty, with all valid bits (V entry in cache) turned off (N). The processor requests the following addresses: 10110_{two} (miss), 11010_{two} (miss), 10110_{two} (hit), 11010_{two} (hit), 10010_{two} (miss), 10000_{two} (hit), 10010_{two} (miss), and 10000_{two} (hit). The figures show the cache contents after each miss in the sequence has been handled. When address 10010_{two} (18) is referenced, the entry for address 11010_{two} (26) must be replaced, and a reference to 11010_{two} will cause a subsequent miss. The tag field will contain only the upper portion of the address. The full address of a word contained in cache block i with tag field j for this cache is $j \times 8 + i$, or equivalently the concatenation of the tag field j and the index i. For example, in cache f above, index 1010_{two} has tag 10_{two} and corresponds to address 10010_{two} .

we have conflicting demands for a block. The word at address $18 (10010_{two})$ should be brought into cache block $2 (010_{two})$. Hence, it must replace the word at address $26 (11010_{two})$, which is already in cache block $2 (010_{two})$. This behavior allows a cache to take advantage of temporal locality: recently referenced words replace less recently referenced words.

This situation is directly analogous to needing a book from the shelves and having no more space on your desk—some book already on your desk must be returned to the shelves. In a direct-mapped cache, there is only one place to put the newly requested item and hence only one choice of what to replace.

We know where to look in the cache for each possible address: the low-order bits of an address can be used to find the unique cache entry to which the address could map. Figure 5.10 shows how a referenced address is divided into

- A tag field, which is used to compare with the value of the tag field of the cache
- A *cache index*, which is used to select the block

The index of a cache block, together with the tag contents of that block, uniquely specifies the memory address of the word contained in the cache block. Because the index field is used as an address to reference the cache, and because an n-bit field has 2^n values, the total number of entries in a direct-mapped cache must be a power of 2. In the MIPS architecture, since words are aligned to multiples of four bytes, the least significant two bits of every address specify a byte within a word. Hence, the least significant two bits are ignored when selecting a word in the block.

The total number of bits needed for a cache is a function of the cache size and the address size, because the cache includes both the storage for the data and the tags. The size of the block above was one word, but normally it is several. For the following situation:

- 32-bit addresses
- A direct-mapped cache
- The cache size is 2^n blocks, so *n* bits are used for the index
- The block size is 2^m words (2^{m+2} bytes), so m bits are used for the word within the block, and two bits are used for the byte part of the address

the size of the tag field is

$$32 - (n + m + 2)$$
.

The total number of bits in a direct-mapped cache is

$$2^n \times (block size + tag size + valid field size).$$

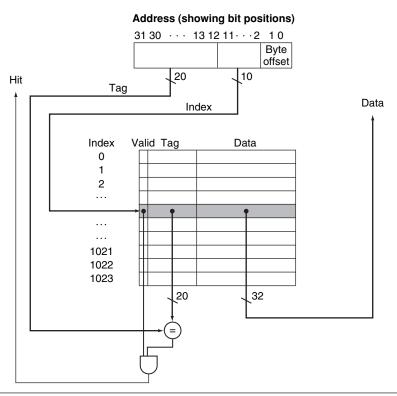


FIGURE 5.10 For this cache, the lower portion of the address is used to select a cache entry consisting of a data word and a tag. This cache holds 1024 words or 4 KiB. We assume 32-bit addresses in this chapter. The tag from the cache is compared against the upper portion of the address to determine whether the entry in the cache corresponds to the requested address. Because the cache has 2^{10} (or 1024) words and a block size of one word, 10 bits are used to index the cache, leaving 32 - 10 - 2 = 20 bits to be compared against the tag. If the tag and upper 20 bits of the address are equal and the valid bit is on, then the request hits in the cache, and the word is supplied to the processor. Otherwise, a miss occurs.

Since the block size is 2^m words (2^{m+5} bits), and we need 1 bit for the valid field, the number of bits in such a cache is

$$2^{n} \times (2^{m} \times 32 + (32 - n - m - 2) + 1) = 2^{n} \times (2^{m} \times 32 + 31 - n - m).$$

Although this is the actual size in bits, the naming convention is to exclude the size of the tag and valid field and to count only the size of the data. Thus, the cache in Figure 5.10 is called a 4 KiB cache.

EXAMPLE

ANSWER

Bits in a Cache

How many total bits are required for a direct-mapped cache with 16 KiB of data and 4-word blocks, assuming a 32-bit address?

We know that 16 KiB is 4096 (2^{12}) words. With a block size of 4 words (2^{2}), there are 1024 (2^{10}) blocks. Each block has 4 \times 32 or 128 bits of data plus a tag, which is 32 - 10 - 2 - 2 bits, plus a valid bit. Thus, the total cache size is

$$2^{10} \times (4 \times 32 + (32 - 10 - 2 - 2) + 1) = 2^{10} \times 147 = 147$$
 Kibibits

or 18.4 KiB for a 16 KiB cache. For this cache, the total number of bits in the cache is about 1.15 times as many as needed just for the storage of the data.

EXAMPLE

ANSWER

Mapping an Address to a Multiword Cache Block

Consider a cache with 64 blocks and a block size of 16 bytes. To what block number does byte address 1200 map?

We saw the formula on page 384. The block is given by

(Block address) modulo (Number of blocks in the cache)

where the address of the block is

 $\frac{\text{Byte address}}{\text{Bytes per block}}$

Notice that this block address is the block containing all addresses between

$$\left| \frac{\text{Byte address}}{\text{Bytes per block}} \right| \times \text{Bytes per block}$$

and

$$\left[\frac{\text{Byte address}}{\text{Bytes per block}}\right] \times \text{Bytes per block} + (\text{Bytes per block} - 1)$$

Thus, with 16 bytes per block, byte address 1200 is block address

$$\left[\frac{1200}{6}\right] = 75$$

which maps to cache block number (75 modulo 64) = 11. In fact, this block maps all addresses between 1200 and 1215.

Larger blocks exploit spatial locality to lower miss rates. As Figure 5.11 shows, increasing the block size usually decreases the miss rate. The miss rate may go up eventually if the block size becomes a significant fraction of the cache size, because the number of blocks that can be held in the cache will become small, and there will be a great deal of competition for those blocks. As a result, a block will be bumped out of the cache before many of its words are accessed. Stated alternatively, spatial locality among the words in a block decreases with a very large block; consequently, the benefits in the miss rate become smaller.

A more serious problem associated with just increasing the block size is that the cost of a miss increases. The miss penalty is determined by the time required to fetch

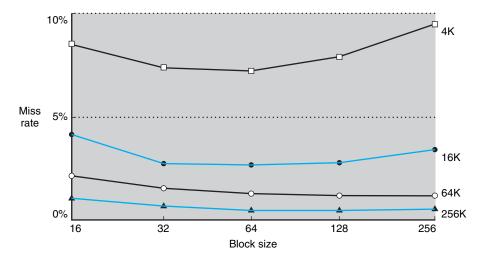


FIGURE 5.11 Miss rate versus block size. Note that the miss rate actually goes up if the block size is too large relative to the cache size. Each line represents a cache of different size. (This figure is independent of associativity, discussed soon.) Unfortunately, SPEC CPU2000 traces would take too long if block size were included, so this data is based on SPEC92.

To take advantage of spatial locality, a cache must have a block size larger than one word. The use of a larger block decreases the miss rate and improves the efficiency of the cache by reducing the amount of tag storage relative to the amount of data storage in the cache. Although a larger block size decreases the miss rate, it can also increase the miss penalty. If the miss penalty increased linearly with the block size, larger blocks could easily lead to lower performance.

To avoid performance loss, the bandwidth of main memory is increased to transfer cache blocks more efficiently. Common methods for increasing bandwidth external to the DRAM are making the memory wider and interleaving. DRAM designers have steadily improved the interface between the processor and memory to increase the bandwidth of burst mode transfers to reduce the cost of larger cache block sizes.

Check Yourself

The speed of the memory system affects the designer's decision on the size of the cache block. Which of the following cache designer guidelines are generally valid?

- 1. The shorter the memory latency, the smaller the cache block
- 2. The shorter the memory latency, the larger the cache block
- 3. The higher the memory bandwidth, the smaller the cache block
- 4. The higher the memory bandwidth, the larger the cache block

5.4

Measuring and Improving Cache Performance

In this section, we begin by examining ways to measure and analyze cache performance. We then explore two different techniques for improving cache performance. One focuses on reducing the miss rate by reducing the probability that two different memory blocks will contend for the same cache location. The second technique reduces the miss penalty by adding an additional level to the hierarchy. This technique, called *multilevel caching*, first appeared in high-end computers selling for more than \$100,000 in 1990; since then it has become common on personal mobile devices selling for a few hundred dollars!

CPU time can be divided into the clock cycles that the CPU spends executing the program and the clock cycles that the CPU spends waiting for the memory system. Normally, we assume that the costs of cache accesses that are hits are part of the normal CPU execution cycles. Thus,

The memory-stall clock cycles come primarily from cache misses, and we make that assumption here. We also restrict the discussion to a simplified model of the memory system. In real processors, the stalls generated by reads and writes can be quite complex, and accurate performance prediction usually requires very detailed simulations of the processor and memory system.

Memory-stall clock cycles can be defined as the sum of the stall cycles coming from reads plus those coming from writes:

$$Memory-stall\ clock\ cycles = (Read-stall\ cycles + Write-stall\ cycles)$$

The read-stall cycles can be defined in terms of the number of read accesses per program, the miss penalty in clock cycles for a read, and the read miss rate:

$$Read-stall\ cycles = \frac{Reads}{Program} \times Read\ miss\ rate \times Read\ miss\ penalty$$

Writes are more complicated. For a write-through scheme, we have two sources of stalls: write misses, which usually require that we fetch the block before continuing the write (see the *Elaboration* on page 394 for more details on dealing with writes), and write buffer stalls, which occur when the write buffer is full when a write occurs. Thus, the cycles stalled for writes equals the sum of these two:

$$Write-stall\ cycles = \left(\frac{Writes}{Program} \times Write\ miss\ rate \times Write\ miss\ penalty\right) \\ + Write\ buffer\ stalls$$

Because the write buffer stalls depend on the proximity of writes, and not just the frequency, it is not possible to give a simple equation to compute such stalls. Fortunately, in systems with a reasonable write buffer depth (e.g., four or more words) and a memory capable of accepting writes at a rate that significantly exceeds the average write frequency in programs (e.g., by a factor of 2), the write buffer stalls will be small, and we can safely ignore them. If a system did not meet these criteria, it would not be well designed; instead, the designer should have used either a deeper write buffer or a write-back organization.

Write-back schemes also have potential additional stalls arising from the need to write a cache block back to memory when the block is replaced. We will discuss this more in Section 5.8.

In most write-through cache organizations, the read and write miss penalties are the same (the time to fetch the block from memory). If we assume that the write buffer stalls are negligible, we can combine the reads and writes by using a single miss rate and the miss penalty:

$$Memory-stall\ clock\ cycles = \frac{Memory\ accesses}{Program} \times Miss\ rate \times Miss\ penalty$$

We can also factor this as

$$\label{eq:memory-stall} \text{Memory-stall clock cycles} = \frac{\text{Instructions}}{\text{Program}} \times \frac{\text{Misses}}{\text{Instruction}} \times \text{Miss penalty}$$

Let's consider a simple example to help us understand the impact of cache performance on processor performance.

Calculating Cache Performance

Assume the miss rate of an instruction cache is 2% and the miss rate of the data cache is 4%. If a processor has a CPI of 2 without any memory stalls and the miss penalty is 100 cycles for all misses, determine how much faster a processor would run with a perfect cache that never missed. Assume the frequency of all loads and stores is 36%.

The number of memory miss cycles for instructions in terms of the Instruction count (I) is

Instruction miss cycles =
$$I \times 2\% \times 100 = 2.00 \times I$$

As the frequency of all loads and stores is 36%, we can find the number of memory miss cycles for data references:

Data miss cycles =
$$I \times 36\% \times 4\% \times 100 = 1.44 \times I$$

EXAMPLE

ANSWER

The total number of memory-stall cycles is 2.00 I + 1.44 I = 3.44 I. This is more than three cycles of memory stall per instruction. Accordingly, the total CPI including memory stalls is 2 + 3.44 = 5.44. Since there is no change in instruction count or clock rate, the ratio of the CPU execution times is

$$\frac{\text{CPU time with stalls}}{\text{CPU time with perfect cache}} = \frac{I \times \text{CPI}_{\text{stall}} \times \text{Clock cycle}}{I \times \text{CPI}_{\text{perfect}} \times \text{Clock cycle}}$$
$$= \frac{\text{CPI}_{\text{stall}}}{\text{CPI}_{\text{perfect}}} = \frac{5.44}{2}$$

The performance with the perfect cache is better by $\frac{5.44}{2} = 2.72$.

What happens if the processor is made faster, but the memory system is not? The amount of time spent on memory stalls will take up an increasing fraction of the execution time; Amdahl's Law, which we examined in Chapter 1, reminds us of this fact. A few simple examples show how serious this problem can be. Suppose we speed-up the computer in the previous example by reducing its CPI from 2 to 1 without changing the clock rate, which might be done with an improved pipeline. The system with cache misses would then have a CPI of 1 + 3.44 = 4.44, and the system with the perfect cache would be

$$\frac{4.44}{1} = 4.44 \text{ times as fast.}$$

The amount of execution time spent on memory stalls would have risen from

$$\frac{3.44}{5.44} = 63\%$$

$$\frac{3.44}{4.44} = 77\%$$

Similarly, increasing the clock rate without changing the memory system also increases the performance lost due to cache misses.

The previous examples and equations assume that the hit time is not a factor in determining cache performance. Clearly, if the hit time increases, the total time to access a word from the memory system will increase, possibly causing an increase in the processor cycle time. Although we will see additional examples of what can increase

hit time shortly, one example is increasing the cache size. A larger cache could clearly have a longer access time, just as, if your desk in the library was very large (say, 3 square meters), it would take longer to locate a book on the desk. An increase in hit time likely adds another stage to the pipeline, since it may take multiple cycles for a cache hit. Although it is more complex to calculate the performance impact of a deeper pipeline, at some point the increase in hit time for a larger cache could dominate the improvement in hit rate, leading to a decrease in processor performance.

To capture the fact that the time to access data for both hits and misses affects performance, designers sometime use *average memory access time* (AMAT) as a way to examine alternative cache designs. Average memory access time is the average time to access memory considering both hits and misses and the frequency of different accesses; it is equal to the following:

 $AMAT = Time for a hit + Miss rate \times Miss penalty$

Calculating Average Memory Access Time

Find the AMAT for a processor with a 1 ns clock cycle time, a miss penalty of 20 clock cycles, a miss rate of 0.05 misses per instruction, and a cache access time (including hit detection) of 1 clock cycle. Assume that the read and write miss penalties are the same and ignore other write stalls.

The average memory access time per instruction is

```
AMAT = Time for a hit + Miss rate \times Miss penalty
= 1 + 0.05 \times 20
= 2 clock cycles
```

or 2 ns.

The next subsection discusses alternative cache organizations that decrease miss rate but may sometimes increase hit time; additional examples appear in Section 5.15, Fallacies and Pitfalls.

Reducing Cache Misses by More Flexible Placement of Blocks

So far, when we place a block in the cache, we have used a simple placement scheme: A block can go in exactly one place in the cache. As mentioned earlier, it is called *direct mapped* because there is a direct mapping from any block address in memory to a single location in the upper level of the hierarchy. However, there is actually a whole range of schemes for placing blocks. Direct mapped, where a block can be placed in exactly one location, is at one extreme.

EXAMPLE

ANSWER

At the other extreme is a scheme where a block can be placed in *any* location in the cache. Such a scheme is called **fully associative**, because a block in memory may be associated with any entry in the cache. To find a given block in a fully associative cache, all the entries in the cache must be searched because a block can be placed in any one. To make the search practical, it is done in parallel with a comparator associated with each cache entry. These comparators significantly increase the hardware cost, effectively making fully associative placement practical only for caches with small numbers of blocks.

The middle range of designs between direct mapped and fully associative is called **set associative**. In a set-associative cache, there are a fixed number of locations where each block can be placed. A set-associative cache with *n* locations for a block is called an *n*-way set-associative cache. An *n*-way set-associative cache consists of a number of sets, each of which consists of *n* blocks. Each block in the memory maps to a unique *set* in the cache given by the index field, and a block can be placed in *any* element of that set. Thus, a set-associative placement combines direct-mapped placement and fully associative placement: a block is directly mapped into a set, and then all the blocks in the set are searched for a match. For example, Figure 5.14 shows where block 12 may be placed in a cache with eight blocks total, according to the three block placement policies.

Remember that in a direct-mapped cache, the position of a memory block is given by

(Block number) modulo (Number of *blocks* in the cache)

fully associative cache A cache structure in which a block can be placed in any location in the cache.

set-associative cache A cache that has a fixed

number of locations (at least two) where each block can be placed.

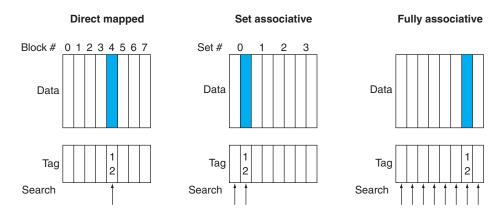


FIGURE 5.14 The location of a memory block whose address is 12 in a cache with eight blocks varies for direct-mapped, set-associative, and fully associative placement. In direct-mapped placement, there is only one cache block where memory block 12 can be found, and that block is given by (12 mod dulo 8) = 4. In a two-way set-associative cache, there would be four sets, and memory block 12 must be in set (12 mod 4) = 0; the memory block could be in either element of the set. In a fully associative placement, the memory block for block address 12 can appear in any of the eight cache blocks.

In a set-associative cache, the set containing a memory block is given by

(Block number) modulo (Number of *sets* in the cache)

Since the block may be placed in any element of the set, all the tags of all the elements of the set must be searched. In a fully associative cache, the block can go anywhere, and all tags of all the blocks in the cache must be searched.

We can also think of all block placement strategies as a variation on set associativity. Figure 5.15 shows the possible associativity structures for an eight-block cache. A direct-mapped cache is simply a one-way set-associative cache: each cache entry holds one block and each set has one element. A fully associative cache with *m* entries is simply an *m*-way set-associative cache; it has one set with *m* blocks, and an entry can reside in any block within that set.

The advantage of increasing the degree of associativity is that it usually decreases the miss rate, as the next example shows. The main disadvantage, which we discuss in more detail shortly, is a potential increase in the hit time.

One-way set associative (direct mapped)

| Block | Tag | Data |
|-------|-----|------|
| 0 | | |
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |
| 6 | | |
| 7 | | |
| | | |

Two-way set associative

| Set | Tag | Data | Tag | Data |
|-----|-----|------|-----|------|
| 0 | | | | |
| 1 | | | | |
| 2 | | | | |
| 3 | | | | |
| | | | | |

Four-way set associative

| Set | Tag | Data | Tag | Data | Tag | Data | Tag | Data |
|-----|-----|------|-----|------|-----|------|-----|------|
| 0 | | | | | | | | |
| 1 | | | | | | | | |

Eight-way set associative (fully associative)

| Tag | g Data | Tag | Data |
|-----|--------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|
| | | | | | | | | | | | | | | | |

FIGURE 5.15 An eight-block cache configured as direct mapped, two-way set associative, four-way set associative, and fully associative. The total size of the cache in blocks is equal to the number of sets times the associativity. Thus, for a fixed cache size, increasing the associativity decreases the number of sets while increasing the number of elements per set. With eight blocks, an eight-way set-associative cache is the same as a fully associative cache.

Misses and Associativity in Caches

Assume there are three small caches, each consisting of four one-word blocks. One cache is fully associative, a second is two-way set-associative, and the third is direct-mapped. Find the number of misses for each cache organization given the following sequence of block addresses: 0, 8, 0, 6, and 8.

EXAMPLE

The direct-mapped case is easiest. First, let's determine to which cache block each block address maps:

ANSWER

| Block address | Cache block |
|---------------|------------------|
| 0 | (0 modulo 4) = 0 |
| 6 | (6 modulo 4) = 2 |
| 8 | (8 modulo 4) = 0 |

Now we can fill in the cache contents after each reference, using a blank entry to mean that the block is invalid, colored text to show a new entry added to the cache for the associated reference, and plain text to show an old entry in the cache:

| Address of memory | Hit | Contents of cache blocks after reference | | | | | | | |
|-------------------|---------|--|---|-----------|---|--|--|--|--|
| block accessed | or miss | 0 | 1 | 2 | 3 | | | | |
| 0 | miss | Memory[0] | | | | | | | |
| 8 | miss | Memory[8] | | | | | | | |
| 0 | miss | Memory[0] | | | | | | | |
| 6 | miss | Memory[0] | | Memory[6] | | | | | |
| 8 | miss | Memory[8] | | Memory[6] | | | | | |

The direct-mapped cache generates five misses for the five accesses.

The set-associative cache has two sets (with indices 0 and 1) with two elements per set. Let's first determine to which set each block address maps:

| Block address | Cache set |
|---------------|------------------|
| 0 | (0 modulo 2) = 0 |
| 6 | (6 modulo 2) = 0 |
| 8 | (8 modulo 2) = 0 |

Because we have a choice of which entry in a set to replace on a miss, we need a replacement rule. Set-associative caches usually replace the least recently used block within a set; that is, the block that was used furthest in the past is replaced. (We will discuss other replacement rules in more detail shortly.) Using this replacement rule, the contents of the set-associative cache after each reference looks like this:

| Address of memory | Hit | Contents of cache blocks after reference | | | | | | |
|-------------------|---------|--|-----------|-------|-------|--|--|--|
| block accessed | or miss | Set 0 | Set 0 | Set 1 | Set 1 | | | |
| 0 | miss | Memory[0] | | | | | | |
| 8 | miss | Memory[0] | Memory[8] | | | | | |
| 0 | hit | Memory[0] | Memory[8] | | | | | |
| 6 | miss | Memory[0] | Memory[6] | | | | | |
| 8 | miss | Memory[8] | Memory[6] | | | | | |

Notice that when block 6 is referenced, it replaces block 8, since block 8 has been less recently referenced than block 0. The two-way set-associative cache has four misses, one less than the direct-mapped cache.

The fully associative cache has four cache blocks (in a single set); any memory block can be stored in any cache block. The fully associative cache has the best performance, with only three misses:

| Address of memory | Hit | Contents of cache blocks after reference | | | | | | |
|-------------------|---------|--|-----------|-----------|---------|--|--|--|
| block accessed | or miss | Block 0 | Block 1 | Block 2 | Block 3 | | | |
| 0 | miss | Memory[0] | | | | | | |
| 8 | miss | Memory[0] | Memory[8] | | | | | |
| 0 | hit | Memory[0] | Memory[8] | | | | | |
| 6 | miss | Memory[0] | Memory[8] | Memory[6] | | | | |
| 8 | hit | Memory[0] | Memory[8] | Memory[6] | | | | |

For this series of references, three misses is the best we can do, because three unique block addresses are accessed. Notice that if we had eight blocks in the cache, there would be no replacements in the two-way set-associative cache (check this for yourself), and it would have the same number of misses as the fully associative cache. Similarly, if we had 16 blocks, all 3 caches would have the same number of misses. Even this trivial example shows that cache size and associativity are not independent in determining cache performance.

How much of a reduction in the miss rate is achieved by associativity? Figure 5.16 shows the improvement for a 64 KiB data cache with a 16-word block, and associativity ranging from direct mapped to eight-way. Going from one-way to two-way associativity decreases the miss rate by about 15%, but there is little further improvement in going to higher associativity.

| Associativity | Data miss rate |
|---------------|----------------|
| 1 | 10.3% |
| 2 | 8.6% |
| 4 | 8.3% |
| 8 | 8.1% |

FIGURE 5.16 The data cache miss rates for an organization like the Intrinsity FastMATH processor for SPEC CPU2000 benchmarks with associativity varying from one-way to eight-way. These results for 10 SPEC CPU2000 programs are from Hennessy and Patterson (2003).

| Tag | Index | Block offset |
|-----|-------|--------------|
|-----|-------|--------------|

FIGURE 5.17 The three portions of an address in a set-associative or direct-mapped **cache.** The index is used to select the set, then the tag is used to choose the block by comparison with the blocks in the selected set. The block offset is the address of the desired data within the block.

Locating a Block in the Cache

Now, let's consider the task of finding a block in a cache that is set associative. Just as in a direct-mapped cache, each block in a set-associative cache includes an address tag that gives the block address. The tag of every cache block within the appropriate set is checked to see if it matches the block address from the processor. Figure 5.17 decomposes the address. The index value is used to select the set containing the address of interest, and the tags of all the blocks in the set must be searched. Because speed is of the essence, all the tags in the selected set are searched in parallel. As in a fully associative cache, a sequential search would make the hit time of a set-associative cache too slow.

If the total cache size is kept the same, increasing the associativity increases the number of blocks per set, which is the number of simultaneous compares needed to perform the search in parallel: each increase by a factor of 2 in associativity doubles the number of blocks per set and halves the number of sets. Accordingly, each factor-of-2 increase in associativity decreases the size of the index by 1 bit and increases the size of the tag by 1 bit. In a fully associative cache, there is effectively only one set, and all the blocks must be checked in parallel. Thus, there is no index, and the entire address, excluding the block offset, is compared against the tag of every block. In other words, we search the entire cache without any indexing.

In a direct-mapped cache, only a single comparator is needed, because the entry can be in only one block, and we access the cache simply by indexing. Figure 5.18 shows that in a four-way set-associative cache, four comparators are needed, together with a 4-to-1 multiplexor to choose among the four potential members of the selected set. The cache access consists of indexing the appropriate set and then searching the tags of the set. The costs of an associative cache are the extra comparators and any delay imposed by having to do the compare and select from among the elements of the set.

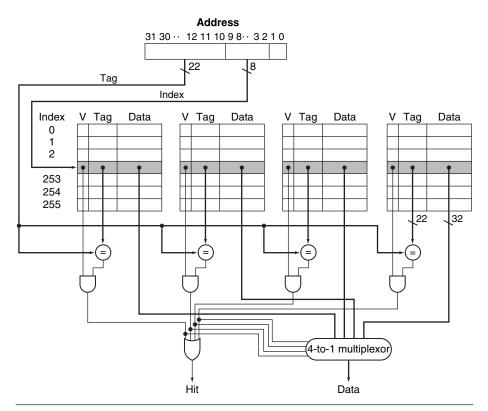


FIGURE 5.18 The implementation of a four-way set-associative cache requires four comparators and a 4-to-1 multiplexor. The comparators determine which element of the selected set (if any) matches the tag. The output of the comparators is used to select the data from one of the four blocks of the indexed set, using a multiplexor with a decoded select signal. In some implementations, the Output enable signals on the data portions of the cache RAMs can be used to select the entry in the set that drives the output. The Output enable signal comes from the comparators, causing the element that matches to drive the data outputs. This organization eliminates the need for the multiplexor.

The choice among direct-mapped, set-associative, or fully associative mapping in any memory hierarchy will depend on the cost of a miss versus the cost of implementing associativity, both in time and in extra hardware.

Elaboration: A Content Addressable Memory (CAM) is a circuit that combines comparison and storage in a single device. Instead of supplying an address and reading a word like a RAM, you supply the data and the CAM looks to see if it has a copy and returns the index of the matching row. CAMs mean that cache designers can afford to implement much higher set associativity than if they needed to build the hardware out of SRAMs and comparators. In 2013, the greater size and power of CAM generally leads to 2-way and 4-way set associativity being built from standard SRAMs and comparators, with 8-way and above built using CAMs.

Choosing Which Block to Replace

When a miss occurs in a direct-mapped cache, the requested block can go in exactly one position, and the block occupying that position must be replaced. In an associative cache, we have a choice of where to place the requested block, and hence a choice of which block to replace. In a fully associative cache, all blocks are candidates for replacement. In a set-associative cache, we must choose among the blocks in the selected set.

The most commonly used scheme is **least recently used** (LRU), which we used in the previous example. In an LRU scheme, the block replaced is the one that has been unused for the longest time. The set associative example on page 405 uses LRU, which is why we replaced Memory(0) instead of Memory(6).

LRU replacement is implemented by keeping track of when each element in a set was used relative to the other elements in the set. For a two-way set-associative cache, tracking when the two elements were used can be implemented by keeping a single bit in each set and setting the bit to indicate an element whenever that element is referenced. As associativity increases, implementing LRU gets harder; in Section 5.8, we will see an alternative scheme for replacement.

least recently used (LRU) A replacement scheme in which the block replaced is the one that has been unused for

the longest time.

Size of Tags versus Set Associativity

Increasing associativity requires more comparators and more tag bits per cache block. Assuming a cache of 4096 blocks, a 4-word block size, and a 32-bit address, find the total number of sets and the total number of tag bits for caches that are direct mapped, two-way and four-way set associative, and fully associative.

EXAMPLE

Since there are $16 (= 2^4)$ bytes per block, a 32-bit address yields 32-4=28 bits to be used for index and tag. The direct-mapped cache has the same number of sets as blocks, and hence 12 bits of index, since $\log_2(4096)=12$; hence, the total number is $(28-12)\times 4096=16\times 4096=66$ K tag bits.

Each degree of associativity decreases the number of sets by a factor of 2 and thus decreases the number of bits used to index the cache by 1 and increases the number of bits in the tag by 1. Thus, for a two-way set-associative cache, there are 2048 sets, and the total number of tag bits is $(28-11) \times 2 \times 2048 = 34 \times 2048 = 70$ Kbits. For a four-way set-associative cache, the total number of sets is 1024, and the total number is $(28-10) \times 4 \times 1024 = 72 \times 1024 = 74$ K tag bits.

For a fully associative cache, there is only one set with 4096 blocks, and the tag is 28 bits, leading to $28 \times 4096 \times 1 = 115$ K tag bits.

ANSWER

Cache Block Replacement Policies edit

Bélády's Algorithm[edit]

The *most* efficient caching algorithm would be to always discard the information that will not be needed for the longest time in the future. This optimal result is referred to as <u>Bélády</u>'s optimal algorithm/simply optimal replacement policy or <u>the clairvoyant algorithm</u>. Since it is generally impossible to predict how far in the future information will be needed, this is generally not implementable in practice. The practical minimum can be calculated only after experimentation, and one can compare the effectiveness of the actually chosen cache algorithm.

| Access | 5 | 0 | 1 | 2 | 0 | 3 | 1 | 2 | 5 | 2 |
|----------|---|---|---|---|---|---|---|---|---|---|
| Sequence | | | | | | | | | | |
| Frame1 | 5 | 5 | 5 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| Frame 2 | | 0 | 0 | 0 | 0 | 3 | 3 | 3 | 3 | 3 |
| Frame 3 | | | 1 | 1 | 1 | 1 | 1 | 1 | 5 | 5 |
| | f | f | f | f | | f | | | f | |

At the moment when a <u>page fault</u> occurs, some set of pages is in memory. In the example, the sequence of '5', '0', '1' is accessed by Frame 1, Frame 2, Frame 3 respectively. Then when '2' is accessed, it replaces value '5', which is in frame 1 since it predicts that value '5' is not going to be accessed in the near future. Because a real-life general purpose operating system cannot actually predict when '5' will be accessed, Bélády's Algorithm cannot be implemented on such a system.

First In First Out (FIFO)[edit]

Using this algorithm the cache behaves in the same way as a <u>FIFO queue</u>. The cache evicts the first block accessed first without any regard to how often or how many times it was accessed before.

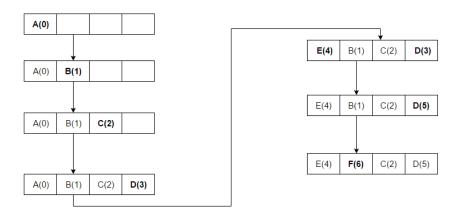
Last In First Out (LIFO)[edit]

Using this algorithm the cache behaves in the exact opposite way as a FIFO queue. The cache evicts the block accessed most recently first without any regard to how often or how many times it was accessed before.

Least Recently Used (LRU)[edit]

Discards the least recently used items first. This algorithm requires keeping track of what was used when, which is expensive if one wants to make sure the algorithm always discards the least recently used item. General implementations of this technique require keeping "age bits" for cache-lines and track the "Least Recently Used" cache-line based on age-bits. In such an implementation, every time a cache-line is used, the age of all other cache-lines changes. LRU is actually a family of caching algorithms with members including 2Q by Theodore Johnson and Dennis Shasha, and LRU/K by Pat O'Neil, Betty O'Neil and Gerhard Weikum.

The access sequence for the below example is A B C D E D F.



In the above example once A B C D gets installed in the blocks with sequence numbers (Increment 1 for each new Access) and when E is accessed, it is a miss and it needs to be installed in one of the blocks. According to the LRU Algorithm, since A has the lowest Rank(A(0)), E will replace A.