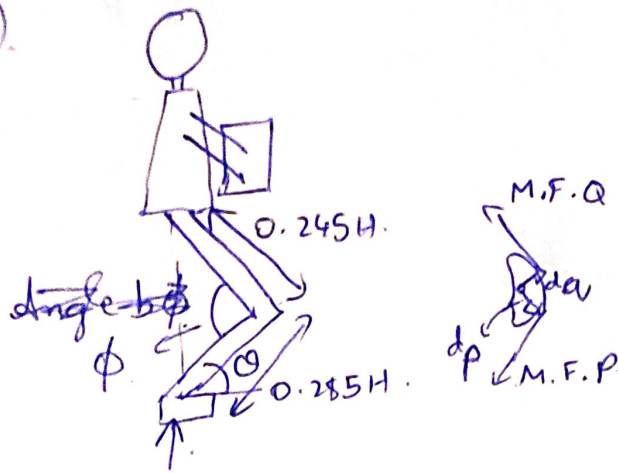


Using anthropometric data from the slide.

(4.)



The ratios of moment arms of the quadriceps and patellofemoral patellar tendon are taken from an online source.

Balancing moment about patellofemoral joint.

$$M.F.Q (\text{quadriceps Muscle force}) \times d_q = M.F.P \times d_p \quad (\text{patellar tendon force})$$

$$\Rightarrow \frac{M.F.Q}{M.F.P} = \frac{d_p}{d_q} = \frac{18.4}{17.1} = 1.076$$

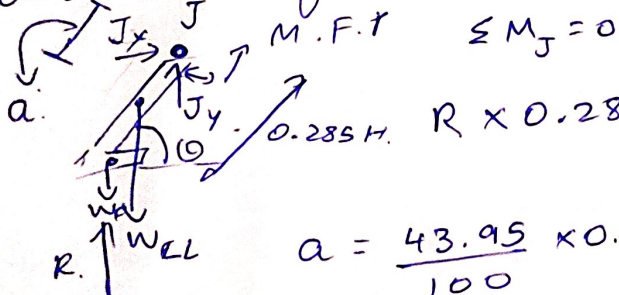
Assuming the leg origination point to be directly above the feet.

$$\Rightarrow 0.285H \times \cos \theta = 0.245 \cos(\phi - \theta)$$

$$\Rightarrow \frac{0.285}{0.245} = \frac{\cos \phi \cos \theta + \sin \phi \sin \theta}{\cos \theta} = \cos \phi + \sin \phi \tan \theta$$

$$\Rightarrow \tan \theta = \tan^{-1} \left[\left(\frac{0.285}{0.245} - \cos \phi \right) \times \frac{1}{\sin \phi} \right]$$

Separating the ~~leg~~ portion below the knee about the tibiofemoral joint (SHANK)



The value of patellofemoral moment arm of patellar tendon about tibiofemoral joint from o

$$R \times 0.285H = W_F \times 0.285H \cos \theta + W_L \times a \cos \theta$$

$$a = \frac{43.95}{100} \times 0.285H = 0.125H$$

$$W_L = \frac{4.33}{100} \times W = 0.0433W$$

$$W_F = 0.0137W$$

d_p = Value of patellar tendon force moment arm about tibiofemoral joint taken from online source = 49 mm

Knowns: W, H, Shank Length, Thigh Length, Shank to Thigh Angle (ϕ), Moment Arm Ratios, Patellar Tendon Force Moment Arm, External Load

Unknowns: Patellar Tendon Force, Patellofemoral Joint Reaction, Tibiofemoral Joint Reaction, Quadriceps Force, Theta.

$$\Rightarrow \frac{\cos(\theta)}{0.049} \left((W+10) \times 0.285H - (0.0137W) \times 0.285H \cos \theta - (0.0433W) \times 0.125H \cos \theta \right) = M.F.P.$$

$$\sum F_x = 0 \Rightarrow J_x = -M.F.P \cos \theta$$

$$\sum F_y = 0 \Rightarrow J_y = W_F + W_{LL} - R = (0.0433 + 0.0137)W - (M.F.P \times \sin(\theta) - (W+10) \sin(\theta))$$

J_x and J_y are the two perpendicular components of the tibiofemoral joint force.

M.F.P \rightarrow patellar tendon force.

Let $Q_x \hat{i} + Q_y \hat{j}$ be the patellofemoral joint force. Then,

$$Q_x = M.F.P \cos \theta + M.F. Q \cos(\phi - \theta)$$

$$Q_y = M.F.P \sin \theta - M.F. Q \sin(\phi - \theta)$$