

# Naive Bayes Classification

- Probabilistic learning  $\rightarrow$  has multiple hypothesis to clear probability initially by.
- Incremental training  $\rightarrow$  training example to probability update to verify by (increase/decrease). Model gets better with time.
- Probabilistic Prediction  $\rightarrow$  To handle uncertainty, there can be multiple hypothesis. Probability by multiple weight change.
- We know whether each of events  $S, M, E$  occurred.
- We want to find out whether event  $P$  is true.  
 $Pr(P | S, M, E) \Rightarrow$  Means ais banday ko computer by Bayes's Theorem: lany ko chance kitna hy.

$$Pr(A | B) = \frac{Pr(A) \times Pr(B | A)}{Pr(B)}$$

$$Pr(P | S, M, E) = \frac{Pr(P) \times Pr(S, M, E | P)}{Pr(S, M, E)}$$

$$= \frac{Pr(P)}{Pr(S, M, E)} \times Pr(S | P) \times Pr(M | P) \times Pr(E | P)$$

- Naive Bayes assumes  $S, M, E$  are independent from each other. When  $P$  is fixed.

- The class (buyer or non-buyer) to predict kaise niklay ga, final prediction is that.



Naive Bayes sometimes called Idiot Bayes

• Naive Bayesian Classification

- Test Set represents a young student with fair credit rating.

$$Pr(P | S, \neg M, \neg E)$$

$$\frac{Pr(P) \times Pr(S, \neg M, \neg E | P)}{Pr(S, \neg M, \neg E)}$$

- statistical independence is assumed

$$\frac{Pr(P) \times Pr(S | P) \cdot Pr(\neg M | P) \cdot Pr(\neg E | P)}{Pr(S, \neg M, \neg E)}$$

• Example:-

Positives (P)  $\Rightarrow$  Buy Computers (9/14)

Negatives (n)  $\Rightarrow$  do not buy computer (5/14)

• Now we calculate probabilities for each column.

1) Age

≤ 30	youth	$P(\text{youth}   P)$	$2/9$	$P(\text{youth}   n)$	$3/5$
31-40	mid	$P(\text{mid}   P)$	$4/9$	$P(\text{youth}   n)$	$0/5$
> 40	senior	$P(\text{senior}   P)$	$3/9$	$P(\text{youth}   n)$	$2/5$

2) Income.

$P(\text{low}   P)$	$3/9$	$P(\text{low}   n)$	$1/5$
$P(\text{medium}   P)$	$4/9$	$P(\text{medium}   n)$	$2/5$
$P(\text{high}   P)$	$2/9$	$P(\text{high}   n)$	$2/5$



3) Student

$$P(\text{yes} | P) = \frac{6}{9} \quad P(\text{yes} | n) = \frac{1}{5}$$

$$P(\text{no} | P) = \frac{3}{9} \quad P(\text{no} | n) = \frac{4}{5}$$

4) Credit

$$P(\text{fair} | P) = \frac{6}{9} \quad P(\text{fair} | n) = \frac{2}{5}$$

$$P(\text{excellent} | P) = \frac{3}{9} \quad P(\text{excellent} | n) = \frac{3}{5}$$

- One new record. X

X = Age = youth, student = yes.

Income = low, credit rating = fair.

	Positives	Negatives
Youth = Age	$\frac{2}{9}$	$\frac{3}{5}$
Yes = student	$\frac{6}{9}$	$\frac{1}{5}$
Fair = credit rating	$\frac{6}{9}$	$\frac{2}{5}$
Low = income	$\frac{3}{9}$	$\frac{1}{5}$

$$\text{Positive} = P(\text{youth} | P) \times P(\text{yes} | P) \times P(\text{fair} | P) \times P(\text{low} | P) \times P(P)$$

$$= \frac{2}{9} \times \frac{6}{9} \times \frac{6}{9} \times \frac{3}{9} = 0.6211$$

$$\text{Negative} = \frac{3}{5} \times \frac{1}{5} \times \frac{2}{5} \times \frac{1}{5} \times \frac{5}{14}$$

$$= 0.0034$$

$P > n$

So he will buy.