

Session-2

122-2041

122-1855

(Tashfeen) (hasiba)

Each basket is subset of items

↑ Date: _____

Association rules (market basket analysis)

↓ generates rules from counts

Support (S) \Rightarrow %age of transactions

$P(A \cap B)$ } measures frequency of association

Confidence (C) \rightarrow

$\text{Conf}(I \rightarrow j) = \frac{\text{support}(I \cup j)}{\text{support}(I)} \frac{P(A \cap B)}{P(A)}$ } strength of association

Parameters :-

- i) Finding all items that appears frequently } min support count
- ii) Find strong associations among frequent items } Confidence

\Rightarrow Frequent itemsets (like threshold = 3)



Now, we see that in each basket the items which are repeated at least 3 times.

\Rightarrow

Confidence

$$\text{Conf}(I \rightarrow j) = \frac{\text{support}(I \cup j)}{\text{support}(I)}$$

\Rightarrow

$$\text{Interest}(I \rightarrow j) = \text{Conf}(I \rightarrow j) - P_N[j]$$



Interesting rules are those with high interest value (> 0.5)

Example:

$$B_1 = \{m, c, b\}$$

$$B_2 = \{m, b\}$$

$$B_3 = \{m, p, b\}$$

$$B_4 = \{c, b, j\}$$

$$B_5 = \{m, p, j\}$$

$$B_6 = \{c, j\}$$

$$B_7 = \{m, c, b, j\}$$

$$B_8 = \{b, c\}$$

\Rightarrow Association rule:- $\{m, b\} \rightarrow c$

$$\text{Confidence} = \frac{2}{4} = 0.5$$

$$\text{Interest} = \left(\left| 0.5 - \frac{5}{8} \right| \right) = \frac{1}{8}$$

\Rightarrow • Support threshold = 3, Confidence = 0.75

• Frequent itemsets:-

$$\{b, m\}, \{b, c\}, \{c, m\}, \{c, j\}, \{m, c, b\}$$

• Generate rules:-

$$b \rightarrow m: c = \frac{4}{4}$$

$$b \rightarrow c: c = \frac{5}{6}$$

$$c \rightarrow m$$

....

Let's say.



Date: _____

⇒ Compressing the output (Maximal / closed)

i)	Items	Support	Maximal (s=3)	closed
	A	4		No
	B	5	:	Yes
	C	3		No
	AB	4		Yes
	AC	2		No
	BC	3		Yes
	ABC	2		Yes.

• 'A' ko items wali list me dikhna hy kis kay set me 'A' hy (e.g., AB, AC, ABC)

• Ab 'A' ki support 4 hy. Aur Ab $A(\text{support}) \geq$

$AB(\text{support}), AC(\text{support}), ABC(\text{support})$

closed ⇒ $A(\text{support}) \geq \text{Superset}(\text{support})$

Maximal ⇒ $A(\text{support}) \geq \text{Threshold}$

• $A(\text{supersets} \rightarrow \text{support}) < \text{Threshold}$



Frequent pairs \Rightarrow no. of sets gets slow with size.

Date: _____

\Rightarrow Naive Algo \rightarrow fails if $(\text{items})^2$ exceed main memory

\Rightarrow Counting pairs in memory

• Approach 1:- Count pairs using matrix (uses 4 bytes per pair)

• Approach 2:- Table of triplets (12 bytes for pair)

\Rightarrow A-Priori Algo (monotonicity)

Example:-

Support = 2

Tid	Items	1 st scan	Itemset	Supp	L_1	Itemset	Supp
10	A, C, D	\rightarrow	A	2	\rightarrow	A	2
20	B, C, E		B	3		B	3
30	A, B, C, E		C	3		C	3
40	B, E		D	1		E	3
			E	3			

Itemset	Supp		Itemset	Supp	C_2	Itemset
A, C	2		A, B	1	\leftarrow 2 nd scan	A, B
B, C	2		A, C	2		A, C
B, E	3	\leftarrow	A, E	1		A, E
C, E	2		B, C	2		B, C
			B, E	3		B, E
			C, E	2		C, E



Date: _____

Itemset	support
A, C, B	1
A, B, E	1
A, C, E	1
B, C, E	2



Itemset	Supp.
B, C, E	2

=> **PCY** (Park-Chen-Yu) Algo
 $s = 3$ Cookies

Items = { milk, coke, ¹pepsi, ~~vanilla~~, juice }

milk = 1, cookies = 3, juice = 5

coke = 2, pepsi = 4

$B_1 = \{1, 2, 3\}$

$B_2 = \{1, 4, 5\}$

$B_3 = \{1, 3\}$

$B_4 = \{2, 5\}$

$B_5 = \{1, 3, 4\}$

$B_6 = \{1, 2, 3, 5\}$

$B_7 = \{2, 3, 5\}$

$B_8 = \{2, 3\}$

Items	frequency
1	5
2	5
3	6
4	2
5	4

② Remove elements having frequency less or equal than 2
 Candidate set = { 1, 2, 3, 4, 5 }



③ Map all candidates sets in pairs and calculate frequency (Sampling)

$$\begin{aligned}
 b_1 &= (1,2), (1,3), (2,3) = (2,4,4) \\
 b_2 &= (1,4), (1,5), (4,5) = (2,2,1) \\
 b_3 &= (1,3) = (4) \\
 b_4 &= (2,5) = (3) \\
 b_5 &= (1,3), (1,4), (3,4) = (4,2,1) \\
 b_6 &= (1,2), (1,3), (1,5), (2,3), (2,5), (3,5) = (2,4,2,4,3,2) \\
 b_7 &= (2,3), (2,5), (3,5) = (4,3,2) \\
 b_8 &= (2,3) = (4)
 \end{aligned}$$

Candidate pairs = $(1,3)$ $(2,3)$ $(2,5)$

④ Apply hash function $h(i,j) = (i+j) \% S = K$

$$(1,3) = 4 \% 5 = 4$$

$$(2,3) = 5 \% 5 = 0$$

$$(2,5) = 7 \% 5 = 2$$

Bucket no	pair	high freq	Candidate set
0	$(2,3)$	4	$(2,3)$
2	$(2,5)$	3	$(2,5)$
4	$(1,3)$	4	$(1,3)$

Candidate pair = 1, 2, 3, 5