

# Topics Covered in Todays Class

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## Unit 3: Database Design Theory and Normalization:

- Informal Design Guidelines for Relation Schemas
- Functional Dependencies
- Normal Forms Based on Primary Keys

# What is Normalization ?

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- Database normalization is the process of organizing data to minimize data redundancy (data duplication), which in turn ensures data consistency.

## Problems of Data Redundancy

1. Disk Space Wastage
2. Data inconsistency
3. DML queries can become slow

# What is Normalization ?

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- ❑ Database Normalization is step by step process.
- ❑ There are five normal forms, First Normal Form (1NF) through fifth Normal Form (5NF)
- ❑ Most databases are in third normal form (3NF).
- ❑ There are certain rules, that each normal form should follow.

# Redundant Information in records and Update Anomaly

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# Example

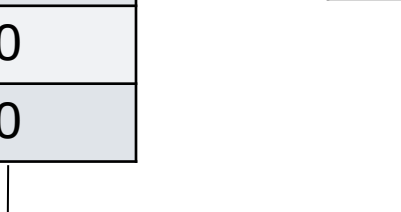
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**Student Table**

| <u>usn</u> | name    | dep_num |
|------------|---------|---------|
| 1BM14CS001 | Avinash | 10      |
| 1BM14CS002 | Balaji  | 10      |
| 1BM14CS003 | Chandan | 10      |
| 1BM14IS001 | Avinash | 20      |
| 1BM14IS002 | Dinesh  | 20      |

**Department Table**

| <u>d_id</u> | dep_name | HOD             |
|-------------|----------|-----------------|
| 10          | CSE      | Dr.Guruprasad   |
| 20          | ISE      | Dr.Gowrishankar |

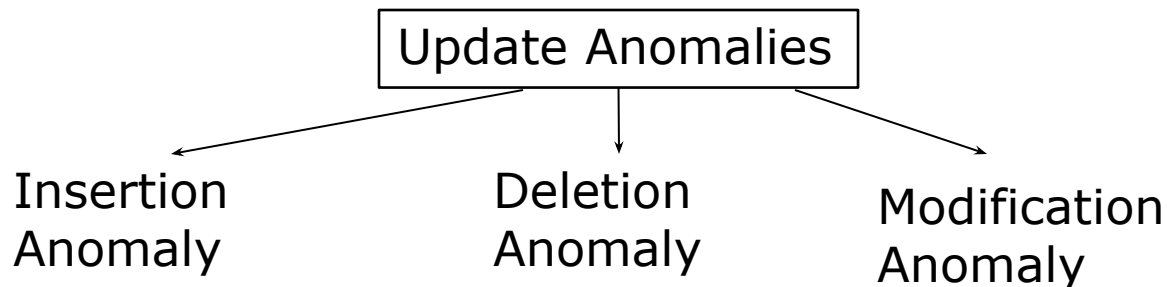


# Example

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name | HOD             |
|------------|---------|---------|----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE      | Dr.Guruprasad   |
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| 1BM14IS001 | Avinash | 20      | ISE      | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE      | Dr.Gowrishankar |

Storing two different independent (student and department) information will cause Update Anomalies



# Insertion Anomaly

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name | HOD             |
|------------|---------|---------|----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE      | Dr.Guruprasad   |
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| 1BM14IS001 | Avinash | 20      | ISE      | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE      | Dr.Gowrishankar |

Say we want to introduce new department with only department details for which students have not joined this department yet ?

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name  | HOD             |
|------------|---------|---------|-----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE       | Dr.Guruprasad   |
| 1BM14IS001 | Avinash | 20      | ISE       | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE       | Dr.Gowrishankar |
| ???        | ???     | 30      | Aerospace | Dr. Satish Jain |

Violating Primary key constraint

# Insertion Anomaly

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name | HOD             |
|------------|---------|---------|----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE      | Dr.Guruprasad   |
| 1BM14IS001 | Avinash | 20      | ISE      | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE      | Dr.Gowrishankar |

Say we want to introduce new department with only department details for which students have not joined this department yet ?

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name  | HOD             |
|------------|---------|---------|-----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE       | Dr.Guruprasad   |
| 1BM14IS001 | Avinash | 20      | ISE       | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE       | Dr.Gowrishankar |
| ???        | ???     | 30      | Aerospace | Dr. Satish Jain |

Violating Primary key constraint

**Insertion anomaly** means that that some data can not be inserted in the database.



# Insertion Anomaly

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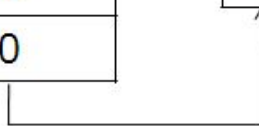
Insertion Anomaly will never occur if the table design was as follows:

**Student Table**

| <u>usn</u> | name    | dep_num |
|------------|---------|---------|
| 1BM14CS001 | Avinash | 10      |
| 1BM14CS002 | Balaji  | 10      |
| 1BM14CS003 | Chandan | 10      |
| 1BM14IS001 | Avinash | 20      |
| 1BM14IS002 | Dinesh  | 20      |

**Department Table**

| <u>d_i<br/>d</u> | dep_name  | HOD             |
|------------------|-----------|-----------------|
| 10               | CSE       | Dr.Guruprasad   |
| 20               | ISE       | Dr.Gowrishankar |
| 30               | Aerospace | Dr. Satish Jain |



# Deletion Anomaly

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**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name  | HOD             |
|------------|---------|---------|-----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE       | Dr.Guruprasad   |
| 1BM14IS001 | Avinash | 20      | ISE       | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE       | Dr.Gowrishankar |
| 1BM14AS001 | Abhijit | 30      | Aerospace | Dr. Satish Jain |

Say we want to delete **Abhijit** record from the table, then the information related to Aerospace department will be lost.

# Deletion Anomaly

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**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name  | HOD             |
|------------|---------|---------|-----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE       | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE       | Dr.Guruprasad   |
| 1BM14IS001 | Avinash | 20      | ISE       | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE       | Dr.Gowrishankar |
| 1BM14AS001 | Abhijit | 30      | Aerospace | Dr. Satish Jain |

Say we want to delete **Abhijit** record from the table, then the information related to Aerospace department will be lost.

**Deletion anomaly means** deleting some data cause other information to be lost.

# Deletion Anomaly

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Deletion Anomaly would not have occurred if the table design was as follows. Here student and department information is stored separately

**Student Table**

| <u>usn</u>            | name               | dep_num       |
|-----------------------|--------------------|---------------|
| 1BM14CS001            | Avinash            | 10            |
| 1BM14CS002            | Balaji             | 10            |
| 1BM14CS003            | Chandan            | 10            |
| 1BM14IS001            | Avinash            | 20            |
| 1BM14IS002            | Dinesh             | 20            |
| <del>1BM14AS001</del> | <del>Abhijit</del> | <del>30</del> |

**Department Table**

| <u>d_id</u> | dep_name  | HOD             |
|-------------|-----------|-----------------|
| 10          | CSE       | Dr.Guruprasad   |
| 20          | ISE       | Dr.Gowrishankar |
| 30          | Aerospace | Dr. Satish Jain |



# Modification Anomaly

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Say we want to **change the name of HOD for the Department CSE**. Then we have to do changes to all the records referring to CSE department

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name | HOD             |
|------------|---------|---------|----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE      | Dr.Guruprasad   |
| 1BM14IS001 | Avinash | 20      | ISE      | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE      | Dr.Gowrishankar |

Changing name of CSE HOD should be reflected in three records

# Modification Anomaly

Say we want to **change the name of HOD for the Department CSE**. Then we have to change all the records referring to CSE department

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name | HOD             |
|------------|---------|---------|----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS002 | Balaji  | 10      | CSE      | Dr.Guruprasad   |
| 1BM14CS003 | Chandan | 10      | CSE      | Dr.Guruprasad   |
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Changing name of CSE HOD should be reflected in three records

**Update anomaly** means we have data redundancy in the database and to make any modification we have to change all copies of the redundant data or else the database will contain incorrect data.

# Modification Anomaly

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Modification Anomaly will never occur if the table design was as follows:

**Student Table**

| <u>usn</u> | name    | dep_num |
|------------|---------|---------|
| 1BM14CS001 | Avinash | 10      |
| 1BM14CS002 | Balaji  | 10      |
| 1BM14CS003 | Chandan | 10      |
| 1BM14IS001 | Avinash | 20      |
| 1BM14IS002 | Dinesh  | 20      |

**Department Table**

| <u>d_id</u> | dep_name | HOD               |
|-------------|----------|-------------------|
| 10          | CSE      | Dr.Guruprasad H S |
| 20          | ISE      | Dr.Gowrishankar   |

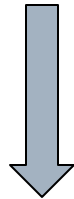
Changing  
in only  
one record



# Normalization

**Student-Department Table**

| <u>usn</u> | name    | dep_num | Dep_name | HOD             |
|------------|---------|---------|----------|-----------------|
| 1BM14CS001 | Avinash | 10      | CSE      | Dr.Guruprasad   |
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| 1BM14IS001 | Avinash | 20      | ISE      | Dr.Gowrishankar |
| 1BM14IS002 | Dinesh  | 20      | ISE      | Dr.Gowrishankar |



Normalized Table Design

**Student Table**

| <u>usn</u> | name    | dep_num |
|------------|---------|---------|
| 1BM14CS001 | Avinash | 10      |
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**Department Table**

| <u>d_id</u> | dep_name | HOD             |
|-------------|----------|-----------------|
| 10          | CSE      | Dr.Guruprasad   |
| 20          | ISE      | Dr.Gowrishankar |





# Informal Design Guidelines for relation Schemas

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Four informal measures of quality for relation schema design

1. Semantics of the Relation Attributes
2. Redundant Information in Tuples and Update Anomalies
3. Null Values in Tuples
4. Spurious Tuples

# Guideline 1: Try to make user interpretation easy

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- GUIDELINE 1: Informally, each tuple in a relation should represent one entity or relationship instance. (Applies to individual relations and their attributes).
  - Attributes of different entities (EMPLOYEEs, DEPARTMENTs, PROJECTs) should not be mixed in the same relation
  - Only foreign keys should be used to refer to other entities
  - Entity and relationship attributes should be kept apart as much as possible.
- Bottom Line: *Design a schema that can be explained easily relation by relation. The semantics of attributes should be easy to interpret.*
- Example:

```
EMP(FNAME, LNAME, SSN)  
WORKS_ON (SSN, PNO)  
PROJECT_LOC(PNO, PLOC)
```

```
EMP(FNAME,LNAME,SSN, PNO,PLOC)
```

Perhaps this schema has too much information to absorb per record ?

## Guideline 2: Try to reduce Redundancy and avoid Update Anomalies

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- Information is stored redundantly
  - Wastes storage
  - Causes problems with update anomalies
    - Insertion anomalies
    - Deletion anomalies
    - Modification anomalies
  
- GUIDELINE 2:
  - Design a schema that does not suffer from the insertion, deletion and update anomalies.
  - If there are any anomalies present, then note them so that applications can be made to take them into account.

# Guideline 3: Avoid too many NULL values

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## Avoid too many NULL values

- ❑ Space is wasted
- ❑ Problems occur when using aggregate functions like count or sum
- ❑ NULLs can have different intentions
  - Attribute does not apply
  - Value unknown and will remain unknown
  - Value unknown at present

# Guideline 4: Spurious Tuples

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- Bad designs for a relational database may result in erroneous results for certain JOIN operations
  - Split a table into smaller tables (with fewer columns in each), When reconstructing the “original” data, should not introduce spurious tuples
  
- GUIDELINE 4:
  - The relations should be designed to satisfy the lossless join condition.
  - No spurious tuples should be generated by doing a natural-join of any relations.

# What is spurious tuples ?

- A spurious tuple is, basically, a record in a database that gets created when two tables are joined badly. In database, spurious tuples are created when two tables are joined on attributes that are neither primary keys nor foreign keys.
- Example, consider

CAR (ID, Make, Color)

|     |        |      |
|-----|--------|------|
| 123 | Toyota | Blue |
| 456 | Audi   | Blue |
| 789 | Toyota | Red  |

CAR1 (ID, Color)

|     |      |
|-----|------|
| 123 | Blue |
| 456 | Blue |
| 789 | Red  |

CAR2 (Color, Make)

|      |        |
|------|--------|
| Blue | Toyota |
| Blue | Audi   |
| Red  | Toyota |

What happens when we join (or combine)  
CAR1 and CAR2 ?

# What is spurious tuples ?

- Example, consider

CAR (ID, Make, Color)

|     |        |      |
|-----|--------|------|
| 123 | Toyota | Blue |
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CAR1 (ID, Color)

|     |      |
|-----|------|
| 123 | Blue |
| 456 | Blue |
| 789 | Red  |

CAR2 (Color, Make)

|      |        |
|------|--------|
| Blue | Toyota |
| Blue | Audi   |
| Red  | Toyota |

What happens when we join (or combine) CAR1 and CAR2 ?

|     |      |        |
|-----|------|--------|
| 123 | Blue | Toyota |
| 123 | Blue | Audi   |
| 456 | Blue | Toyota |
| 456 | Blue | Audi   |
| 789 | Red  | Toyota |

# What is spurious tuples ?

- Example, consider

CAR (ID, Make, Color)

|     |        |      |
|-----|--------|------|
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|     |      |
|-----|------|
| 123 | Blue |
| 456 | Blue |
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CAR2 (Color, Make)

|      |        |
|------|--------|
| Blue | Toyota |
| Blue | Audi   |
| Red  | Toyota |

What happens when we join CAR1 and CAR2 ?

Spurious  
Records

|     |      |        |
|-----|------|--------|
| 123 | Blue | Toyota |
| 123 | Blue | Audi   |
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| 456 | Blue | Audi   |
| 789 | Red  | Toyota |



# So, What we will learn next

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## A **theory of schema design**

- ☐ **Functional dependencies** and **normalization**
- ☐ Using functional dependencies we define “normal forms” of schema

# Functional Dependency

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- Functional Dependency **represents relationship among attributes.**
- Functional dependency (FD) is a set of constraints between two attributes in a relation.
- Functional dependency says that if two tuples have same values for attributes  $A_1, A_2, \dots, A_n$ , then those two tuples must have to have same values for attributes  $B_1, B_2, \dots, B_n$ .
- Functional dependency is **represented** by an arrow sign ( $\rightarrow$ ) that is,  **$X \rightarrow Y$ , where  $X$  functionally determines  $Y$ .** The left-hand side attributes determine the values of attributes on the right-hand side.

# Functional Dependency

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## □ Example

Student Table

| USN        | Name    | Grade |
|------------|---------|-------|
| 1BM14CS001 | Avinash | S     |
| 1BM14CS002 | Balaji  | A     |
| 1BM14CS003 | Chandan | B     |
| 1BM14IS001 | Avinash | C     |
| 1BM14IS002 | Balaji  | A     |

What is the Grade of **Avinash** ?

# Functional Dependency

---

## □ Example

Student Table

| USN        | Name    | Grade |
|------------|---------|-------|
| 1BM14CS001 | Avinash | S     |
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| 1BM14CS003 | Chandan | B     |
| 1BM14IS001 | Avinash | C     |
| 1BM14IS002 | Balaji  | A     |

What is the Grade of **Avinash** ?

Which **Avinash** grade ?

Is it **1BM14CS001** or **1BM14IS001**

# Functional Dependency

## □ Example

Student Table

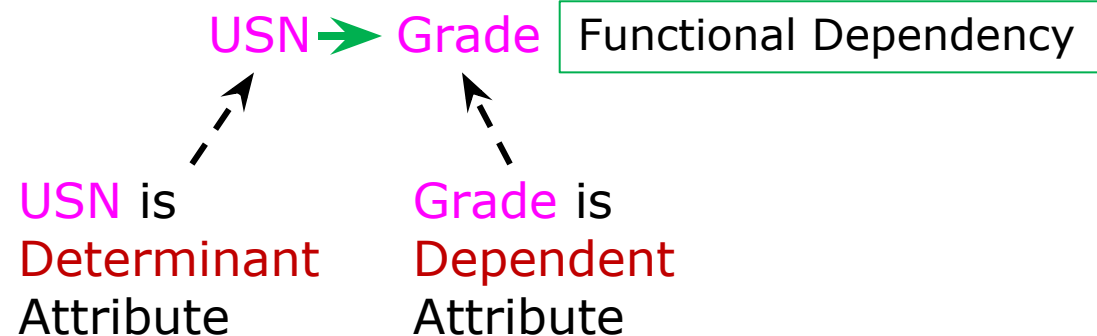
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| 1BM14IS001 | Avinash | C     |
| 1BM14IS002 | Balaji  | A     |

What is the Grade of **Avinash** ?

Which **Avinash** grade ?

Is it **1BM14CS001** or **1BM14IS001**

Here **USN** will help to **determine**  
**Grade** of the student



# Functional Dependency

## □ Example

Student Table

| USN        | Name    | Grade |
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| 1BM14CS001 | Avinash | S     |
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| 1BM14CS003 | Chandan | B     |
| 1BM14IS001 | Avinash | C     |
| 1BM14IS002 | Balaji  | A     |

What is the Grade of **Avinash** ?

Which **Avinash** grade ?

Is it **1BM14CS001** or **1BM14IS001**

Here **USN** will help to **determine**  
**Grade** of the student

**USN** → **Grade** Functional Dependency

Note that the **attribute to the right** of the **arrow** is **functionally dependent** on the **attribute in the left** of the arrow.

# Functional Dependency

## □ Example

Student Table

| USN        | Name    | Grade |
|------------|---------|-------|
| 1BM14CS001 | Avinash | S     |
| 1BM14CS002 | Balaji  | A     |
| 1BM14CS003 | Chandan | B     |
| 1BM14IS001 | Avinash | C     |
| 1BM14IS002 | Balaji  | A     |

What is the Grade of **Avinash** ?

Which **Avinash** grade ?

Is it **1BM14CS001** or **1BM14IS001**

Here **USN** will help to **determine**  
**Grade** of the student

In this table **Name** alone cannot  
Determine **Grade** of the student  
And also **Name** alone does not  
identify the **entire row** in the table.  
So **Name Cannot be PRIMARY KEY.**

**USN** → **Grade** Functional Dependency

# Functional Dependency

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## □ Example

### Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
| 1BM14CS001 | Avinash | 9449189795 | 10        | DBMS        | 6       | S     |
| 1BM14CS001 | Avinash | 9449189795 | 20        | Maths       | 4       | A     |
| 1BM14CS002 | Avinash | 8441609444 | 30        | DC          | 6       | A     |
| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

What is the **Grade** of **Avinash** ?



# Functional Dependency

---

## □ Example

### Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
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| 1BM14CS001 | Avinash | 9449189795 | 20        | Maths       | 4       | A     |
| 1BM14CS002 | Avinash | 8441609444 | 30        | DC          | 6       | A     |
| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

What is the **Grade** of **Avinash** ?

Which **USN** Avinash **Grade** and in which **Course** ?

# Functional Dependency

## Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
| 1BM14CS001 | Avinash | 9449189795 | 10        | DBMS        | 6       | S     |
| 1BM14CS001 | Avinash | 9449189795 | 20        | Maths       | 4       | A     |
| 1BM14CS002 | Avinash | 8441609444 | 30        | DC          | 6       | A     |
| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

What is the **Grade** of **Avinash** ?

Which **USN** Avinash **Grade** and in which **Course** ?

(USN, Course-ID) → Grade

| (USN, Course-ID) | Grade |
|------------------|-------|
| -----            |       |
| (1BM14CS001, 10) | S     |
| (1BM14CS001, 20) | A     |

Here two attributes  
**(USN, Course-ID)** or **(USN, Course-Name)**  
Will determine the **Grade**

# Functional Dependency

---

## Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
| 1BM14CS001 | Avinash | 9449189795 | 10        | DBMS        | 6       | S     |
| 1BM14CS001 | Avinash | 9449189795 | 20        | Maths       | 4       | A     |
| 1BM14CS002 | Avinash | 8441609444 | 30        | DC          | 6       | A     |
| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

What is the **Mobile** number of **Avinash** ?

Which **USN** Avinash **mobile number** ?

USN → Mobile

| USN        | Mobile     |
|------------|------------|
| -----      |            |
| 1BM14CS001 | 9449189795 |
| 1BM14CS002 | 8441609444 |

USN → Name

| USN        | Name    |
|------------|---------|
| -----      |         |
| 1BM14CS001 | Avinash |
| 1BM14CS002 | Avinash |

# Functional Dependency

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## □ Example

### Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
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| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

What is the **Course-Name** whose **Credits** is **6** ?

# Functional Dependency

---

## □ Example

### Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
| 1BM14CS001 | Avinash | 9449189795 | 10        | DBMS        | 6       | S     |
| 1BM14CS001 | Avinash | 9449189795 | 20        | Maths       | 4       | A     |
| 1BM14CS002 | Avinash | 8441609444 | 30        | DC          | 6       | A     |
| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

What is the **Course-Name** whose **Credits** is **6** ?

Course-ID → (Course-Name, Credits)

|           |                        |
|-----------|------------------------|
| Course-ID | (Course-Name, Credits) |
| -----     |                        |
| 10        | (DBMS,6)               |
| 30        | (DC,6)                 |

# Functional Dependency

---

## □ Example

### Student-Course Table

| USN        | Name    | Mobile     | Course-ID | Course-name | Credits | Grade |
|------------|---------|------------|-----------|-------------|---------|-------|
| 1BM14CS001 | Avinash | 9449189795 | 10        | DBMS        | 6       | S     |
| 1BM14CS001 | Avinash | 9449189795 | 20        | Maths       | 4       | A     |
| 1BM14CS002 | Avinash | 8441609444 | 30        | DC          | 6       | A     |
| 1BM14CS003 | Balaji  | 7958994491 | 10        | DBMS        | 6       | B     |
| 1BM14CS003 | Balaji  | 7958994491 | 20        | Maths       | 4       | C     |

USN → (Name, Mobile)

(USN, Course-ID) → Grade

Course-ID → (Course-Name, Credits)

# Functional dependency

---

| Attribute<br>A | FD | Attribute<br>B |
|----------------|----|----------------|
| a1             | →  | b3             |
| a2             | →  | b3             |
| a3             | →  | b4             |

| Attribute<br>A | Not FD | Attribute<br>B |
|----------------|--------|----------------|
| a1             | →      | b3             |
| a1             | →      | b2             |

# To DO

---

- Determine all Functional Dependencies in the following table

| A              | B              | C              | D              |
|----------------|----------------|----------------|----------------|
| a <sub>1</sub> | b <sub>1</sub> | c <sub>1</sub> | d <sub>1</sub> |
| a <sub>1</sub> | b <sub>2</sub> | c <sub>1</sub> | d <sub>2</sub> |
| a <sub>2</sub> | b <sub>2</sub> | c <sub>2</sub> | d <sub>2</sub> |
| a <sub>2</sub> | b <sub>2</sub> | c <sub>2</sub> | d <sub>3</sub> |
| a <sub>3</sub> | b <sub>3</sub> | c <sub>2</sub> | d <sub>4</sub> |



# To Do

---

| A | B | C | D | E |
|---|---|---|---|---|
| 1 | 2 | 4 | 3 | 6 |
| 3 | 2 | 5 | 1 | 8 |
| 1 | 4 | 4 | 5 | 7 |
| 1 | 2 | 4 | 3 | 6 |
| 3 | 2 | 5 | 1 | 8 |

Find at least *three* FDs which hold on this instance

|   |   |                          |   |   |
|---|---|--------------------------|---|---|
| { | } | <input type="checkbox"/> | { | } |
| { | } | <input type="checkbox"/> | { | } |
| { | } | <input type="checkbox"/> | { | } |

# Functional Dependency

---

- Given that  $X$ ,  $Y$ , and  $Z$  are sets of attributes in a relation  $R$ , one can derive several properties of functional dependencies. Among the most important are Armstrong's axioms, which are used in database normalization:
- Subset Property (Axiom of Reflexivity): If  $Y$  is a subset of  $X$ , then  $X \twoheadrightarrow Y$
- Augmentation (Axiom of Augmentation): If  $X \twoheadrightarrow Y$ , then  $XZ \twoheadrightarrow YZ$
- Transitivity (Axiom of Transitivity): If  $X \twoheadrightarrow Y$  and  $Y \twoheadrightarrow Z$ , then  $X \twoheadrightarrow Z$
- Union: If  $X \twoheadrightarrow Y$  and  $X \twoheadrightarrow Z$ , then  $X \twoheadrightarrow YZ$
- Decomposition: If  $X \twoheadrightarrow YZ$ , then  $X \twoheadrightarrow Y$  and  $X \twoheadrightarrow Z$
- Pseudotransitivity: If  $X \twoheadrightarrow Y$  and  $YZ \twoheadrightarrow W$ , then  $XZ \twoheadrightarrow W$

# Unit 3

---

Super key, Candidate key and Primary key

# Recall: Functional Dependency

---

Functional Dependencies provide a formal mechanism to express Constraints between attributes.

It is a mean of identifying how values of certain attributes are Determined by values of other attributes.

A functional dependency (FD) generalizes the concept of a key.

Book (acc\_no, yr\_pub, title)

Acc\_no is Primary Key

Formal representation of Constraints

acc\_no  $\longrightarrow$  yr\_pub

acc\_no  $\longrightarrow$  title

# Normalization

---

- Normalization is a process of removing redundancy using functional dependencies.
- To reduce redundancy it is necessary to decompose a relation into a number of smaller relations.
- There are several normal forms
  - First Normal Form (1 NF)
  - Second Normal Form (2 NF)
  - Third Normal Form (3 NF)
  - Boyce-Codd Normal Form (BCNF)
  - Fourth Normal Form
  - Fifth Normal Form

# To Understand “First Normal form”

---

To understand “First Normal Form”, we will look at the definitions of Super key, Candidate key and Primary key.

# Database Table Keys

---

- A **Key** is a **single** or combination of multiple fields in a table.
- Its is used to **fetch or retrieve records**/data-rows from data table according to the condition/requirement.
- Keys are also used to **create relationship among different database tables** or views.

# What is Super Key, Candidate Key, Primary Key ?

---

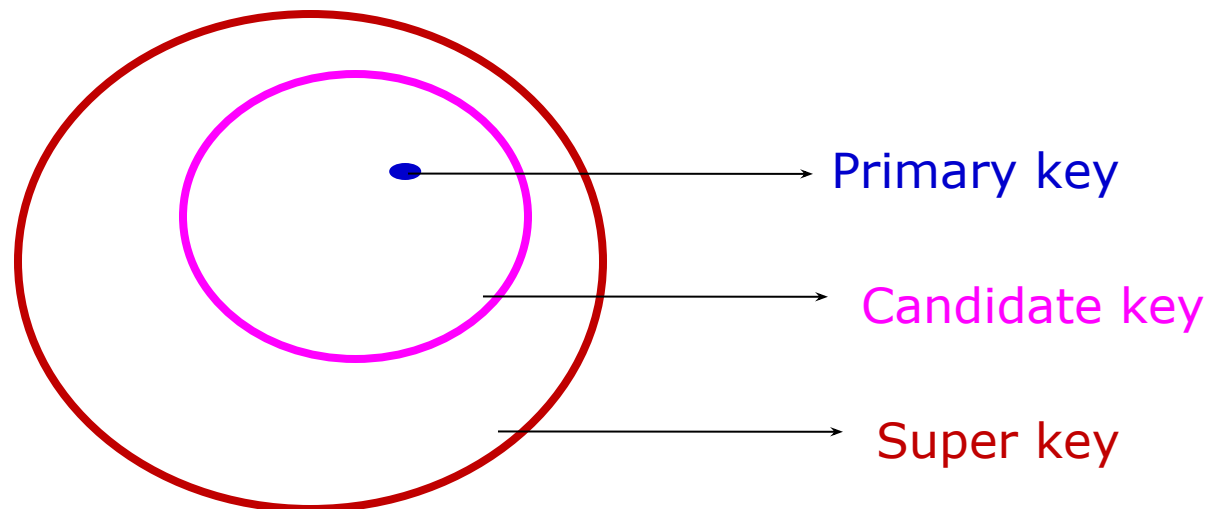
- ❑ **Super Key:** Super key is a set of one or more than one keys that can be used to identify a record uniquely in a table.  
*In super key redundant attributes can exist.*
- ❑ **Candidate Key:** A Candidate Key is a set of one or more fields/columns that can identify a record uniquely in a table. There can be multiple Candidate Keys in one table. Each Candidate Key can work as Primary Key.  
*In candidate key no redundant attributes.*
- ❑ **Primary Key:** Primary key is a set of one or more fields/columns of a table that uniquely identify a record in database table. It can not accept null, duplicate values. Only one Candidate Key can be Primary Key.  
*Primary key is one of the instance of Candidate Key*



# What is Super Key, Candidate Key, Primary Key ?

---

- ❑ **Super Key:** Super key is a set of one or more than one keys that can be used to identify a record uniquely in a table.  
*In super key redundant attributes can exist.*
- ❑ **Candidate Key:** A Candidate Key is a set of one or more fields/columns that can identify a record uniquely in a table. There can be multiple Candidate Keys in one table. Each Candidate Key can work as Primary Key.  
*In candidate key no redundant attributes.*
- ❑ **Primary Key:** Primary key is a set of one or more fields/columns of a table that uniquely identify a record in database table. It can not accept null, duplicate values. Only one Candidate Key can be Primary Key.  
*Primary key is one of the instance of Candidate Key*



# What is Super Key, Candidate Key, Primary Key ?

---

- ❑ Super Key: Specifies that **no two distinct records** have the **same value** for Super Key.
- ❑ Super key *may have redundant attributes*.
- ❑ Example

| Book ID        | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

# What is Super Key, Candidate Key, Primary Key ?

---

- ❑ Super Key: Specifies that **no two distinct records** have the **same value** for Super Key.
- ❑ Super key *may have redundant attributes*.
- ❑ Example

| BookID         | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

## Super Keys

{BookID}  
{BookID, Name}  
{BookID, Author}  
{Name, Author}  
{BookID, Name, Author}

# Super Key

- ❑ Super Key: Specifies that no two distinct records have the same value for Super Key.
- ❑ Super key may have redundant attributes.
- ❑ Example

| BookID         | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

## Super Keys

{BookID}  
{BookID, Name}  
{BookID, Author}  
{Name, Author}  
{BookID, Name, Author}

|                        | Super Key<br>With <b>redundant<br/>Attributes</b> |
|------------------------|---|
| {BookID, Name, Author} | Name and Author                                   |

# Candidate Key

---

- Candidate Key is a super key without redundancy
- Not reducible
- More than one possible candidate keys

| BookID         | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

## Candidate Keys

|  |
|--|
| $\{\text{BookID}\}$<br>$\{\text{Name, Author}\}$ |
|--|

# Primary Key

---

- Primary is one of the instance of Candidate Key.
- Primary key chosen by Database designer, which will **not have null** values

| BookID         | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

Primary Key

{BookID}

# Relation between Super, Candidate and Primary key

| BookID         | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

## Super Keys

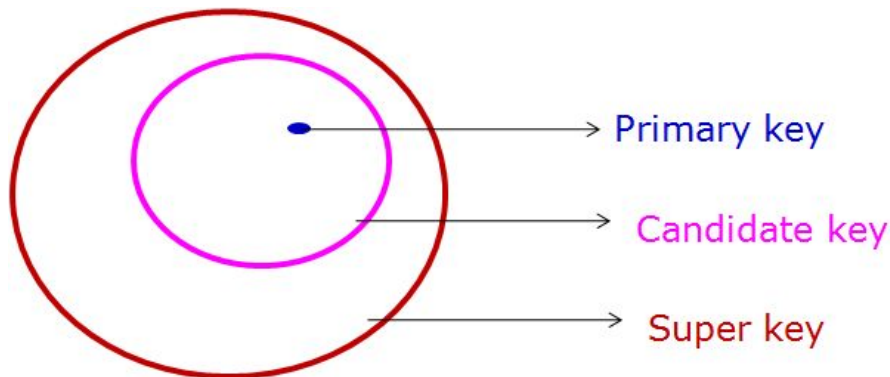
{BookID}  
{BookID, Name}  
{BookID, Author}  
{Name, Author}  
{BookID, Name, Author}

## Candidate Keys

{BookID}  
{Name, Author}

## Primary Key

{BookID}



# Summarizing

---

- **Candidate Key:** are **individual columns** in a table that qualifies for uniqueness of **each row**.
- **Primary Key:** is the **column** you choose to maintain uniqueness in a table at **row level**.
- **Super Key:** If you **add any other Column** to a **Primary Key** then it **become a Super Key**



# We will next learn

---

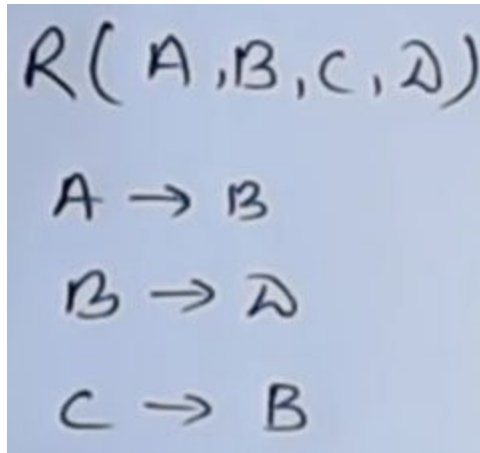
How to **find candidate keys** from the given functional dependencies

For this we have to understand **Closure of Attributes**

# Finding Closure of Attributes

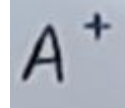
---

- Consider following functional dependencies



$R(A, B, C, D)$   
 $A \rightarrow B$   
 $B \rightarrow D$   
 $C \rightarrow B$

Closure of Attribute **A** is written as



$A^+$

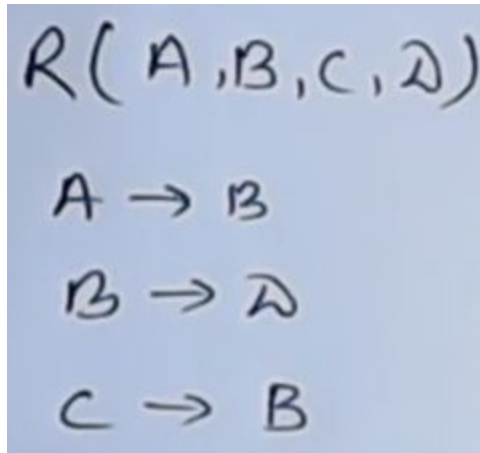
Closure of attribute is set  
Of attributes which can be  
determined by A

Closure of  $A^+$  is  $\{A, B, D\}$

# Finding Closure of Attributes

---

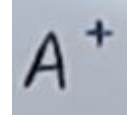
- Consider following functional dependencies



Handwritten text on a light blue background showing the functional dependencies for a relation  $R(A, B, C, D)$ :

$$\begin{aligned} R(A, B, C, D) \\ A &\rightarrow B \\ B &\rightarrow D \\ C &\rightarrow B \end{aligned}$$

Closure of Attribute **A** is written as



Handwritten notation for the closure of attribute A,  $A^+$ .

Closure of attribute is set  
Of attributes which can be  
determined by A

Closure of  $A^+$  is  $\{A, B, D\}$

What is closure of B and C ?

# Finding Candidate Keys

- Find candidate key using following Functional Dependencies

$R(A, B, C, D, E, F)$   
 $A \rightarrow C$   
 $C \rightarrow D$   
 $D \rightarrow B$   
 $E \rightarrow F$

To find a Candidate key, **First try** this approach

- Step 1: Find the attributes that are neither on the left and right side
- Step 2: Find attributes that are only on the right side
- Step 3: Find attributes that are only on the left side
- Step 4: Combine the attributes on step 1 and 3
- Step 5: Test if the closures of attributes on step 4 can determine all the attributes

To find all possible candidate key, **Second try** this approach

Step 1:

(a) Find all Single Attributes closures

A+: B+: C+: D+: E+: F+:

(b) Find all Two Attribute closures

AB+: AC+: AD+: AE+: AF+: BC+: BD+: BE+: BF+: CD+: CE+: CF+: EF+:

(c) Find all Three attribute closures

ABC+: ABD+ .....

(d) Find all Four attribute closures

ABCD+: BCDE+:

(e) Find all Five attribute closures

ABCDE+.....

Step 2:

Candidate Keys will be: From the above closures above identify which will determine all attributes of the relation and they are minimal i.e. subsets of the attributes is not a key already.

# Finding Candidate Keys

Compute following closures and determine which all are candidate keys.  
Note: Candidate Keys will be the closures which will determine all attributes of the relation and they are minimal i.e. subsets of the attributes is not a key already.

$A^+ = ACDBF$

$B^+ =$

$C^+ =$

$D^+ =$

$E^+ =$

$F^+ =$

$AB^+ =$

$AC^+ =$

$AD^+ =$

$AE^+ =$

$AF^+ =$

$BC^+ =$

$BD^+ =$

$BE^+ =$

$BF^+ =$

$CD^+ =$

$CE^+ =$

$CF^+ =$

$EF^+ =$

$ABC^+ =$

$ABD^+ =$

$ABE^+ =$

$ABF^+ =$

$ACD^+ =$

$ACE^+ =$

$ACF^+ =$

$ADE^+ =$

$ADF^+ =$

$BCD^+ =$

$BCE^+ =$

$BCF^+ =$

$CDE^+ =$

$CDF^+ =$

$DEF^+ =$

$R(A, B, C, D, E, F)$

$A \rightarrow C$

$C \rightarrow D$

$D \rightarrow B$

$E \rightarrow F$

$ABCD^+ =$

$ABCE^+ =$

$ABCF^+ =$

$BCDE^+ =$

$BCDF^+ =$

$CDEF^+ =$

$ABCDEF^+ = ABCDEF$

# Finding Candidate Keys

---

Solve the given problems to identify candidate key

1.  $R\{A,B,C,D,E,F,G\}$   
FD's  $AB \rightarrow F$  ,  $AD \rightarrow E$ ,  $F \rightarrow G$

Answer: One possible CK is  $\{ABCD\}$

2.  $R\{F,O,R,UM\}$   
FD's  $FO \rightarrow U$  ,  $ORU \rightarrow M$

Answer: One possible CK is  $\{FOR\}$

# Trivial Functional Dependency

---

If  $Y \subset X$ ,  $Y$  is **subset** of  $X$   
then we have trivial functional dependency  
 $X \rightarrow Y$

Example:

$\{BC\} \subset \{ABC\}$  So the trivial functional dependency  $ABC \rightarrow BC$   
 $Y \subset X$   $X \rightarrow Y$

# Trivial Functional Dependency

---

Some functional dependencies are said to be trivial because they are satisfied by all relations. Functional dependency of the form  $A \rightarrow B$  is trivial if  $B \subset A$  or  $A$  trivial Functional Dependency is the one where **RHS is a subset of LHS**.

Example,

$A \rightarrow A$  is satisfied by all relations involving attribute  $A$ .

$SSN \rightarrow SSN$

$PNUMBER \rightarrow PNUMBER$

$SSN \ PNUMBER \rightarrow PNUMBER$

$SSN \ PNUMBER \rightarrow SSN \ PNUMBER$



# Non Trivial Functional Dependency

---

If a functional dependency  $X \rightarrow Y$  holds true where  $Y$  is **not a subset** of  $X$  then this dependency is called non trivial Functional dependency.

□ **For example:**

An employee table with three attributes: emp\_id, emp\_name, emp\_address.

The following functional dependencies are **non-trivial**:

emp\_id  $\rightarrow$  emp\_name (emp\_name is not a subset of emp\_id)

emp\_id  $\rightarrow$  emp\_address (emp\_address is not a subset of emp\_id)

- On the other hand, the following dependencies are **trivial**:
- {emp\_id, emp\_name}  $\rightarrow$  emp\_name [emp\_name is a subset of {emp\_id, emp\_name}]

## **Completely non trivial FD:**

If a FD  $X \rightarrow Y$  holds true where  $X \cap Y$  is null then this dependency is said to be completely non trivial function dependency.

Example: SSN  $\rightarrow$  Ename, PNUMBER  $\rightarrow$  PNAME, PNUMBER  $\rightarrow$  BDATE

# Unit 3

---

Normalization:  
First Normal Form  
Second Normal Form

# Doubt Clarification on Super and Candidate key

| BookID         | Name | Author         |
|----------------|------|----------------|
| B <sub>1</sub> | XYZ  | A <sub>1</sub> |
| B <sub>2</sub> | ABC  | A <sub>1</sub> |
| B <sub>3</sub> | XYZ  | A <sub>2</sub> |
| B <sub>4</sub> | PQR  | A <sub>3</sub> |
| B <sub>5</sub> | LSP  | A <sub>1</sub> |
| B <sub>6</sub> | ABC  | A <sub>3</sub> |

Candidate Key: Is Super key without Redundancy and Not reducible

A super key  $K = \{A_1, A_2, \dots, A_n\}$  is Candidate Key iff  $K - \{A_i\}$  is not already a key for any  $A_i, 1 \leq i \leq n$

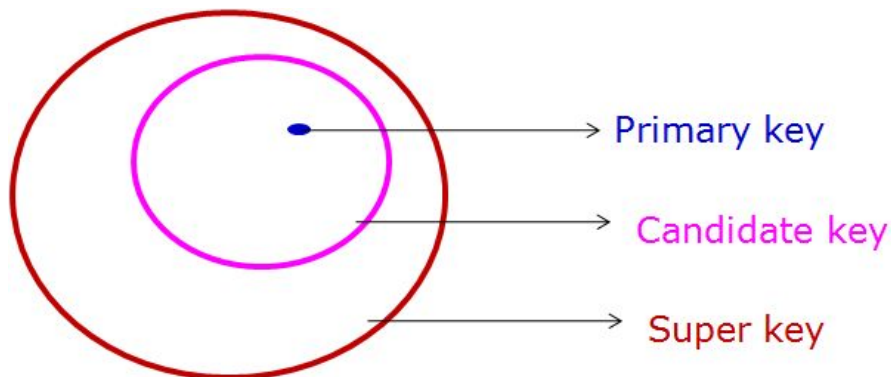
Identifying which of the Super keys Can become candidate keys

## Super Keys

$\{BookID\}$   
 $\{BookID, Name\}$   
 $\{BookID, Author\}$   
 $\{Name, Author\}$   
 $\{BookID, Name, Author\}$

## Candidate Keys

$\{BookID\}$   
 $\{Name, Author\}$



# Various Database table Normal Forms

---

- ☐ First Normal Form (1 NF)
- ☐ Second Normal Form (2 NF)
- ☐ Third Normal Form (3 NF)
- ☐ Boyce-Codd Normal Form (BCNF)
- ☐ Fourth Normal Form
- ☐ Fifth Normal Form

# Practical Use of Normal Forms

---

- **Normalization** is carried out in practice so that the resulting designs are of high quality and meet the desirable properties
- The practical utility of these normal forms becomes questionable when the constraints on which they are based are **hard to understand** or to **detect**
- The database designers ***need not*** normalize to the highest possible normal form. (usually up to 3NF, BCNF or 4NF)
- **Denormalization:** the process of storing the join of higher normal form relations as a base relation—which is in a lower normal form

# First Normal Form (1 NF)

---

A database table is said to be in **1 NF** if

- ❑ Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- ❑ **All entries** in any **column** must be of the **same kind**
- ❑ Each **column** must have **a unique name**
- ❑ **No two rows** are **identical**

1NF: Disallows composite attributes, multivalued attributes, and **nested relations**; attributes whose values *for an individual record* are non-atomic.

# First Normal Form (1 NF)

---

A database table is said to be in **1 NF** if

- ❑ Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- ❑ **All entries** in any **column** must be of the **same kind**
- ❑ Each **column** must have **a unique name**
- ❑ **No two rows** are **identical**

| Roll | Name  | Courses            |
|------|-------|--------------------|
| 101  | Asif  | DBMS, CN<br>CD, SE |
| 102  | Amit  | CO, OS             |
| 103  | Arpit | CD, OS, CN<br>DBMS |

Whether this table is in  
First Normal form ?

# First Normal Form (1 NF)

A database table is said to be in **1 NF** if

- ❑ Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- ❑ **All entries** in any **column** must be of the **same kind**
- ❑ Each **column** must have **a unique name**
- ❑ **No two rows** are **identical**

| STUDENT |       |                    |
|---------|-------|--------------------|
| Roll    | Name  | Courses            |
| 101     | Asif  | DBMS, CN<br>CD, SE |
| 102     | Amit  | CO, OS             |
| 103     | Arpit | CD, OS, CN<br>DBMS |

Not atomic values

Whether this table is in  
First Normal form ?



# First Normal Form (1 NF)

A database table is said to be in **1 NF** if

- Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- All entries in any column must be of the same kind
- Each column must have a unique name
- **No two rows are identical**

| Roll | Name  | Courses            |
|------|-------|--------------------|
| 101  | Asif  | DBMS, CN<br>CD, SE |
| 102  | Amit  | CO, OS             |
| 103  | Arpit | CD, OS, CN<br>DBMS |

1 NF



| Roll | Name  | Courses |
|------|-------|---------|
| 101  | Asif  | DBMS    |
| 101  | Asif  | CN      |
| 101  | Asif  | CD      |
| 101  | Asif  | SE      |
| 102  | Amit  | CO      |
| 102  | Amit  | OS      |
| 103  | Arpit | CD      |
| 103  | Arpit | DS      |
| 103  | Arpit | CN      |
| 103  | Arpit | DBMS    |

# First Normal Form (1 NF)

---

A database table is said to be in **1 NF** if

- ❑ Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- ❑ All entries in any column must be of the same kind
- ❑ Each column must have a unique name
- ❑ No two rows are identical

Convert following table to 1 NF

**TABLE\_PRODUCT**

| Product ID | Color        | Price |
|------------|--------------|-------|
| 1          | red, green   | 15.99 |
| 2          | yellow       | 23.99 |
| 3          | green        | 17.50 |
| 4          | yellow, blue | 9.99  |
| 5          | red          | 29.99 |

1 NF



# First Normal Form (1 NF)

A database table is said to be in **1 NF** if

- Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- All entries in any column must be of the same kind
- Each column must have a unique name
- No two rows are identical

Convert following table to 1 NF

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|------------|--------------|-------|
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| 2          | yellow       | 23.99 |
| 3          | green        | 17.50 |
| 4          | yellow, blue | 9.99  |
| 5          | red          | 29.99 |

1 NF



Solution 1

| Product ID | Color  | Price |
|------------|--------|-------|
| 1          | red    | 15.99 |
| 1          | green  | 15.99 |
| 2          | yellow | 23.99 |
| 3          | green  | 17.50 |
| 4          | yellow | 9.99  |
| 4          | blue   | 9.99  |
| 5          | red    | 29.99 |

# First Normal Form (1 NF)

A database table is said to be in **1 NF** if

- ❑ Values of each attribute is **atomic**. An atomic value is a value that **cannot be divided**.
- ❑ All entries in any column must be of the same kind
- ❑ Each column must have a unique name
- ❑ No two rows are identical

Given ProductID is Primary Key  
Solution 2

Convert following table to 1 NF

TABLE\_PRODUCT

| Product ID | Color        | Price |
|------------|--------------|-------|
| 1          | red, green   | 15.99 |
| 2          | yellow       | 23.99 |
| 3          | green        | 17.50 |
| 4          | yellow, blue | 9.99  |
| 5          | red          | 29.99 |

1 NF

TABLE\_PRODUCT\_PRICE

| Product ID | Price |
|------------|-------|
| 1          | 15.99 |
| 2          | 23.99 |
| 3          | 17.50 |
| 4          | 9.99  |
| 5          | 29.99 |

TABLE\_PRODUCT\_COLOR

| Product ID | Color  |
|------------|--------|
| 1          | red    |
| 1          | green  |
| 2          | yellow |
| 3          | green  |
| 4          | yellow |
| 4          | blue   |
| 5          | red    |

# We will next learn Second Normal Form

---

For this we have to understand  
**Prime and non-prime attribute**

**Transitive Functional Dependency**

**Fully functional dependent attribute**  
**Partial functional dependent attribute**

# Prime And Non-prime attribute

---

- Prime attribute: Attribute present in candidate key
- Non-prime attribute: Attribute not present in candidate key

## Prime attribute

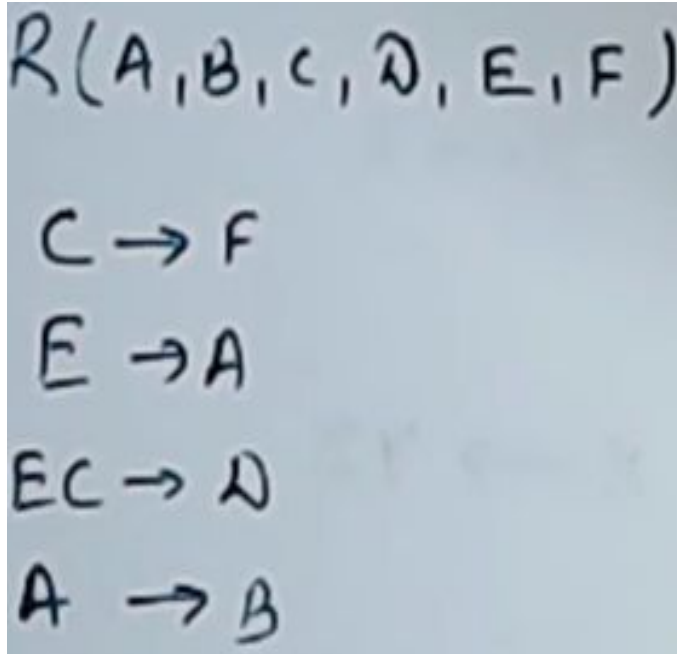
If attribute is a part of candidate key then it will be prime attribute

## Non-prime attribute,

An attribute which is never included in any candidate key.

# Identify prime and non-prime attribute for given functional dependencies

---



Handwritten text showing the relation  $R(A, B, C, D, E, F)$  and the functional dependencies:

- $C \rightarrow F$
- $E \rightarrow A$
- $EC \rightarrow D$
- $A \rightarrow B$

First find Candidate Key

Candidate Key is  $\{CE\}$

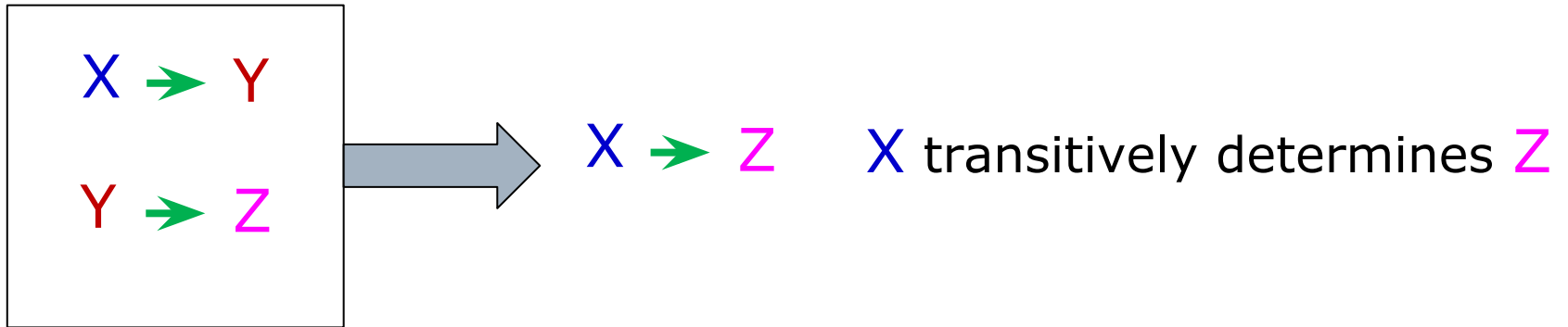
So

Prime attributes are  $\{C, E\}$

Non-Prime attributes are  $\{A, B, D, F\}$

# Transitive Functional Dependency

---





# Fully Functional Dependent Attribute

---

$X \rightarrow Y$

$Y$  is fully functional dependent on  $X$

Only if  $Y$  cannot be determined by **any proper subset** of  $X$ , i.e., removal of any attribute  $A$  from  $X$  means that the dependency does not hold

Example

We say for the Functional Dependency  $ABC \twoheadrightarrow D$ ,  
 $D$  is fully functional dependent on  $ABC$

Only if we **do not have** the FD's

$\{A \twoheadrightarrow D,$   
 $B \twoheadrightarrow D,$   
 $C \twoheadrightarrow D,$   
 $AB \twoheadrightarrow D$   
 $BC \twoheadrightarrow D,$   
 $AC \twoheadrightarrow D, \}$

# Partial Functional Dependent Attribute

---

$X \twoheadrightarrow Y$   $Y$  is partially functional dependent on  $X$   
Only if  $Y$  can be determined by **any proper subset** of  $X$

Note: A functional dependency  $X \rightarrow Y$  is partial dependency if some attribute  $A \in X$  can be removed from  $X$  and the dependency still holds; that is, for some  $A \in X$ ,  $(X - \{A\}) \rightarrow Y$  holds

# Partial Functional Dependent Attribute

---

$X \twoheadrightarrow Y$   $Y$  is partially functional dependent on  $X$   
Only if  $Y$  can be determined by **any proper subset** of  $X$

Example

We say for the Functional Dependency  $AC \twoheadrightarrow P$ ,  
 $P$  attribute is partially functional dependent on  $AC$

Only if we **have** the FD's

$\{A \twoheadrightarrow P\}$

or

$\{C \twoheadrightarrow P\}$

# Announcement

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DBMS Extra Class on  
Wednesday, 2-3-2016, 8:55am, Room number 5002

# Normal Forms Based on a Primary Key

---

## 1 NF: is independent of Primary Key

Disallows composite attributes, multivalued attributes, and nested relations; attributes whose values *for an individual tuple* are **non-atomic**

2 NF: A relation schema R is in second normal form (2NF) if it is in **1 NF** and if every **non-prime attribute A in R** is **fully functionally dependent on the primary key**

3 NF: A relation schema R is in third normal form (3NF) if it is in **2NF** and **no non-prime attribute A in R** is **transitively dependent on the primary key**

# Example: Normalization into 1NF

**1 NF:** is independent of Primary Key

Disallows composite attributes, multivalued attributes, and nested relations; attributes whose values for an

**individual tuple are non-atomic**

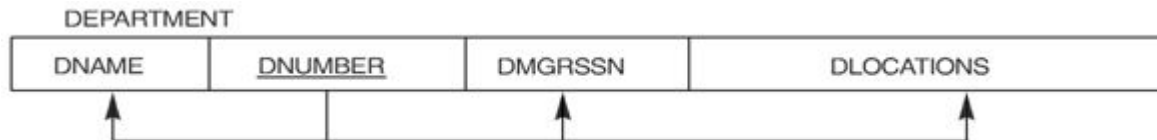
1NF: Removes repeating groups

Table Department with

Attributes DNAME, DNUMBER, DLOCATIONS

Primary Key DNUMBER

Functional Dependency DNUMBER -> (DNAME,DMGRSSN,DLOCATIONS)



| DEPARTMENT     |                |           |                                |
|----------------|----------------|-----------|--------------------------------|
| DNAME          | <u>DNUMBER</u> | DMGRSSN   | DLOCATIONS                     |
| Research       | 5              | 333445555 | {Bellaire, Sugarland, Houston} |
| Administration | 4              | 987654321 | {Stafford}                     |
| Headquarters   | 1              | 888665555 | {Houston}                      |

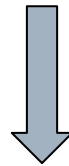
Not atomic values

Not in 1NF

# Example: Normalization into 1NF

## Approach 1

| DEPARTMENT     |                |           |                                |
|----------------|----------------|-----------|--------------------------------|
| DNAME          | <u>DNUMBER</u> | DMGRSSN   | DLOCATIONS                     |
| Research       | 5              | 333445555 | {Bellaire, Sugarland, Houston} |
| Administration | 4              | 987654321 | {Stafford}                     |
| Headquarters   | 1              | 888665555 | {Houston}                      |



Conversion to 1NF

| DEPARTMENT     |                |           |                  |
|----------------|----------------|-----------|------------------|
| DNAME          | <u>DNUMBER</u> | DMGRSSN   | <u>DLOCATION</u> |
| Research       | 5              | 333445555 | Bellaire         |
| Research       | 5              | 333445555 | Sugarland        |
| Research       | 5              | 333445555 | Houston          |
| Administration | 4              | 987654321 | Stafford         |
| Headquarters   | 1              | 888665555 | Houston          |

Disadvantage: Introducing redundancy in the table.

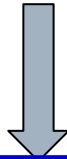
# Example: Normalization into 1NF

## Approach 2

| DEPARTMENT     |                |           |                                |
|----------------|----------------|-----------|--------------------------------|
| DNAME          | <u>DNUMBER</u> | DMGRSSN   | DLOCATIONS                     |
| Research       | 5              | 333445555 | {Bellaire, Sugarland, Houston} |
| Administration | 4              | 987654321 | {Stafford}                     |
| Headquarters   | 1              | 888665555 | {Houston}                      |

Conversion to 1NF

If given DNUMBER is primary Key



| DNAME          | <u>DNUMBER</u> | DMGRSSN   |
|----------------|----------------|-----------|
| Research       | 5              | 333445555 |
| Administration | 4              | 987654321 |
| Headquarters   | 1              | 888665555 |

| <u>DNUMBER</u> | <u>DLOCATIONS</u> |
|----------------|-------------------|
| 5              | Bellaire          |
| 5              | Sugarland         |
| 5              | Houston           |
| 4              | Stafford          |
| 1              | Houston           |

Propagating  
Primary  
Key

Advantage: This approach does not suffer from redundancy.

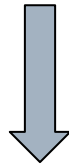


# Example: Normalization into 1NF

## Approach 3

| DEPARTMENT     |                |           |                                |
|----------------|----------------|-----------|--------------------------------|
| DNAME          | <u>DNUMBER</u> | DMGRSSN   | DLOCATIONS                     |
| Research       | 5              | 333445555 | {Bellaire, Sugarland, Houston} |
| Administration | 4              | 987654321 | {Stafford}                     |
| Headquarters   | 1              | 888665555 | {Houston}                      |

Conversion to 1NF



If given that at most maximum  
Three department locations can exist

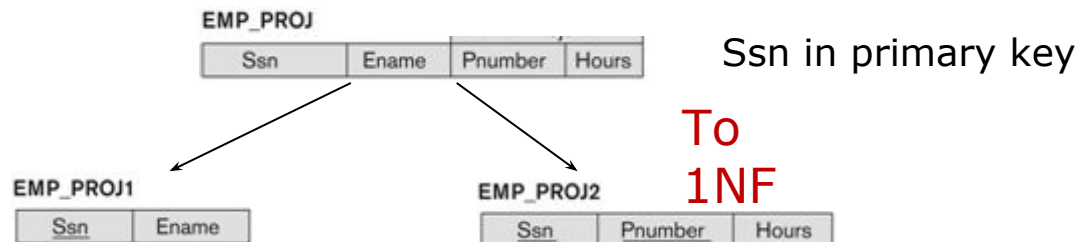
| DNAME          | DNUMBER | DMGRSSN   | <b>DLOCATIONS 1</b> | <b>DLOCATIONS2</b> | <b>DLOCATIONS 3</b> |
|----------------|---------|-----------|---------------------|--------------------|---------------------|
| Research       | 5       | 333445555 | Bellaire            | Sugarland          | Houston             |
| Administration | 4       | 987654321 | Stafford            |                    |                     |
| Headquarters   | 1       | 888665555 | Houston             |                    |                     |

Disadvantage: This approach introduces NULL values for most departments having fewer than three locations.

# Example: Normalization to 1NF

EMP\_PROJ

| Ssn       | Ename                | Pnumber | Hours |
|-----------|----------------------|---------|-------|
| 123456789 | Smith, John B.       | 1       | 32.5  |
|           |                      | 2       | 7.5   |
| 666884444 | Narayan, Ramesh K.   | 3       | 40.0  |
| 453453453 | English, Joyce A.    | 1       | 20.0  |
|           |                      | 2       | 20.0  |
| 333445555 | Wong, Franklin T.    | 2       | 10.0  |
|           |                      | 3       | 10.0  |
|           |                      | 10      | 10.0  |
|           |                      | 20      | 10.0  |
| 999887777 | Zelaya, AliciaJ.     | 30      | 30.0  |
|           |                      | 10      | 10.0  |
| 987987987 | Jabbar, Ahmad V.     | 10      | 35.0  |
|           |                      | 30      | 5.0   |
| 987654321 | Wallace, Jennifer S. | 30      | 20.0  |
|           |                      | 20      | 15.0  |
| 888665555 | Borg, James E.       | 20      | NULL  |



## Example: Normalizing to 2 NF based on Primary Key

---

**2 NF:** A relation schema R is in second normal form (2NF)  
if it is in **1 NF**  
and  
if every non-prime attribute A in R is fully functionally dependent  
on the primary key

2NF: Removes Partial dependencies

**Note:** For tables where primary key contains multiple attributes, no nonkey attribute should be functionally dependent on a part of primary key.

## Example: Normalizing to 2 NF based on Primary Key

**2 NF:** A relation schema R is in second normal form (2NF)

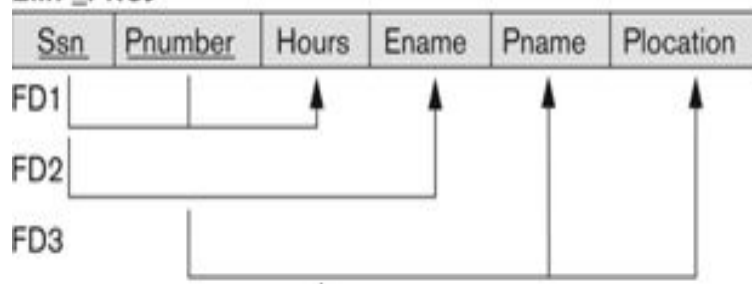
if it is in **1 NF**

and

if every **non-prime attribute A** in R is fully functionally dependent on the primary key

**Question:** Is the following table **EMP\_PROJ** satisfies 2 NF

EMP\_PROJ



Given

Primary key (Ssn, Pnumber)

FD's

FD 1: (Ssn,Pnumber) -> Hours

FD 2: (Ssn) -> Ename

FD 3: (Pnumber) -> (Pname,Plocation)

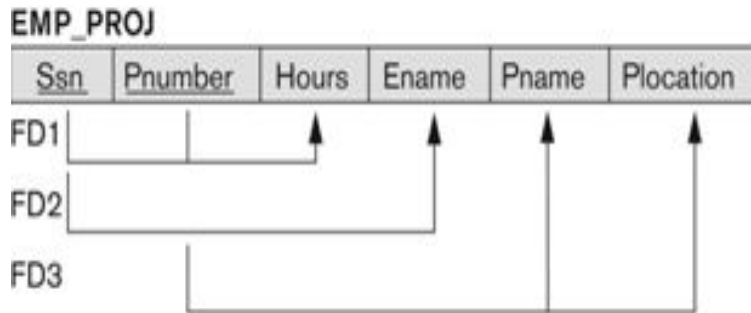
## Example: Normalizing to 2 NF based on Primary Key

**2 NF:** A relation schema R is in **second normal form (2NF)** if it is in 1 NF and if every **non-prime attribute A** in R is **fully functionally dependent** on the primary key

### Examples of FULL and PARTIAL

{SSN, PNUMBER}  $\rightarrow$  HOURS is a full FD since neither SSN  $\rightarrow$  HOURS nor PNUMBER  $\rightarrow$  HOURS holds

{SSN, PNUMBER}  $\rightarrow$  ENAME is *not* a full FD, it is called a *partial dependency* because SSN  $\rightarrow$  ENAME also holds



Given

Primary key (Ssn, Pnumber)

FD's

FD 1: (Ssn,Pnumber)  $\rightarrow$  Hours

FD 2: (Ssn)  $\rightarrow$  Ename

FD 3: (Pnumber)  $\rightarrow$  (Pname,Plocation)

Relation EMP\_PROJ(Ssn,Pnumber,Hours,Ename,Pname,Plocation) is **not in 2 NF**

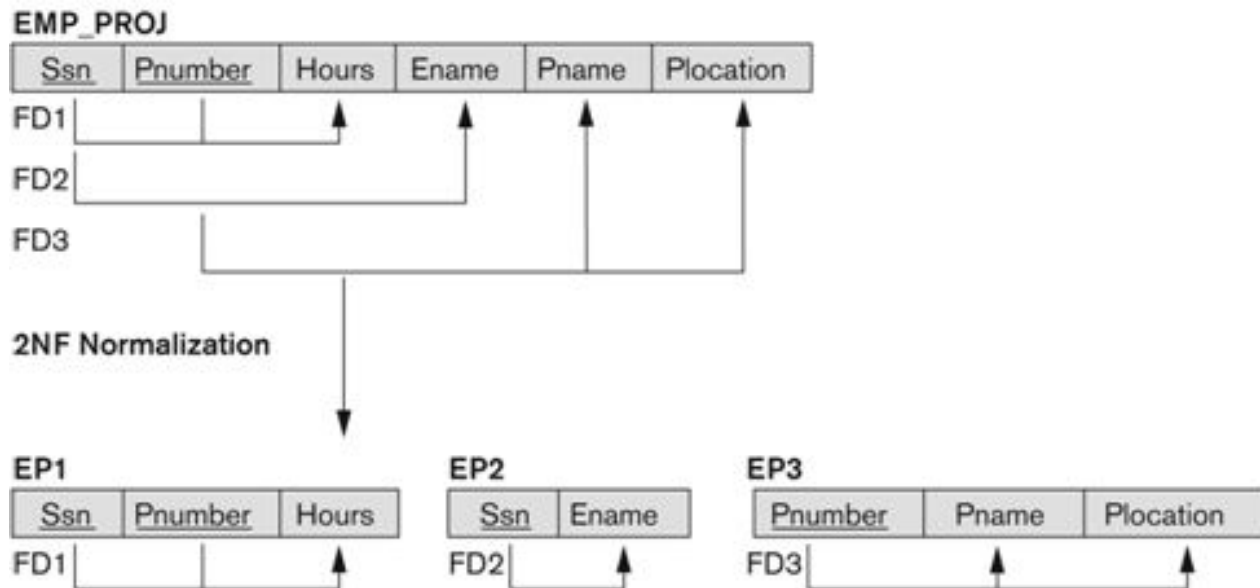
Because in FD 2: (Ssn)  $\rightarrow$  Ename, Ssn alone can determine Ename

Ssn is part of primary key (Ssn,Pnumber) i.e Ssn proper subset of (Ssn,Ename)

Similarly in FD 3 : (Pnumber)  $\rightarrow$  (Pname,Plocation), Pnumber is part of primary key (Ssn,Ename)

## Example: Normalizing to 2 NF based on Primary Key

**2 NF:** A relation schema R is in **second normal form (2NF)** if it is in 1 NF and if every **non-prime attribute A** in R is fully functionally dependent on the primary key

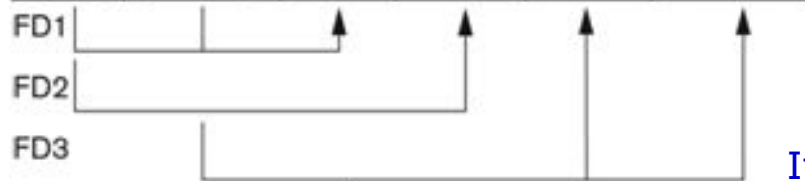


## Example: Normalizing to 2 NF based on Primary Key

**2 NF:** A relation schema R is in **second normal form (2NF)** if it is in 1 NF and if **every non-prime attribute A in R is fully functionally dependent on the primary key**

EMP\_PROJ

| <u>Ssn</u> | <u>Pnumber</u> | Hours | Ename | Pname | Plocation |
|------------|----------------|-------|-------|-------|-----------|
|------------|----------------|-------|-------|-------|-----------|



2NF Normalization

EP1

| <u>Ssn</u> | <u>Pnumber</u> | Hours |
|------------|----------------|-------|
|------------|----------------|-------|

FD1: Ssn → Hours

EP2

| <u>Ssn</u> | Ename |
|------------|-------|
|------------|-------|

FD2: Ssn → Ename

EP3

| <u>Pnumber</u> | Pname | Plocation |
|----------------|-------|-----------|
|----------------|-------|-----------|

FD3: Pnumber → Pname

FD4: Pnumber → Plocation

If a table is not in 2 NF, it can be normalized to 2 NF By breaking into number of 2 NF tables in which nonprime attributes are associated only with part of primary key On which they are fully dependent.

Note:

English words meaning **Table** or **Relation** are one and the same w.r.t. database

# Normalizing to 3 NF based on Primary Key

---

**3 NF:** A relation schema R is in third normal form (3NF)

if it is in 2NF

*and*

no non-prime attribute A in R is transitively dependent on the primary key.

3NF: Removes transitive dependencies



# Normalizing to 3 NF based on Primary Key

**3 NF:** A relation schema R is in third normal form (3NF)

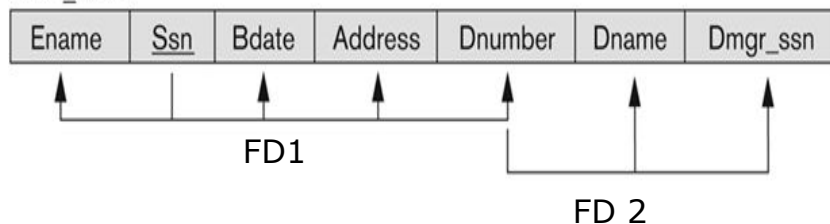
if it is in 2NF

and

no non-prime attribute A in R is transitively dependent on the primary key.

**Question:** In the following table **EMP\_PROJ** , what is the transitive dependency that exist on primary key

EMP\_DEPT



Given

Primary key {Ssn}

FD 1: Ssn -> {Ename,Bdate,Address, Dnumber}

FD 2: Dnumber -> {Dname,Dmgr\_ssn}

# Normalizing to 3 NF based on Primary Key

**3 NF:** A relation schema R is in third normal form (3NF)

if it is in 2NF

and

no non-prime attribute A in R is transitively dependent on the primary key.

**Question:** Is the following table **EMP\_PROJ** satisfies 3 NF

EMP\_DEPT

| Ename | <u>Ssn</u> | Bdate | Address | Dnumber | Dname | Dmgr_ssn |
|-------|------------|-------|---------|---------|-------|----------|
| ↑     | ↑          | ↑     | ↑       | ↑       | ↑     | ↑        |

Given

Primary key {Ssn}

FD 1: Ssn -> {Ename,Bdate,Address, Dnumber}

FD 2: Dnumber -> {Dname,Dmgr\_ssn}

- SSN -> DMGRSSN is a **transitive** FD
  - Since SSN -> DNUMBER and DNUMBER -> DMGRSSN hold
- SSN -> ENAME is **non-transitive**
  - Since there is no set of attributes X where SSN -> X and X -> ENAME

## Example: Normalizing to 3 NF based on Primary Key

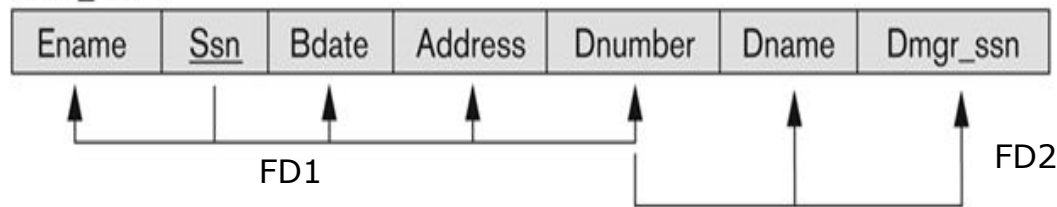
Given

Primary key {Ssn}

FD 1: Ssn → {Ename, Bdate, Address, Dnumber}

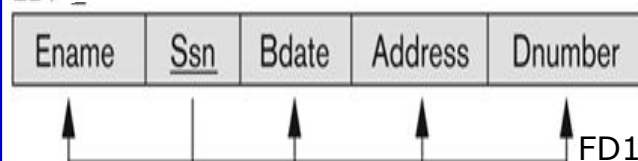
FD 2: Dnumber → {Dname, Dmgr\_ssn}

EMP\_DEPT

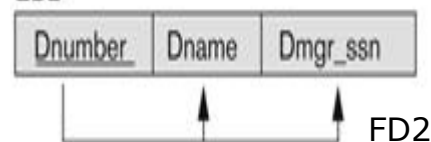


Converting to 3 NF

ED1



ED2



# Until now What we have learned

---

**First Normal Form.**

**Second** and **Third** Normal form based on PRIMARY KEY.

Next we will learn **Second** and **Third** Normal form based on ALL CANDIDATE KEYS in a given relation.

## General definition of Second Normal Form

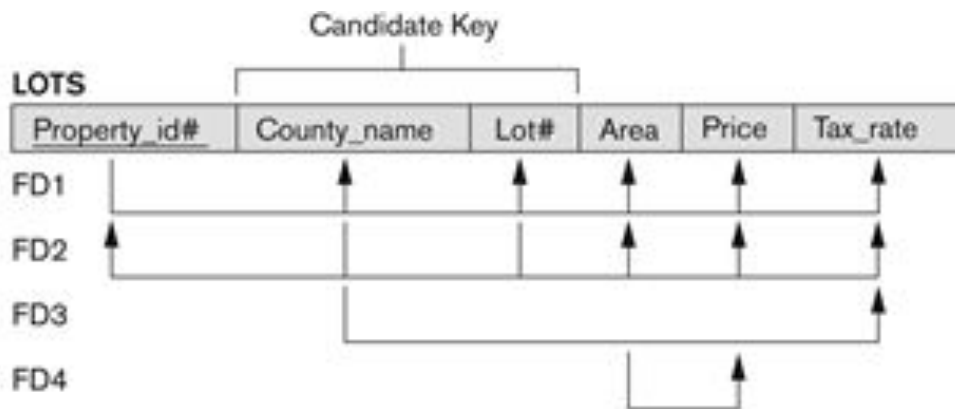
---

- General definitions of 2NF take into account relations with multiple candidate keys.

**2 NF:** A relation schema R is in second normal form (2NF) if every **non-prime attribute** A in R is **fully functionally dependent** on **every key** of R

# Example: Normalizing into 2 NF

**2 NF:** A relation schema R is in second normal form (2NF) if **every non-prime attribute** A in R is **fully functionally dependent** on **every key** of R



Given

Primary Key {Property\_id#}

Candidate key {County\_name, Lot#}

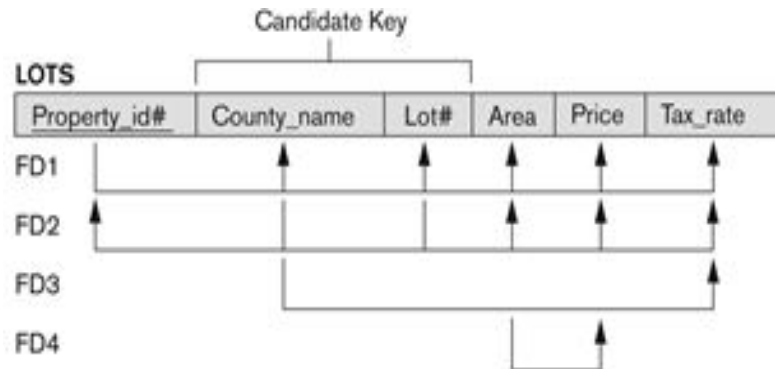
## Question

Which attributes are prime, which are nonprime?

Are any nonprime attributes partially dependent on prime attributes?

# Example: Normalizing into 2 NF

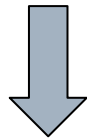
**2 NF:** A relation schema R is in **second normal form (2NF)** if every non-prime attribute A in R is **fully functionally dependent** on **every key** of R



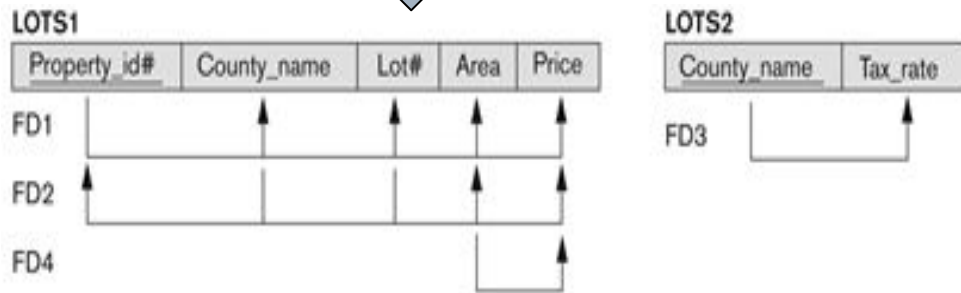
Given

Primary Key {Property\_id#}

Candidate key {County\_name, Lot#}



Converting to 2 NF



## General definition of Third Normal Form

---

- General definition of 3 NF take into account relations with multiple candidate keys.

**3 NF:** A relation schema R is in 3 NF if **every nonprime attribute** of R meets both of the following conditions:

- (a) It is fully functionally dependent on every key of R
- (b) It is **non-transitively** dependent on **every key** of R

Note: There should not be any Transitive Functional Dependency, i.e., **there should not be any functional dependencies like a non-key (non-prime) attribute depends on another non-key (non-prime) attributes**. Simply, we need all the non-key attributes must depend on the key only



## General definition of Third Normal Form

---

- General definition of 3 NF take into account relations with multiple candidate keys.

**3 NF:** A relation schema R is in 3 NF if **every nonprime attribute** of R meets both of the following conditions:

- (a) It is fully functionally dependent on every key of R
- (b) It is **non-transitively** dependent on **every key** of R

Note: There should not be any Transitive Functional Dependency, i.e., there should not be any functional dependencies like a non-key (non-prime) attribute depends on another non-key (non-prime) attributes. Simply, we need all the non-key attributes must depend on the key only

**Example:** R(A,B, C, D, E). Consider candidate keys as {A}, {BC} with FD's {A->BCDE, BC->ADE, D->E}

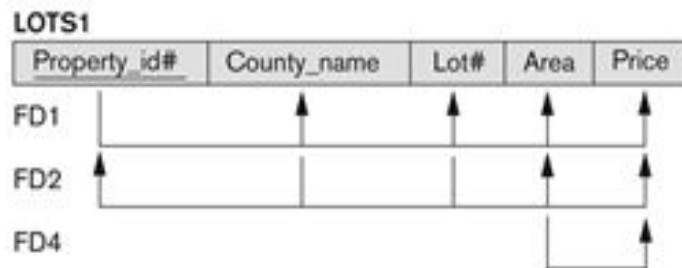
Then Non-prime attributes are {D,E}. The functional dependency {D->E} violates the condition of 3NF because D and E are non-prime attributes

## Example: Normalizing into 3 NF

**3 NF:** A relation schema R is in 3 NF if **every nonprime attribute** of R meets both of the following conditions:

- (a) It is fully functionally dependent on every key of R
- (b) It is **non-transitively** dependent on **every key** of R

Note: There should not be any Transitive Functional Dependency, i.e., there should not be any functional dependencies like a non-key (non-prime) attribute depends on another non-key (non-prime) attributes. Simply, we need all the non-key attributes must depend on the key only



Given

Primary Key {Property\_id#}

Candidate key {County\_name, Lot#}

### Question

Are any nonprime attribute dependent on nonprime attribute?

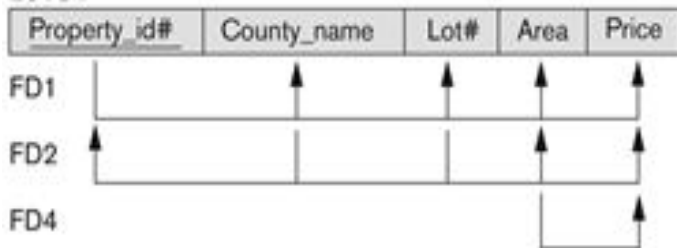
# Example: Normalizing into 3 NF

**3 NF:** A relation schema R is in 3 NF if **every nonprime attribute** of R meets both of the following conditions:

- (a) It is fully functionally dependent on every key of R
- (b) It is **non-transitively** dependent on **every key** of R

Note: There should not be any Transitive Functional Dependency, i.e., there should not be any functional dependencies like a non-key (non-prime) attribute depends on another non-key (non-prime) attributes. Simply, we need all the non-key attributes must depend on the key only

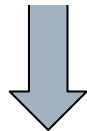
LOTS1



Given

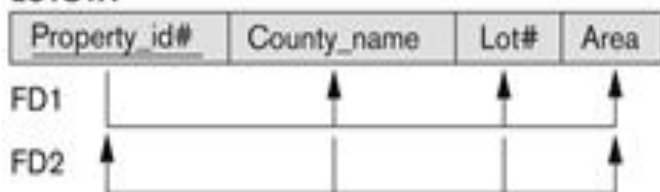
Primary Key {Property\_id#}

Candidate key {County\_name, Lot#}



Converting to 3 NF

LOTS1A



LOTS1B



# Summarizing 1NF, 2NF, 3 NF

---

1NF: Removes  
repeating groups

## **1NF**

Column values should atomic

First Restriction

2NF: Removes  
Partial dependencies

## **2NF**

Non-Prime attributes should be Fully Dependent on each candidate key

Second Restriction

3NF: Removes  
transitive dependencies

## **3NF**

Non-Prime attributes should not Determined by a non-prime attribute

Third Restriction

# Summarizing 1NF, 2NF, 3 NF

---

**1NF:** No Multivalued attributes or All columns should be atomic

**2NF:** It should be in **1 NF** and All non-prime attributes should be fully functionally dependent on primary key or each candidate key

**3NF:**

For relation R to be in 3 NF check

(a) R should be in **2 NF**

(b) No non-prime attribute should be transitively dependent on Candidate key or There should not be the case that a non-prime attribute is determined by another non-prime attribute.

## Problem to Solve: Normalizing to 2 NF and 3 NF

---

Consider the relation  $R = \{A, B, C, D, E, F, G, H, I, J\}$  and the set of functional dependencies

$F = \{\{A, B\} \rightarrow \{C\},$   
 $\{A\} \rightarrow \{D, E\},$   
 $\{B\} \rightarrow \{F\},$   
 $\{F\} \rightarrow \{G, H\},$   
 $\{D\} \rightarrow \{I, J\}\}.$

|     |                              |
|-----|------------------------------|
| FD1 | $\{A, B\} \rightarrow \{C\}$ |
| FD2 | $\{A\} \rightarrow \{D, E\}$ |
| FD3 | $\{B\} \rightarrow \{F\}$    |
| FD4 | $\{F\} \rightarrow \{G, H\}$ |
| FD5 | $\{D\} \rightarrow \{I, J\}$ |

Given the **Key** of **R** as  **$\{AB\}$**

- (a) Decompose R into 2NF.
- (b) Decompose R into 3NF.

## Problem to Solve: Normalizing to 2 NF and 3 NF

Consider the relation  $R = \{A, B, C, D, E, F, G, H, I, J\}$  and the set of functional dependencies  $F = \{\{A, B\} \rightarrow \{C\}, \{A\} \rightarrow \{D, E\}, \{B\} \rightarrow \{F\}, \{F\} \rightarrow \{G, H\}, \{D\} \rightarrow \{I, J\}\}$ . Given the Key of R as  $\{AB\}$

- (a) Decompose R into 2NF.
- (b) Decompose R into 3NF.

Splitting out attributes based on relations only partially dependent on the key gives:

$R_1 = \{\underline{A}, D, E, I, J\}$  preserves the functional dependencies  
 $\{\{A\} \rightarrow \{D, E\}, \{D\} \rightarrow \{I, J\}\}$   
 $R_2 = \{\underline{B}, F, G, H\}$  preserves  $\{\{B\} \rightarrow \{F\}, \{F\} \rightarrow \{G, H\}\}$   
 $R_3 = \{\underline{A}, \underline{B}, C\}$  preserves  $\{\{A, B\} \rightarrow \{C\}\}$

The primary keys of these subrelations are underlined.

Decompose R into 2NF

Further splitting attributes with transitive dependencies on their keys gives:

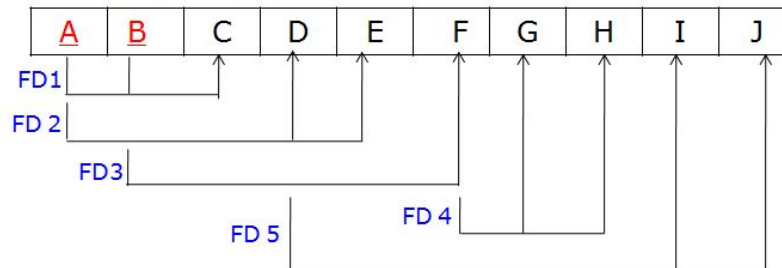
$R_{1a} = \{\underline{A}, D, E\}$   
 $R_{1b} = \{\underline{D}, I, J\}$   
 $R_{2a} = \{\underline{B}, F\}$   
 $R_{2b} = \{\underline{F}, G, H\}$   
 $R_3 = \{\underline{A}, \underline{B}, C\}$

Decompose R into 3NF

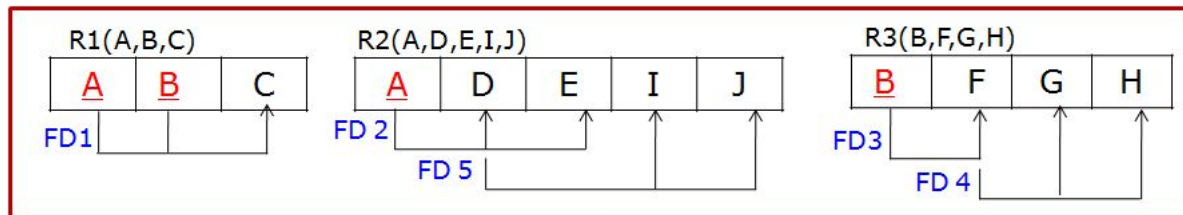
# Problem to Solve: Normalizing to 2 NF and 3 NF

Consider the relation  $R = \{A, B, C, D, E, F, G, H, I, J\}$  and the set of functional dependencies  $F = \{\{A, B\} \rightarrow \{C\}, \{A\} \rightarrow \{D, E\}, \{B\} \rightarrow \{F\}, \{F\} \rightarrow \{G, H\}, \{D\} \rightarrow \{I, J\}\}$ . Given the Key of R as  $\{AB\}$  (a) Decompose R into 2NF. (b) Decompose R into 3NF.

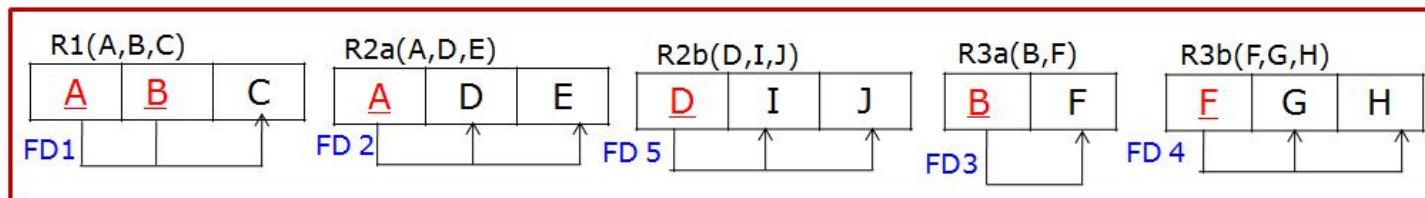
$R(A, B, C, D, E, F, G, H, I, J)$



↓ Converting to 2 NF



↓ Converting to 3 NF





# Problem to Solve: Normalizing to 2 NF and 3 NF

---

Consider the relation  $R = \{A, B, C, D, E, F, G, H, I, J\}$  and the set of functional dependencies

$F = \{\{A, B\} \rightarrow \{C\},$   
     $\{B, D\} \rightarrow \{E, F\},$   
     $\{A, D\} \rightarrow \{G, H\},$   
     $\{A\} \rightarrow \{I\},$   
     $\{H\} \rightarrow \{J\}\}.$

Given the **Key** of **R** as **{ABD}**

- (a) Decompose R into 2NF.
- (b) Decompose R into 3NF.

# Problem to Solve

---

Given relation  $R(A,B,C,D,E)$   
with dependencies

$AB \rightarrow C$

$CD \rightarrow E$

$DE \rightarrow B$

Is  $AB$  a candidate key of this relation?

If not, is  $ABD$ ? Explain your answer.

# Problem to Solve

---

Given relation  $R(A,B,C,D,E)$

with dependencies  $AB \rightarrow C$   $CD \rightarrow E$   $DE \rightarrow B$

is  $AB$  a candidate key of this relation?

If not, is  $ABD$ ? Explain your answer.

## Answers:

Closure of  $AB^+ = \{A,B,C\}$

**NO**,  $AB$  is NOT KEY

Because  $AB$  cannot determine all attributes, Closure of  $AB^+$  is  $\{A,B,C\}$  which is proper subset of  $\{A,B,C,D,E\}$

# Problem to Solve

---

Given relation  $R(A,B,C,D,E)$  with dependencies  $AB \rightarrow C$ ,  $CD \rightarrow E$ ,  $DE \rightarrow B$   
is  $AB$  a candidate key of this relation? If not, is  $ABD$ ? Explain your answer.

**Answers:** Yes,  $ABD^+ = \{A,B,C,D,E\}$ . Yes,  **$ABD$**  is a candidate key. No subset of its attributes is a key.

**$A \rightarrow A$**

**$B \rightarrow B$**

$C \rightarrow C$

**$D \rightarrow D$**

$E \rightarrow E$

**$AB \rightarrow ABC$**

$AC \rightarrow AC$

**$AD \rightarrow AD$**

$AE \rightarrow AE$

$BC \rightarrow BC$

**$BD \rightarrow BD$**

$BE \rightarrow BE$

$CD \rightarrow BCDE$

$CE \rightarrow CE$

$DE \rightarrow BDE$

**$ABD \rightarrow ABCDE$**

# Problem to Solve

---

Consider the following relation:

| A  | B  | C  | TUPLE# |
|----|----|----|--------|
| 10 | b1 | c1 | #1     |
| 10 | b2 | c2 | #2     |
| 11 | b4 | c1 | #3     |
| 12 | b3 | c4 | #4     |
| 13 | b1 | c1 | #5     |
| 14 | b3 | c4 | #6     |

(a) Given the above extension (state), which of the following dependencies may hold in the above relation? If the dependency cannot hold, explain why by specifying the tuples that cause the violation.

i.  $A \rightarrow B$ , ii.  $B \rightarrow C$ , iii.  $C \rightarrow B$ , iv.  $B \rightarrow A$ , v.  $C \rightarrow A$

# Problem to Solve

| A  | B  | C  | TUPLE# |
|----|----|----|--------|
| 10 | b1 | c1 | #1     |
| 10 | b2 | c2 | #2     |
| 11 | b4 | c1 | #3     |
| 12 | b3 | c4 | #4     |
| 13 | b1 | c1 | #5     |
| 14 | b3 | c4 | #6     |

- 1.
- $A \rightarrow B$  **NO**  
For  $A=10$ ,  $B=b1, b2$  Ex: tuple 1,2
  - $A \rightarrow C$  **NO**  
For  $A=10$ ,  $C=c1, c2$  Ex: tuple 1,2
  - $B \rightarrow C$  **Yes**  
For  $B=b4$ ,  $C=c1$  ;  $B=b1$ ,  $C=c1$  Ex: tuple 3,5 (or Ex: tuple 4,6)
  - $C \rightarrow B$  **NO**  
For  $C=c1$ ,  $B=b1, b4$  Ex: tuple 1,3
  - $B \rightarrow A$  **NO**  
For  $B=b3$ ,  $A=12, 14$  Ex: tuple 4,6
  - $C \rightarrow A$  **NO**  
For  $C=c1$ ,  $A=10, 11, 13$  Ex: tuple 1,3,5
  - $AB \rightarrow C$  **YES**
  - $AC \rightarrow B$  **YES**
  - $BC \rightarrow A$  **NO** For  $(b1, c1) \rightarrow 10$  ;  $(b1, c1) \rightarrow 13$  Tuple 1,5

# Problem to Solve

---

Consider a relation with schema  $R(A, B, C, D)$   
and

$FD = \{AB \rightarrow C,$   
           $C \rightarrow D,$   
           $D \rightarrow A\}$

- (a) What are all the non-trivial FDs that follow from the given FD's?
- (b) What are all the candidate keys of R?
- (c) What are all the superkeys of R that are not candidate keys?

# Non Trivial Functional Dependency

---

If a functional dependency  $X \rightarrow Y$  holds true where  $Y$  is **not a subset** of  $X$  then this dependency is called non trivial Functional dependency.

□ **For example:**

An employee table with three attributes: emp\_id, emp\_name, emp\_address.

The following functional dependencies are **non-trivial**:

emp\_id  $\rightarrow$  emp\_name (emp\_name is not a subset of emp\_id)

emp\_id  $\rightarrow$  emp\_address (emp\_address is not a subset of emp\_id)

- On the other hand, the following dependencies are **trivial**:
- {emp\_id, emp\_name}  $\rightarrow$  emp\_name [emp\_name is a subset of {emp\_id, emp\_name}]

## **Completely non trivial FD:**

If a FD  $X \rightarrow Y$  holds true where  **$X$  intersection  $Y$  is null** then this dependency is said to be completely non trivial function dependency.

Example: SSN  $\rightarrow$  Ename, PNUMBER  $\rightarrow$  PNAME, PNUMBER  $\rightarrow$  BDATE



# Answers

---

Consider a relation with schema  $R(A, B, C, D)$  and  $FD = \{AB \rightarrow C, C \rightarrow D, D \rightarrow A\}$

(a) What are all the non-trivial FDs that follow from the given FD's?

We need to compute the closures of all 15 nonempty sets of attributes.

**Single Attributes:**

$A^+ = A$

$B^+ = B$

$C^+ = ACD$  (New dependency:  $C \rightarrow A$ )

$D^+ = AD$

**Pairs of Attributes:**

$AB^+ = ABCD$  (New dependency:  $AB \rightarrow D$ )

$AC^+ = ACD$  (New dependency:  $AC \rightarrow D$ )

$AD^+ = AD$

$BC^+ = ABCD$  (New dependencies:  $BC \rightarrow A$  and  $BC \rightarrow D$ )

$BD^+ = ABCD$  (New dependencies:  $BD \rightarrow A$  and  $BD \rightarrow C$ )

$CD^+ = ACD$  (New dependencies:  $CD \rightarrow A$ )

**Triples of Attributes:**

$ABC^+ = ABCD$  (New dependencies:  $ABC \rightarrow D$ )

$ACD^+ = ACD$

$BCD^+ = ABCD$  (New dependencies:  $BCD \rightarrow A$ )

$ABD^+ = ABCD$  (New dependencies:  $ABD \rightarrow C$ )

**All the Attributes:**

$ABCD^+ = ABCD$

So, we get a total of 11 non-trivial FDs.

# Answers

---

(b) What are all the candidate keys of R?

From the closures above, we find that **AB**, **BC**, and **BD** are keys, because they have ABCD as the closure, and they are minimal.

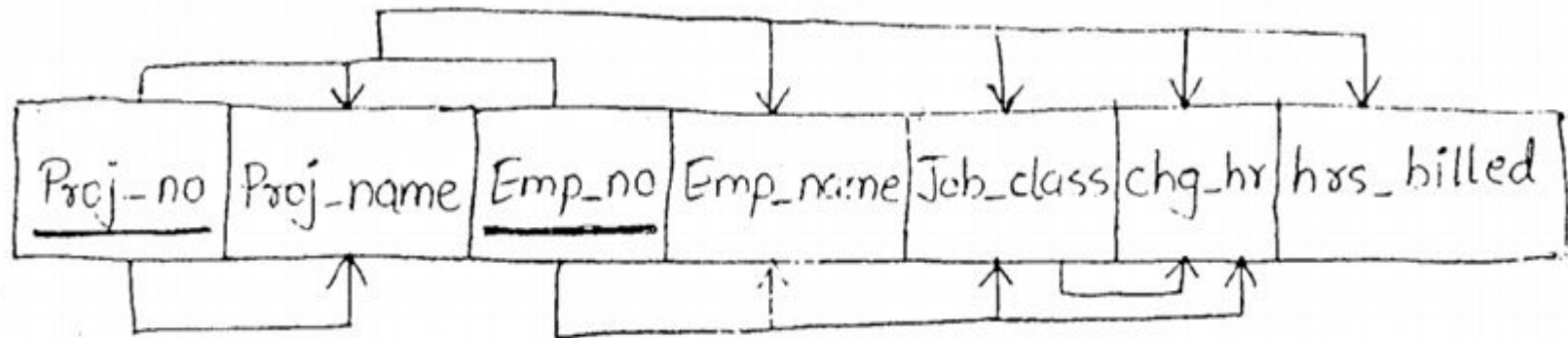
(c) What are all the superkeys of R that are not candidate keys?

The superkeys are all those that contain one of those three candidate keys. Thus, the **superkeys** are **ABC**, **ABD**, **BCD**, and **ABCD**.

# Problem to Solve

---

Consider a dependency diagram of relation R and normalize it up to third normal form.



# Why we remove Partial Functional Dependency in second Normal form ?

---

Because **Partial Functional Dependency** is "BAD"

## Why we remove Partial functional Dependency in second Normal form ?

---

Student(USN,Subject,Grade,Name,DOB)

| <u>USN</u> | <u>Subject</u> | Grade | Name    | DOB        |
|------------|----------------|-------|---------|------------|
| 1BM14CS001 | DBMS           | S     | Avinash | 14/11/1997 |
| 1BM14CS001 | OS             | B     | Avinash | 14/11/1997 |
| 1BM14CS002 | DBMS           | A     | Balaji  | 11/03/1998 |
| 1BM14CS002 | OS             | C     | Balaji  | 11/03/1998 |
| 1BM14CS003 | DBMS           | B     | Mohan   | 21/08/1996 |

**Primary Key (USN,Subject)**

**Full** Functional Dependency (USN,Subject) -> (Grade)

**Partial** Functional Dependency (USN) -> (Name,DOB)

## Why we remove Partial functional Dependency in second Normal form ?

Student(USN,Subject,Grade,Name,DOB)

| <u>USN</u> | <u>Subject</u> | Grade | Name    | DOB        |
|------------|----------------|-------|---------|------------|
| 1BM14CS001 | DBMS           | S     | Avinash | 14/11/1997 |
| 1BM14CS001 | OS             | B     | Avinash | 14/11/1997 |
| 1BM14CS002 | DBMS           | A     | Balaji  | 11/03/1998 |
| 1BM14CS002 | OS             | C     | Balaji  | 11/03/1998 |
| 1BM14CS003 | DBMS           | B     | Mohan   | 21/08/1996 |

**Primary Key (USN,Subject)**

**Full** Functional Dependency (USN,Subject) -> (Grade)

**Partial** Functional Dependency (USN) -> (Name,DOB)

Student(USN,Subject,Grade,Name,DOB)

Student\_1(USN,Name,DOB)

Student\_2(USN,Subject,Grade)

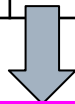
Converting To 2NF

## Why we remove Partial functional Dependency in second Normal form ?

Student(USN,Subject,Grade,Name,DOB)

| <u>USN</u> | <u>Subject</u> | Grade | Name    | DOB        |
|------------|----------------|-------|---------|------------|
| 1BM14CS001 | DBMS           | S     | Avinash | 14/11/1997 |
| 1BM14CS001 | OS             | B     | Avinash | 14/11/1997 |
| 1BM14CS002 | DBMS           | A     | Balaji  | 11/03/1998 |
| 1BM14CS002 | OS             | C     | Balaji  | 11/03/1998 |
| 1BM14CS003 | DBMS           | B     | Mohan   | 21/08/1996 |

Redundant  
Name and DOB



Converting To 2NF

| <u>USN</u> | Name    | DOB        |
|------------|---------|------------|
| 1BM14CS001 | Avinash | 14/11/1997 |
| 1BM14CS002 | Balaji  | 11/03/1998 |
| 1BM14CS003 | Mohan   | 21/08/1996 |

| <u>USN</u> | <u>Subject</u> | Grade |
|------------|----------------|-------|
| 1BM14CS001 | DBMS           | S     |
| 1BM14CS001 | OS             | B     |
| 1BM14CS002 | DBMS           | A     |
| 1BM14CS002 | OS             | C     |
| 1BM14CS003 | DBMS           | B     |

# Why we remove Transitive Functional Dependency in Third Normal form ?

---

Because **Transitive Functional Dependency** is "BAD"



## Why we remove Transitive Functional Dependency in Third Normal form ?

---

Project(Project-Num, Manager, Mgr\_City)

| <u>Project-Num</u> | Manager | Mgr_City  |
|--------------------|---------|-----------|
| P1                 | Avinash | Bangalore |
| P2                 | Avinash | Bangalore |
| P3                 | Balaji  | Chennai   |
| P4                 | Balaji  | Chennai   |
| P5                 | Mohan   | Mumbai    |

**Primary Key (Project-Num)**

Functional Dependency (Project-Num) -> (Manager, Mgr\_City)

Functional Dependency (Manager) -> (Mgr\_City)      non-prime attribute determining non-prime

## Why we remove Transitive Functional Dependency in Third Normal form ?

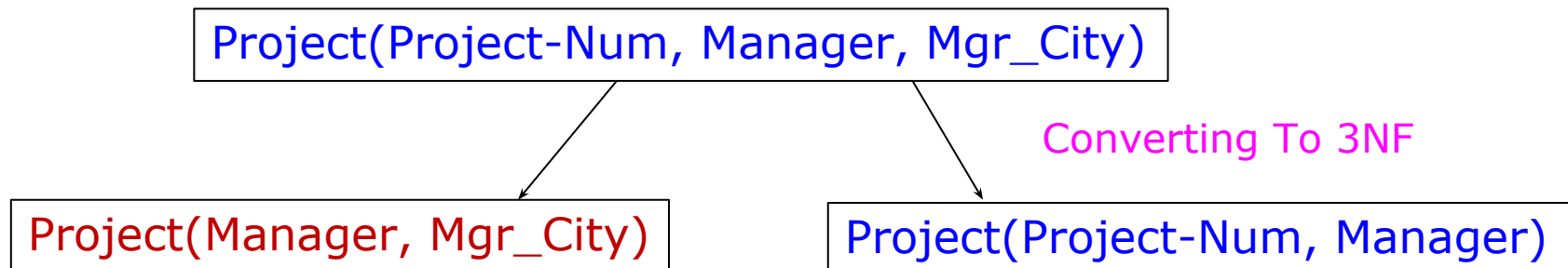
Project(Project-Num, Manager, Mgr\_City)

| <u>Project-Num</u> | Manager | Mgr_City  |
|--------------------|---------|-----------|
| P1                 | Avinash | Bangalore |
| P2                 | Avinash | Bangalore |
| P3                 | Balaji  | Chennai   |
| P4                 | Balaji  | Chennai   |
| P5                 | Mohan   | Mumbai    |

**Primary Key (Project-Num)**

Functional Dependency (Project-Num) -> (Manager, Mgr\_City)

Functional Dependency (Manager) -> (Mgr\_City)      non-prime attribute determining non-prime



## Why we remove Transitive Functional Dependency in Third Normal form ?

Project(Project-Num, Manager, Mgr\_City)

| <u>Project-Num</u> | Manager | Mgr_City  |
|--------------------|---------|-----------|
| P1                 | Avinash | Bangalore |
| P2                 | Avinash | Bangalore |
| P3                 | Balaji  | Chennai   |
| P4                 | Balaji  | Chennai   |
| P5                 | Mohan   | Mumbai    |

Redundant  
Mgr\_City



Converting To 3NF

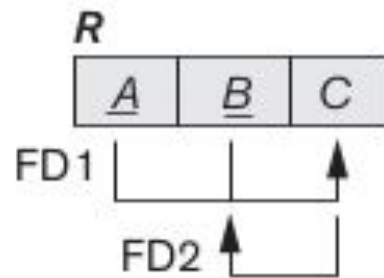
| Manager | Mgr_City  |
|---------|-----------|
| Avinash | Bangalore |
| Balaji  | Chennai   |
| Mohan   | Mumbai    |

| <u>Project-Num</u> | Manager |
|--------------------|---------|
| P1                 | Avinash |
| P2                 | Avinash |
| P3                 | Balaji  |
| P4                 | Balaji  |
| P5                 | Mohan   |

# Boyce-Codd Normal Form

---

A relation schema  $R$  is in *BCNF* if whenever a *nontrivial* functional dependency  $X \rightarrow A$  holds in  $R$ , then  $X$  is a **superkey/candidate key** of  $R$ .



Relation  $R(A, B, C)$

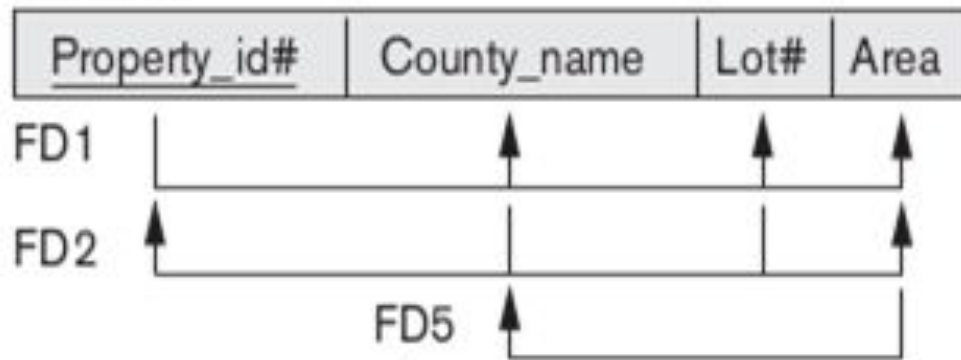
With key  $(AB)$  is in 3 NF but not in BCNF

Because in FD,  $C \rightarrow B$ ,  $C$  is not a super key

# Boyce-Codd Normal Form

A relation schema  $R$  is in *BCNF* if whenever a *nontrivial* functional dependency  $X \rightarrow A$  holds in  $R$ , then  $X$  is a **superkey/candidate key** of  $R$ .

LOTS1A



Given

Primary Key {Property\_id#}

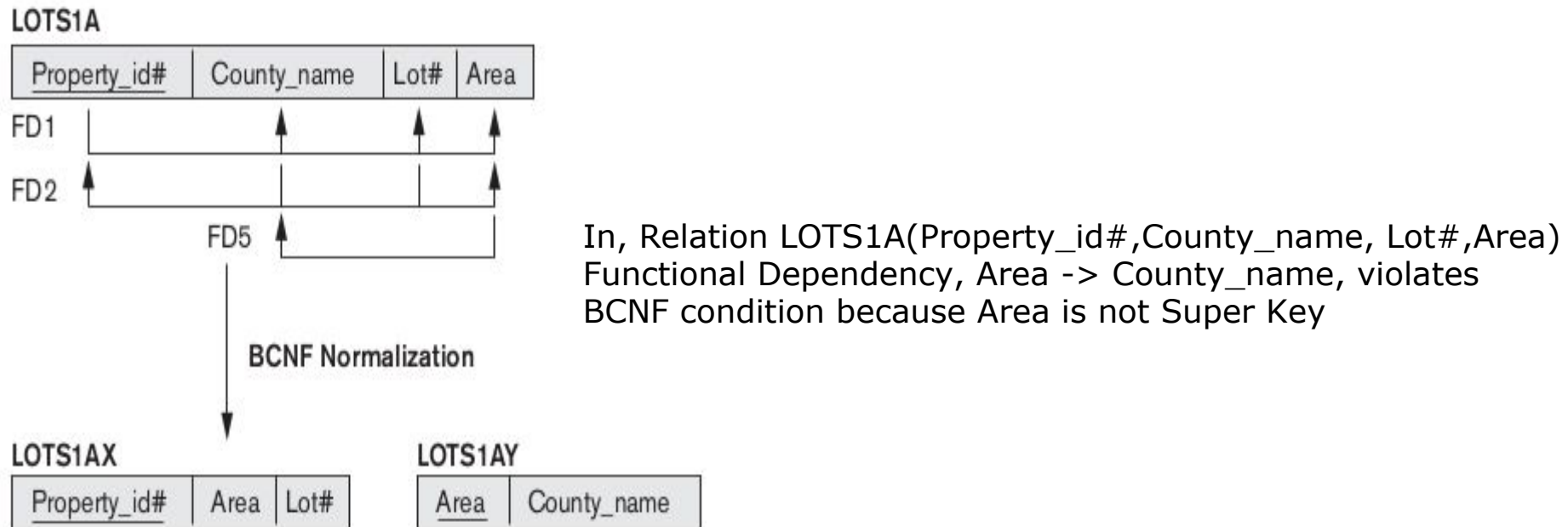
Candidate key {County\_name, Lot#}

## Question

Which Function Dependency Violates BCNF in the relation LOTS1A ?

# Boyce-Codd Normal Form

A relation schema  $R$  is in *BCNF* if whenever a *nontrivial* functional dependency  $X \rightarrow A$  holds in  $R$ , then  $X$  is a **superkey/candidate key** of  $R$ .



Problem To Solve:

Check whether the given FD's satisfies BCNF

---

Consider a relation with schema  $R(A,B,C,D)$  and FDs  $\{AB \rightarrow CD, D \rightarrow A\}$ .

Candidate keys are: AB, BC, and BD

List out among the give FD's which violates BCNF for R

**$D \rightarrow A$** , because D is not Super key

Why in BCNF we remove functional dependency  $X \rightarrow Y$ , if  $X$  is not a Key ?

---



# Problems BCNF overcomes

---

BCNF: Every determinant is a candidate key    FD:  $X \rightarrow Y$ , X is determinant

StudMajor(StudNo,Major,Advisor)

| <u>StudNo</u> | <u>Major</u> | Advisor |
|---------------|--------------|---------|
| 123           | PHYSICS      | Eshwar  |
| 123           | MUSIC        | Mohan   |
| 456           | BIOLOGY      | Dinesh  |
| 789           | PHYSICS      | Balaji  |
| 999           | PHYSICS      | Eshwar  |

Candidate Key (StudNo,Major)

FD's

(StudNo,Major)  $\rightarrow$  Advisor  
(Advisor)  $\rightarrow$  Major

# Problems BCNF overcomes

---

BCNF: Every determinant is a candidate key    FD:  $X \rightarrow Y$ ,  $X$  is determinant

StudMajor(StudNo, Major, Advisor)

| <u>StudNo</u> | <u>Major</u> | Advisor |
|---------------|--------------|---------|
| 123           | PHYSICS      | Eshwar  |
| 123           | MUSIC        | Mohan   |
| 456           | BIOLOGY      | Dinesh  |
| 789           | PHYSICS      | Balaji  |
| 999           | PHYSICS      | Eshwar  |

Candidate Key (StudNo, Major)

FD's

(StudNo, Major)  $\rightarrow$  Advisor  
(Advisor)  $\rightarrow$  Major

## ANOMALIES

**Deleting** student deletes advisor info

**Insert** a new advisor – need a student

**Update** – inconsistencies

# Problems BCNF overcomes

---

BCNF: Every determinant is a candidate key    FD:  $X \rightarrow Y$ ,  $X$  is determinant

StudMajor(StudNo, Major, Advisor)

| <u>StudNo</u> | <u>Major</u> | Advisor |
|---------------|--------------|---------|
| 123           | PHYSICS      | Eshwar  |
| 123           | MUSIC        | Mohan   |
| 456           | BIOLOGY      | Dinesh  |
| 789           | PHYSICS      | Balaji  |
| 999           | PHYSICS      | Eshwar  |

Candidate Key (StudNo, Major)

FD's

(StudNo, Major)  $\rightarrow$  Advisor  
(Advisor)  $\rightarrow$  Major

If the record for student 456 is deleted we lose not only information on student 456 but also the fact that Dinesh advises in BIOLOGY.

We cannot record the fact that Vignesh can advise on COMPUTING until we have a student majoring in COMPUTING to whom we can assign Vignesh as an advisor.

# Problems BCNF overcomes

| <u>StudNo</u> | <u>Major</u> | Advisor |
|---------------|--------------|---------|
| 123           | PHYSICS      | Eshwar  |
| 123           | MUSIC        | Mohan   |
| 456           | BIOLOGY      | Dinesh  |
| 789           | PHYSICS      | Balaji  |
| 999           | PHYSICS      | Eshwar  |

Candidate Key (StudNo, Major)

FD's  
(StudNo, Major) -> Advisor  
(Advisor) -> Major

In BCNF we have two tables:

| <u>StudNo</u> | Advisor |
|---------------|---------|
| 123           | Eshwar  |
| 123           | Mohan   |
| 456           | Dinesh  |
| 789           | Balaji  |
| 999           | Eshwar  |

| <u>Advisor</u> | Major   |
|----------------|---------|
| Eshwar         | PHYSICS |
| Mohan          | MUSIC   |
| Dinesh         | BIOLOGY |
| Balaji         | PHYSICS |

# Next we will learn

---

Fourth Normal Form based on Multivalued Dependencies

# Fourth Normal Form

---

- ❑ It should be in BCNF
- ❑ There should not be any **Multivalued Dependency**.

# What is Multivalued Dependency ?

**Multivalued Dependency** is a kind of dependency which comes when there is two 1:N relationship in single table

| Name   | Skill             | Language                  |
|--------|-------------------|---------------------------|
| Smitha | {Cooking, Typing} | {Kannada, Hindi, English} |



1 NF

| Name   | Skill   | Language |
|--------|---------|----------|
| Smitha | Cooking | Kannada  |
| Smitha | Cooking | Hindi    |
| Smitha | Cooking | English  |
| Smitha | Typing  | Kannada  |
| Smitha | Typing  | Hindi    |
| Smitha | Typing  | English  |

Multivalued Dependency (MVD)

**Name ->-> Skill**

**Name ->-> Language**

# What is Multivalued Dependency ?

**Multivalued Dependency** is a kind of dependency which comes when there is two 1:N relationship in single table

| Name   | Skill             | Language                  |
|--------|-------------------|---------------------------|
| Smitha | {Cooking, Typing} | {Kannada, Hindi, English} |



1 NF

| Name   | Skill   | Language |
|--------|---------|----------|
| Smitha | Cooking | Kannada  |
| Smitha | Cooking | Hindi    |
| Smitha | Cooking | English  |
| Smitha | Typing  | Kannada  |
| Smitha | Typing  | Hindi    |
| Smitha | Typing  | English  |

Multivalued Dependency (MVD)

**Name ->-> Skill**

**Name ->-> Language**

**Problem**

w.r.t Insertion or Deletion of Skill or Language for Smitha



# Normalizing to Fourth Normal Form

| Name   | Skill   | Language |
|--------|---------|----------|
| Smitha | Cooking | Kannada  |
| Smitha | Cooking | Hindi    |
| Smitha | Cooking | English  |
| Smitha | Typing  | Kannada  |
| Smitha | Typing  | Hindi    |
| Smitha | Typing  | English  |

Multivalued Dependency (MVD)

**Name ->-> Skill**

**Name ->-> Language**



**4 NF**

| Name   | Skill   |
|--------|---------|
| Smitha | Cooking |
| Smitha | Typing  |

| Name   | Language |
|--------|----------|
| Smitha | Kannada  |
| Smitha | Hindi    |
| Smitha | English  |

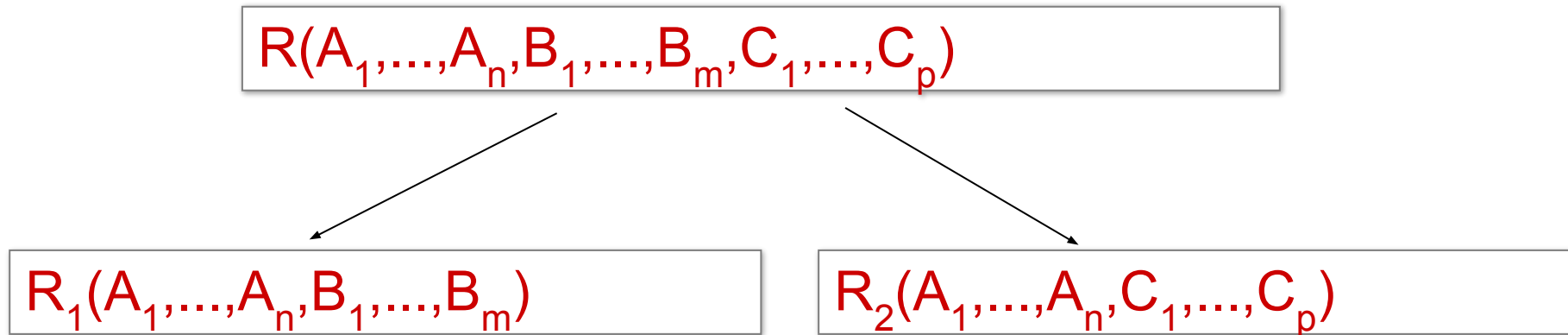
## Next we will learn **Fifth Normal Form**

---

To understand Fifth Normal Form, We should know **JOIN  
DEPENDENCY**

# Decompositions in General

---



$R_1$  = the *projection* of  $R$  on  $A_1, \dots, A_n, B_1, \dots, B_m$

$R_2$  = the *projection* of  $R$  on  $A_1, \dots, A_n, C_1, \dots, C_p$

# Theory of Decomposition

Product

| Name     | Price | Category |
|----------|-------|----------|
| Gizmo    | 19.99 | Gadget   |
| OneClick | 24.99 | Camera   |
| Gizmo    | 19.99 | Camera   |

Sometimes a decomposition is "correct"

i.e. it is a **Lossless decomposition**

Product 1



| Name     | Price |
|----------|-------|
| Gizmo    | 19.99 |
| OneClick | 24.99 |
| Gizmo    | 19.99 |

Product 2



| Name     | Category |
|----------|----------|
| Gizmo    | Gadget   |
| OneClick | Camera   |
| Gizmo    | Camera   |

# Lossy Decomposition

Product

| Name     | Price | Category |
|----------|-------|----------|
| Gizmo    | 19.99 | Gadget   |
| OneClick | 24.99 | Camera   |
| Gizmo    | 19.99 | Camera   |

*However  
sometimes it  
isn't*

What's wrong  
here?

Product 1

| Name     | Category |
|----------|----------|
| Gizmo    | Gadget   |
| OneClick | Camera   |
| Gizmo    | Camera   |

Product 2

| Price | Category |
|-------|----------|
| 19.99 | Gadget   |
| 24.99 | Camera   |
| 19.99 | Camera   |

# Question

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Marks

| <u>Student</u> | <u>Assignment</u> | Group | Mark |
|----------------|-------------------|-------|------|
| Ann            | A1                | G1    | 80   |
| Ann            | A2                | G3    | 60   |
| Bob            | A1                | G2    | 60   |

SGM

| <u>Student</u> | <u>Group</u> | <u>Mark</u> |
|----------------|--------------|-------------|
| Ann            | G1           | 80          |
| Ann            | G3           | 60          |
| Bob            | G2           | 60          |

AM

| <u>Assignment</u> | <u>Mark</u> |
|-------------------|-------------|
| A1                | 80          |
| A2                | 60          |
| A1                | 60          |

Joining two tables SGM and AM  
Produces Spurious tuples or not ?

# Answer

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SGM

| <u>Student</u> | <u>Group</u> | <u>Mark</u> |
|----------------|--------------|-------------|
| Ann            | G1           | 80          |
| Ann            | G3           | 60          |
| Bob            | G2           | 60          |

AM

| <u>Assignment</u> | <u>Mark</u> |
|-------------------|-------------|
| A1                | 80          |
| A2                | 60          |
| A1                | 60          |

Joining on marks

| Student | Assignment | Group | Mark |
|---------|------------|-------|------|
| Ann     | A1         | G1    | 80   |
| Ann     | A2         | G3    | 60   |
| Ann     | A1         | G3    | 60   |
| Bob     | A2         | G2    | 60   |
| Bob     | A1         | G2    | 60   |

ORIGINAL Table

Marks

| <u>Student</u> | <u>Assignment</u> | <u>Group</u> | <u>Mark</u> |
|----------------|-------------------|--------------|-------------|
| Ann            | A1                | G1           | 80          |
| Ann            | A2                | G3           | 60          |
| Bob            | A1                | G2           | 60          |

# What is Join Dependency ?

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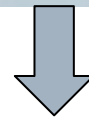
- Join Dependency: Denoted by  $JD(R_1, R_2, \dots, R_n)$  specified on relation schema  $R$  specifies a constraint on the states  $r$  of  $R$ .
  - Every legal state  $r$  of  $R$  should have non additive join decomposition in to  $R$



# Example Join Dependency

| <u>Supp</u> | <u>parts</u> | <u>proj</u> | $R$ |
|-------------|--------------|-------------|-----|
| $S_1$       | $P_1$        | $r_1$       |     |
| $S_1$       | $P_2$        | $r_2$       |     |
| $S_2$       | $P_1$        | $r_1$       |     |
| $S_2$       | $P_1$        | $r_2$       |     |

Supplier  $S_1$  supplies part  $P_1$  to project  $r_1$  and part  $P_2$  to project  $r_2$



Decomposing

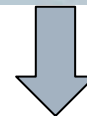
| $R_1$       |              | $R_2$       |             | $R_3$        |             |
|-------------|--------------|-------------|-------------|--------------|-------------|
| <u>Supp</u> | <u>parts</u> | <u>Supp</u> | <u>proj</u> | <u>parts</u> | <u>proj</u> |
| $S_1$       | $P_1$        | $S_1$       | $r_1$       | $P_1$        | $r_1$       |
| $S_1$       | $P_2$        | $S_1$       | $r_2$       | $P_1$        | $r_2$       |
| $S_2$       | $P_1$        | $S_2$       | $r_1$       | $P_2$        | $r_2$       |
|             |              | $S_2$       | $r_2$       |              |             |

# Example Join Dependency

| $R_1$       |              | $R_2$       |             | $R_3$        |             |
|-------------|--------------|-------------|-------------|--------------|-------------|
| <u>supp</u> | <u>parts</u> | <u>supp</u> | <u>proj</u> | <u>parts</u> | <u>proj</u> |
| $S_1$       | $P_1$        | $S_1$       | $r_1$       | $P_1$        | $r_1$       |
| $S_1$       | $P_2$        | $S_1$       | $r_2$       | $P_1$        | $r_2$       |
| $S_2$       | $P_1$        | $S_2$       | $r_1$       | $P_2$        | $r_2$       |
|             |              | $S_2$       | $r_2$       |              |             |

Original Table

| <u>supp</u> | <u>parts</u> | <u>proj</u> | $R$ |
|-------------|--------------|-------------|-----|
| $S_1$       | $P_1$        | $r_1$       |     |
| $S_1$       | $P_2$        | $r_2$       |     |
| $S_2$       | $P_1$        | $r_1$       |     |
| $S_2$       | $P_1$        | $r_2$       |     |



Joining any two  $R_1$  &  $R_3$  tables

| <u>supp</u> | <u>parts</u> | <u>proj</u> |
|-------------|--------------|-------------|
| $S_1$       | $P_1$        | $r_1$       |
| $S_1$       | $P_1$        | $r_2$       |
| $S_1$       | $P_2$        | $r_2$       |

Table after joining

**ADDITIVE JOIN**

Because it  
Generates  
spurious tuples

# Fifth Normal Form

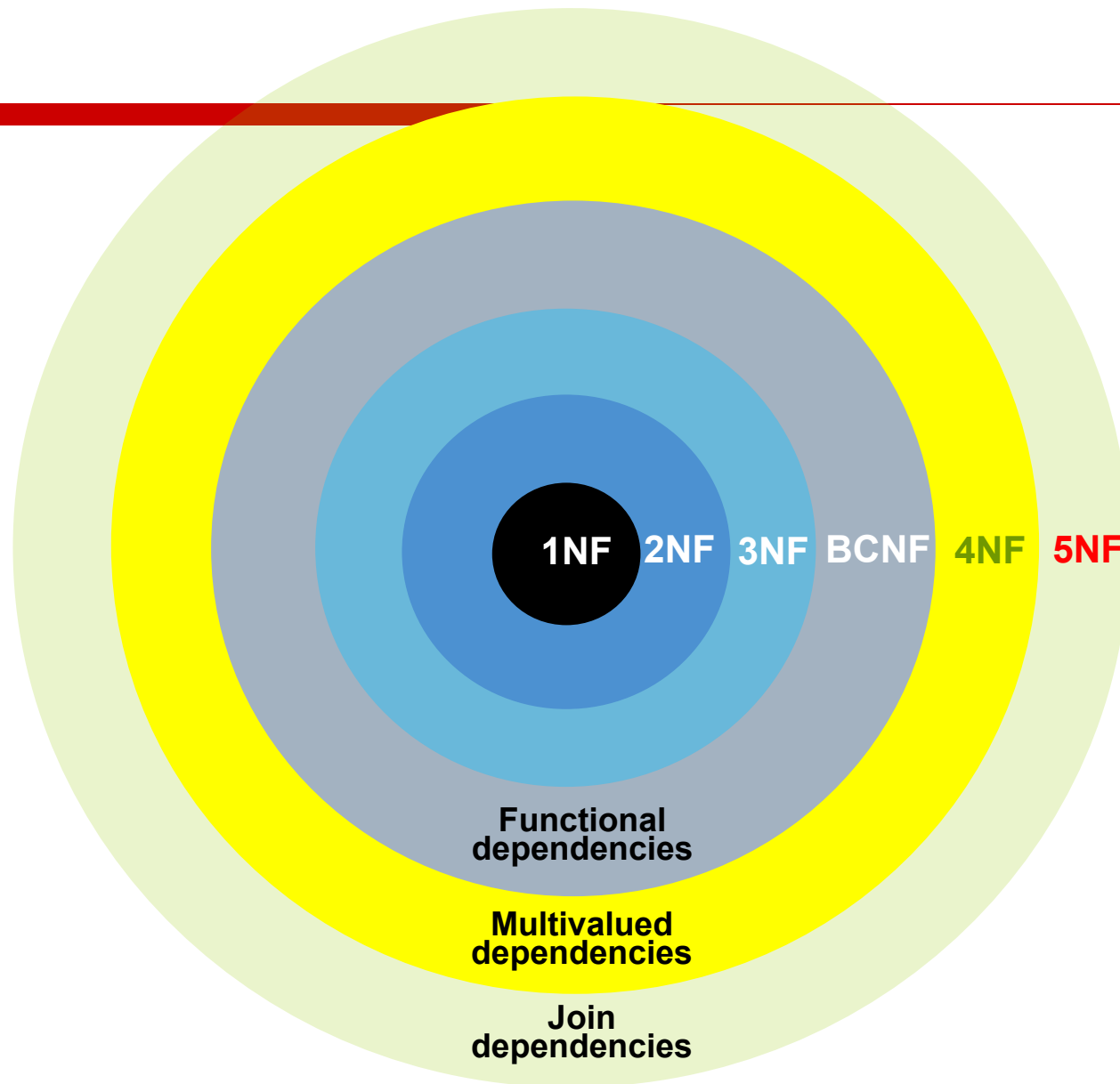
---

- 5NF requires that there are no non-trivial join dependencies that not follow from the key constraints.
- A table is said to be in the 5NF if and only if it is in 4NF and every join dependency in it is implied by the candidate keys.
  
- It should be in fourth normal form
- If Join dependency does not exist then it will be in 5NF
- Else if Join Dependency Exist
  - If Only trivial Join dependency then it is in 5NF
  - Else
    - If (All  $R_i$  is superkey  $R=(R_1,R_2,.....R_n)$  then it is in fifth normal form
    - Else not in 5NF

Trivial JD: When  $R$  is broken into  $R_1,R_2,R_3$  and one of the  $R_i$  is  $R$  it self

# Normal Forms

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# Summarizing 1NF, 2NF, 3 NF,BCNF, 4NF, 5NF

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1NF: Removes  
repeating groups

**1NF** Column values should be atomic

First Restriction

2NF: Removes  
Partial dependencies

**2NF**

Non-Prime attributes should be Fully Dependent on each candidate key

Second Restriction

3NF: Removes  
transitive dependencies

**3NF** Non-Prime attributes should not be Determined by a non-prime attribute

Third Restriction

BCNF: Make Sure every  
Determinant is a candidate  
key

**BCNF**

Determinant should be key

Fourth Restriction

4NF: Removes  
Multivalued dependencies

**4NF**

No more than two multi valued dependency in a single table

Fifth Restriction

5NF: Removes  
join dependencies

**5NF:** A table is said to be in the 5NF if and only if it is in 4NF and every join dependency in it is implied by the candidate keys.

Sixth Restriction

# A brief history of normal forms:

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- ❑ First, Second, Third Normal Forms (1NF, 2NF, 3NF) (Codd 1972)
- ❑ Boyce-Codd Normal Form (BCNF) (1974)
- ❑ Fourth Normal Form (4NF) (Zaniolo 1976, Fagin 1977)
- ❑ Fifth Normal Form (5NF) (Fagin 1979)
  
- ❑ NF hierarchy:  $5NF \Rightarrow 4NF \Rightarrow BCNF \Rightarrow 3NF \Rightarrow 2NF \Rightarrow 1NF$
  
- ❑ 1NF allows most redundancy; 5NF allows least redundancy.

# Normal Forms – Basic Rules and Solutions

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## First Normal Form (1NF)

- A relation schema R is in 1NF if and only if,
- All the attributes of the relation are atomic (indivisible into meaningful sub parts),
- Every attribute contains single value (per record).

How to convert un-normalized table into 1NF normalized table?

- Expand the table by duplicating records for every value of multi-valued attributes (Flatten the table).

# Normal Forms – Basic Rules and Solutions

---

## Second Normal Form (2NF)

A relation schema R is in 2NF if and only if,

- At the first place the table is in 1NF,
- All the non-key attributes of the table are fully functionally dependent on the Primary key of the table.

How to convert un-normalized or 1NF table into 2NF normalized table?

- It can be done using decomposition. That is, by breaking Non-2NF relations into smaller tables using the Functional Dependencies derived.



# Normal Forms – Basic Rules and Solutions

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## Third Normal Form (3NF)

A relation schema R is in 3NF if and only if,

- The table is in 2NF,
- There is no Functional Dependency such that both Left Hand Side and Right Hand Side attributes of the FD are non-key attributes. In other words, no transitive dependency is allowed.

How to convert un-normalized or 2NF table into 3NF normalized table?

- It can be done using decomposition. That is, by breaking Non-3NF relations into smaller tables using the Functional Dependencies derived. Especially, by creating a separate table for non-key attributes dependencies.

# Normal Forms – Basic Rules and Solutions

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## **Boyce-Codd Normal Form (BCNF)**

A relation schema R is in BCNF if and only if,  
The table is in 3NF

- For all the non-trivial FDs held on R, the left hand side of those non-trivial FDs must be Super Keys.

# Thanks for Listening

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