

Exercise 1. Answer Sheet

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Problem 1. (30 points) For each function $f(n)$ and time T in the following table, determine the largest size n of a problem that can be solved in time T , assuming that the algorithm to solve the problem takes $f(n)$ milliseconds.

$f(n)$	$T = 1$ second	$T = 1$ minute	$T = 1$ hour	$T = 1$ day	$T = 1$ month (30 days)
\sqrt{n}	10^{12}	$36 \cdot 10^{14}$	$1296 \cdot 10^{16}$	$746496 \cdot 10^{18}$	$6718464 \cdot 10^{18}$
n	10^6	$6 \cdot 10^7$	$36 \cdot 10^8$	$864 \cdot 10^8$	$2592 \cdot 10^9$
n^2	1000	7745	60000	293938	1609968
n^3	100	391	1532	4420	13736
2^n	19	25	31	36	41

Problem 2. (30 points) Consider sorting n numbers stored in array A by first finding the smallest element of A and exchanging it with the first element of the array, i.e. $A[1]$. Then find the second smallest element of A , and exchange it with $A[2]$. Continue in this manner for the first $n-1$ elements of A .

a) Write a pseudo-code for this algorithm which is known as “**Selection Sort**”.

```
SELECTION-SORT(A):  
  for i=1 to A.length-1  
    min=i  
    for j=i+1 to A.length  
      if A[j] < A[min]  
        min = j  
    temp = A[i]  
    A[i] = A[min]  
    A[min] = temp
```

b) What is the time complexity of the Selection Sort algorithm?

$$\begin{aligned} & c_1(n) + c_2(n-1) + c_3(n(n+1)/2) + c_4(n-1) + c_5(n-1) + c_6(n-1) \\ &= c_3/2 * n^2 + (c_1 + c_2 + c_3/2 + c_4 + c_5 + c_6)*n + (c_2 - c_4 - c_6) \\ &= a*n^2 + b*n + c \end{aligned}$$

Hence, Answer is $O(n^2)$

Problem 3. (40 points) Using the pseudo-code for **Merge Sort** algorithm given at the lecture, write a program implementing the **Merge Sort** algorithm. Use any programming language you know. Upload your source code with instructions how to compile/run it. Give the input data and the program output in the space below.

```
public class MergeSort {

    public static void mergeSort(int[] list) {
        if (list.length > 1) {
            int[] firstHalf = new int[list.length / 2];
            System.arraycopy(list, 0, firstHalf, 0, list.length / 2);
            mergeSort(firstHalf);

            int secondHalfLength = list.length - list.length / 2;
            int[] secondHalf = new int[secondHalfLength];
            System.arraycopy(list, list.length / 2,
                secondHalf, 0, secondHalfLength);
            mergeSort(secondHalf);

            int[] temp = merge(firstHalf, secondHalf);
            System.arraycopy(temp, 0, list, 0, temp.length);
        }
    }

    private static int[] merge(int[] list1, int[] list2) {

        int current1 = 0;
        int current2 = 0;
        int current3 = 0;

        while (current1 < list1.length && current2 < list2.length) {

            if (list1[current1] < list2[current2])
                temp[current3++] = list1[current1++];
            else
                temp[current3++] = list2[current2++];
        }
        while (current1 < list1.length)
            temp[current3++] = list1[current1++];
        while (current2 < list2.length)
            temp[current3++] = list2[current2++];

        return temp;
    }

    public static void main(String[] args) {
        int[] list = {5,4,7,28,3,27,327,54,1000};
        mergeSort(list);
        for (int i = 0; i < list.length; i++)
            System.out.print(list[i] + " ");
    }
}
```