

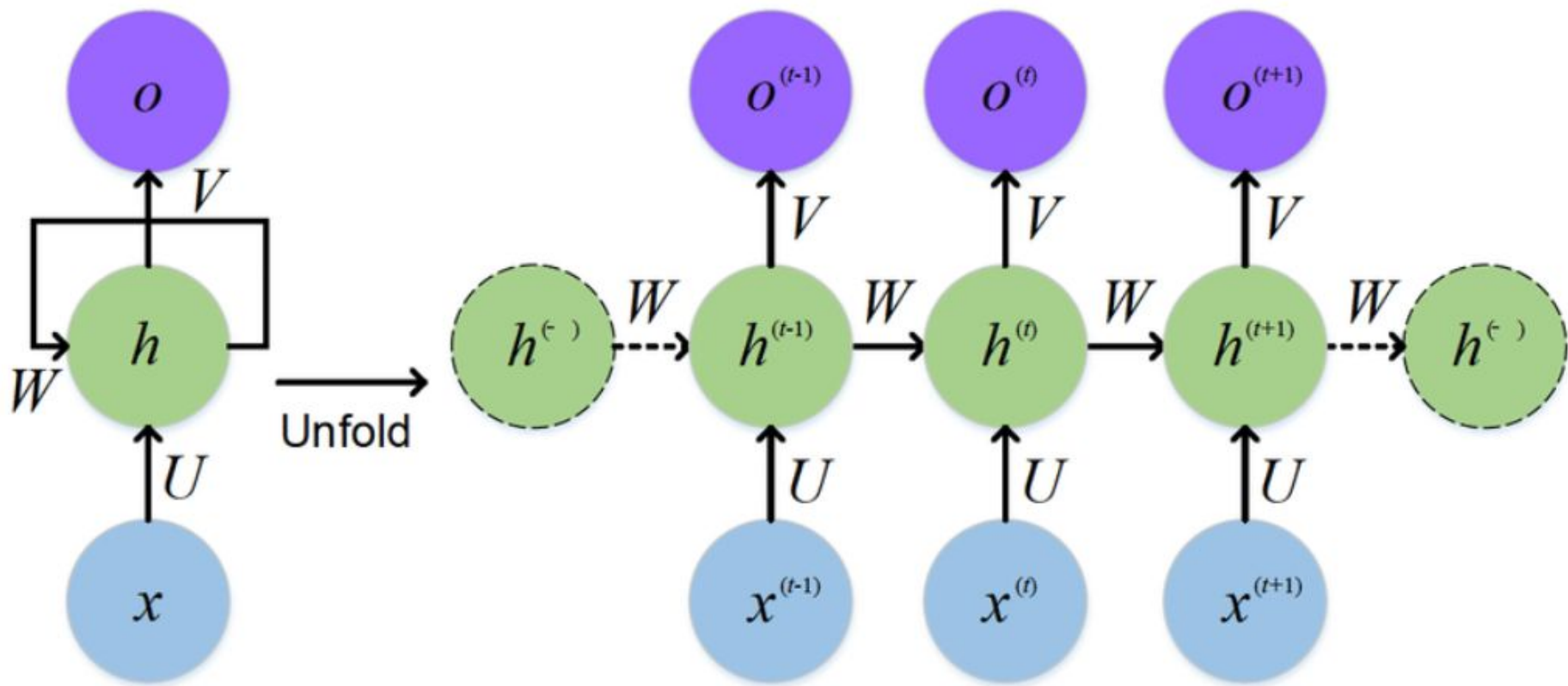
Transformers

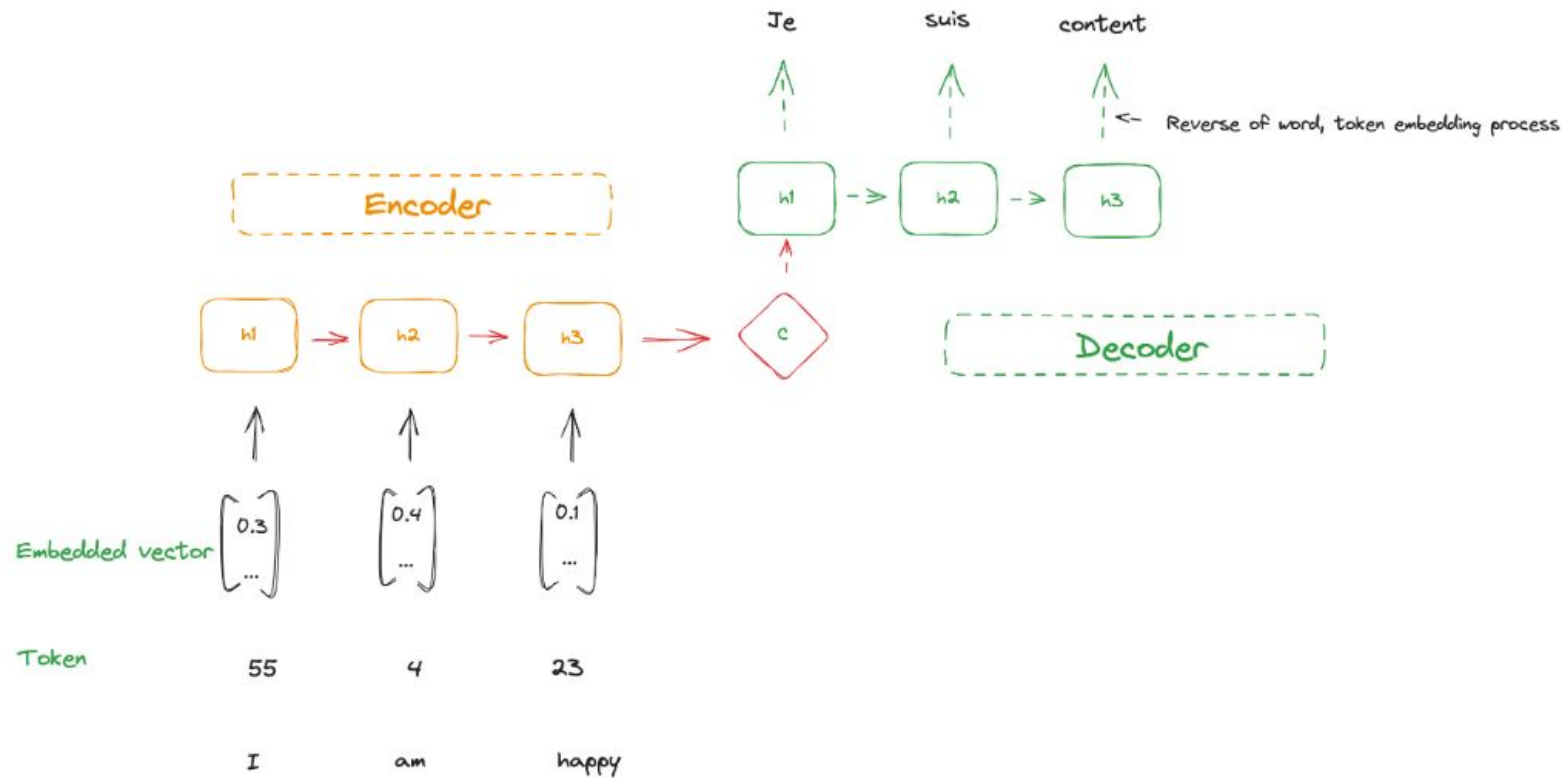
1 Why should you care about Transformers?



ChatGPT

2 RNNs: Problems and progress

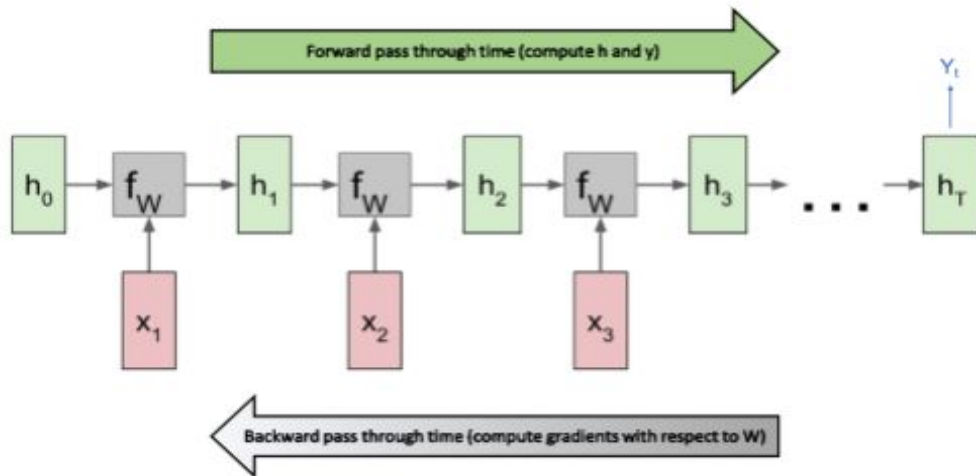




What are the key issues we face here?

1. Information bottleneck at interface
2. Vanishing gradient problem
3. We have to compute the entire sequence recursively (makes scaling very hard!)

RNNs suffer from vanishing gradient through time



What does this mean for our performance?

A simplification of problems with RNNs:

*Sally adored reading; when she received a book on her birthday
she was **older***

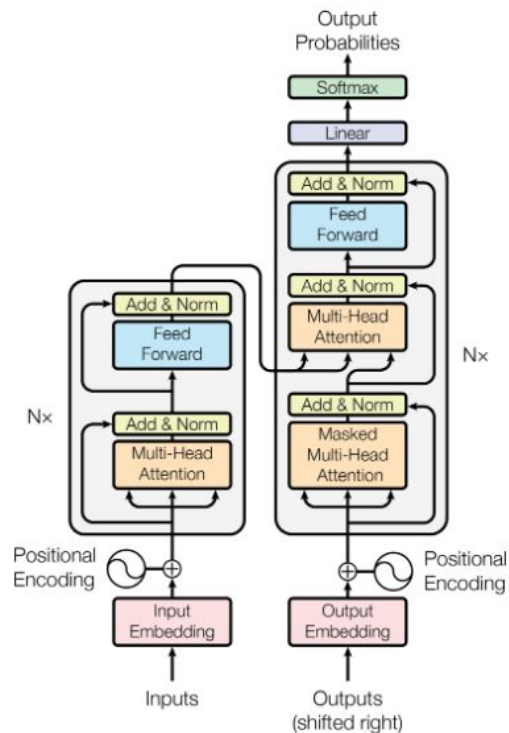
What we'd like:

*Sally adored reading; when she received a book on her birthday
she was **happy!***

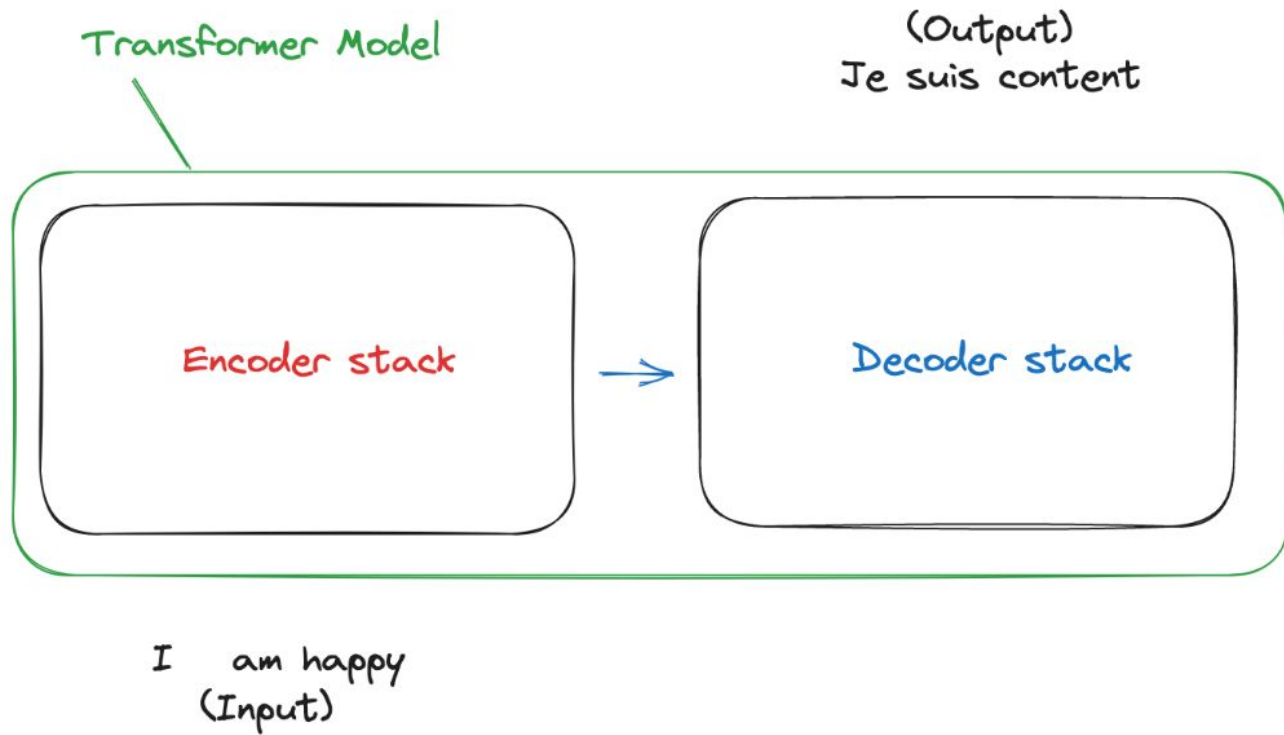
RNNs are likely to miss out on **important context** from earlier in the sentence because of their recency bias 🤖

3 Transformers

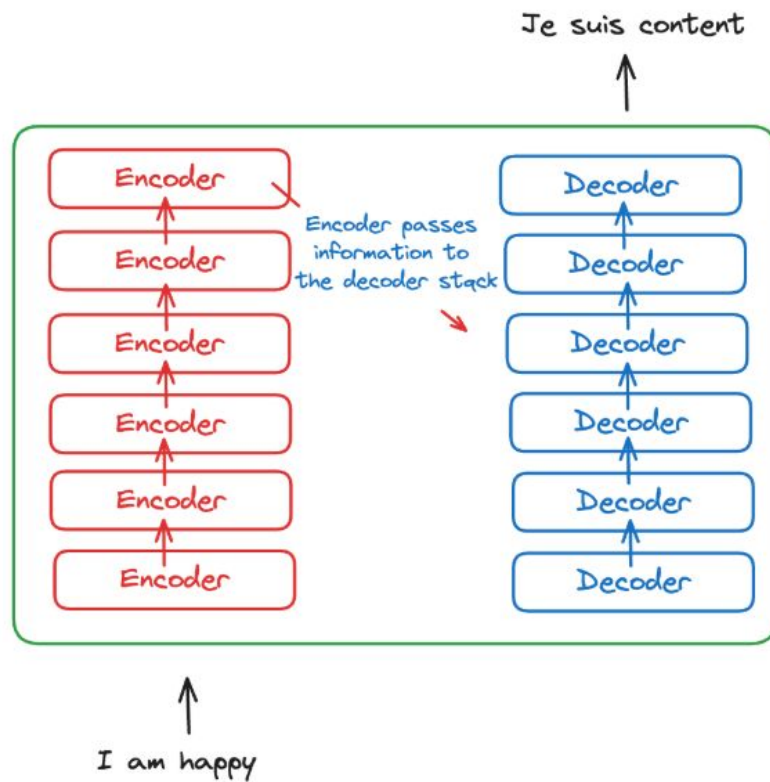
The paper that started it all: [Attention is All You Need](#)



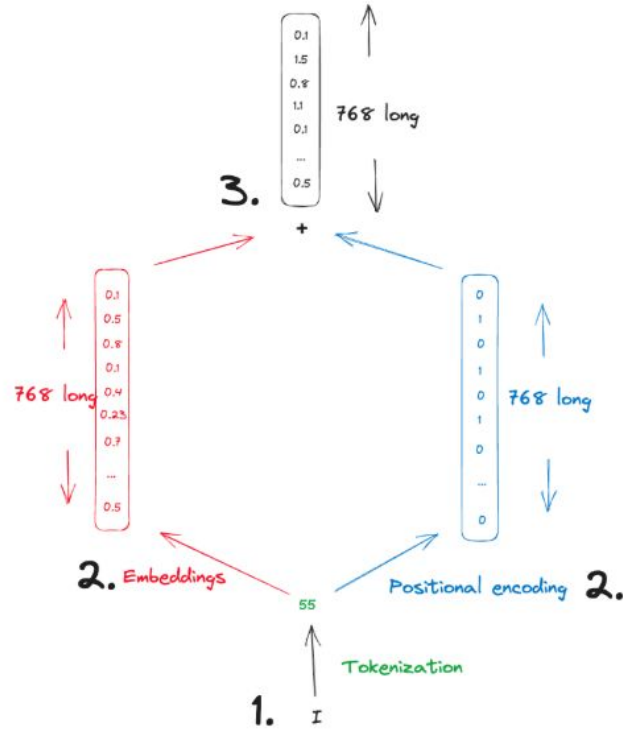
The highest level view:



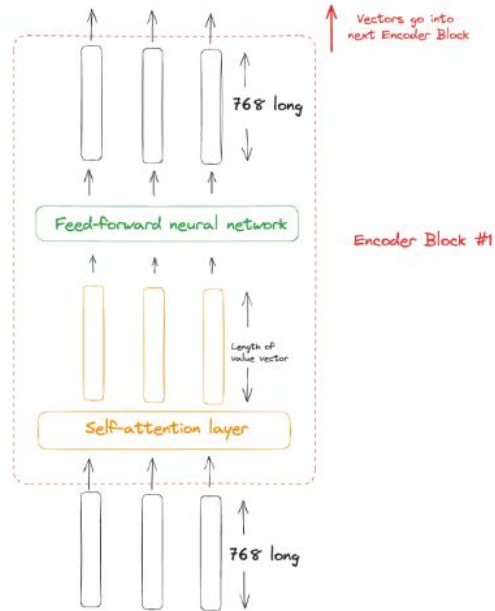
Broken down a bit more:



Before we talk about what's going on inside the encoder layers, let's talk about what's going into it!



Zooming in on one of the encoders:



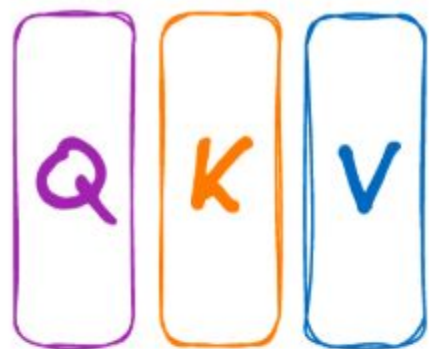
- Usually the **embedding size** is 768
- The **hidden dimension** (the length of the projected Q, K and V vectors) is also 768
- In the example we'll use size 2 for simplicity

? What's going on in this strange self-attention layer?

- 1) Each token (word) embedding gets **projected** → into 3 further vectors: the **query, key and value vectors**
- 2) We compute a **scaled dot-product** ● on the query and key vectors to work out how much each word relates to those around it
- 3) Take these scores and **normalize with softmax** ↴
- 4) **Multiply by our value vectors** ⊗, sum and pass to our dense neural network.

An example sentence

Sally adored reading; when she received a book for her birthday she was...



Sally



adored



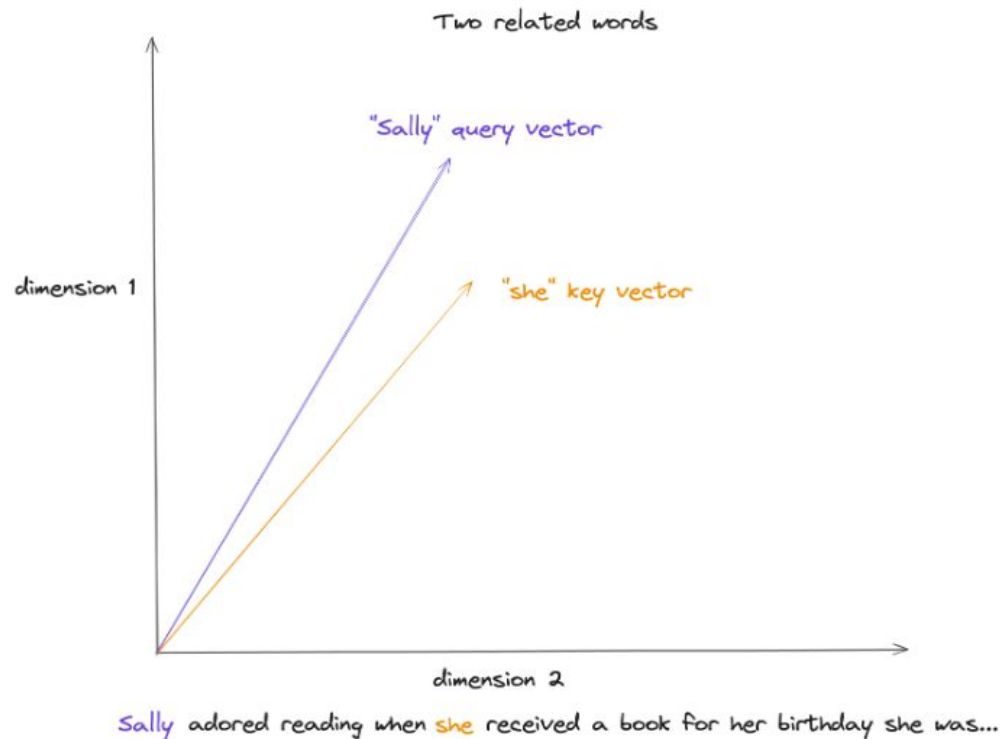
reading

...

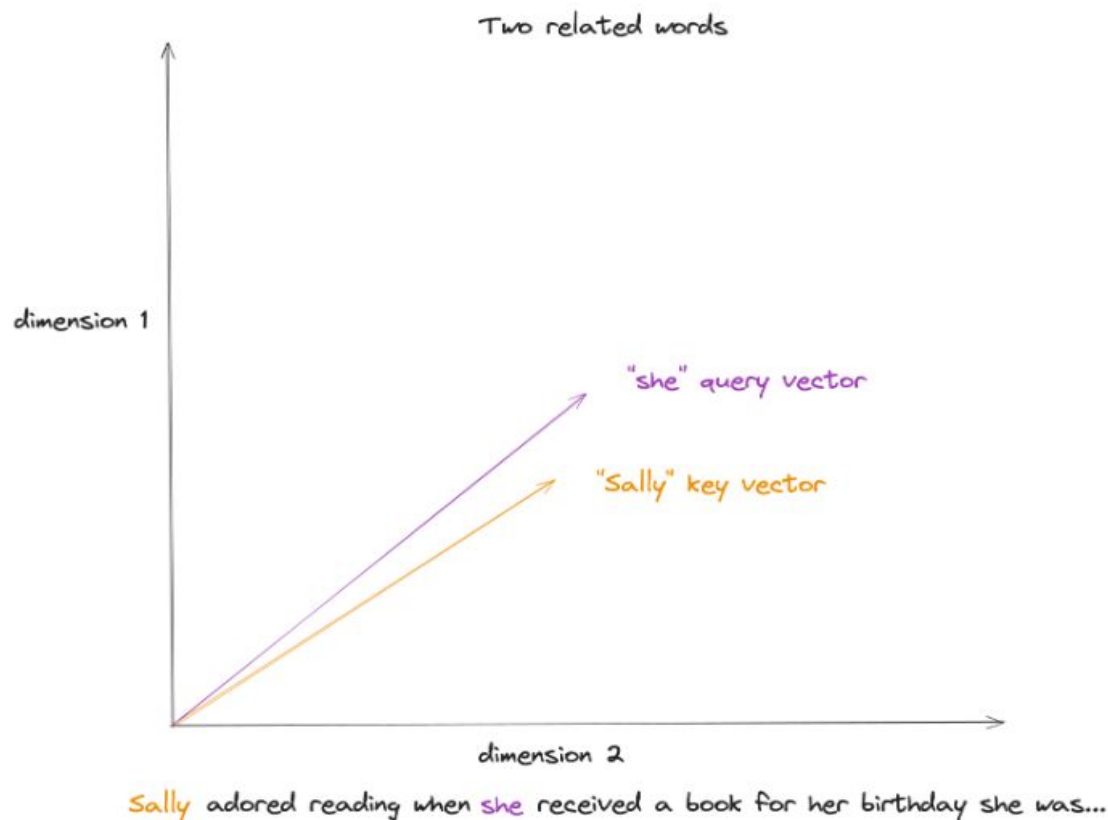
...

Three zoomed-in examples:

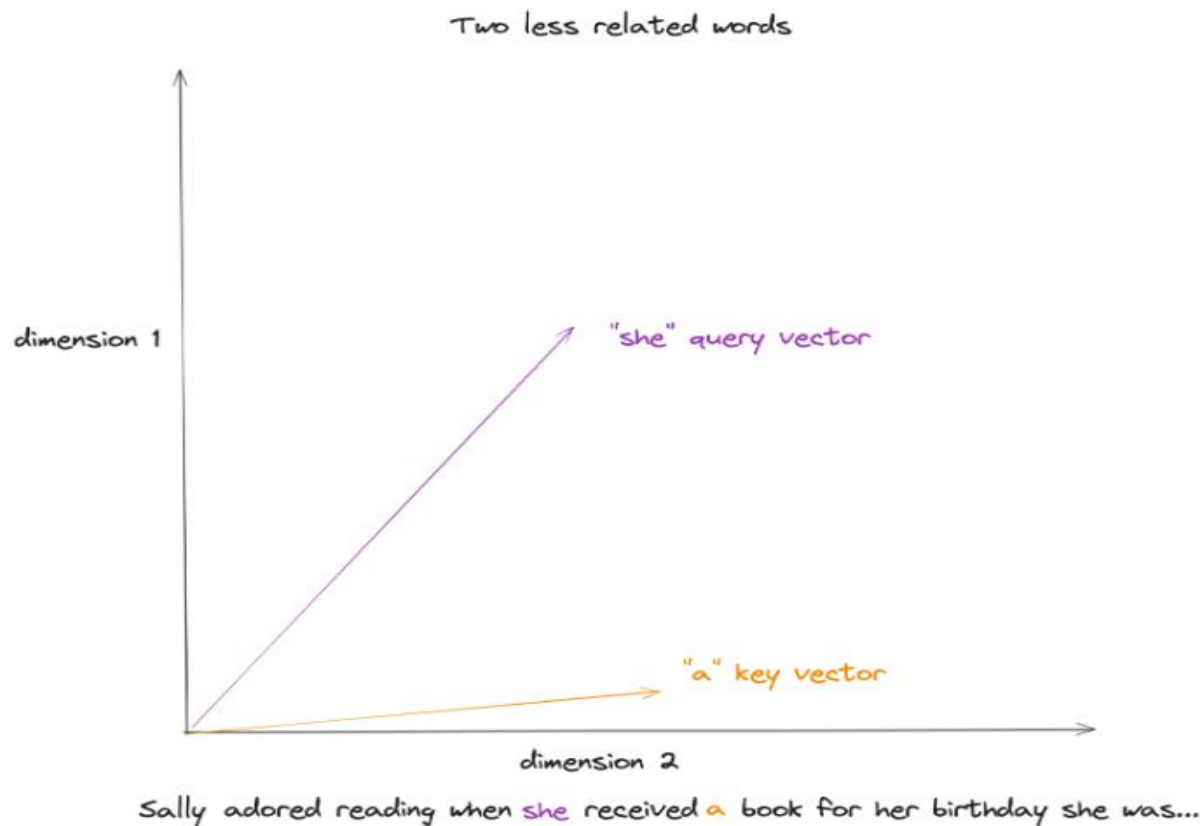
Two words in a sentence that are closely related



The same two words but seen from the other perspective:



Finally, two words with a weak connection:



Let's look at one dot product

To keep it really simple, we're going to imagine our Q, K and V have only been projected into two dimensions

"Sally" Query vector $\begin{bmatrix} 7 & 7 \end{bmatrix} \cdot \begin{matrix} \text{"she"} \\ \text{Key vector} \\ \text{(transposed)} \\ \begin{bmatrix} 10 \\ 5 \end{bmatrix} \end{matrix} = 105$

What happens once we have our dot products?

Dot-product between vectors

| | | | | | |
|--------------------|--------------------|---------------------|----------------------|-------------------|------------------|
| | Sally _K | adored _K | reading _K | when _K | she _K |
| Sally _Q | 112 | 75 | 60 | 12 | 105 |

Then we scale:

Scaled dot-product between vectors

We divide by $\sqrt{\text{hidden_dimension}}$ of embedding

In our case the root of 2 ≈ 1.4

| | | | | | |
|--------------------|--------------------|---------------------|----------------------|-------------------|------------------|
| | Sally _K | adored _K | reading _K | when _K | she _K |
| Sally _Q | 80 | 53 | 43 | 8.5 | 75 |

Finally we apply softmax:

Apply softmax

$$\sigma(\vec{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}}$$

| | Sally _K | adored _K | reading _K | when _K | she _K |
|--------------------|--------------------|---------------------|----------------------|-------------------|------------------|
| Sally _Q | 0.48 | 0.08 | 0.03 | 0.01 | 0.32 |

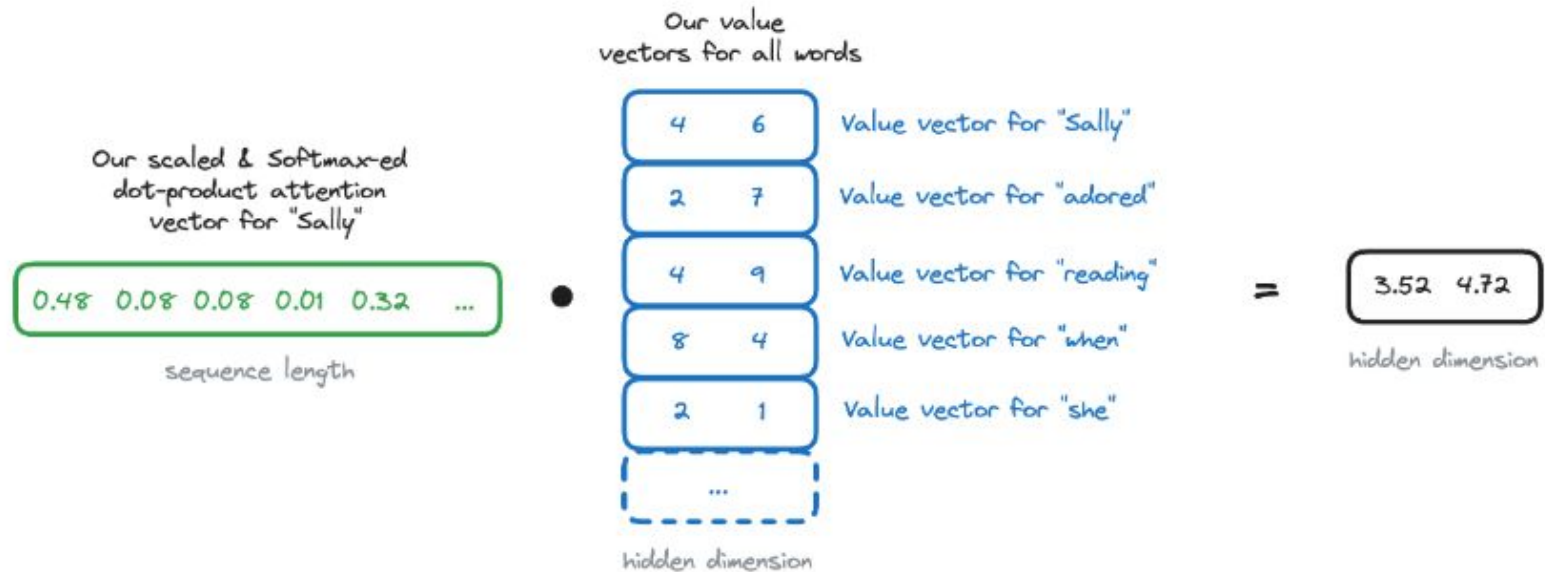
We have to do this for each word in our sentence

You can see how this becomes a matrix operation 🧐

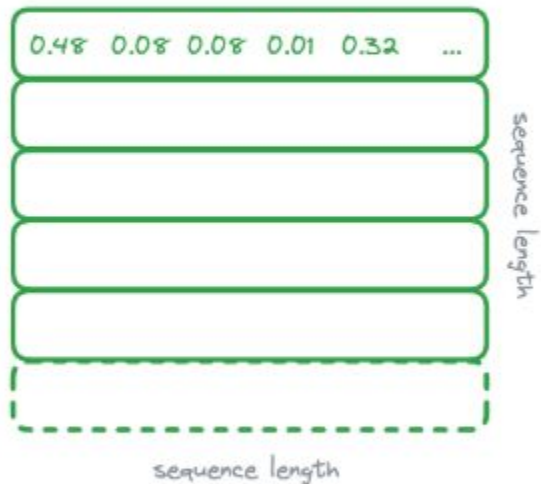
We get the scaled dot-product attention for all of our Query and Key vectors:

| | Sally _K | adored _K | reading _K | when _K | she _K | ... |
|----------------------|--------------------|---------------------|----------------------|-------------------|------------------|-----|
| Sally _Q | 0.48 | 0.08 | 0.03 | 0.01 | 0.32 | ... |
| adored _Q | 0.04 | 0.03 | 0.52 | 0.3 | 0.01 | ... |
| reading _Q | 0.01 | 0.02 | 0.13 | 0.86 | 0.01 | ... |
| when _Q | 0.01 | 0.03 | 0.02 | 0.58 | 0.01 | ... |
| she _Q | 0.13 | 0.12 | 0.02 | 0.01 | 0.04 | ... |
| ... | ... | ... | ... | ... | ... | ... |

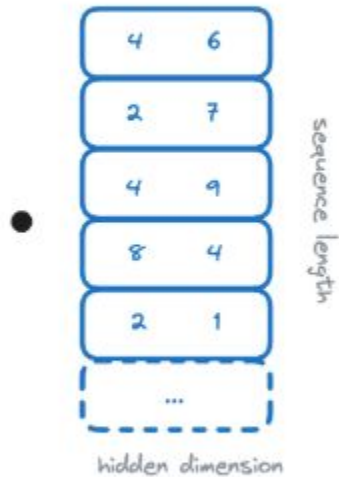
And then multiply our "similarity score" with all of our Value vectors



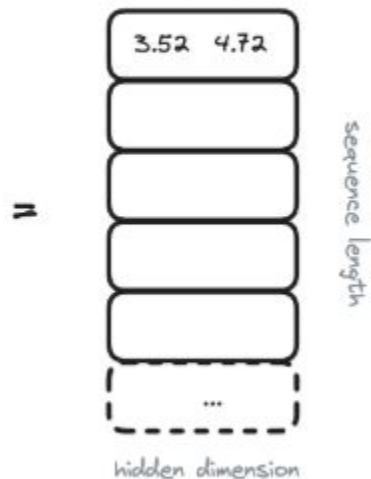
Our scaled & Softmax-ed
dot-product attention
vector for all words



Our value
vectors for all words



Our final matrix
that then goes into our
feed-forward network



So really the entire thing can be written like this:

$$\text{softmax}\left(\frac{\overset{\text{Q}}{\begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array}} \times \overset{\text{K}^T}{\begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \square \\ \hline \end{array}}}{\sqrt{d_k}}\right) \overset{\text{V}}{\begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array}}$$
$$= \overset{\text{Z}}{\begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array}}$$

We are done with our multiplications

Now we just need to normalize and pass through to the feed-forward neural network

The neural network will output vectors of our original embedding dimension (e.g. 768)

🦉 Computing one set of all of these Q, K, V multiplications and processes is what we call "single-headed attention".

When we are doing our initial linear projections (used to create the Q, K and V vectors) we can express these operations as matrices of weights too!

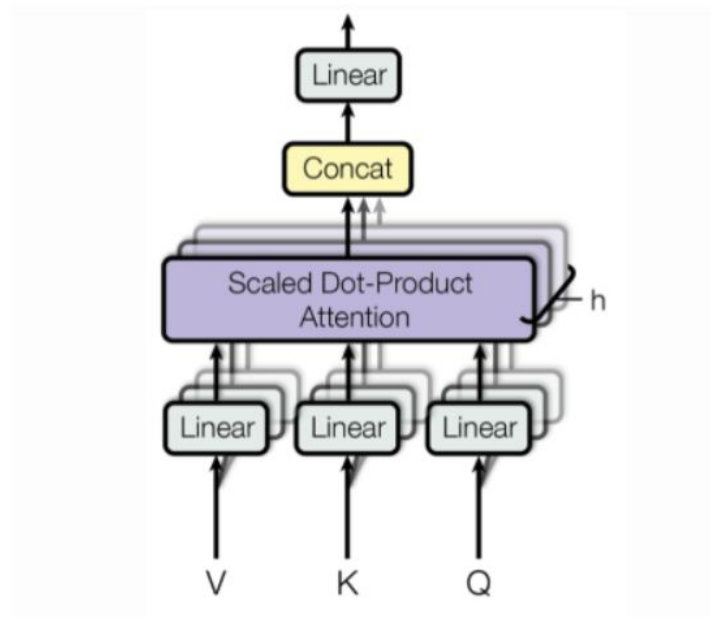
$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|c|c|} \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \end{array} \end{matrix} \times \begin{matrix} W^Q \\ \begin{array}{|c|c|c|c|} \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \end{array} \end{matrix} = \begin{matrix} Q \\ \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \end{array} \end{matrix}$$

$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|c|c|} \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \end{array} \end{matrix} \times \begin{matrix} W^K \\ \begin{array}{|c|c|c|c|} \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \end{array} \end{matrix} = \begin{matrix} K \\ \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \end{array} \end{matrix}$$

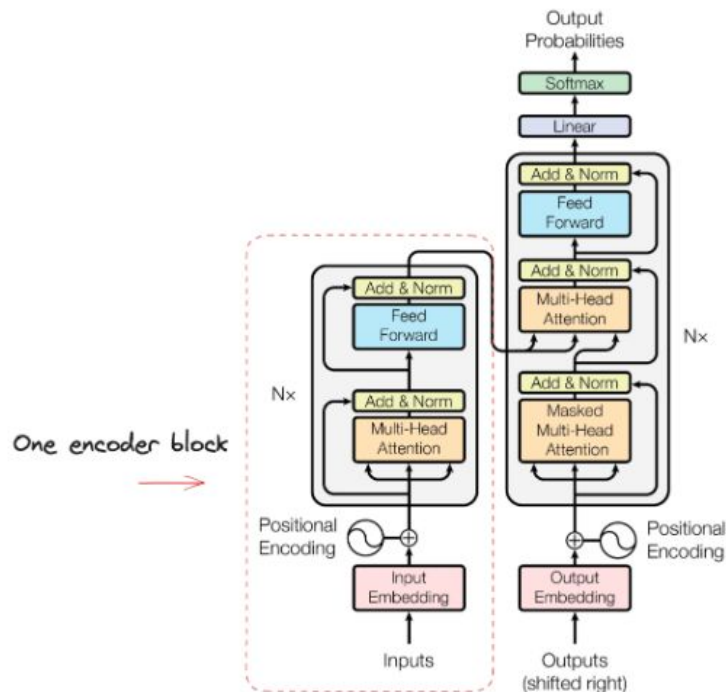
$$\begin{matrix} \text{X} \\ \begin{array}{|c|c|c|c|} \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \end{array} \end{matrix} \times \begin{matrix} W^V \\ \begin{array}{|c|c|c|c|} \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \square & \square & \square & \square \\ \hline \end{array} \end{matrix} = \begin{matrix} V \\ \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \end{array} \end{matrix}$$

Multi-headed?

- We can use multiple heads to split up and analyze different parts of our embedding
- Each can focus a different part of the embedding eg. working on semantic vs syntactic features of our sentences 🧐 🧐 🧐



Let's check in with our original diagram:



What about the decoder?

At the highest level view, its job is to choose the **most likely next token**:

Ex 1.



Ex 2.

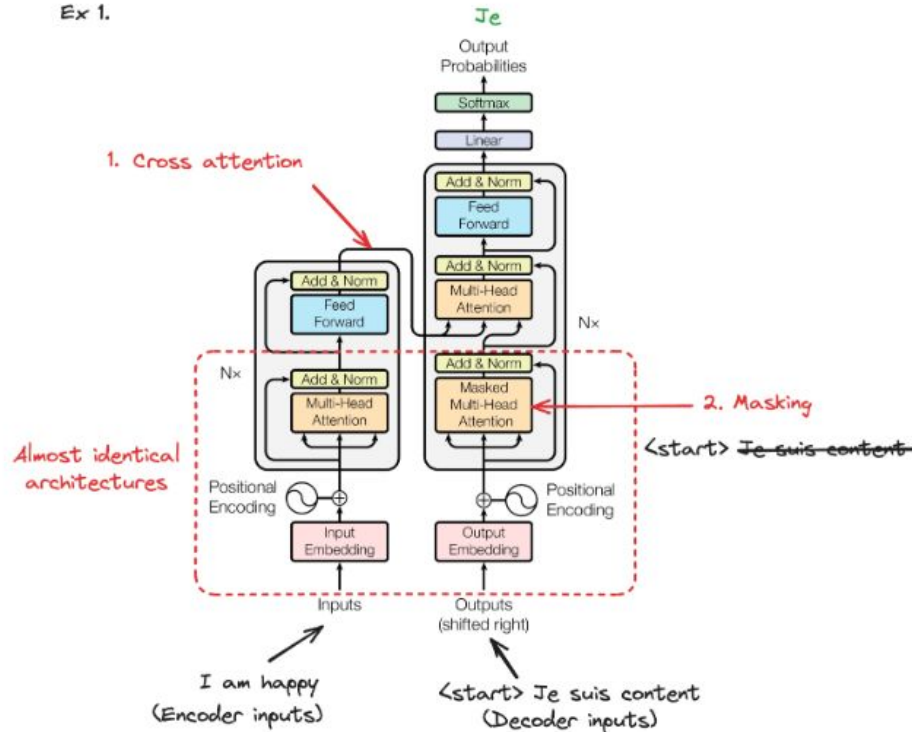


Ex 3.

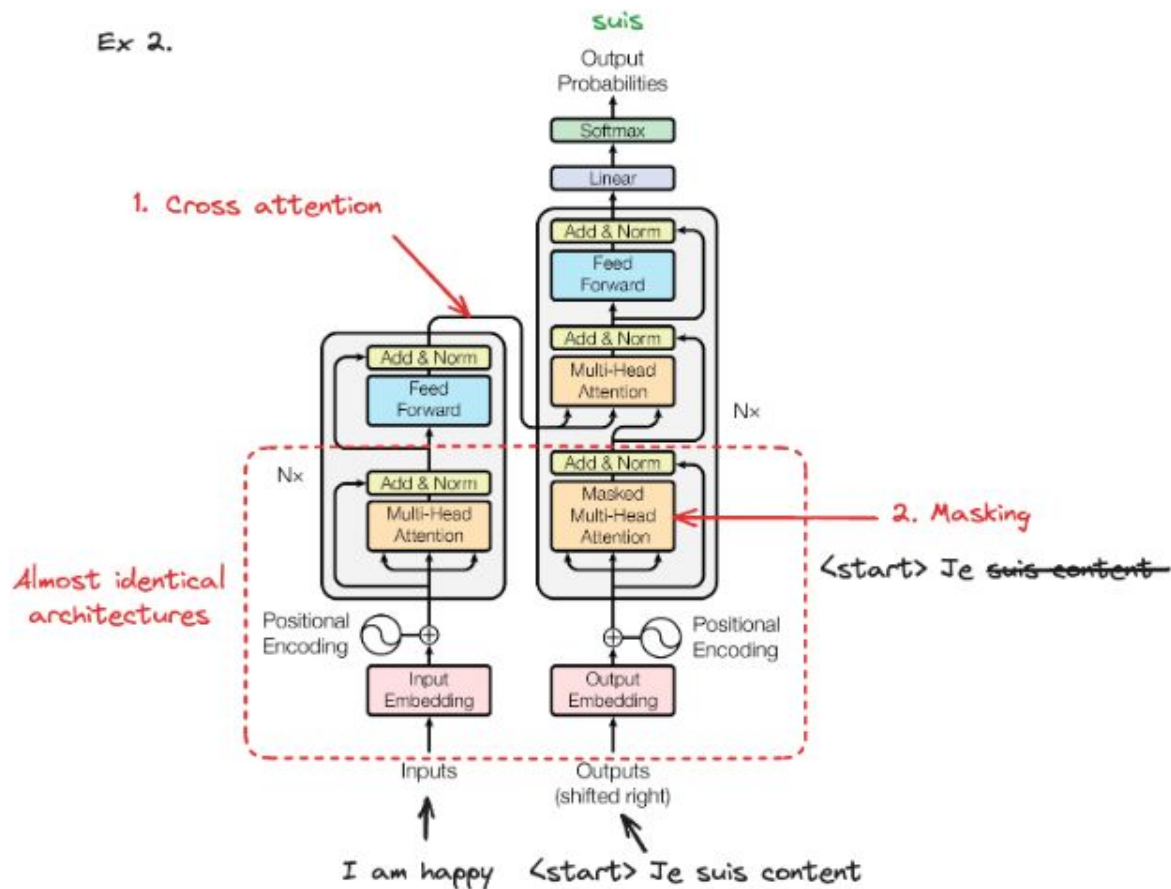


How does it do this? And what happened to all the work the encoder did?

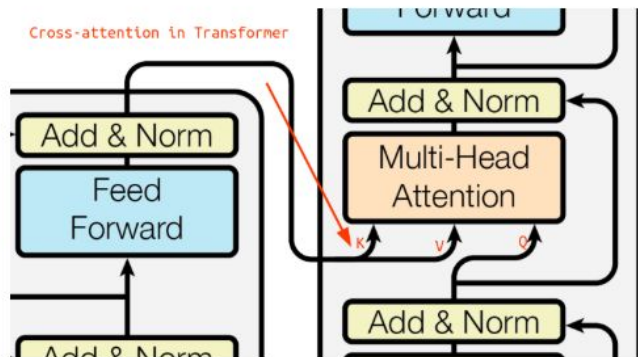
Ex 1.



Ex 2.



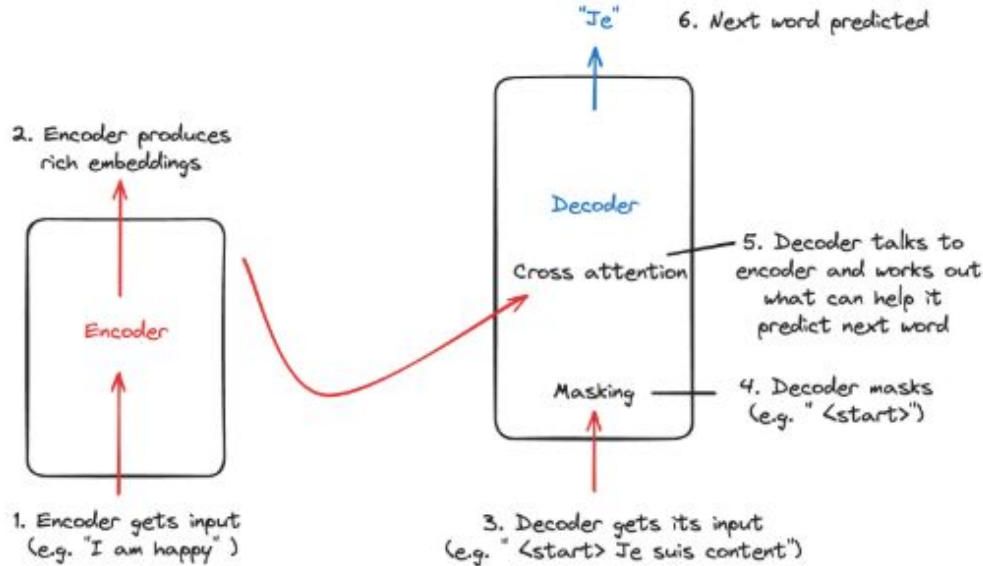
Cross attention



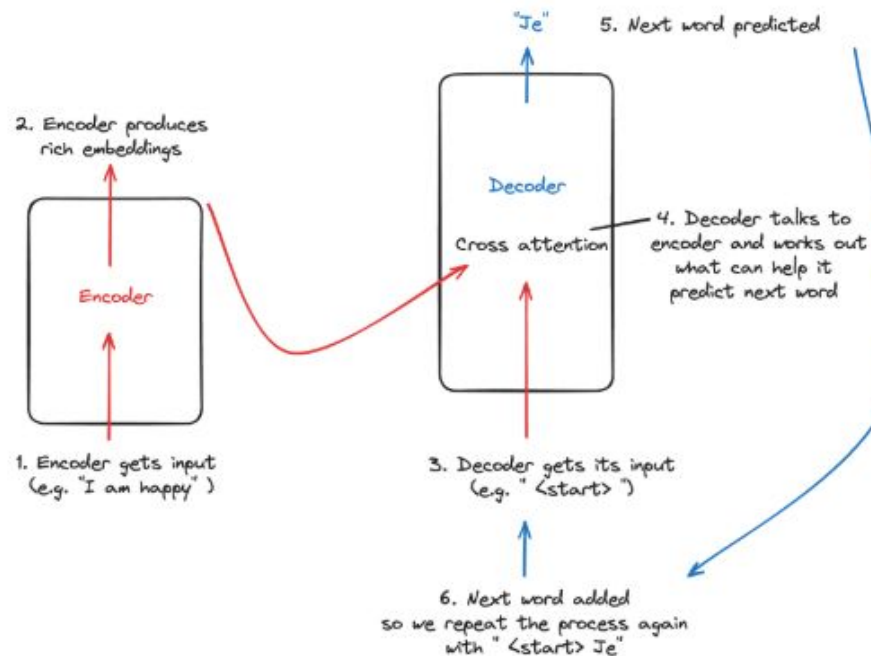
Attention between encoder and decoder (a.k.a. cross-attention):

- **Self-attention** operates within a single sequence and captures the relationships between tokens within that sequence.
- **Cross-attention** operates between two different sequences and captures the relationships between tokens from the source sequence and tokens from the target sequence, allowing the model to generate relevant output based on the information in the source sequence.

Let's recap the training process at a high level



So what does inference look like?



That's all there is to it!

