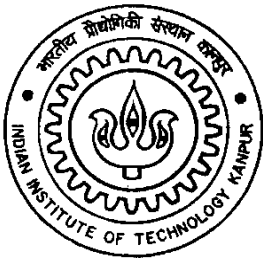


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# Sensors and Actuators

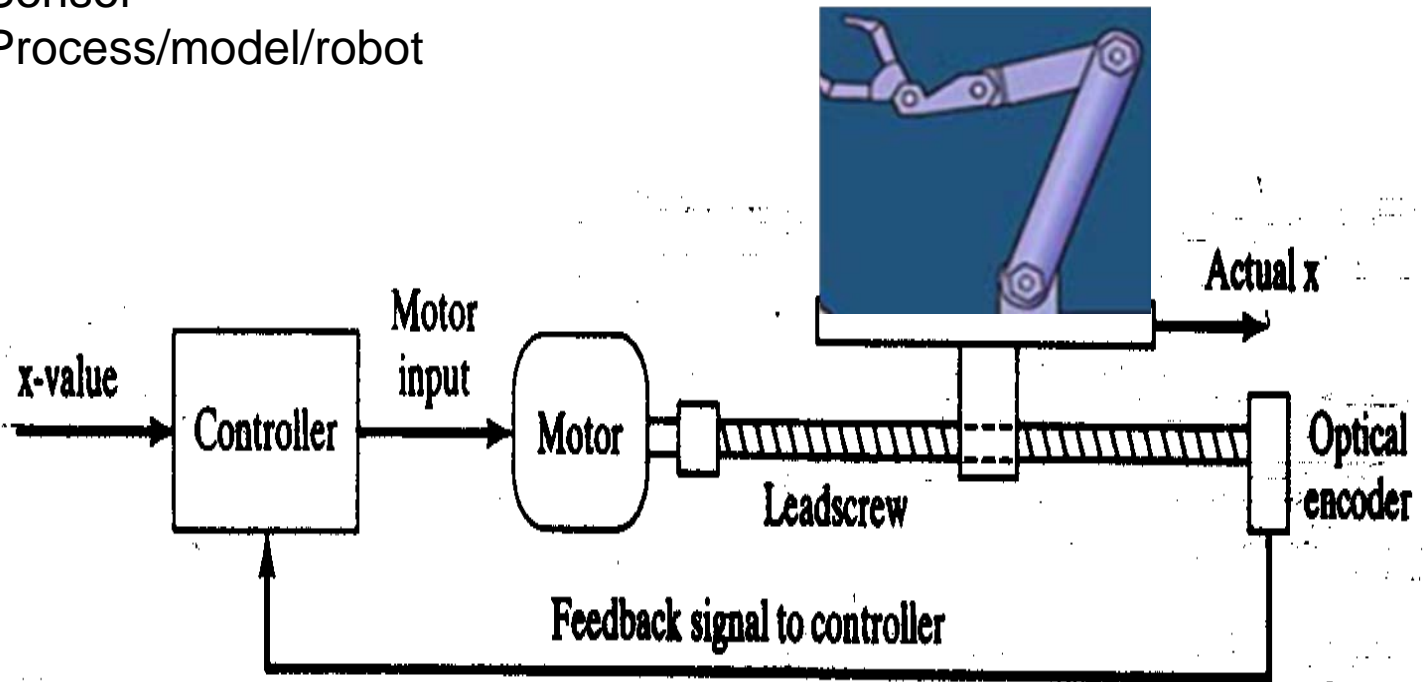
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**Dr. Ashish Dutta**  
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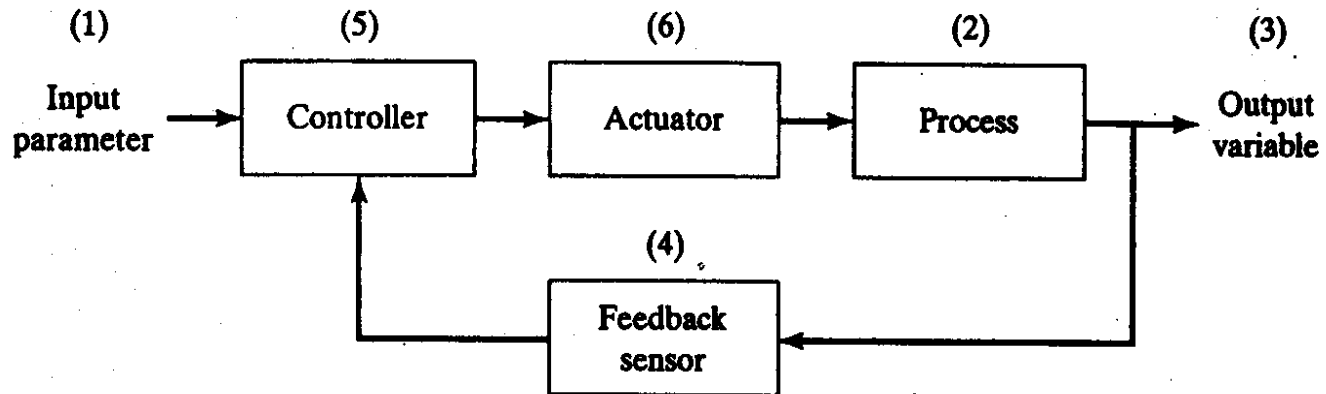
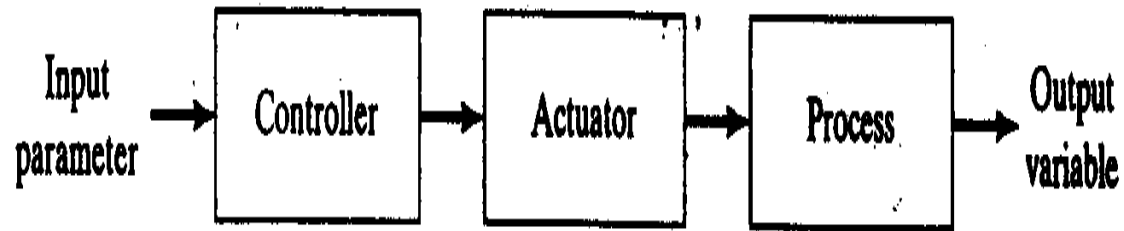
# Sub-systems in robot control

- Controller
- Actuator
- Sensor
- Process/model/robot



SIZE EFFECT ?

# Open loop and closed loop



# Basic elements

- Sensors
- Actuators
- Controllers
- System model

---

# General Classification of Sensors

- **Internal sensors:** required for basic working of the system (e.g. position, velocity, ).
- **External sensors:** interaction with the environment (vision, force, ...).

---

# **Sensors used for closed loop position control: Internal sensors**

- **Position**
- **Velocity**
- **Acceleration**

**e.g. potentiometers, encoders, LVDT,  
Tachometers, Accelerometers**

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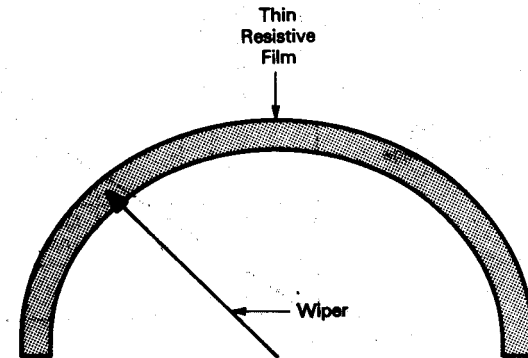
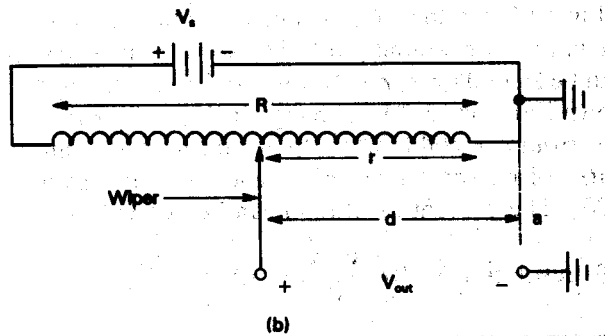
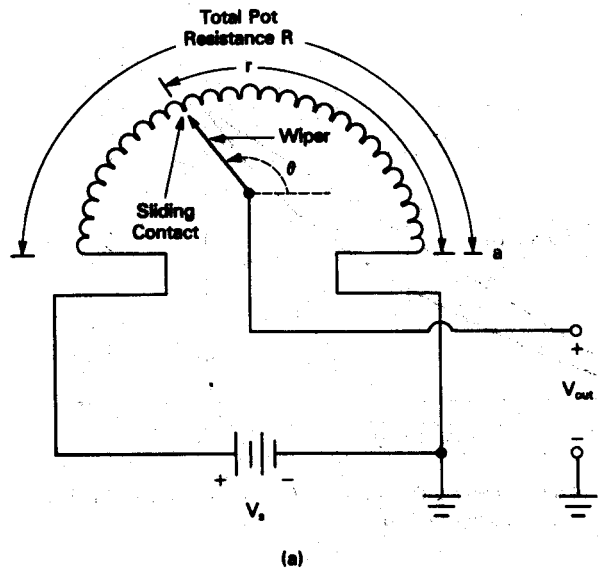
# Sensors for interaction with the environment: External sensors

- Touch
- Force
- Pressure
- Slip
- Proximity
- Vision

e.g. on/off switches, ultrasonic, force sensor, hall effect, inductive sensor, piezo sensor

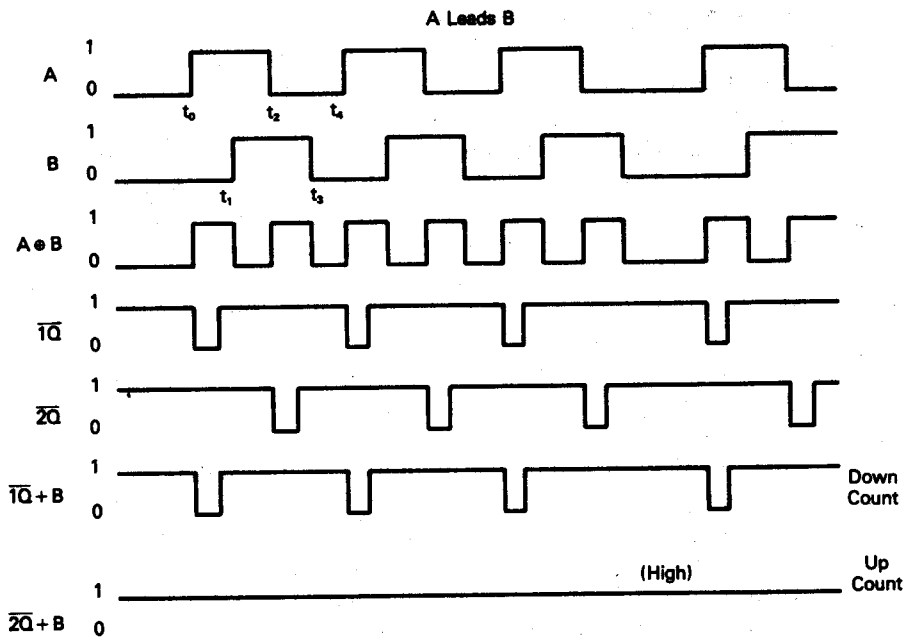
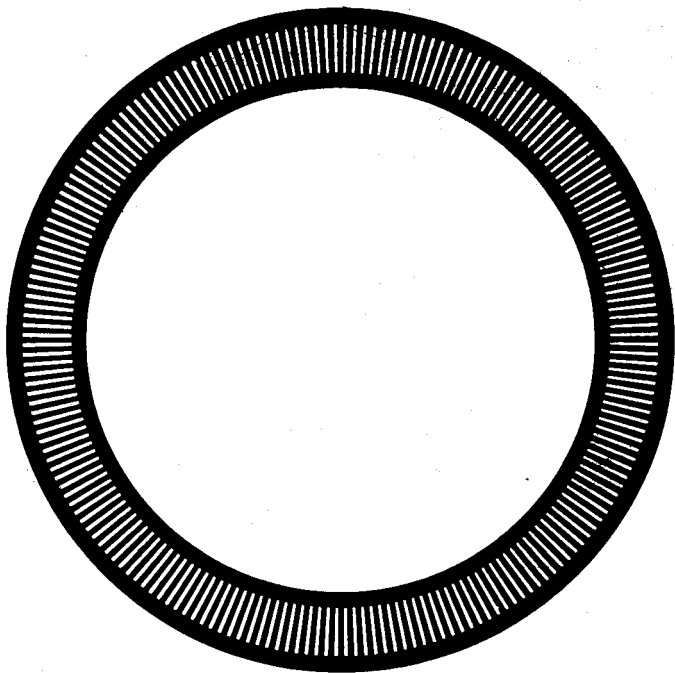
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# Position Sensor : Potentiometer





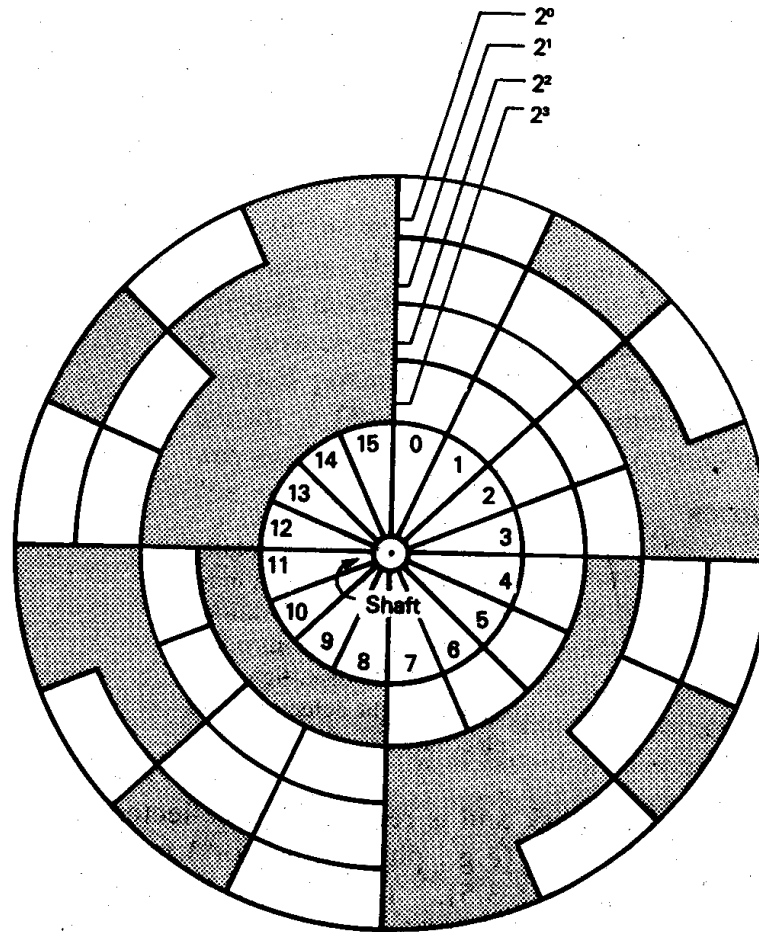
# Position sensor: Incremental Encoder



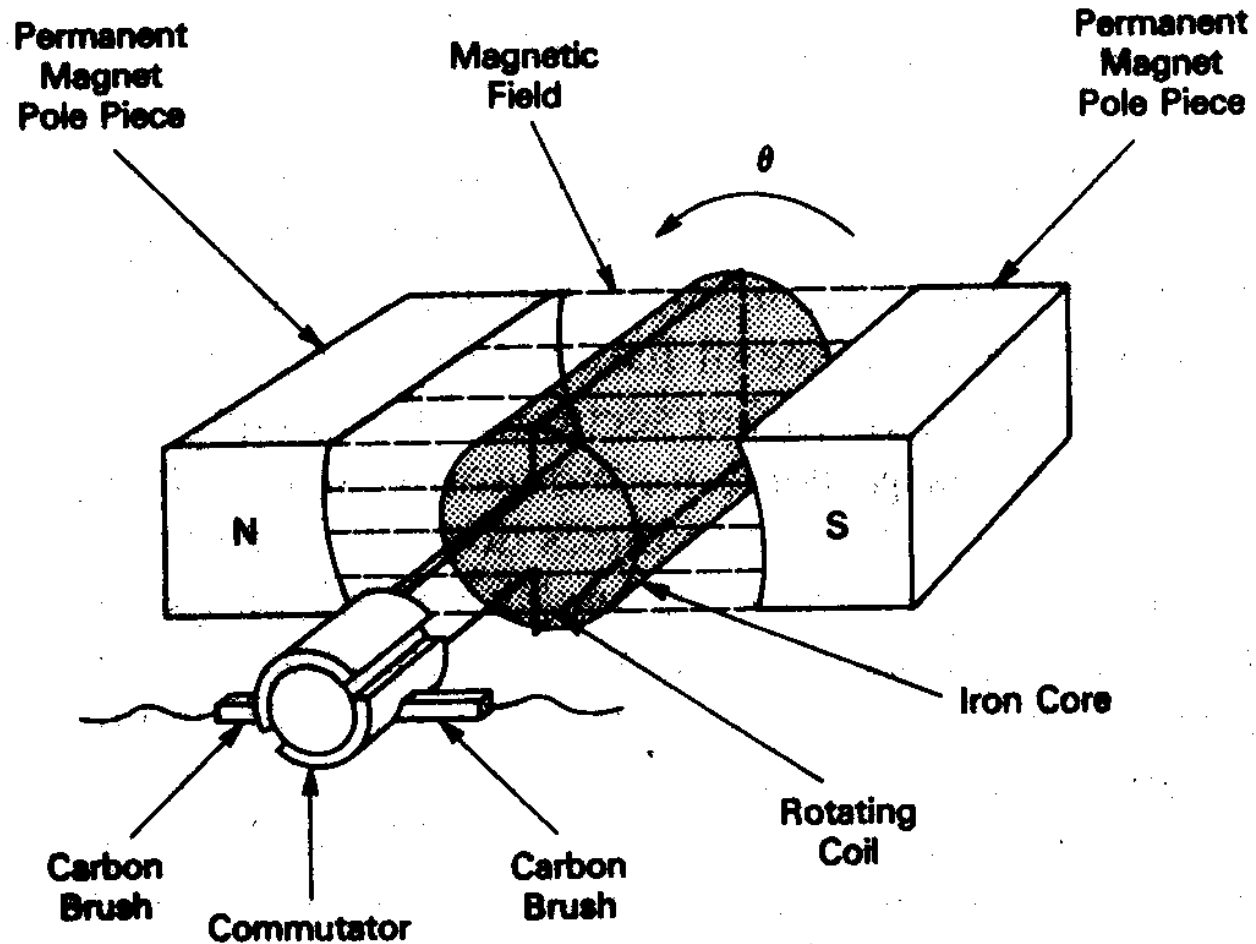
Using XOR gate

# Position sensor : Absolute encoder

Grey code



# Velocity and acceleration sensors

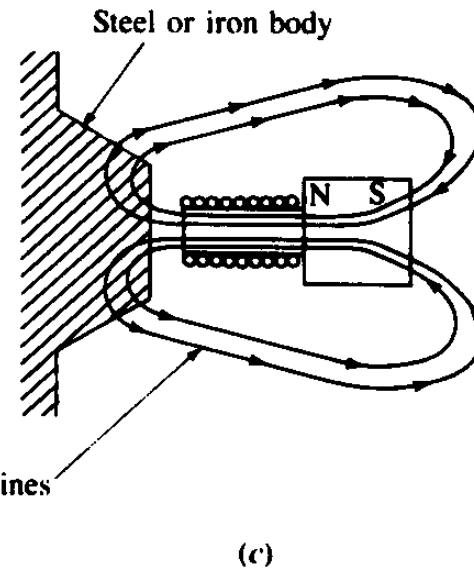
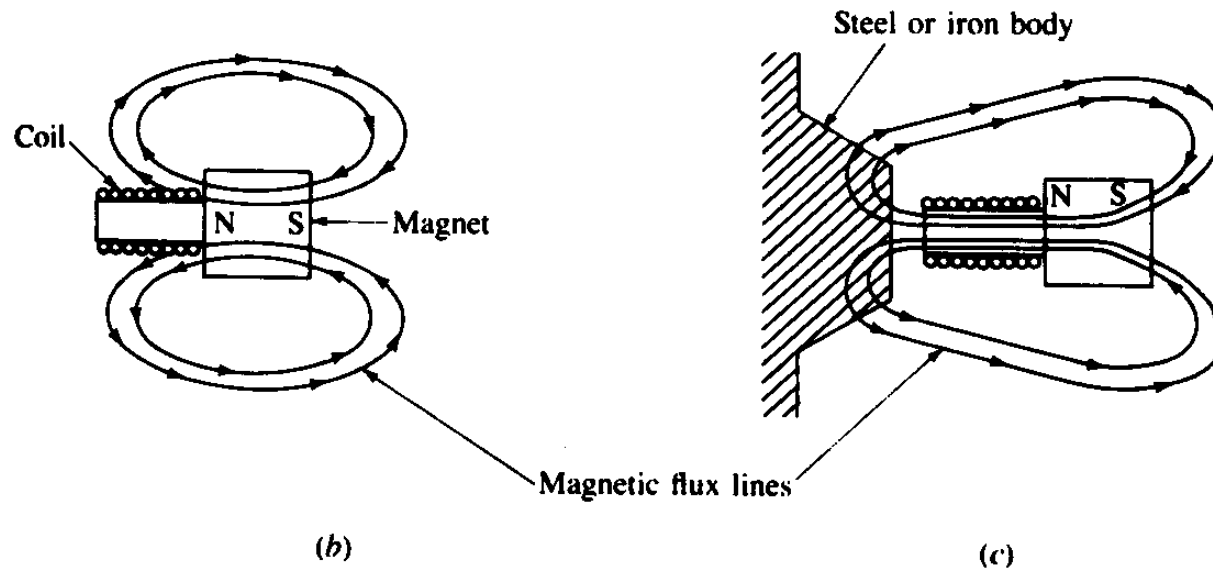
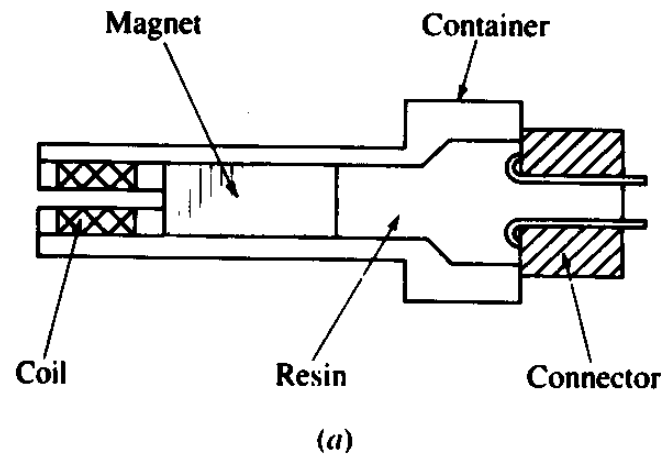


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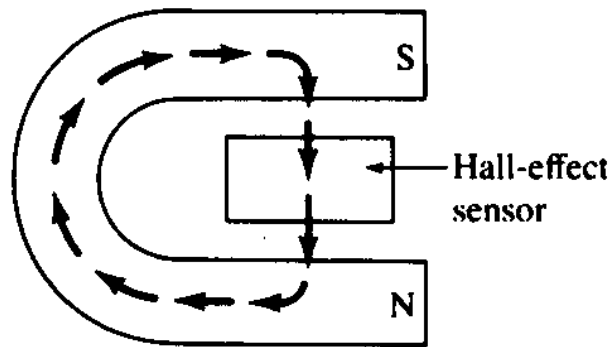
# Touch sensors

- **On /Off switches**
  - **Emitter / receiver pairs.**
  - **Thermal / pressure sensors**
-

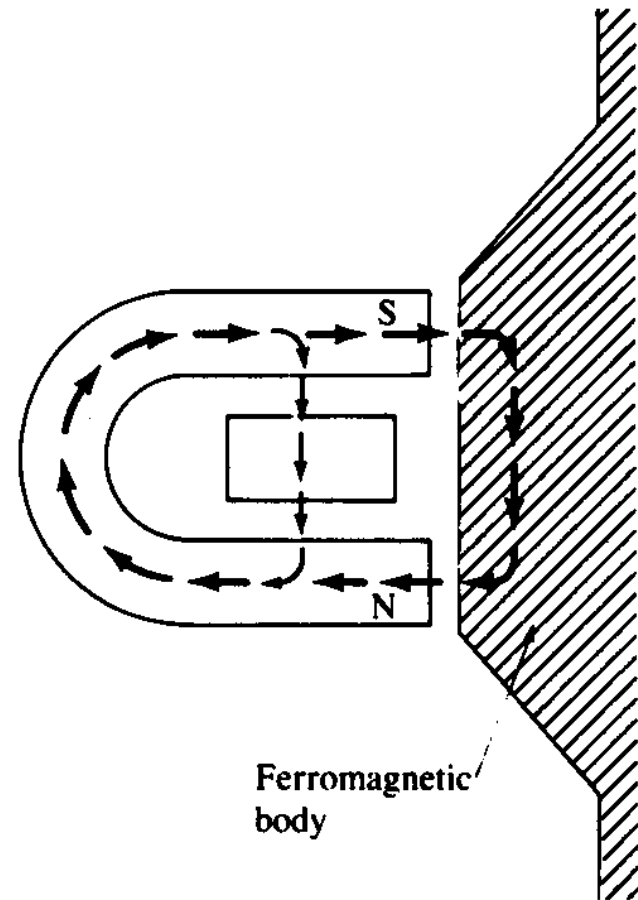
# Proximity sensor : Inductive sensor



# Proximity sensor: Hall effect sensor

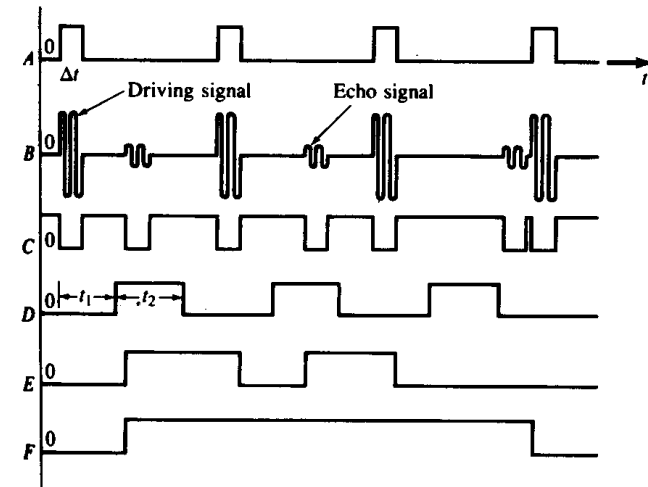
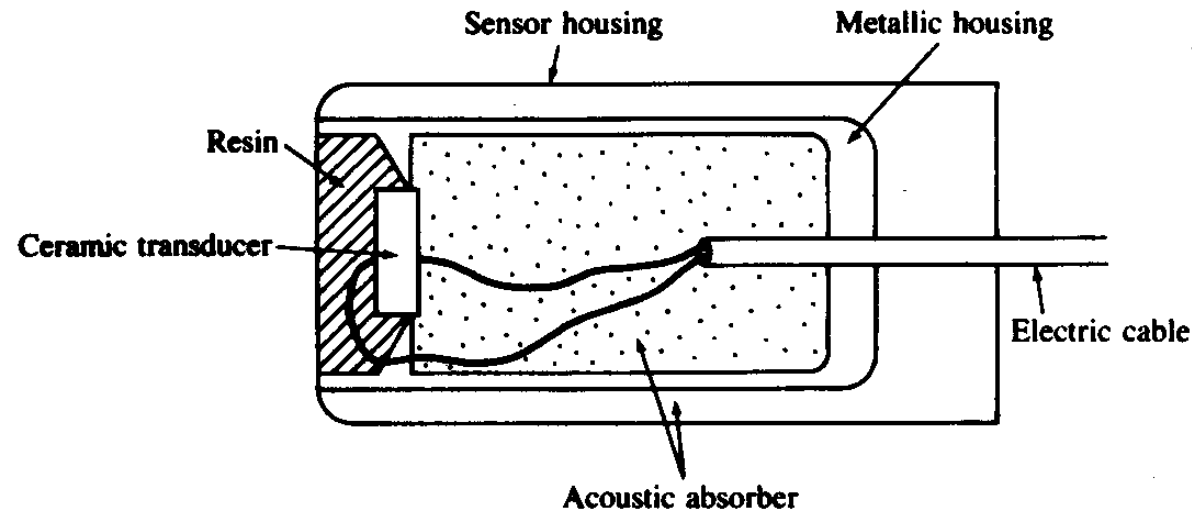


(a)

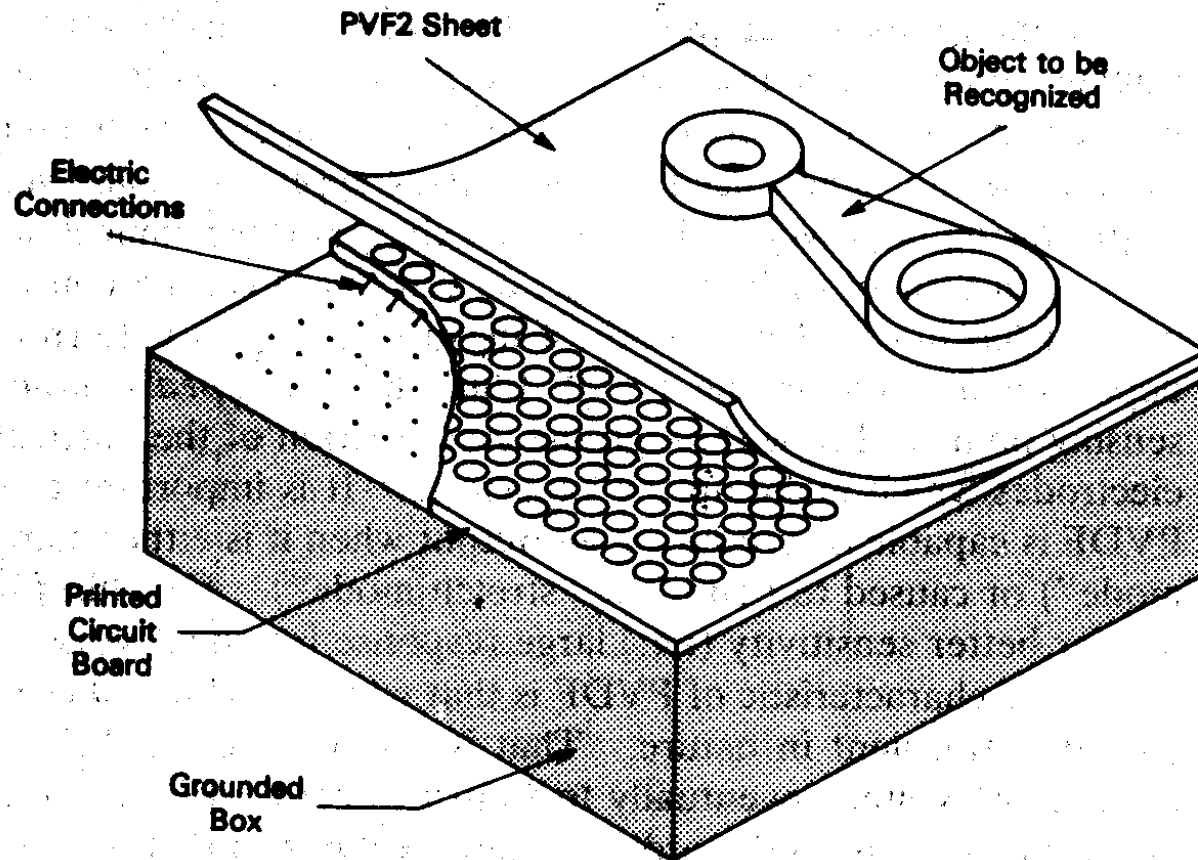


(b)

# Range sensor : Ultrasonic sensor

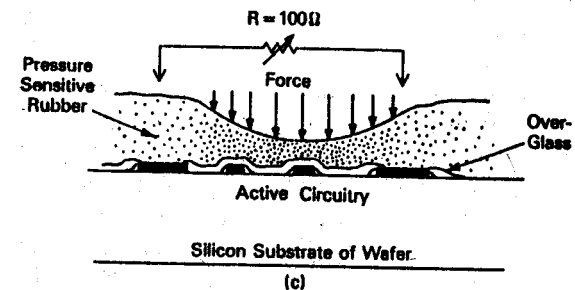
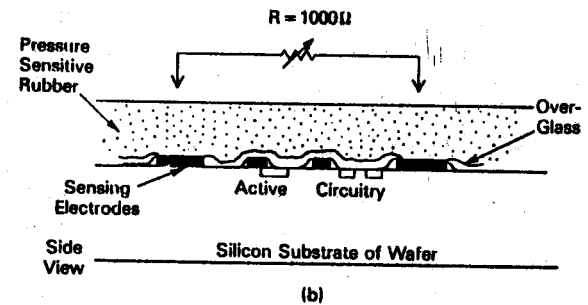
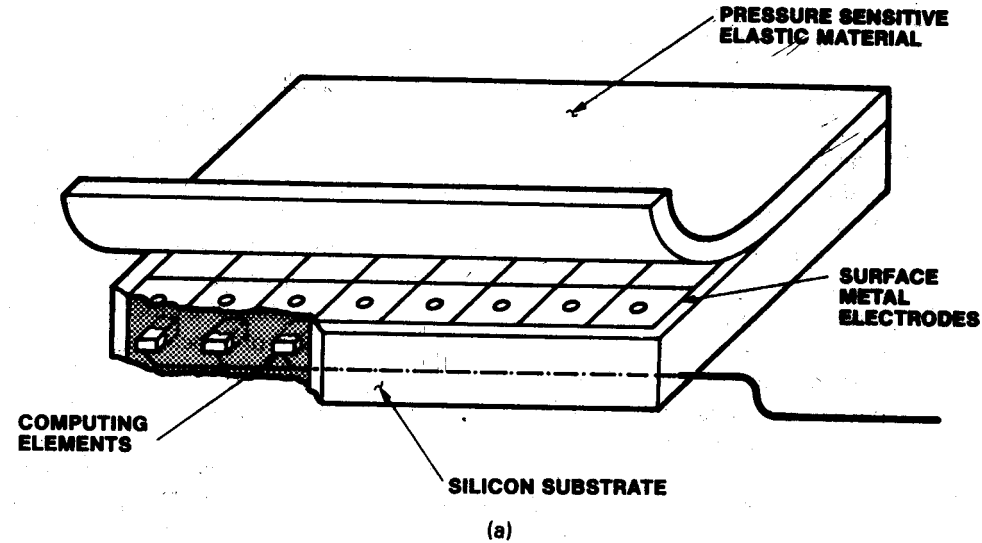
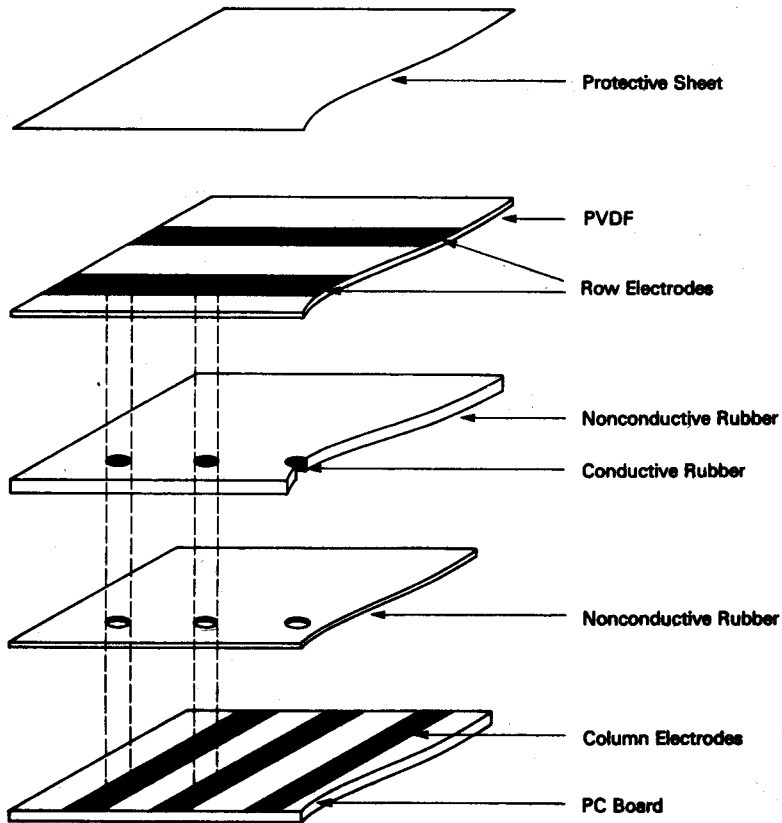


# Touch sensor

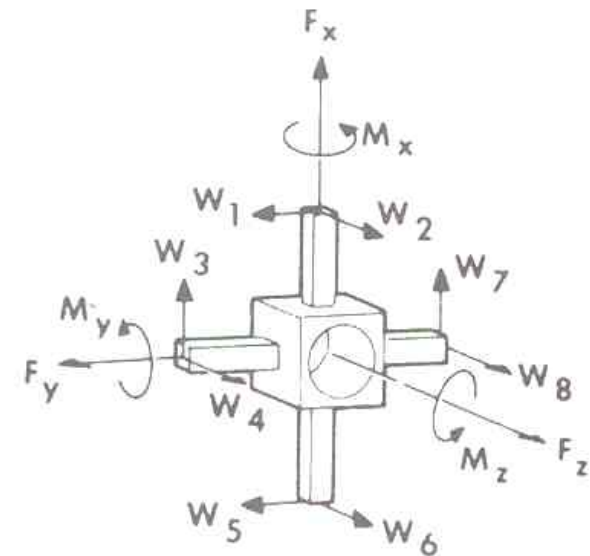
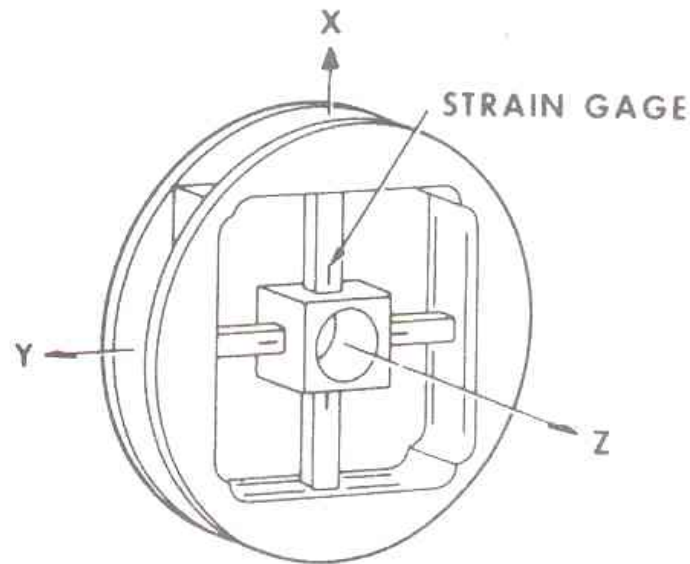




# Pressure sensor



# Force sensors



TRANSFORMATION MATRIX  
UNDER IDEAL CONDITIONS

$$\begin{array}{l}
 \text{FORCES AND TORQUES REFERENCED TO X-Y-Z SENSOR COORDINATES} \\
 \begin{bmatrix} F_x \\ F_y \\ F_z \\ M_x \\ M_y \\ M_z \end{bmatrix} = \begin{bmatrix} 0 & 0 & k_{13} & 0 & 0 & 0 & k_{17} & 0 \\ k_{21} & 0 & 0 & 0 & k_{25} & 0 & 0 & 0 \\ 0 & k_{32} & 0 & k_{34} & 0 & k_{36} & 0 & k_{38} \\ 0 & 0 & 0 & k_{44} & 0 & 0 & 0 & k_{48} \\ 0 & k_{52} & 0 & 0 & 0 & k_{56} & 0 & 0 \\ k_{61} & 0 & k_{63} & 0 & k_{65} & 0 & k_{67} & 0 \end{bmatrix} \begin{bmatrix} W_1 \\ W_2 \\ W_3 \\ W_4 \\ W_5 \\ W_6 \\ W_7 \\ W_8 \end{bmatrix} \\
 \text{FORCES SENSED AT SPOKE ELEMENTS}
 \end{array}$$

# Actuators

- *Electrical* : stepper motors, DC servo motors
  - *Pneumatic* : air pressure
  - *Hydraulic* : fluid pressure (oil pressure).
  - *Advanced actuators* : ultrasonic motors, artificial muscles, molecular motors.
-

# Mapping



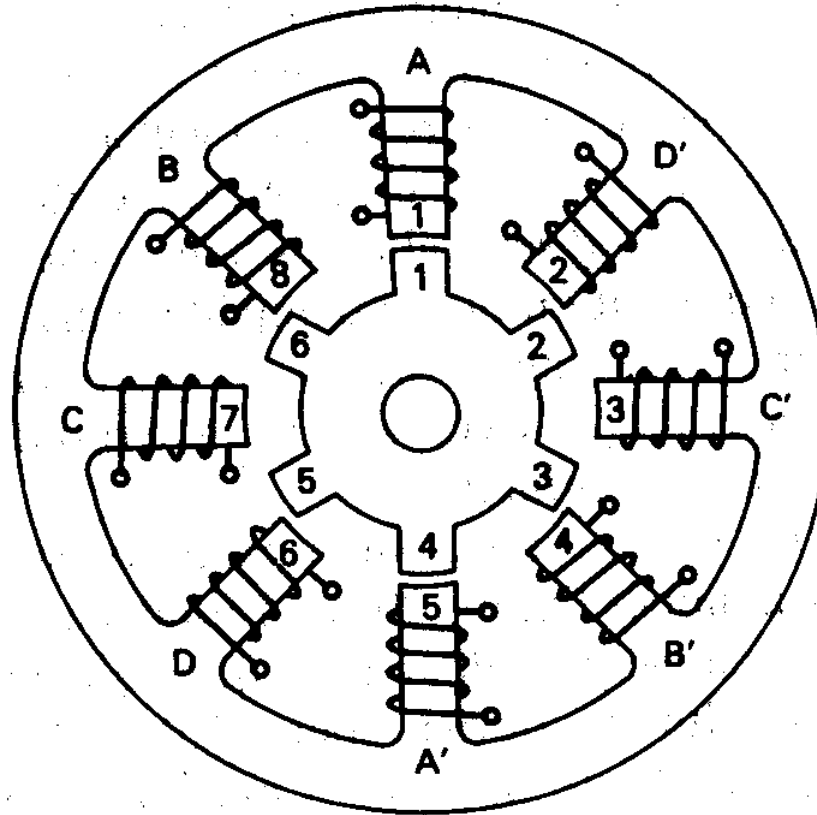
Actuator  
Space

Joint  
Space



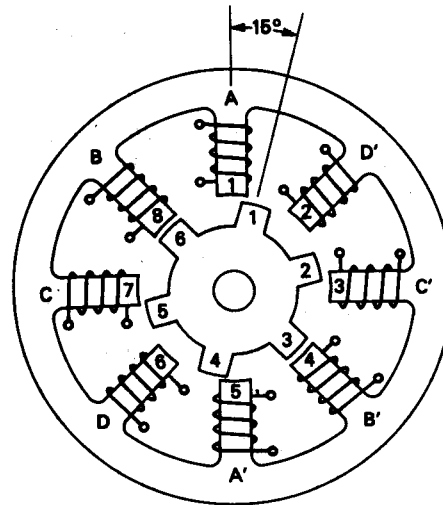
End effector  
Space

# Stepper motors : Variable reluctance, permanent magnet

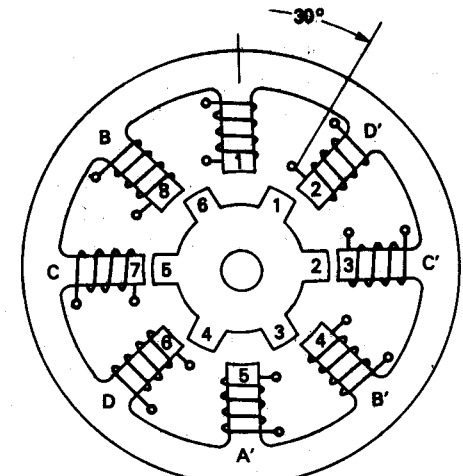


# Working of a stepper motor

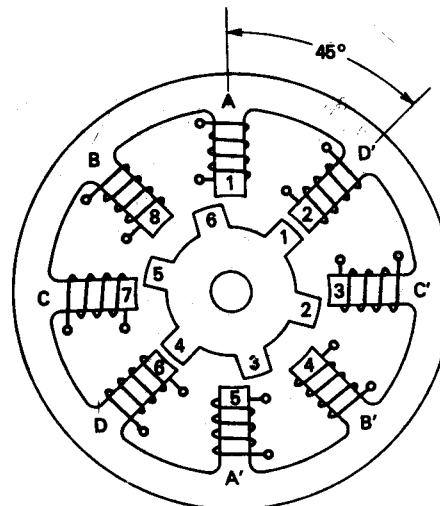
Sequence of rotation  
(CW): B – C – D – A'



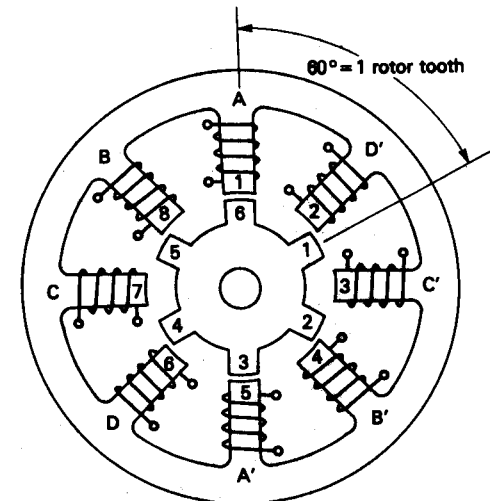
Phase B Energized  
(a)



Phase C Energized  
(b)

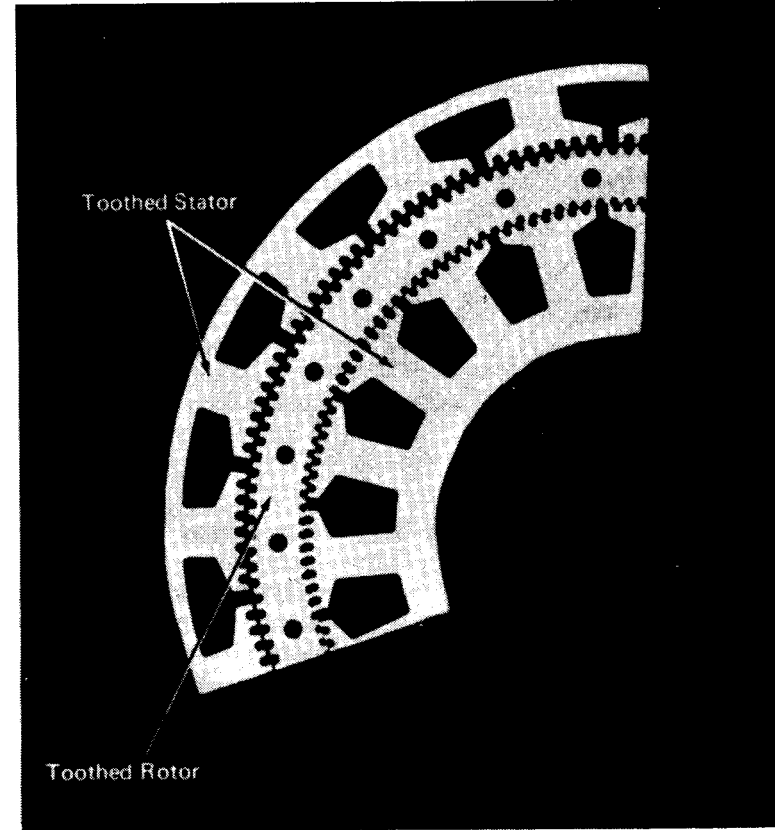
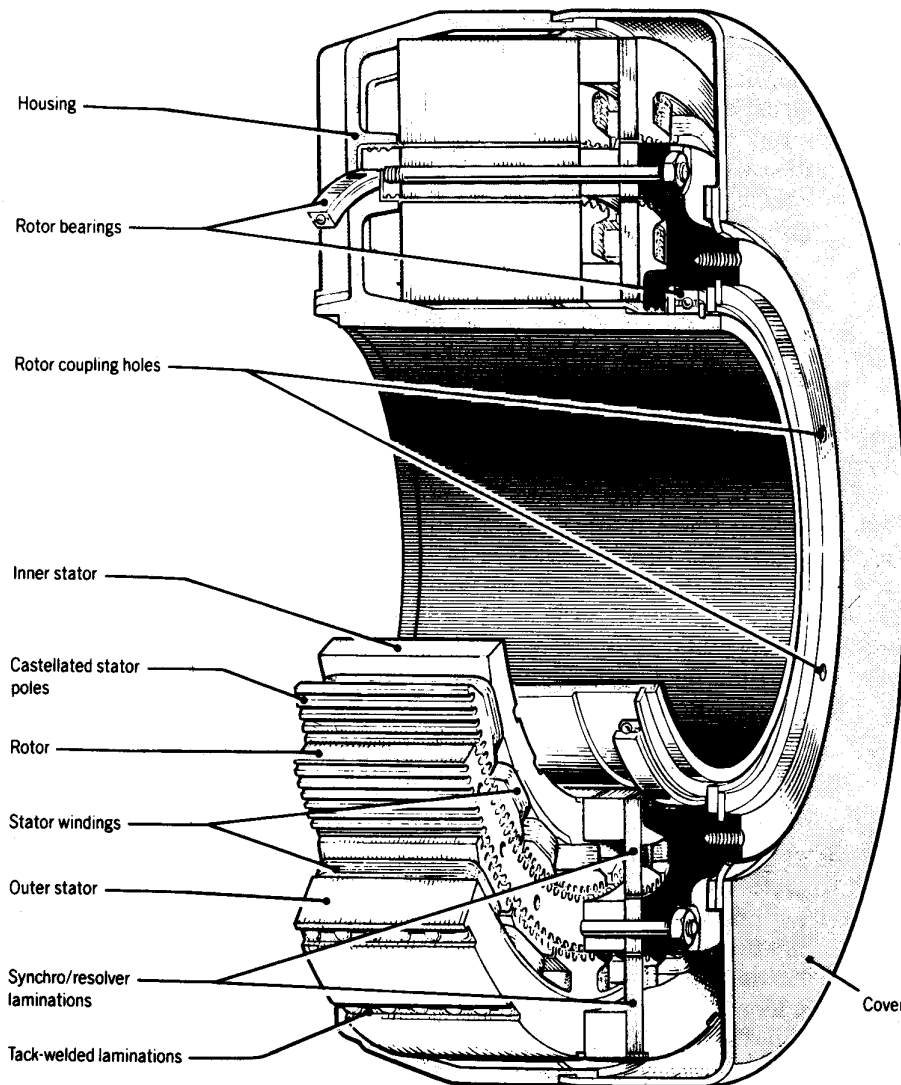


Phase D Energized  
(c)

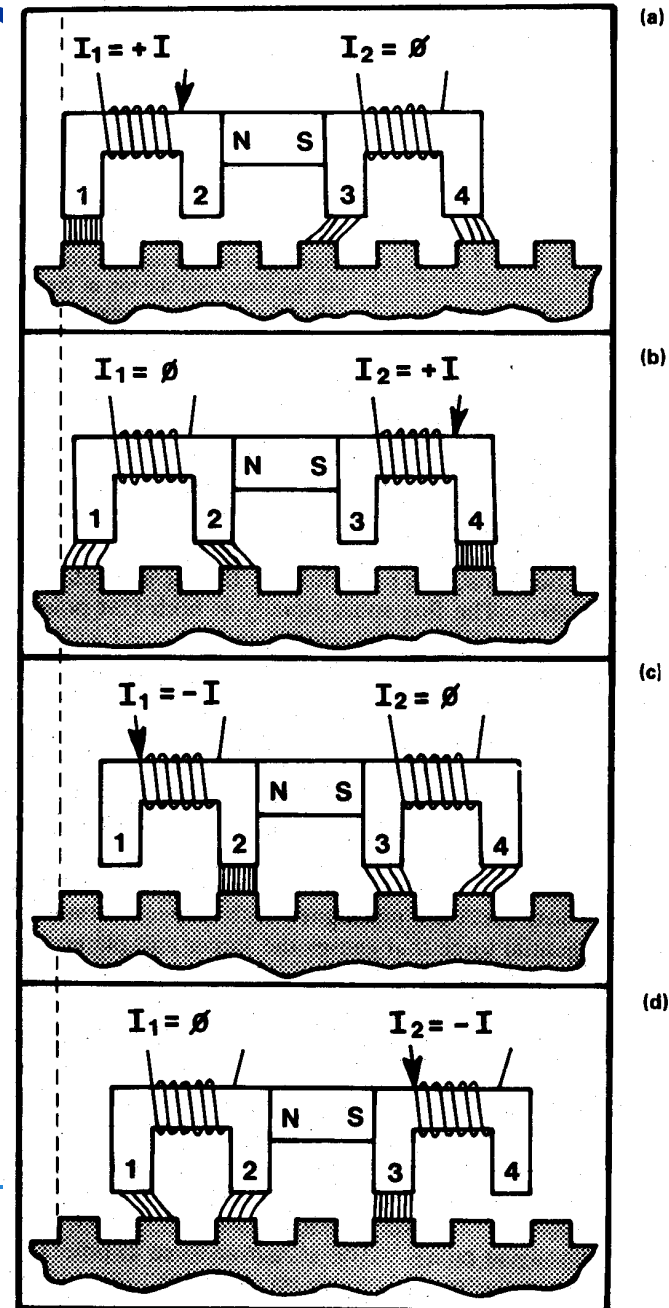
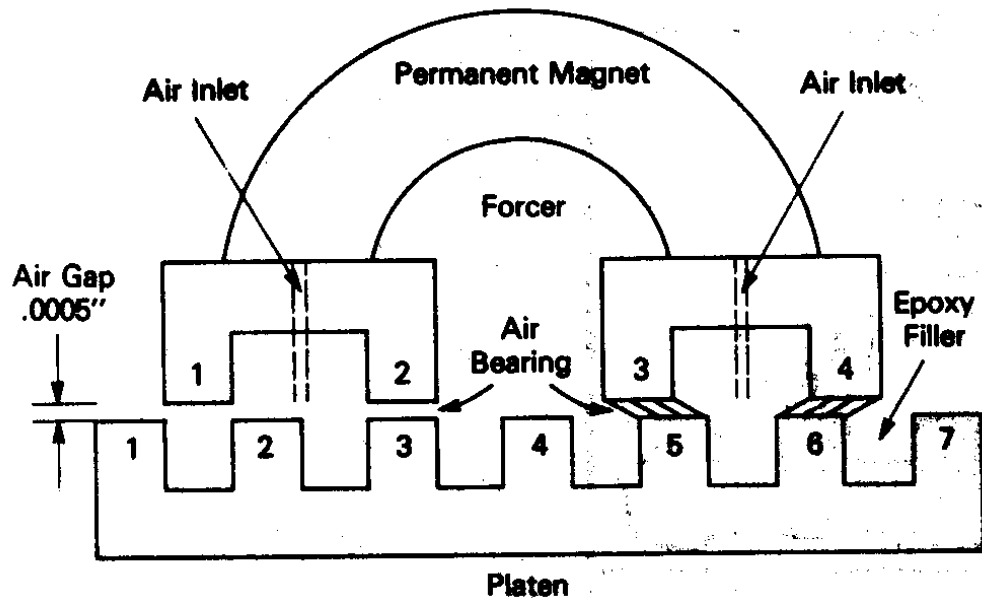


Phase A Energized  
(d)

# Mega-torque motors

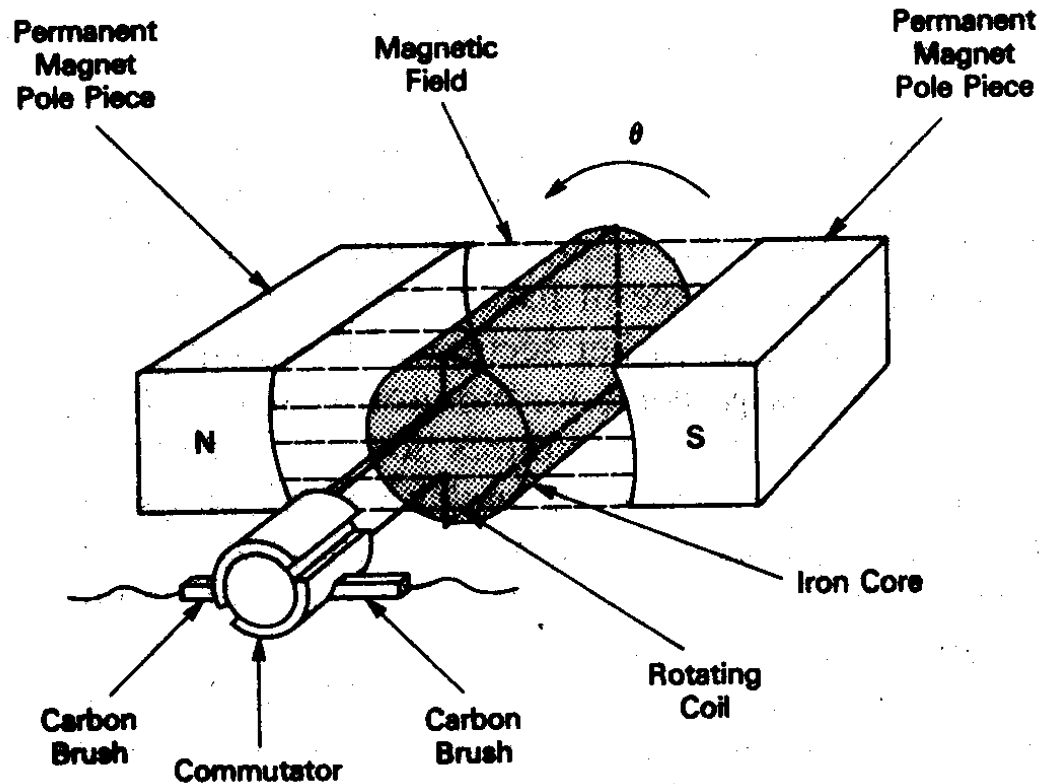


# Linear stepper motor

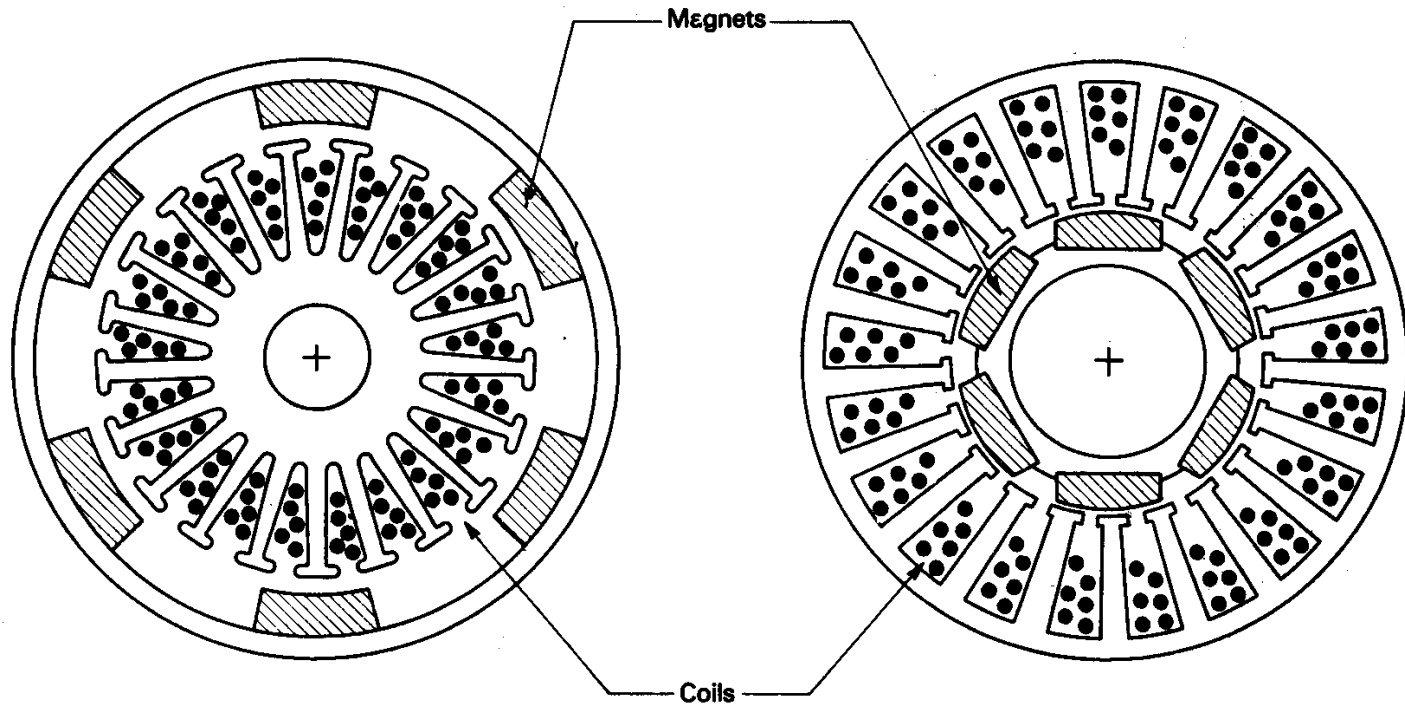




# DC Motors : basic working



# Brushless DC motors

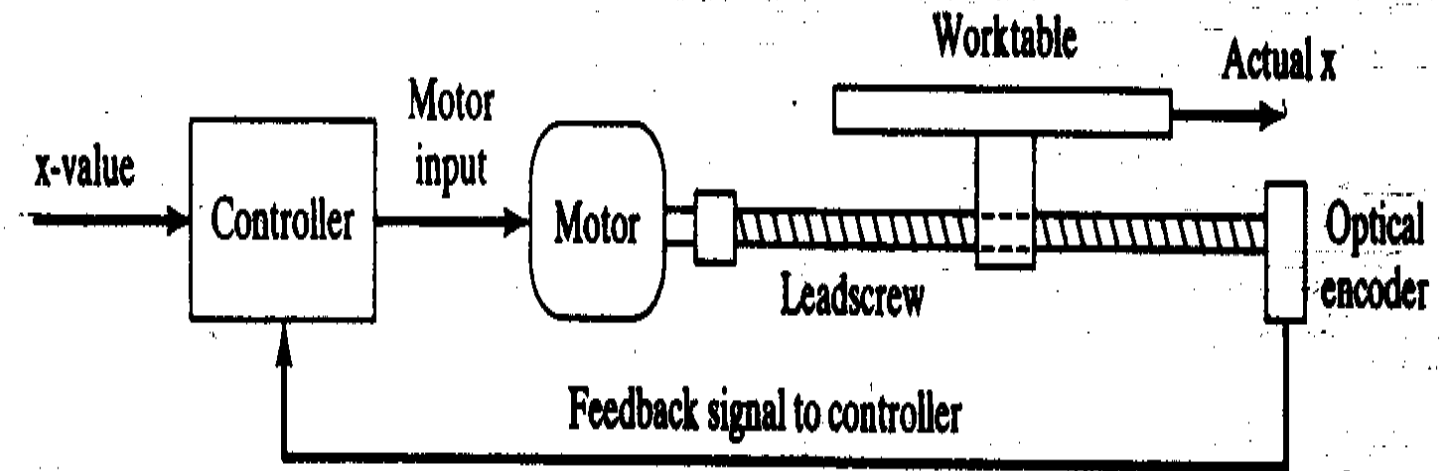


**Fig. Brush type DC motor**

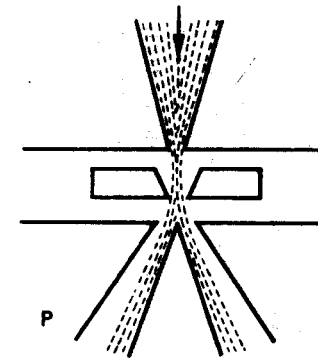
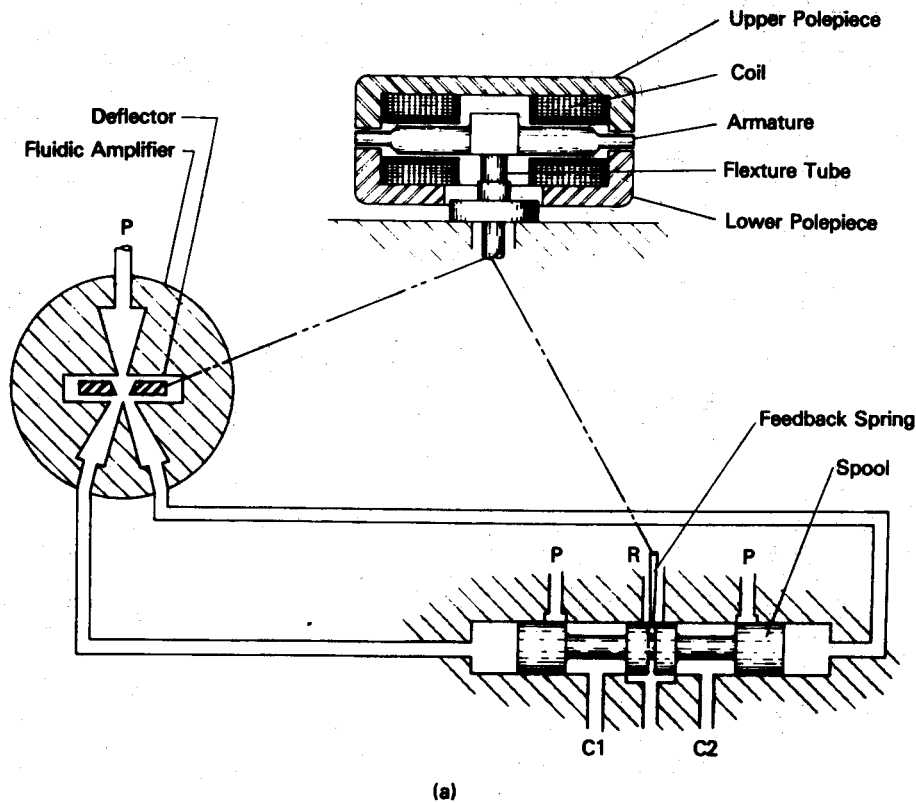
**Fig. Brushless DC motor**

# DC servo motors

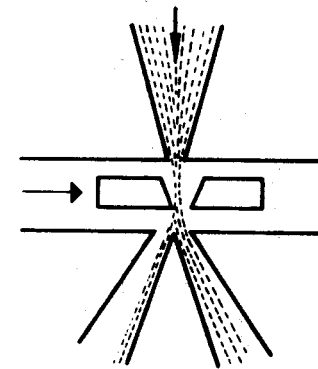
- DC motors working in closed loop position control.



# Pneumatic actuators

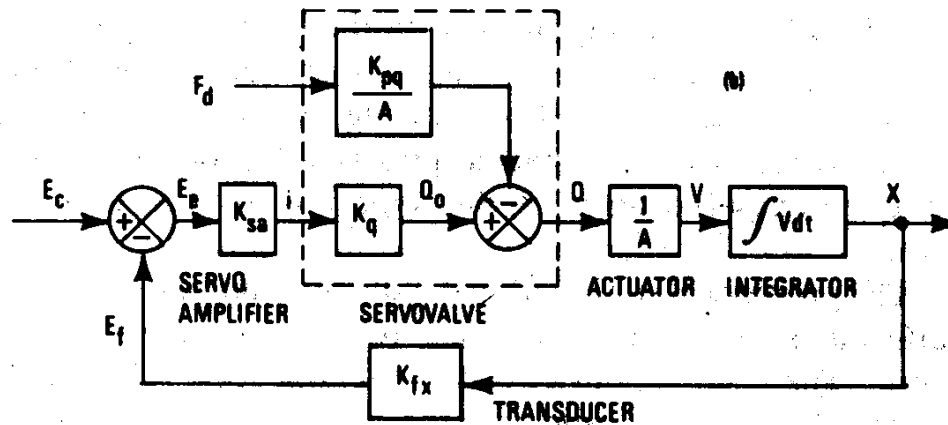
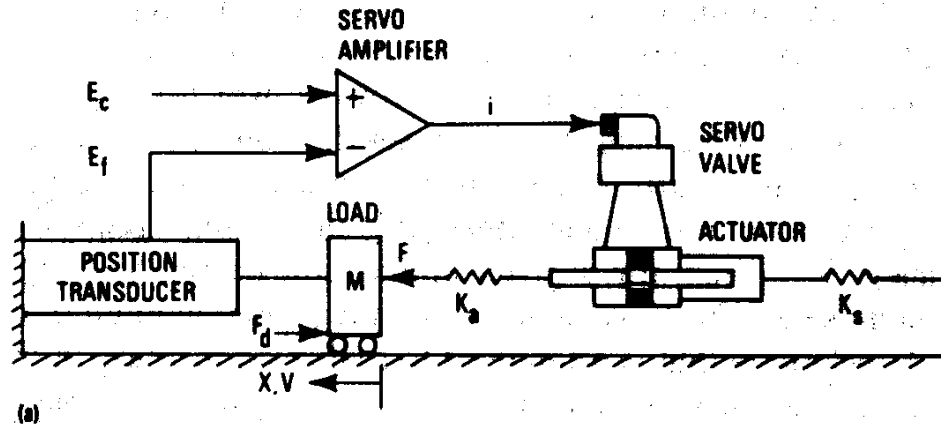


(b)



(c)

# Hydraulic actuators: piston cylinder mechanism

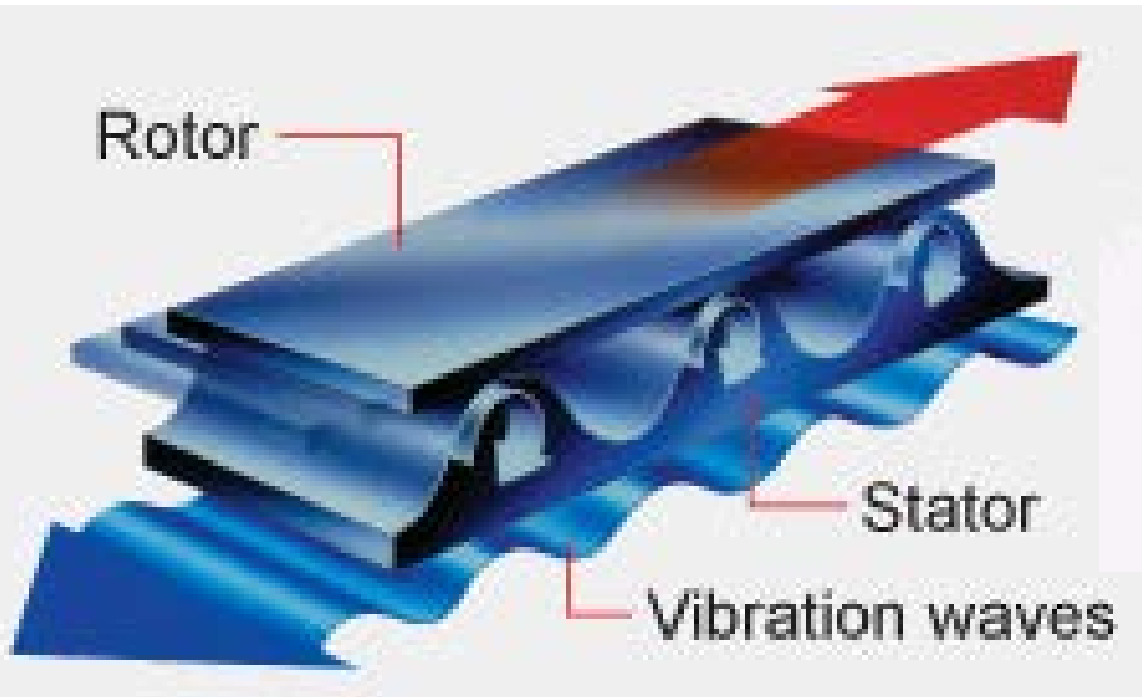


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# Advanced actuators: small, low power consumption, micro motion

- **Ultrasonic motors** : micro robots, cameras, micro motion devices ..
  - **Artificial muscles** : prosthetic, bio applications..
  - **Molecular motors** : bio applications
-

# Ultrasonic motors



**Fig. Motion due to dry friction and vibration.**



**Fig. Ring motors used in cameras.**

# Comparison of smart actuators

- ◆ Piezo electric materials- large forces, small strains and fast response time.
- ◆ IPMCs- small forces, large strains, slower response times.
- ◆ (power) IPMC = (1/100) Natural Muscle.

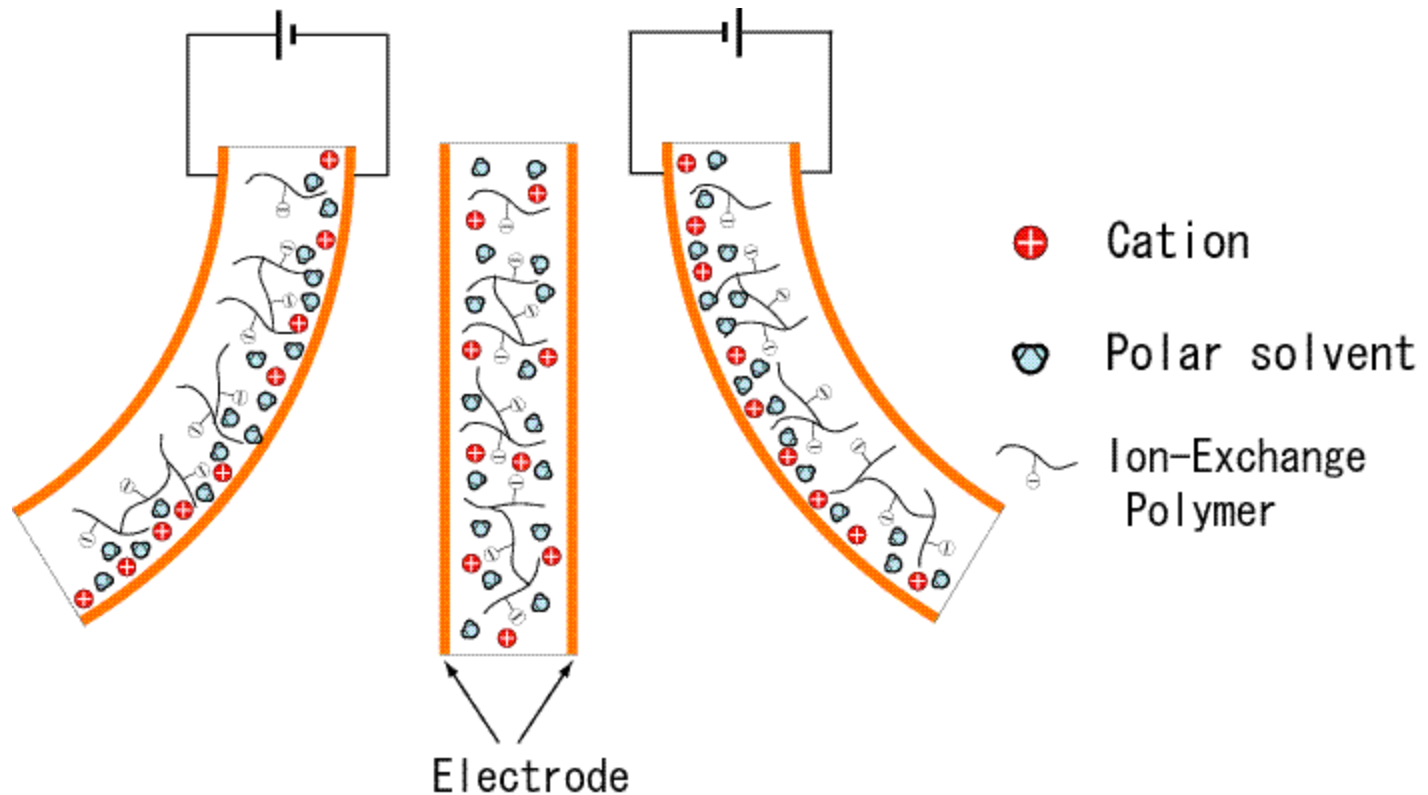
TABLE 1: Comparison of the properties of IPMC, SMA and EAC

Property	Ionic polymer-Metal Composites (IPMC)	Shape Memory Alloys (SMA)	Electroactive Ceramics (EAC)
Actuation displacement	>10%	<8% short fatigue life	0.1 - 0.3 %
Force (MPa)	10 - 30	about 700	30-40
Reaction speed	μsec to sec	sec to min	μsec to sec
Density	1- 2.5 g/cc	5 - 6 g/cc	6-8 g/cc
Drive voltage	4 - 7 V	NA	50 - 800 V
Power consumption	watts	watts	watts
Fracture toughness	resilient, elastic	elastic	fragile



# Electro active Polymers

- Movement of ions and creations of micro channels.



# IPMC motion



# IPMC

- **Ionomeric polymer metal composite (IPMC)**
  - a polymer coated with a metal electrode.

**Material – Nafion 117**

**Electrode – Platinum, Gold**

**Electroplating by electrolysis**

---

# **Working Mechanism**

**The actual mechanism at work in the polymers is debated.**

- ▶ **Pressure gradients, electric fields, elastic deformation, ion transport etc.**

## **Two Theories**

- A. Movement of Ions.**
  - B. Creation of Micro- channels.**
-

# Motion of Water in the IPMC



# Modeling

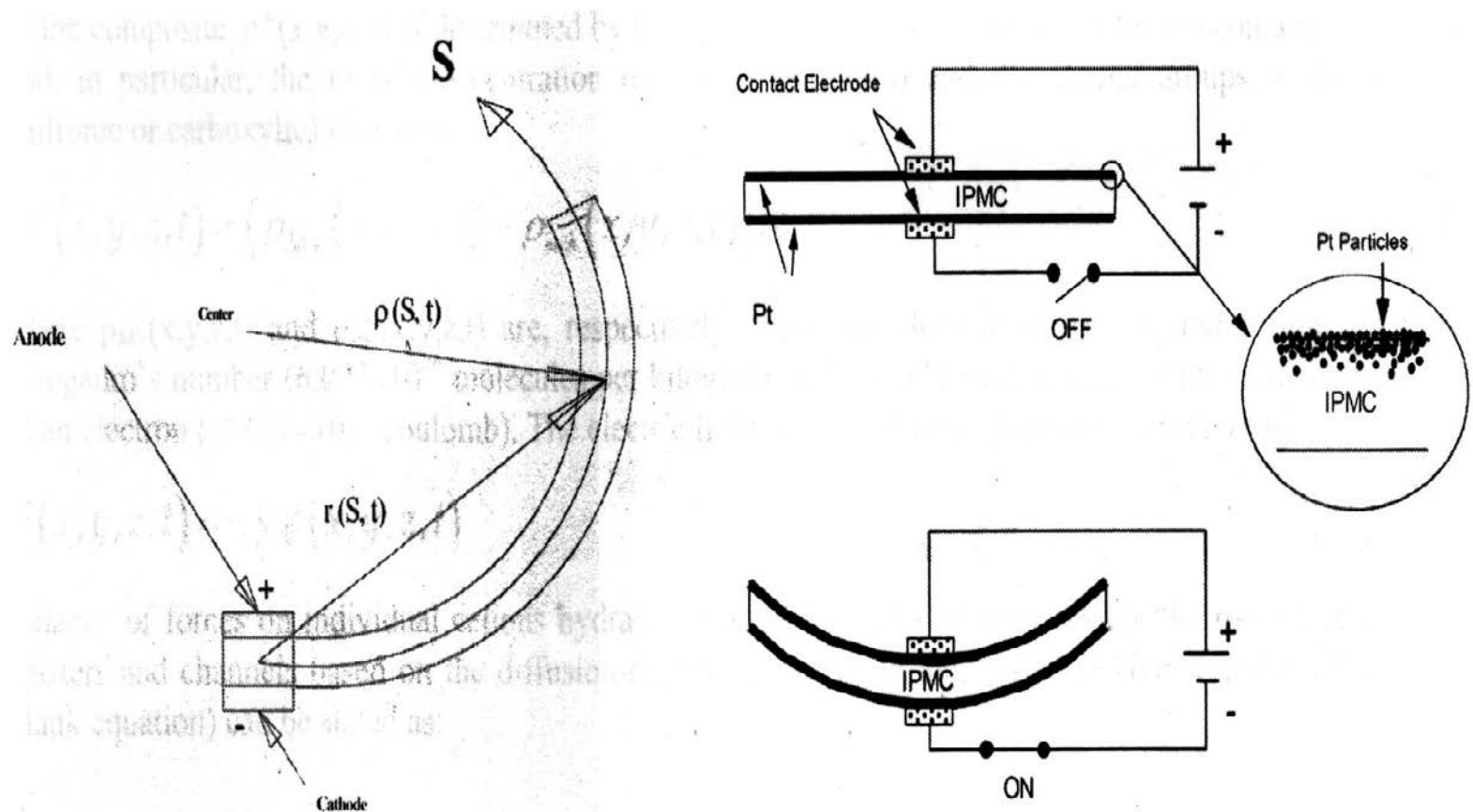


Fig. 9. Bending of an Ionic Gel Strip Due to an Imposed Electric Field Gradient

$$\rho^*(x, y, z, t) = (\rho_{M+}(x, y, z, t) - \rho_{so3}(x, y, z, t))N_e \quad (2)$$

where  $\phi(x, y, z, t)$  is an electric potential,  $\rho(x, y, z, t)$  is an electric charge density and  $\epsilon$  is the dielectric constant of the composite.  $\rho^*(x, y, z, t)$  is determined by the equivalent weight of the precursor ion containing polymer and, in particular, the molar concentration of cations (Lithium) and the charge groups in the polymer (sulfonic or carboxylic) such that:

$$\rho^*(x, y, z, t) = (\rho_{M+}(x, y, z, t) - \rho_{so3}(x, y, z, t))N_e \quad (3)$$

where  $\rho_{M+}(x, y, z, t)$  and  $\rho_{so3}(x, y, z, t)$  are, respectively, the molal density of cations and sulfons,  $N$  is the Avogadro's number ( $6.023 \times 10^{26}$  molecules per kilogram-mole in mks units), and  $e$  is the elementary charge of an electron ( $-1.602 \times 10^{-19}$  coulomb). The electric field within the ionic polymeric structure is:

$$\underline{E}(x, y, z, t) = -\nabla \phi(x, y, z, t) \quad (4)$$

Balance of forces on individual cations hydrated with  $n$  molecules of water inside the molecular network, clusters and channels based on the diffusion-drift model of ionic media due to Nernst and Plank (Nernst-Plank equation) can be stated as:

$$N_e \rho_{M+} E_x(x, y, z, t) = N(\rho_{M+} M_{M+} + n \rho_w M_w) \left( \frac{dv_x}{dt} \right) + N \rho_{M+} \eta v_x + N \rho_{M+} kT \left( \frac{\partial \ln(\rho_{M+} + n \rho_w)}{\partial x} \right) + \left( \frac{\partial P}{\partial x} \right) \quad (5)$$

$$N_e \rho_{M+} E_y(x, y, z, t) = N(\rho_{M+} M_{M+} + n \rho_w M_w) \left( \frac{dv_y}{dt} \right) + N \rho_{M+} \eta v_y + N \rho_{M+} kT \left( \frac{\partial \ln(\rho_{M+} + n \rho_w)}{\partial y} \right) + \left( \frac{\partial P}{\partial y} \right) \quad (6)$$

$$N_e \rho_{M+} E_z(x, y, z, t) = N(\rho_{M+} M_{M+} + n \rho_w M_w) \left( \frac{dv_z}{dt} \right) + N \rho_{M+} \eta v_z + N \rho_{M+} kT \left( \frac{\partial \ln(\rho_{M+} + n \rho_w)}{\partial z} \right) + \left( \frac{\partial P}{\partial z} \right) \quad (7)$$

$$kT \left( \frac{\partial \ln [\rho_{M+}(x, y, z, t) + n\rho_w(x, y, z, t)]}{\partial y} \right) \quad (13)$$

$$kT \left( \frac{\partial \ln [\rho_{M+}(x, y, z, t) + n\rho_w(x, y, z, t)]}{\partial z} \right) \quad (14)$$

and the force vector due to inertial effects on an individual hydrated cation is:

$$(M_{M+} + nM_w) \left( \frac{dv}{dt} \right) \quad (15)$$

such that in a compact vectorial form the force balance equation reads:

$$N_e \rho_{M+} \underline{\underline{E}} = N (\rho_{M+} M_{M+} + n\rho_w M_w) \left( \frac{d\underline{\underline{v}}}{dt} \right) + N \rho_{M+} \eta \underline{\underline{v}} + N \rho_{M+} kT \nabla \ln(\rho_{M+} + n\rho_w) + \nabla P_f \cdot \underline{\underline{\sigma}}^* \quad (16)$$

where the stress tensor  $\underline{\underline{\sigma}}^*$  can be expressed in terms of the deformation gradients in a non-linear manner such as in Neo-Hookean or Mooney-Rivlin type constitutive equations as suggested by Segalman, Adolf, Witkowski and Shahinpoor, [1991- 1993]. The flux of hydrated cations is given by:

$$\underline{\underline{Q}} = [\rho_{M+}(x, y, z, t) + \eta \rho_w(x, y, z, t)] \underline{\underline{v}}(x, y, z, t) \quad (17)$$

Such that the equation of continuity becomes:

$$\left( \frac{\partial [\rho_{M+}(x, y, z, t) + n\rho_w(x, y, z, t)]}{\partial t} \right) = -\nabla \cdot \underline{\underline{Q}} \quad (18)$$



$$e\vec{E}(x, y, z, t) = \left[ eE(x, y, z, t)_x, eE(x, y, z, t)_y, eE(x, y, z, t)_z \right]^T \quad (8)$$

is the force vector on an individual cation due to electro-osmotic motion of an ion in an electric field,  $k$  is the Boltzmann's constant and ,

$$\vec{v}(x, y, z, t) = \left[ v_x(x, y, z, t), v_y(x, y, z, t), v_z(x, y, z, t) \right]^T \quad (9)$$

is the velocity vector of the hydrated cations, and

$$\vec{\nabla}p(x, y, z, t) = \frac{L}{K} \vec{E}(x, y, z, t) \quad (10)$$

is the force vector of the viscous resistance to the motion of individual hydrated cations in the presence of a viscous fluid medium with a viscosity of  $\eta$ , and

$$kT\vec{\nabla}[\ln(\rho_{M+}(x, y, z, t) + n\rho_w(x, y, z, t))] \quad (11)$$

is the force vector due to diffusion of individual cations and accompanying molecules of hydrated water in the polymer network with the following  $x$ ,  $y$ , and  $z$  components, respectively:

$$kT \left( \frac{\partial \ln[\rho_{M+}(x, y, z, t) + n\rho_w(x, y, z, t)]}{\partial x} \right) \quad (12)$$

$$\nabla p(x, y, z, t) = \frac{L}{K} \underline{E}(x, y, z, t) \quad (21)$$

This  $\nabla p(x, y, z, t)$  will, in turn, induce a curvature  $\underline{\kappa}$  proportional to  $\nabla p(x, y, z, t)$ . The relationships between the curvature  $\underline{\kappa}$  and pressure gradient  $\nabla p(x, y, z, t)$  are fully derived and described in de Gennes, Okumura, Shahinpoor and Kim [2000]. Let us just mention that  $(1/\rho_c) = \mathbf{M}(\mathbf{E})/YI$ , where  $\mathbf{M}(\mathbf{E})$  is the local induced bending moment and is a function of the imposed electric field  $\mathbf{E}$ ,  $Y$  is the Young's modulus (elastic stiffness) of the strip which is a function of the hydration  $H$  of the IPMC and  $I$  is the moment of inertia of the strip. Note that locally  $\mathbf{M}(\mathbf{E})$  is related to the pressure gradient such that in a simplified scalar format:

$$\nabla \nabla p(x, y, z, t) = \left( \frac{2P}{t^*} \right) = \left( \frac{M}{I} \right) = \frac{Y}{\rho_c} = Y_{\kappa} \quad (22)$$

Now from equation (22) it is clear that the vectorial form of curvature  $\underline{\kappa}_E$  is related to the imposed electric field  $\mathbf{E}$  by:

$$\underline{\kappa}_E \cong \left[ \frac{2\delta_{\max}}{l_g^2 + \delta_{\max}^2} \right] \cong \frac{2\delta_{\max}}{l_g^2} \cong \left( \frac{L}{KY} \right) \underline{E} \quad (23)$$

Based on this simplified model the tip bending deflection  $\delta_{\max}$  of an IPMC strip of length  $l_g$  should be almost linearly related to the imposed electric field due to the fact that:

$$\underline{\kappa}_E \cong \left[ \frac{2\delta_{\max}}{l_g^2 + \delta_{\max}^2} \right] \cong \frac{2\delta_{\max}}{l_g^2} \cong \left( \frac{L}{KY} \right) \underline{E} \quad (24)$$

# Displacement verses voltage

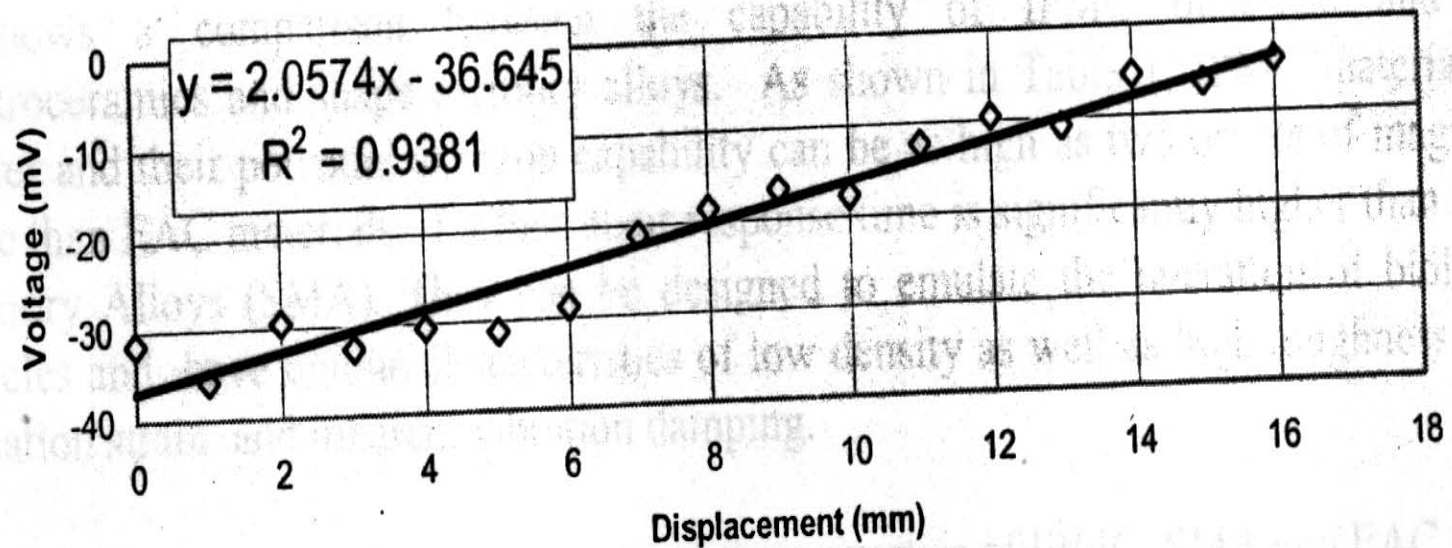


Figure 3. Inverted IPMC film sensor response for positive displacement input.

# Artificial muscles



Fig. Hand.



Fig. Flying robot.

END



# Molecular motors

**Protein**-based molecular motors harness the chemical **free energy** released by the **hydrolysis** of **ATP** in order to perform mechanical work.

