

Sokolova, Biehl TSA Competition

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```
library(lubridate)
library(ggplot2)
library(forecast)
library(Kendall)
library(tseries)
library(outliers)
library(tidyverse)
library(smooth)
library(zoo)
library(kableExtra)
library(readxl)
```

```
#Importing data
```

```
load <- read_excel("./Data/load.xlsx")
```

```
#Aggregating from hourly to daily and omitting NAs from the calculation
```

```
DailyAvgLoad <- rowMeans(load[,3:26], na.rm=TRUE)
```

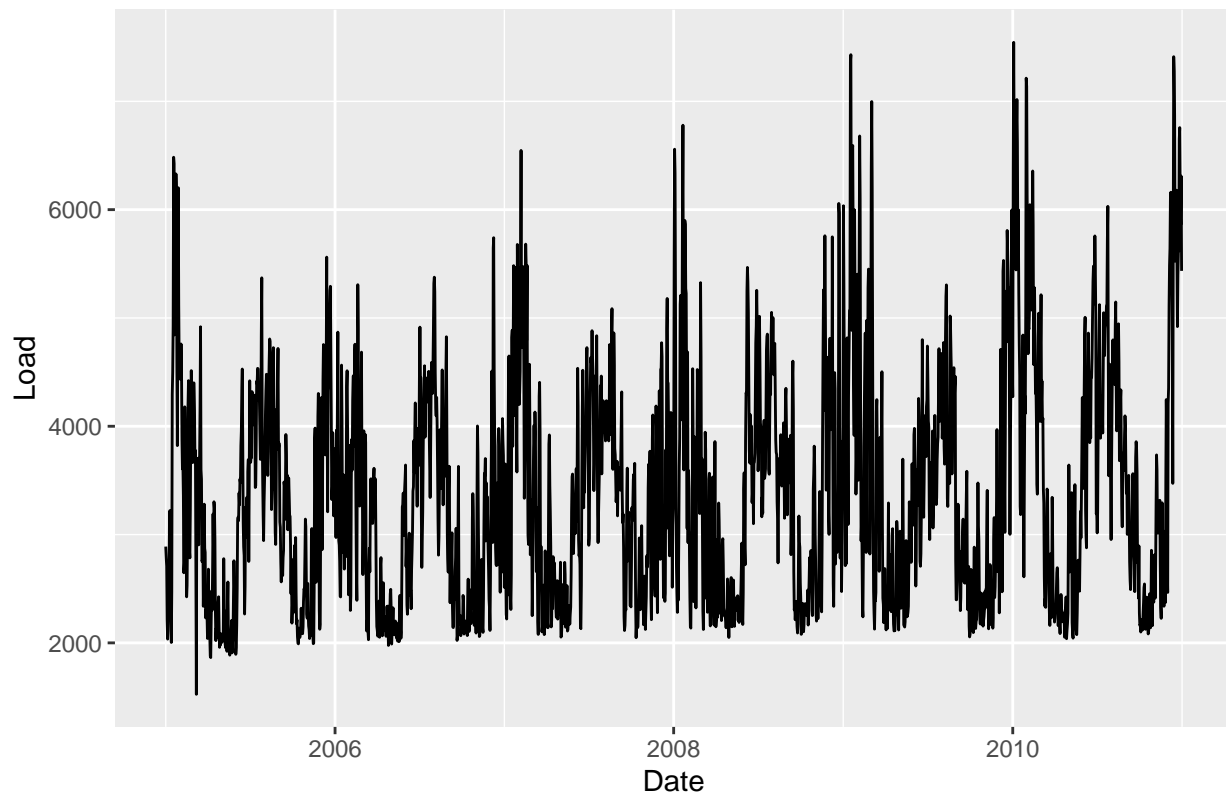
```
DailyAvgLoad <- data.frame(load$date,DailyAvgLoad)
```

```
colnames(DailyAvgLoad) <- c("Date","Load")
```

```
DailyAvgLoad$Date <- ymd(DailyAvgLoad$Date)
```

```
ggplot(DailyAvgLoad, aes(x=Date,y=Load)) +
  geom_line() +
  ggtitle("Average Daily Load")+
  ylab("Load")
```

Average Daily Load



```
summary(DailyAvgLoad$Load)
```

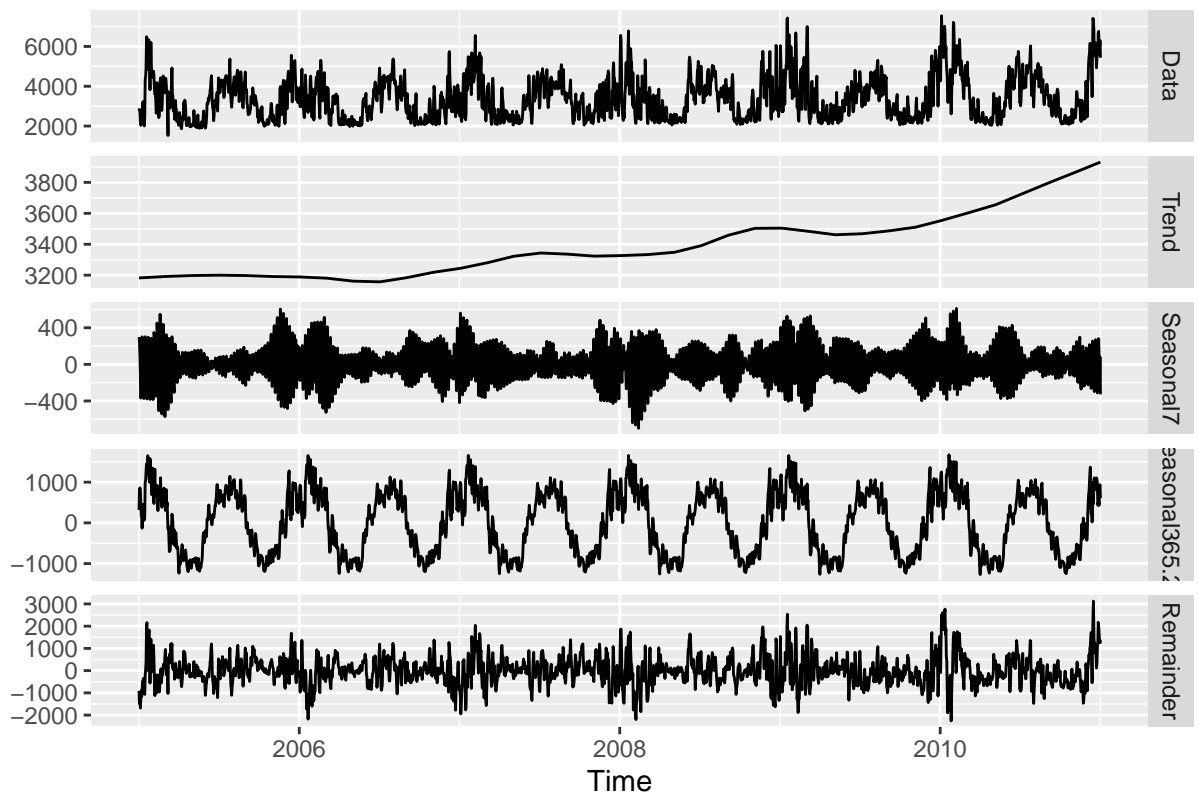
```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      1525   2453   3220   3382   4046   7545
```

```
#Making time series
```

```
ts_DailyAvgLoad <- msts(DailyAvgLoad$Load,
                        seasonal.periods =c(7,365.25),
                        start=c(2005,1,1))
```

```
#Decomposing the series
```

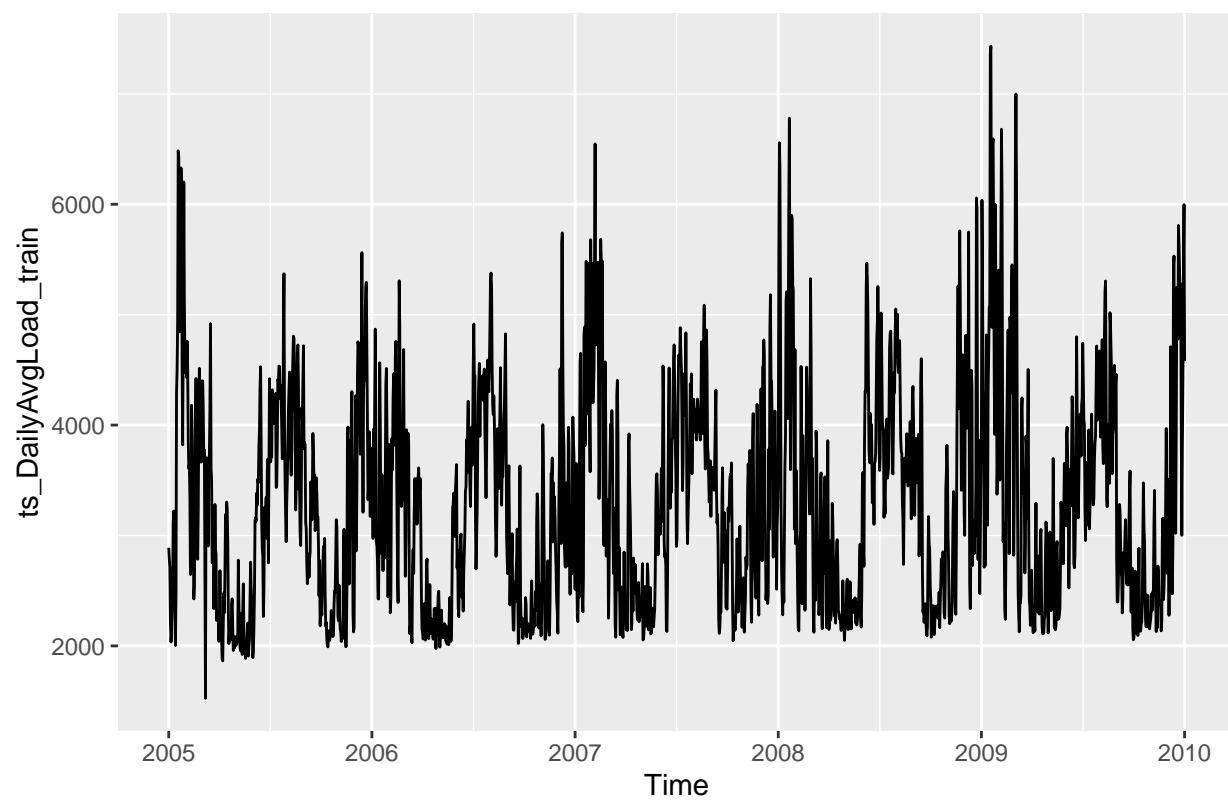
```
ts_DailyAvgLoad %>% mstl() %>%
  autoplot()
```



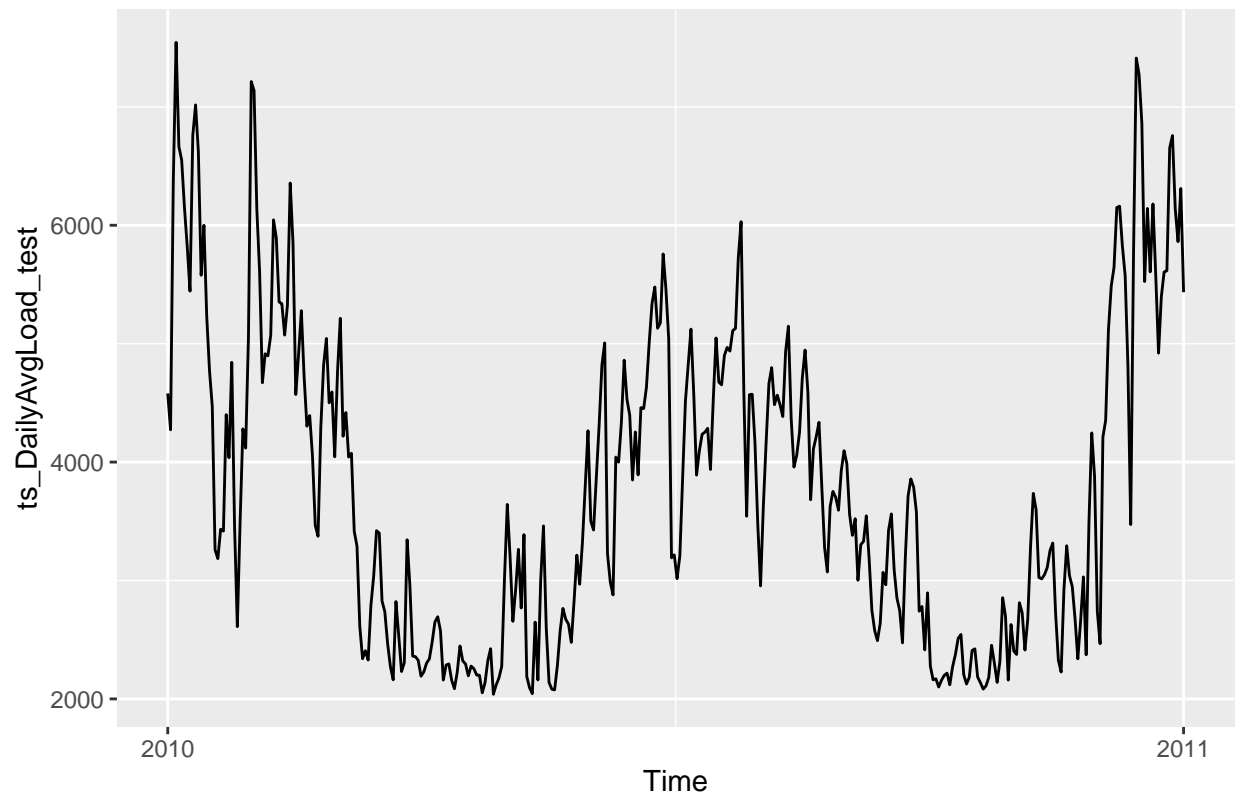
```
#subset for training
n_forecast = 365
ts_DailyAvgLoad_train <- subset(ts_DailyAvgLoad,
                                end = length(ts_DailyAvgLoad)-n_forecast)

#subset for testing
ts_DailyAvgLoad_test <- subset(ts_DailyAvgLoad,
                                start = length(ts_DailyAvgLoad)-n_forecast)

autoplot(ts_DailyAvgLoad_train)
```



```
autoplot(ts_DailyAvgLoad_test)
```



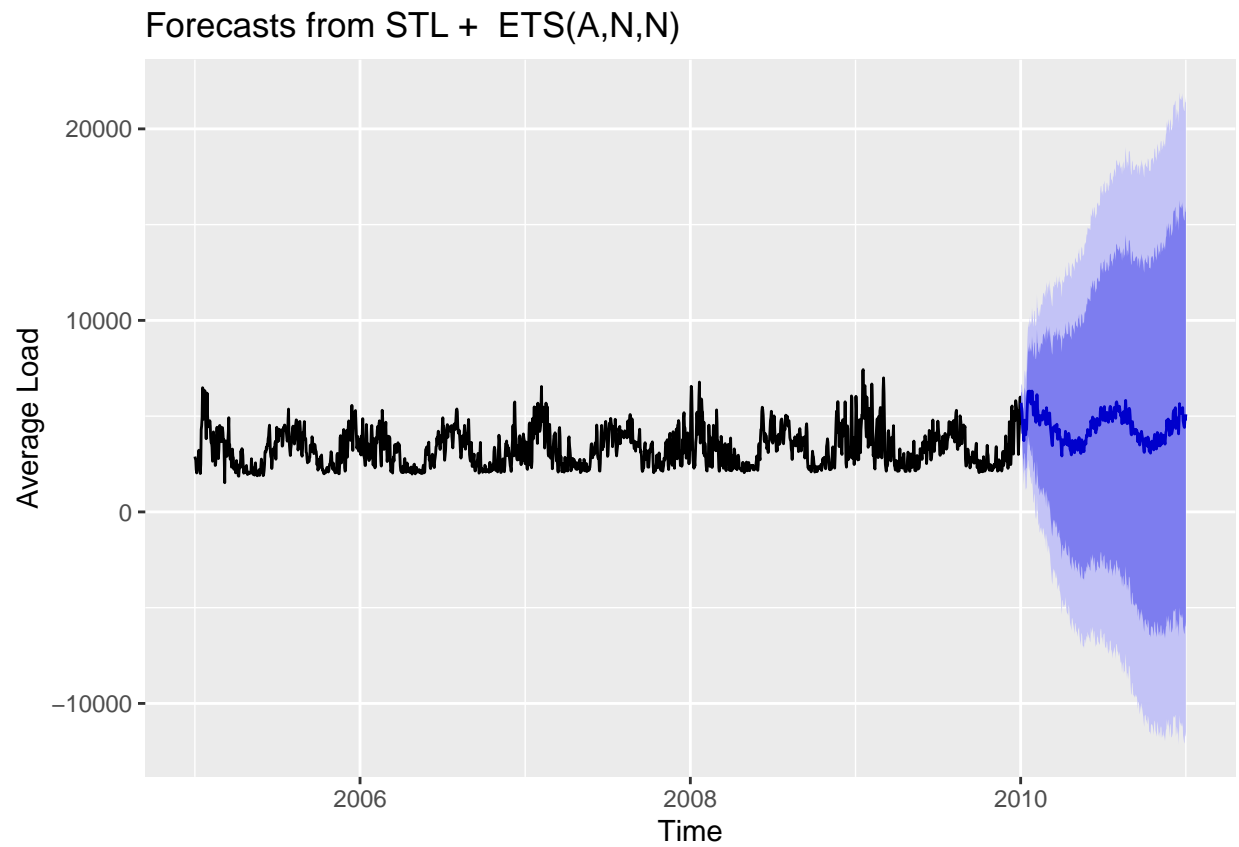
#Forecasting using STL+ETS (Model 1)

#Fit and forecast STL + ETS model to data

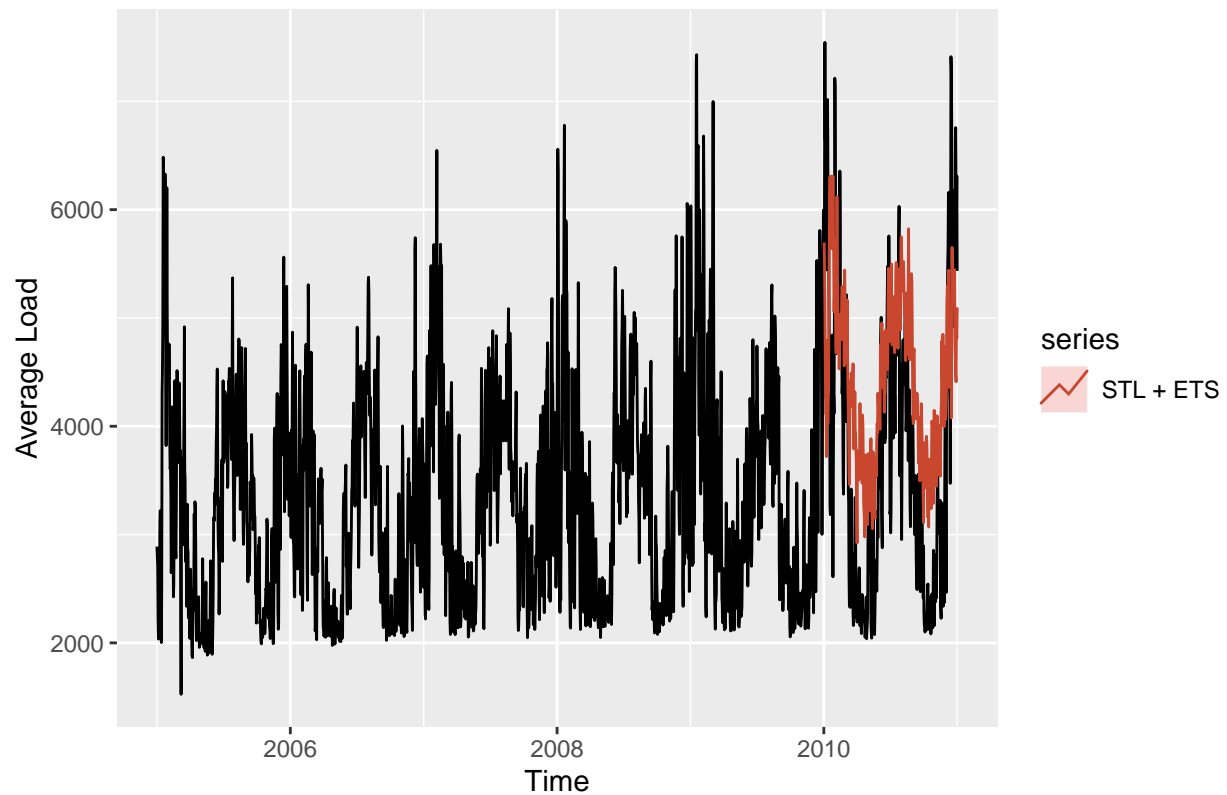
```
ETS_fit <- stlf(ts_DailyAvgLoad_train,h=365)
```

#Plot foresting results

```
autoplot(ETS_fit) + ylab("Average Load") #ANN = additive, no trend, non-seasonal
```



```
#Plot model + observed data  
autoplot(ts_DailyAvgLoad) +  
  autolayer(ETS_fit, series="STL + ETS",PI=FALSE) +  
  ylab("Average Load")
```



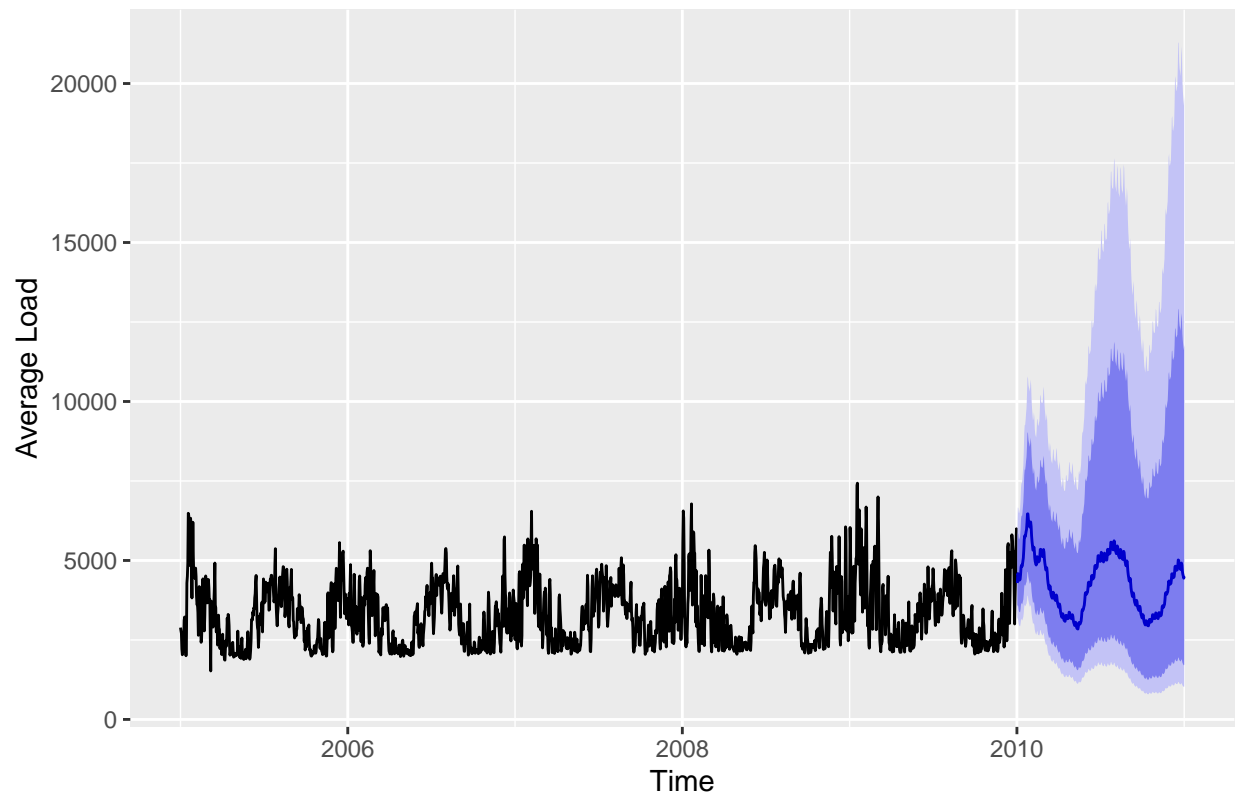
#Forecasting using ARIMA + Fourier (Model 2)

```
ARIMA_Four_fit <- auto.arima(ts_DailyAvgLoad_train,
                             seasonal=FALSE, #P,D,Q = 0
                             lambda=0,
                             xreg=fourier(ts_DailyAvgLoad_train,
                                             K=c(2,12))
                             )

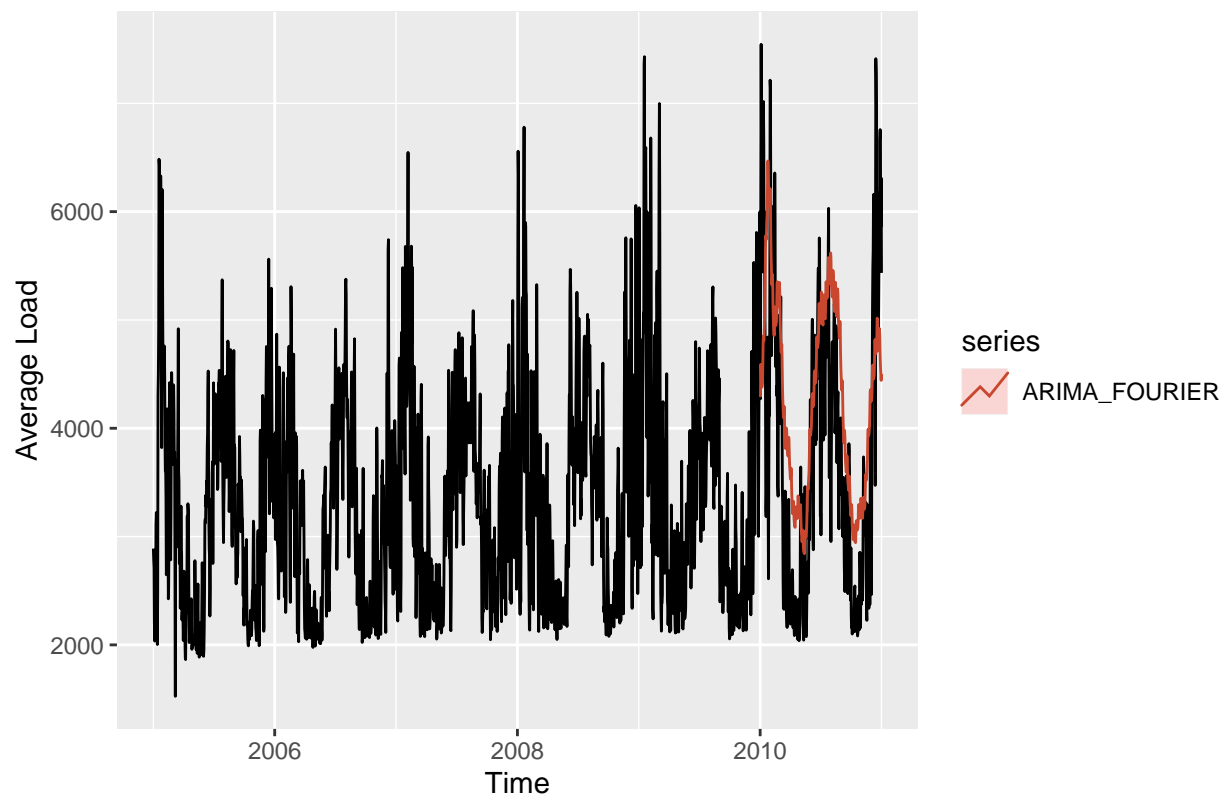
#Forecast with ARIMA fit
ARIMA_Four_for <- forecast::forecast(ARIMA_Four_fit,
                                     xreg=fourier(ts_DailyAvgLoad_train,
                                             K=c(2,12),
                                             h=365), #generates fourier terms 365 step ahead of time
                                     h=365
                                     )

#Plot forecasting results
autoplot(ARIMA_Four_for) + ylab("Average Load")
```

Forecasts from Regression with ARIMA(0,1,2) errors



```
#Plot model + observed data  
autoplot(ts_DailyAvgLoad) +  
  autolayer(ARIMA_Four_for, series="ARIMA_FOURIER",PI=FALSE) +  
  ylab("Average Load")
```

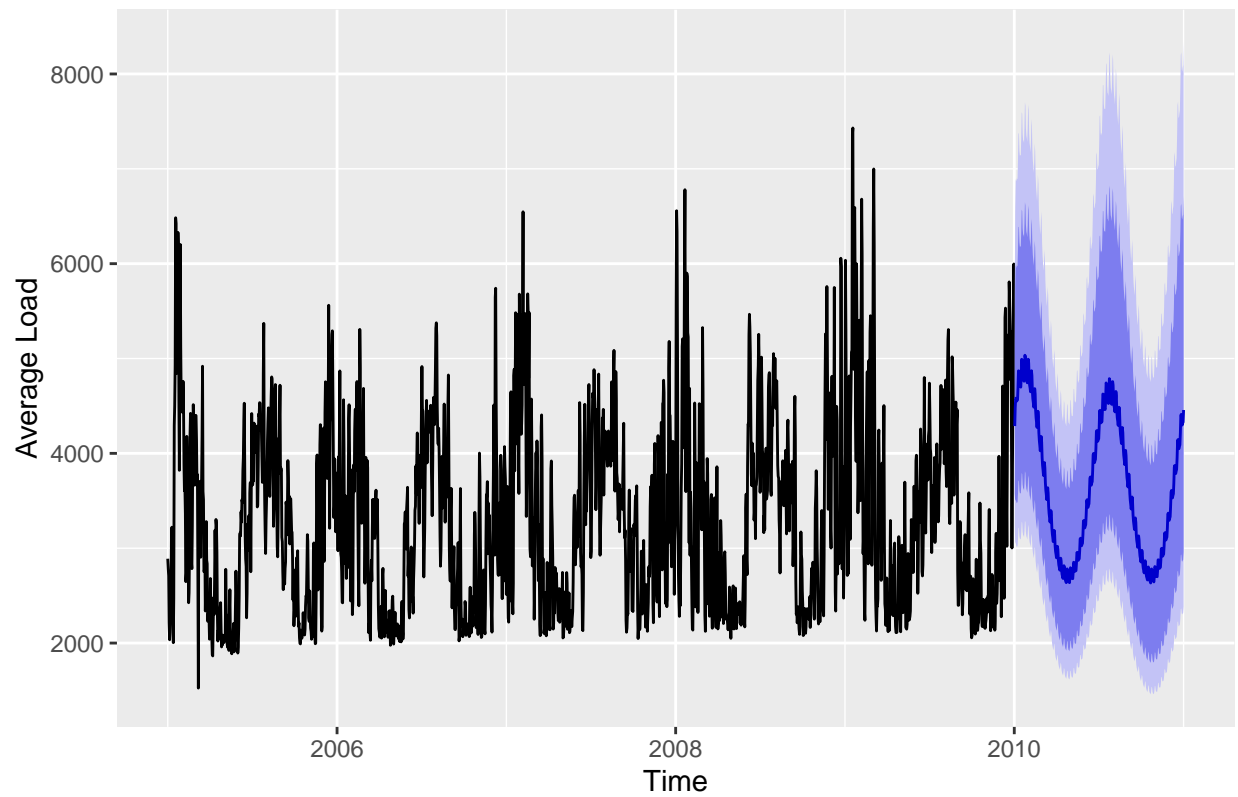
#Forecasting using TBATS (Model 3)

```
TBATS_fit <- tbats(ts_DailyAvgLoad_train)

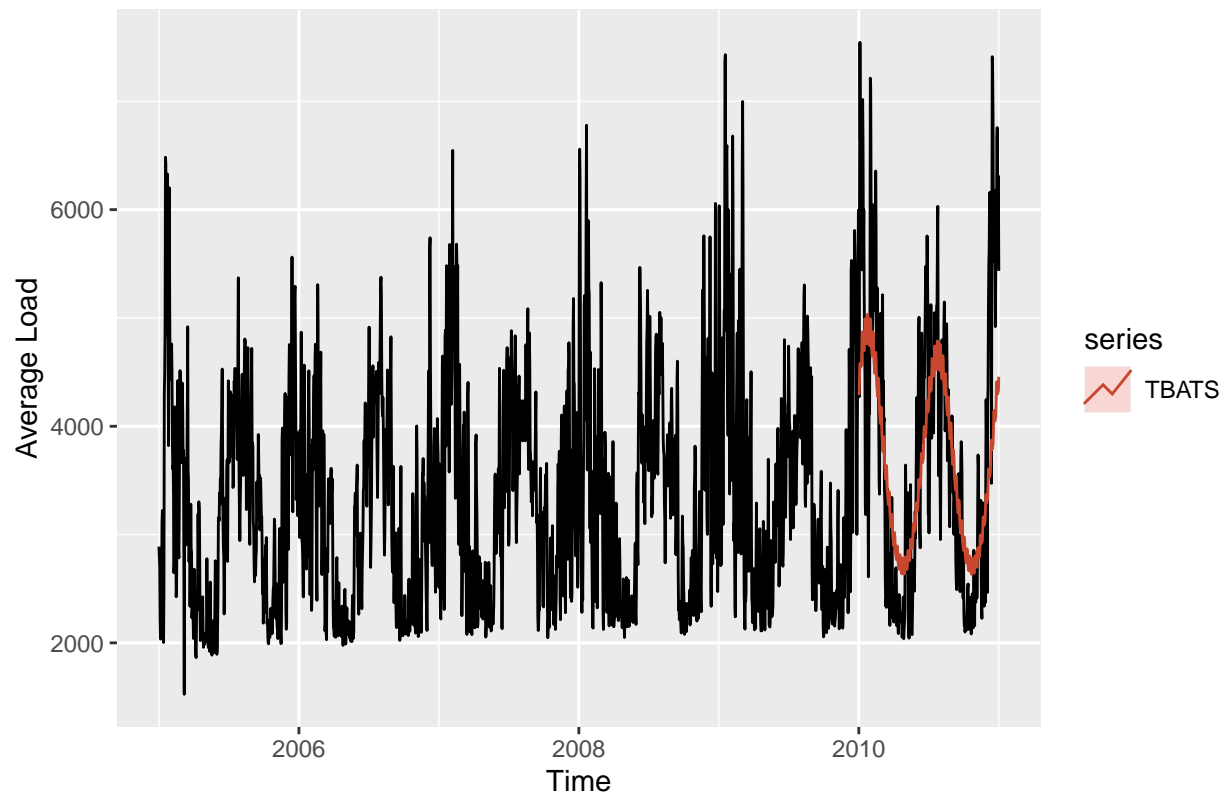
TBATS_for <- forecast::forecast(TBATS_fit, h=365)

#Plot forecasting results
autoplot(TBATS_for) +
  ylab("Average Load")
```

Forecasts from TBATS(0, {0,3}, −, {<7,2>, <365.25,2>})



```
#Plot model + observed data
autoplot(ts_DailyAvgLoad) +
  autolayer(TBATS_for, series="TBATS",PI=FALSE)+
  ylab("Average Load")
```



#Forecasting using Neural Network Time Series (Model 4)

```

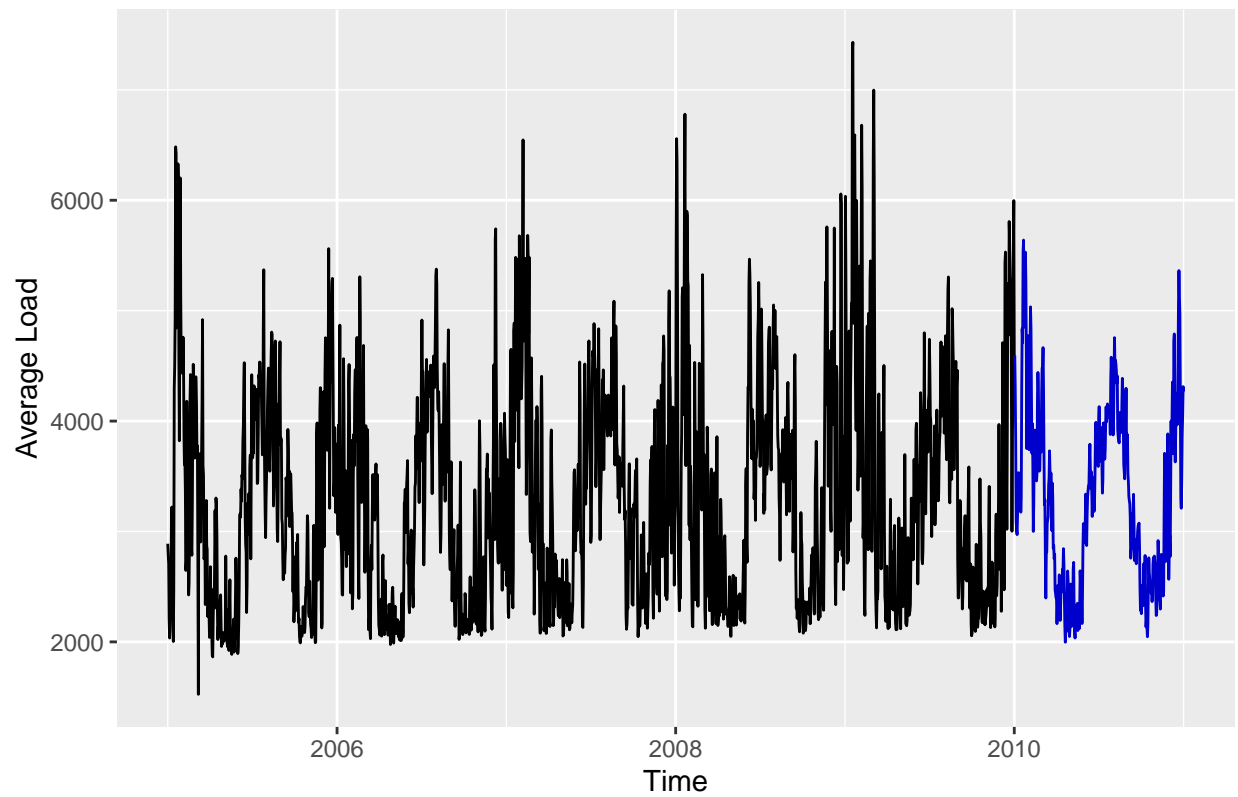
NN_fit <- nnetar(ts_DailyAvgLoad_train,p=1,P=0,xreg=fourier(ts_DailyAvgLoad_train, K=c(2,12)))

NN_for <- forecast::forecast(NN_fit, h=365,xreg=fourier(ts_DailyAvgLoad_train,
                                                         K=c(2,12),h=365))

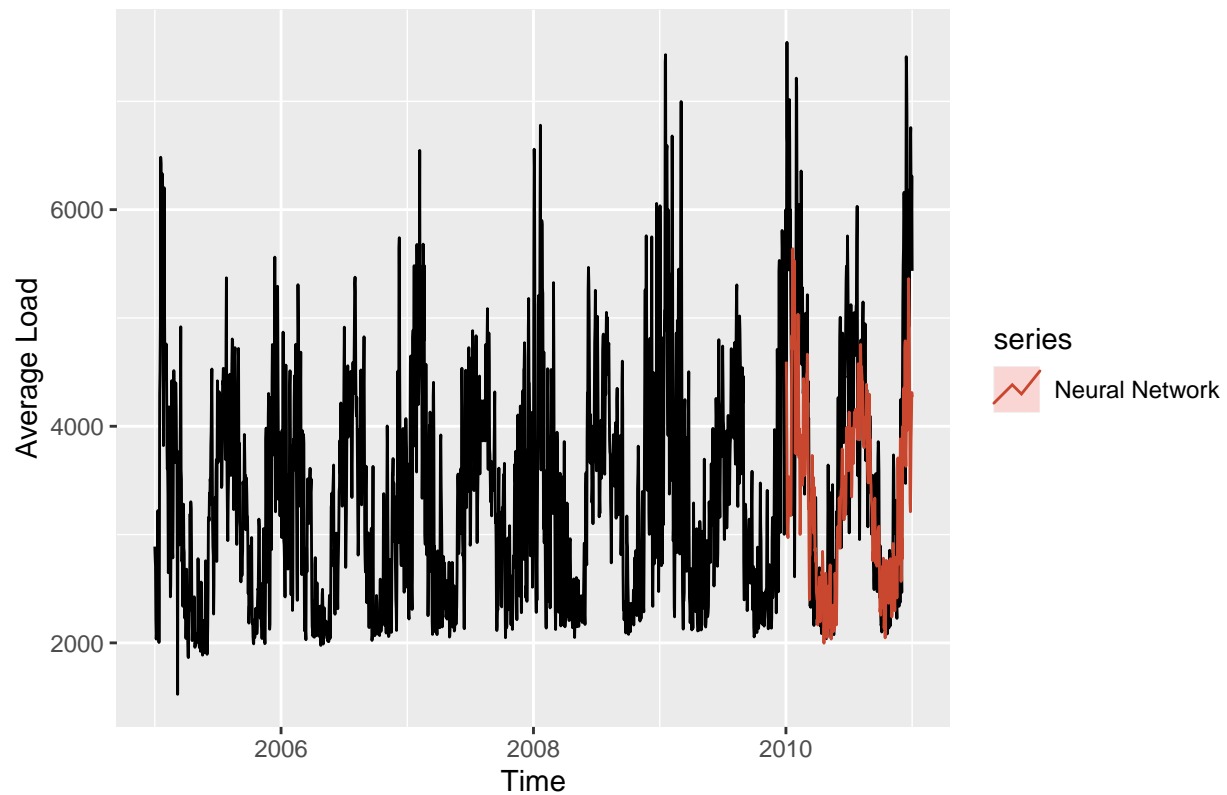
#Plot forecasting results
autoplot(NN_for) +
  ylab("Average Load")

```

Forecasts from NNAR(1,15)



```
#Plot model + observed data  
autoplot(ts_DailyAvgLoad) +  
  autolayer(NN_for, series="Neural Network",PI=FALSE)+  
  ylab("Average Load")
```



Checking accuracy of the models

```
#Model 1: STL + ETS
ETS_scores <- accuracy(ETS_fit$mean,ts_DailyAvgLoad_test)

#Model 2: ARIMA + Fourier
ARIMA_scores <- accuracy(ARIMA_Four_for$mean,ts_DailyAvgLoad_test)

# Model 3: TBATS
TBATS_scores <- accuracy(TBATS_for$mean,ts_DailyAvgLoad_test)

# Model 4: Neural Network
NN_scores <- accuracy(NN_for$mean,ts_DailyAvgLoad_test)
```

Comparing Performance metrics

```
#creating data frame
scores <- as.data.frame(
  rbind(ETS_scores, ARIMA_scores, TBATS_scores, NN_scores)
)
```

```

row.names(scores) <- c("STL+ETS", "ARIMA+Fourier", "TBATS", "NN")

#choosing model with lowest RMSE
best_model_index_RMSE <- which.min(scores[, "RMSE"])
#choosing model with lowest MAPE
best_model_index_MAPE <- which.min(scores[, "MAPE"])

#printing results
cat("The best model by RMSE is:", row.names(scores[best_model_index_RMSE,]))

```

The best model by RMSE is: TBATS

```

cat("The best model by MAPE is:", row.names(scores[best_model_index_MAPE,]))

```

The best model by MAPE is: NN

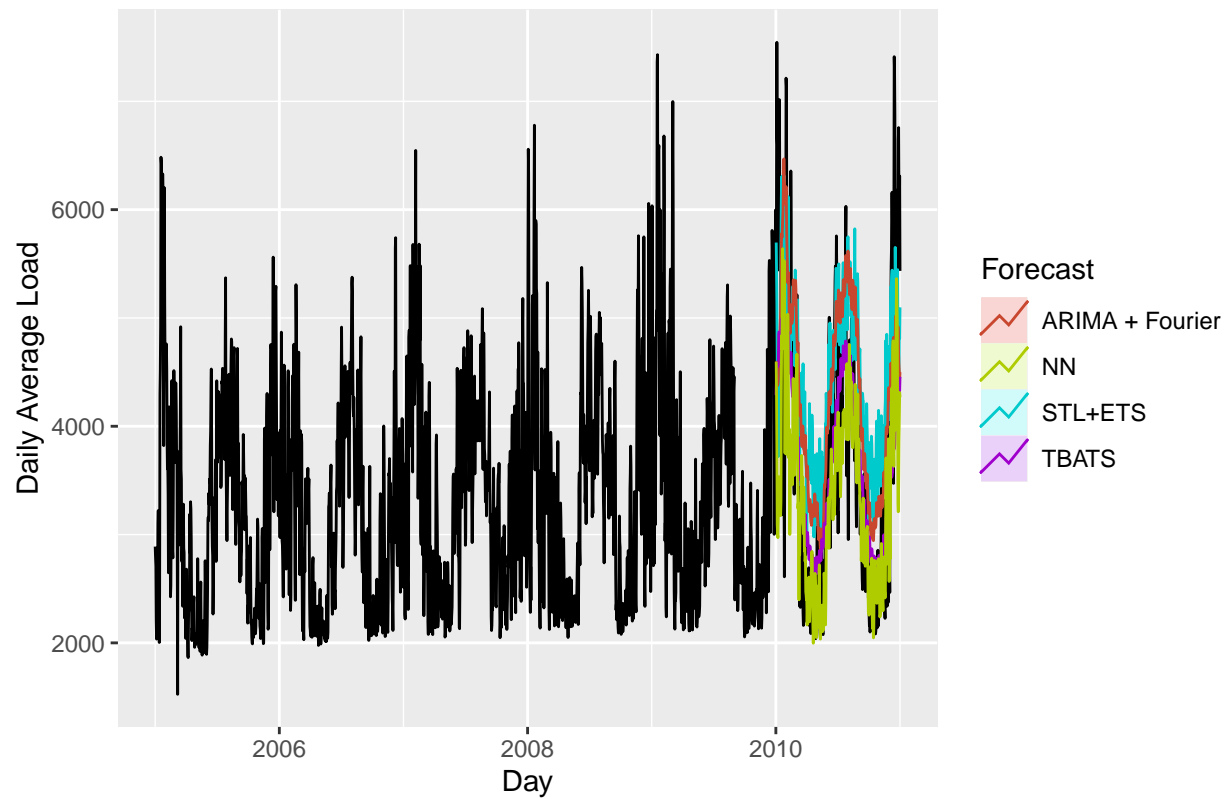
Table 1: Forecast Accuracy for Daily Average Load

	ME	RMSE	MAE	MPE	MAPE	ACF1	Theil's U
STL+ETS	-664.6880	1230.3995	1039.9902	-27.15911	33.22800	0.79970	2.80673
ARIMA+Fourier	-506.1649	1080.7349	898.1974	-20.91309	27.48365	0.84141	2.29946
TBATS	118.6917	912.2884	688.5789	-3.18910	18.35719	0.82733	1.54891
NN	444.2615	1095.3214	755.3310	6.52168	17.74768	0.81794	1.61877

```

autoplot(ts_DailyAvgLoad) +
  autolayer(ETS_fit, PI=FALSE, series="STL+ETS") +
  autolayer(ARIMA_Four_for, PI=FALSE, series="ARIMA + Fourier") +
  autolayer(TBATS_for, PI=FALSE, series="TBATS") +
  autolayer(NN_for, PI=FALSE, series="NN") +
  xlab("Day") + ylab("Daily Average Load") +
  guides(colour=guide_legend(title="Forecast"))

```



#Forecasting Daily Demand for January 2011

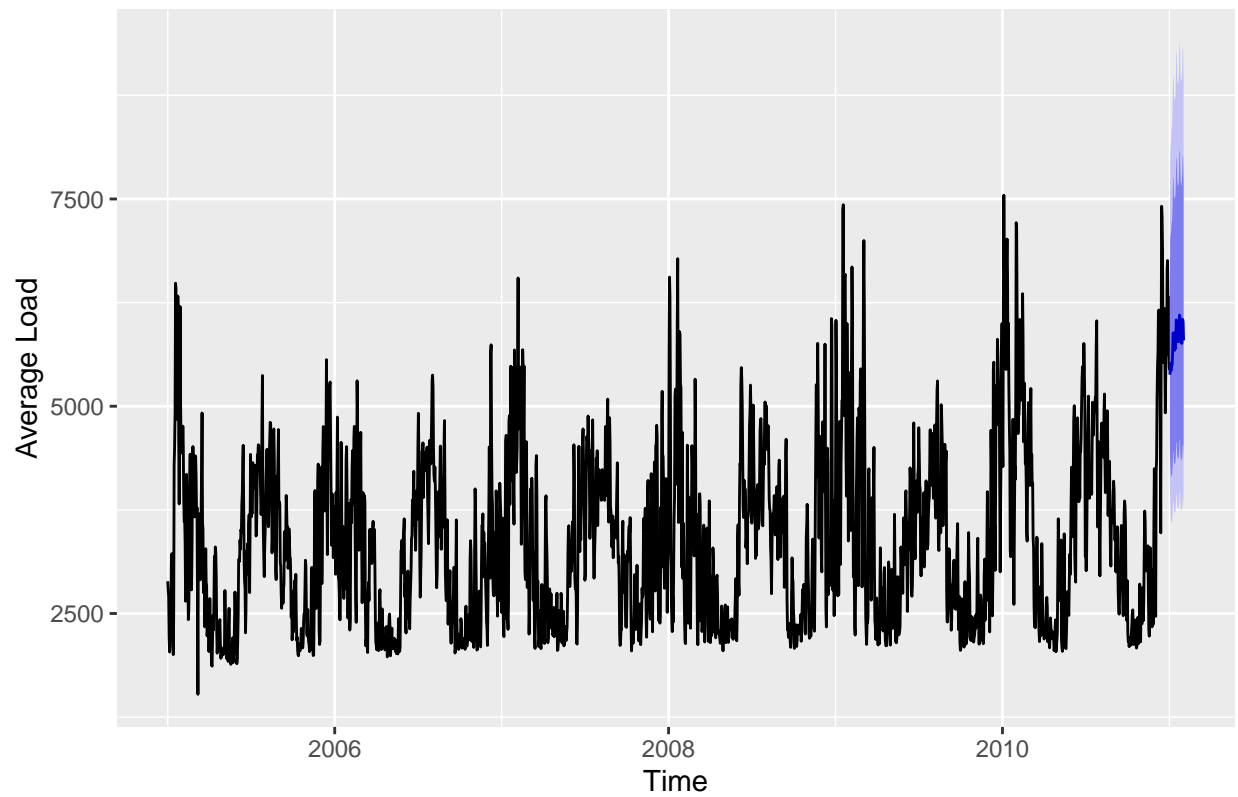
Since TBATS was determined to be the best model by RMSE:

```
TBATS11_fit <- tbats(ts_DailyAvgLoad)

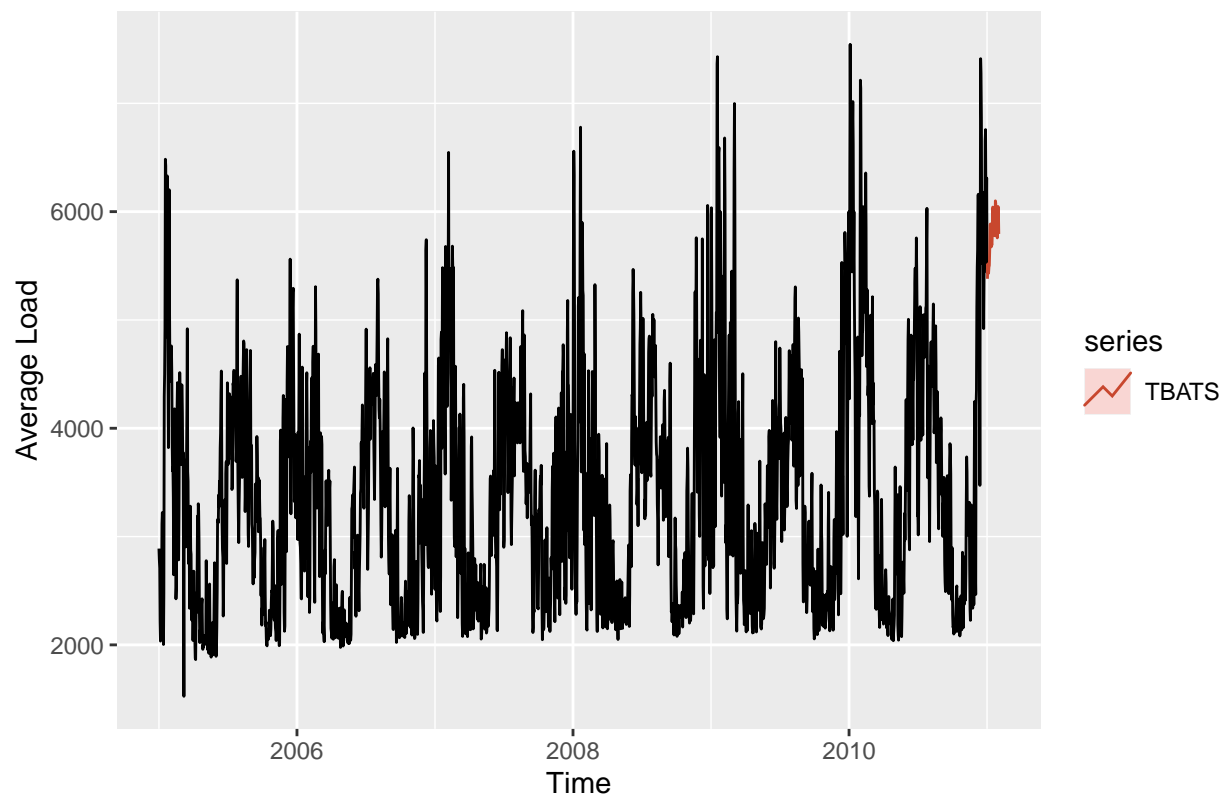
TBATS11_for <- forecast::forecast(TBATS11_fit, h=31)

#Plot forecasting results
autoplot(TBATS11_for) +
  ylab("Average Load")
```

Forecasts from TBATS(0.001, {1,2}, -, {<7,2>, <365.25,2>})



```
#Plot model + observed data  
autoplot(ts_DailyAvgLoad) +  
  autolayer(TBATS11_for, series="TBATS",PI=FALSE)+  
  ylab("Average Load")
```

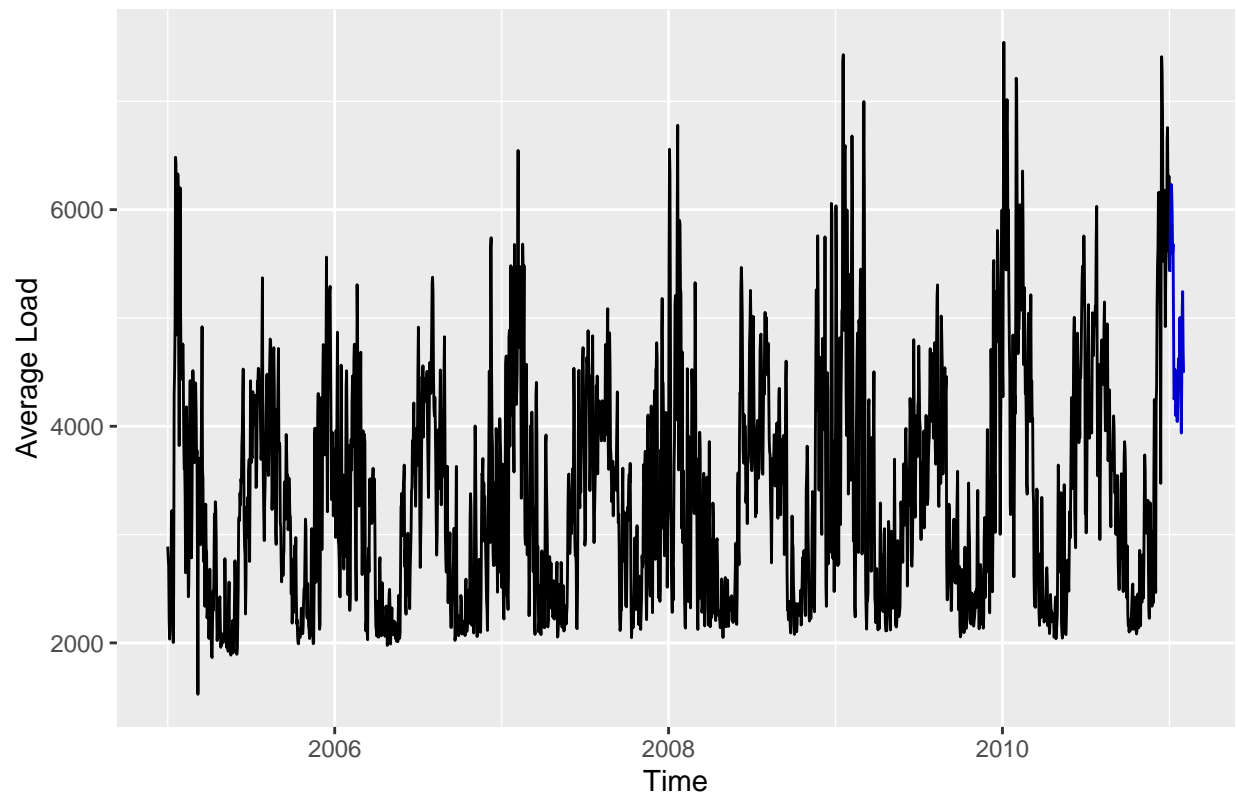
```
write.csv(TBATS11_for, file="./Outputs/TBATS_forecast.csv")
```

Since Neural Network was determined to be the best model by MAPE:

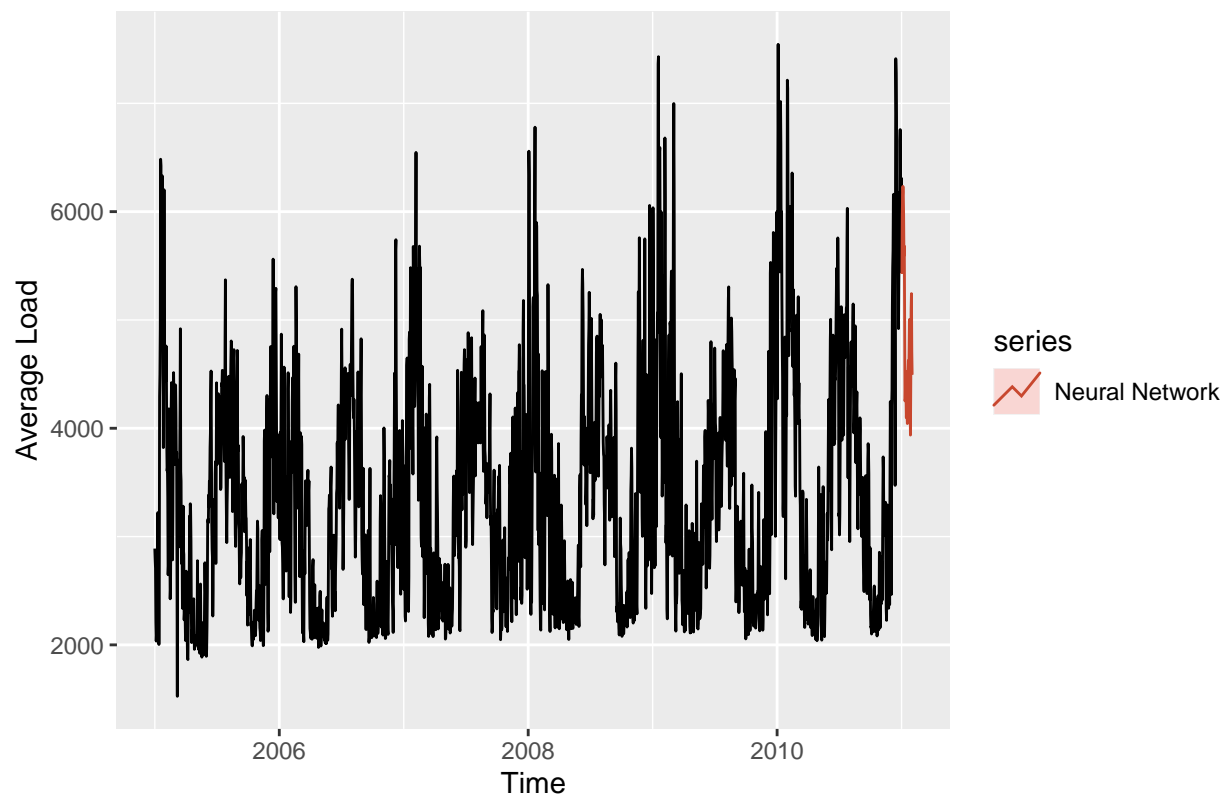
```
NN11_fit <- nnetar(ts_DailyAvgLoad,p=1,P=0,xreg=fourier(ts_DailyAvgLoad, K=c(2,12)))
NN11_for <- forecast::forecast(NN11_fit, h=31,xreg=fourier(ts_DailyAvgLoad,
K=c(2,12),h=31))

#Plot forecasting results
autoplot(NN11_for) +
  ylab("Average Load")
```

Forecasts from NNAR(1,15)



```
#Plot model + observed data
autoplot(ts_DailyAvgLoad) +
  autolayer(NN11_for, series="Neural Network",PI=FALSE)+
  ylab("Average Load")
```



```
#write.csv(NN11_for, file="./Outputs/NN_forecast.csv")
```

```
#Forecasting using ARIMA (Model 5)
```

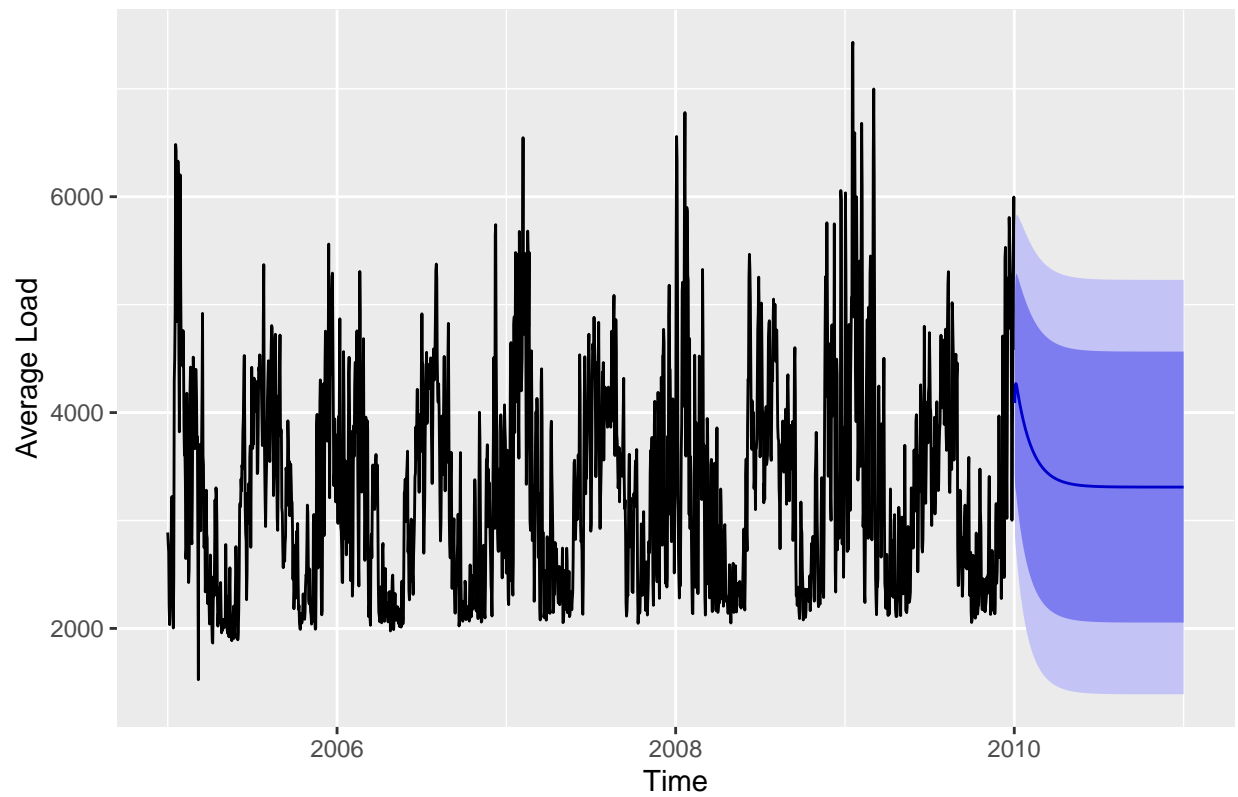
```
autofit_SARIMA <- auto.arima(ts_DailyAvgLoad_train)
print(autofit_SARIMA)
```

```
## Series: ts_DailyAvgLoad_train
## ARIMA(2,0,2) with non-zero mean
##
## Coefficients:
##          ar1      ar2      ma1      ma2      mean
##          1.3695 -0.3870 -0.3882 -0.3988 3309.6332
## s.e.    0.0428  0.0401  0.0406  0.0245  142.2393
##
## sigma^2 = 259410: log likelihood = -13970.89
## AIC=27953.78  AICc=27953.82  BIC=27986.84
```

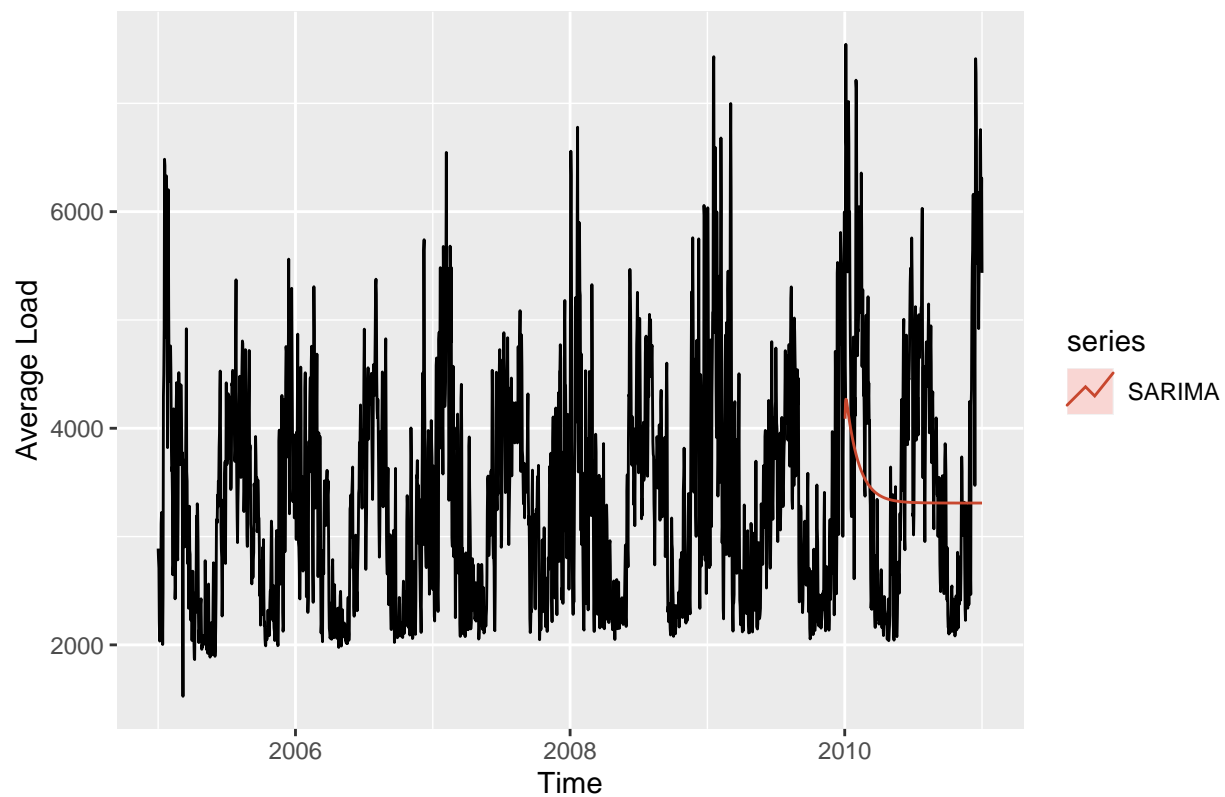
```
SARIMA_for <- forecast::forecast(object = autofit_SARIMA, h = n_forecast)
```

```
#Plot results
autoplot(SARIMA_for) +
  ylab("Average Load")
```

Forecasts from ARIMA(2,0,2) with non-zero mean



```
#Plot model + observed data  
autoplot(ts_DailyAvgLoad) +  
  autolayer(SARIMA_for, series="SARIMA",PI=FALSE)+  
  ylab("Average Load")
```



Not a great fit, but the results are valuable nonetheless. Since ARIMA(2,0,2) was selected, Will try incorporating $P=2$ into the neural network.

#Forecasting using Neural Network & $P = 2$ (Model 6)

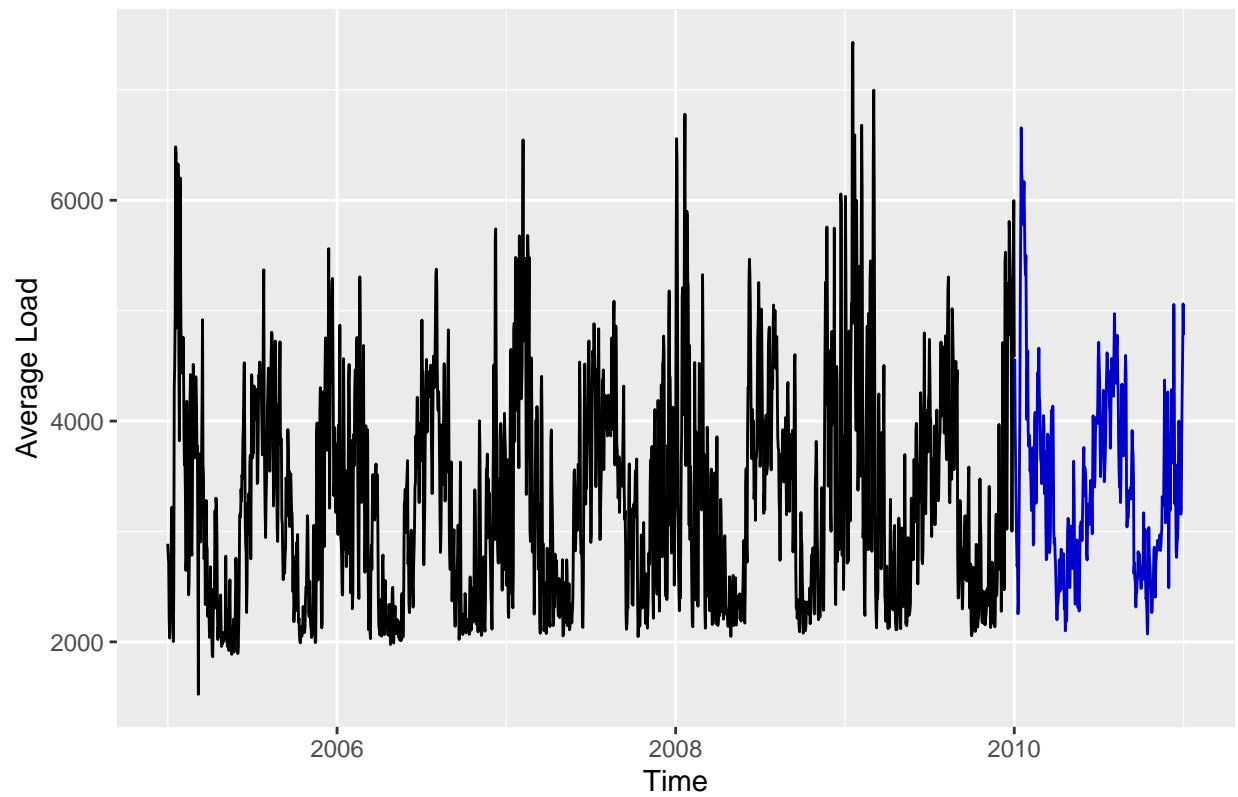
```

NN_fit_P2 <- nnetar(ts_DailyAvgLoad_train,p=1,P=2,xreg=fourier(ts_DailyAvgLoad_train, K=c(2,12)))
NN_for_P2 <- forecast::forecast(NN_fit_P2, h=365,xreg=fourier(ts_DailyAvgLoad_train,
                                                              K=c(2,12),h=365))

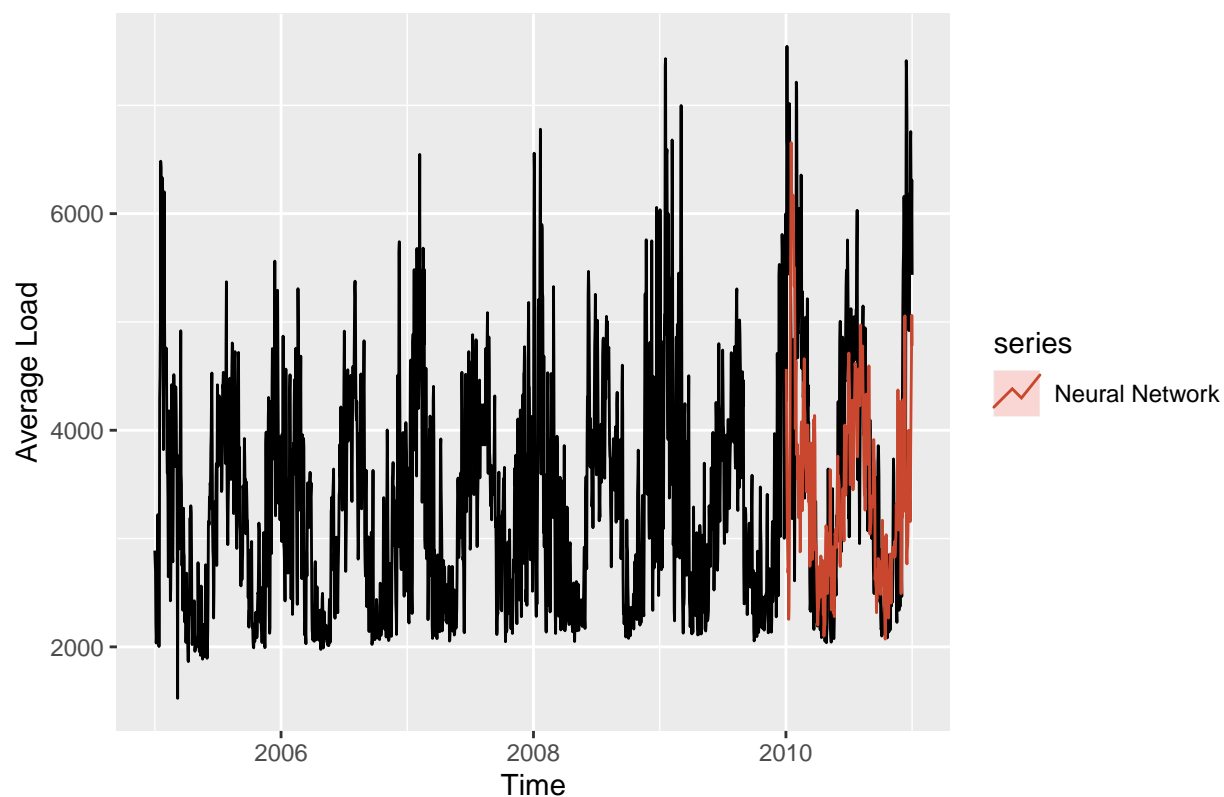
#Plot foresting results
autoplot(NN_for_P2) +
  ylab("Average Load")

```

Forecasts from NNAR(1,2,16)[365]



```
#Plot model + observed data
autoplot(ts_DailyAvgLoad) +
  autolayer(NN_for_P2, series="Neural Network",PI=FALSE)+
  ylab("Average Load")
```



```
# Model 5: SARIMA
SARIMA_scores <- accuracy(SARIMA_for$mean,ts_DailyAvgLoad_test)

# Model 6: Neural Network with P = 2
NN_P2_scores <- accuracy(NN_for_P2$mean,ts_DailyAvgLoad_test)

scores <- rbind(scores,SARIMA_scores,NN_P2_scores)
row.names(scores) <- c("STL+ETS", "ARIMA+Fourier","TBATS","NN","SARIMA","NNP2")
```

Table 2: Forecast Accuracy for Daily Average Load

	ME	RMSE	MAE	MPE	MAPE	ACF1	Theil's U
STL+ETS	-664.6880	1230.3995	1039.9902	-27.15911	33.22800	0.79970	2.80673
ARIMA+Fourier	-506.1649	1080.7349	898.1974	-20.91309	27.48365	0.84141	2.29946
TBATS	118.6917	912.2884	688.5789	-3.18910	18.35719	0.82733	1.54891
NN	444.2615	1095.3214	755.3310	6.52168	17.74768	0.81794	1.61877
SARIMA	360.0236	1302.5216	1059.3662	-1.12886	28.26034	0.90536	2.28572
NNP2	324.1190	1263.2820	893.4443	1.43542	21.95963	0.86088	1.97477

As indicated by higher MAPE and RMSE, the Neural Network with P=2 seems to be a worse fit than P=0.

#Averaging forecast from Neural Network & TBATS (Model 7)

```

#Create dates vector for forecast period
forecast_dates <- seq(as.Date("2011-01-01"), as.Date("2011-01-31"), by="days")

#Create df of average forecasted TBATS and NN load values
TBATS_NN_avg_for <- data.frame(cbind(forecast_dates,rowMeans(cbind(TBATS11_for$mean,NN11_for$mean))))
colnames(TBATS_NN_avg_for) <- c("date","load")

#format dates
TBATS_NN_avg_for$date <- seq(as.Date("2011-01-01"), as.Date("2011-01-31"), by="days")

#write.csv(TBATS_NN_avg_for, file="./Outputs/TBATS_NN_avg_forecast.csv")

```